

Supporting Information for

**“Selective visible-light driven highly efficient photocatalytic
reduction of CO₂ to C₂H₅OH by two-dimensional Cu₂S monolayers”**

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Computational details

The binding energy, $E_b(\text{CO})$ and $E_b(\text{CHO})$, is defined as

$$E_b(\text{CO}) = E(\text{CO}^*) - E^* - E[\text{CO}_{(\text{g})}]$$
$$E_b(\text{CHO}) = E(\text{CHO}^*) - E^* - E[\text{CO}_{(\text{g})}] - \frac{1}{2}E[\text{H}_{2(\text{g})}]$$

where E^* , $E[\text{(g)}]$ and $E(^*)$ represent the total energies of the clean slab, the isolated adsorbed molecule and the slab after adsorption, respectively.

The Gibbs free energy change (ΔG) of each elementary reaction was calculated as

$$\Delta G = \Delta E + \Delta E_{\text{ZPE}} - T\Delta S + \Delta G_{\text{pH}} + \Delta G_{\text{U}} + \int C_p dT$$

where ΔE is the total energy difference directly obtained from DFT calculations, ΔE_{ZPE} is the change in zero-point energies, T is the temperature, ΔS is the entropy change and C_p is the heat capacity. $\Delta G_{\text{U}} = -neU$, where n is the number of ($\text{H}^+ + e^-$) pairs transferred in CO_2RR and U is the electrode potential versus the reversible hydrogen electrode (RHE). ΔG_{pH} is the correction of the H^+ free energy by the concentration, $\Delta G_{\text{pH}} = k_{\text{B}}T \times \ln 10 \times \text{pH}$, where k_{B} is the Boltzmann constant, and the value of pH was set to be zero for acidic condition. Zero-point energies and entropies of the CO_2RR intermediates were computed from the vibrational frequencies.

The limiting potential U_{L} was obtained from the maximum free energy change (ΔG_{max}) of the whole reaction process by using the relation $U_{\text{L}} = -\Delta G_{\text{max}}/e$.

The energy barrier of E_{barrier} was calculated according to the following formula

$$E_{\text{barrier}} = E_{\text{TS}} - E_{\text{IS}}$$

where E_{TS} and E_{IS} are energies of the transition state and initial state, respectively.

The optical absorption coefficient $\alpha(\omega)$ was calculated from the following relation:

$$\alpha(\omega) = \sqrt{2} \frac{\omega}{c} \left[\sqrt{\varepsilon_1^2(\omega) + \varepsilon_2^2(\omega)} - \varepsilon_1(\omega) \right]^{1/2}$$

where $\varepsilon_1(\omega)$ and $\varepsilon_2(\omega)$ are the real part and imaginary part of dielectric function, respectively.

The imaginary part of dielectric function is selected as the optical absorption.

The conduction band minimum (CBM) and valence band maximum (VBM) edge positions of Cu_2S catalysts with respect to NHE were calculated by using the following equations:

$$E_{\text{CBM}} = -\Phi + 0.5E_{\text{g}}$$

$$E_{\text{VBM}} = -\Phi - 0.5E_{\text{g}}$$

$$E'_{\text{CBM/VBM}} = -E_{\text{CBM/VBM}} - 4.45$$

where Φ is the work function, E_g is the band gap, $E'_{\text{CBM/VBM}}$ represent energy levels relative to NHE.

Zero-point energy (ZPE) and entropy corrections (TS)

The entropies of the gaseous molecules were taken from the NIST Chemistry WebBook and the zero-point energy (ZPE) was calculated according to:

$$E_{\text{ZPE}} = \sum_{i=1}^{3N} \frac{h\nu_i}{2}$$

The entropy change for adsorbed intermediates was calculated within the harmonic approximation:

$$\Delta S_{\text{ads}}(0 \rightarrow T, P^0) = S_{\text{vib}} = \sum_{i=1}^{3N} \left[\frac{N_A h \nu_i}{T (e^{h\nu_i/K_B T} - 1)} - R \ln (1 - e^{-h\nu_i/K_B T}) \right]$$

Where ν_i is DFT-calculated normal-mode frequency for species of $3N$ degree of freedom (N =number of atoms) adsorbed on Cu_2S monolayers, N_A is the Avogadro's constant ($6.022 \times 10^{23} \text{ mol}^{-1}$), h is the Planck's constant ($6.626 \times 10^{-34} \text{ J s}$), and k_B is the Boltzmann constant ($1.38 \times 10^{-23} \text{ JK}^{-1}$), R is the ideal gas constant ($8.314 \text{ J K}^{-1} \text{ mol}^{-1}$), and T is the system temperature, and $T=298\text{K}$ in this work. The energy corrections of gas-phase species, including zero point energies and entropies, are listed below:

Table S1. Free energy corrections for gas-phase species.

Molecule	ZPE (eV)	T Δ S (eV)
CO_2	0.31	0.66
CO	0.13	0.61
H_2	0.28	0.40
H_2O	0.57	0.67
C_2H_4	1.36	0.71
$\text{C}_2\text{H}_5\text{OH}$	2.11	0.83

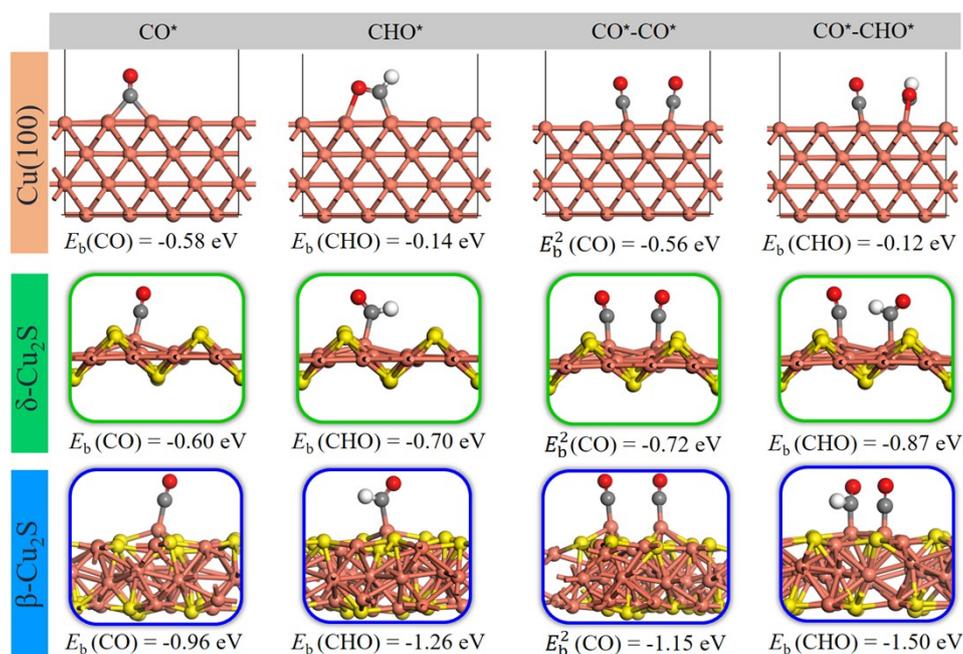


Figure S1. Optimized geometries of CO* and CHO* adsorbed on Cu(100), $\delta\text{-Cu}_2\text{S}$ and $\beta\text{-Cu}_2\text{S}$.

Binding energies of CHO* and CO* also shown in the Figure. $E_b^2(\text{CO})$ represent the binding energy of the second carbon monoxide.

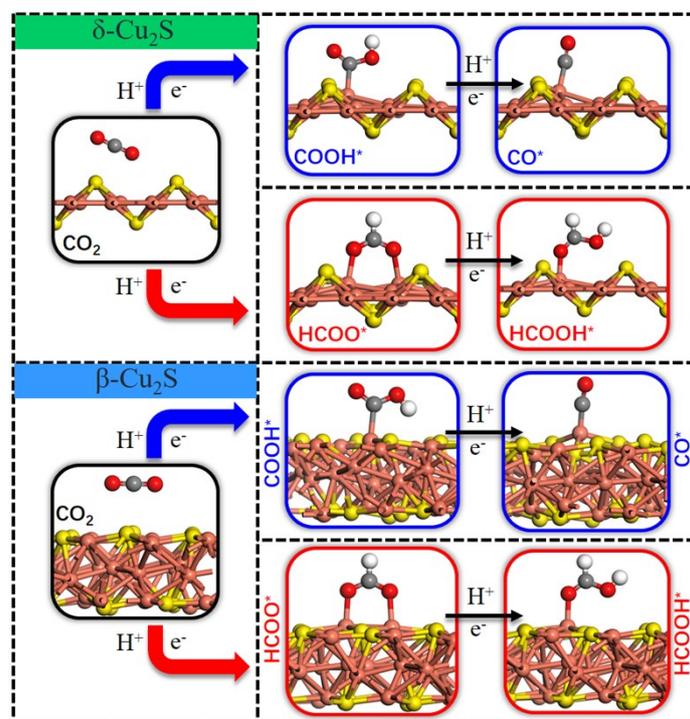


Figure S2. Optimized geometric of various intermediates along the most favorable two paths:

I) $\text{CO}_2 \rightarrow \text{COOH}^* \rightarrow \text{CO}^*$; **II**) $\text{CO}_2 \rightarrow \text{HCOO}^* \rightarrow \text{HCOOH}^*$ in the CO₂RR proceeded on $\delta\text{-Cu}_2\text{S}$ and $\beta\text{-Cu}_2\text{S}$ when two proton/electron pairs ($\text{H}^+ + \text{e}^-$) are transferred.

Table S2. The free energy of CO₂ hydrogenation to CO* and HCOOH* on δ -Cu₂S and β -Cu₂S.

	CO ₂	COOH*/HCOO*	CO*+H ₂ O/HCOOH*
δ -Cu ₂ S	0.00	0.21/-0.56	-0.86/-0.10
β -Cu ₂ S	0.00	0.08/-0.44	-0.71/-0.01

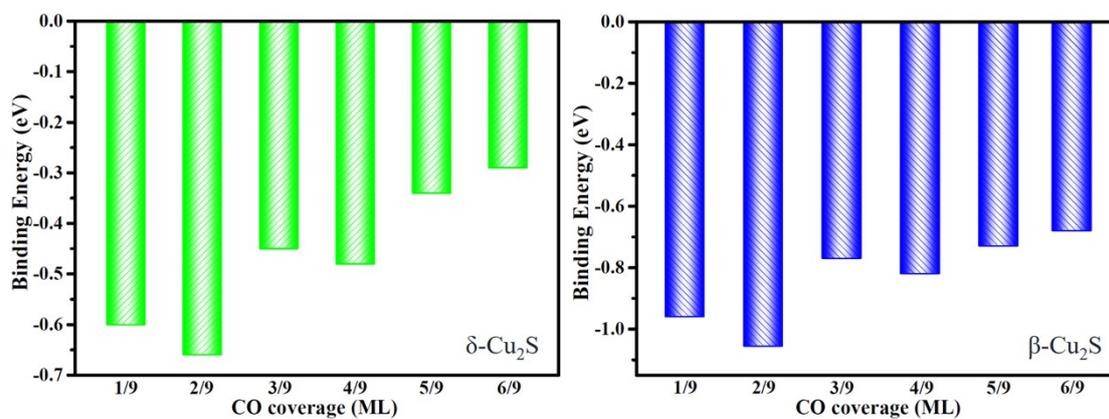


Figure S3. The relation between the CO coverage and the binding energies for δ -Cu₂S and β -Cu₂S.

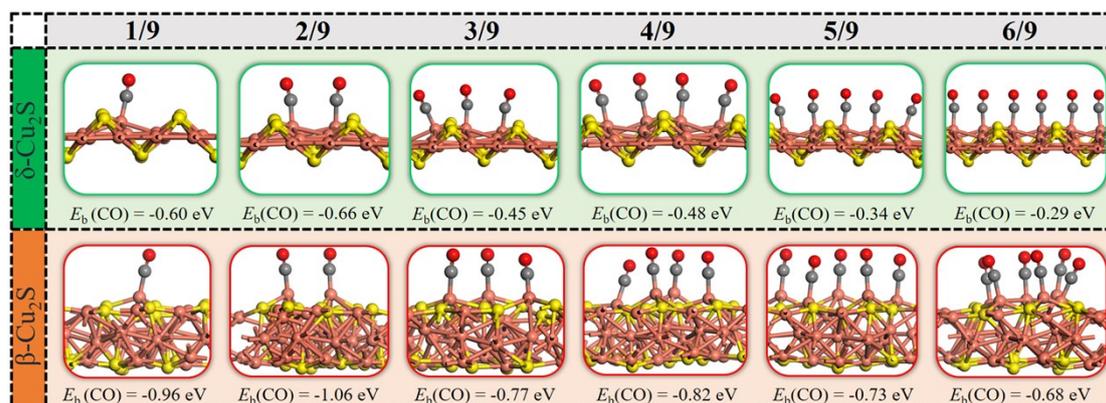


Figure S4. Detailed adsorption configurations and binding energies of CO molecule for different surface coverage.

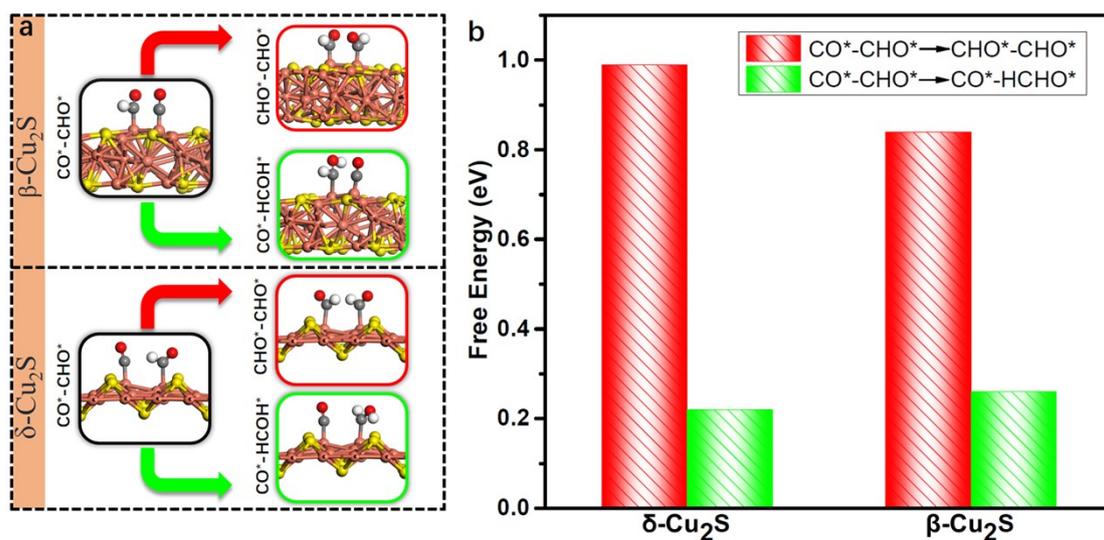


Figure S5. (a) Optimized geometric of various intermediates along the most favorable two paths: **I**) CO*-CHO* → CHO*-CHO*; **II**) CO*-CHO* → CO*-HCOH*. (b) Free energy of the hydrogenation of CO*-CHO* into CHO*-CHO* and CO*-HCOH* on δ -Cu₂S and β -Cu₂S.

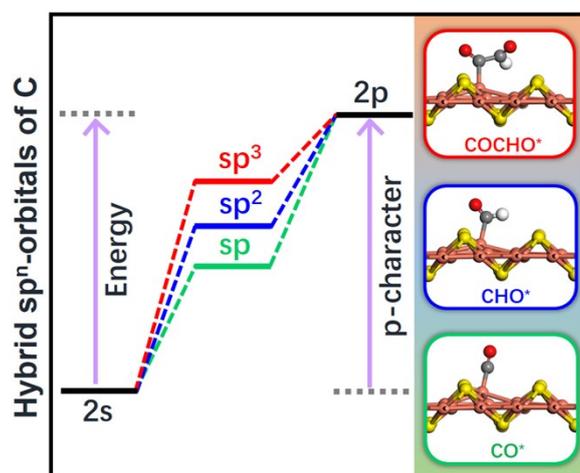


Figure S6. Schematic molecular orbital energy diagram for spⁿ ($n = 1, 2$ and 3) hybridization of C atom in CO*, CHO* and COCHO* species.

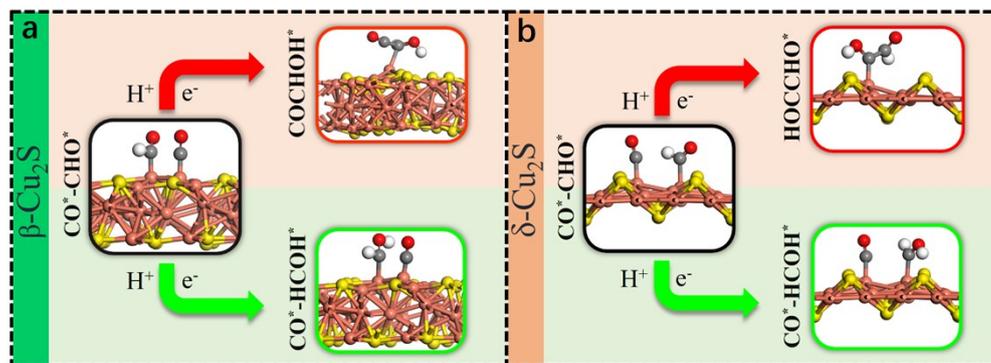


Figure S7. Optimized geometric of the intermediates along C₁ path: CO*-CHO* → CHO*-HCOH*; C₂ path: CO*-CHO* → COCHOH*/HOCCHO* on (a) β -Cu₂S and (b) δ -Cu₂S.

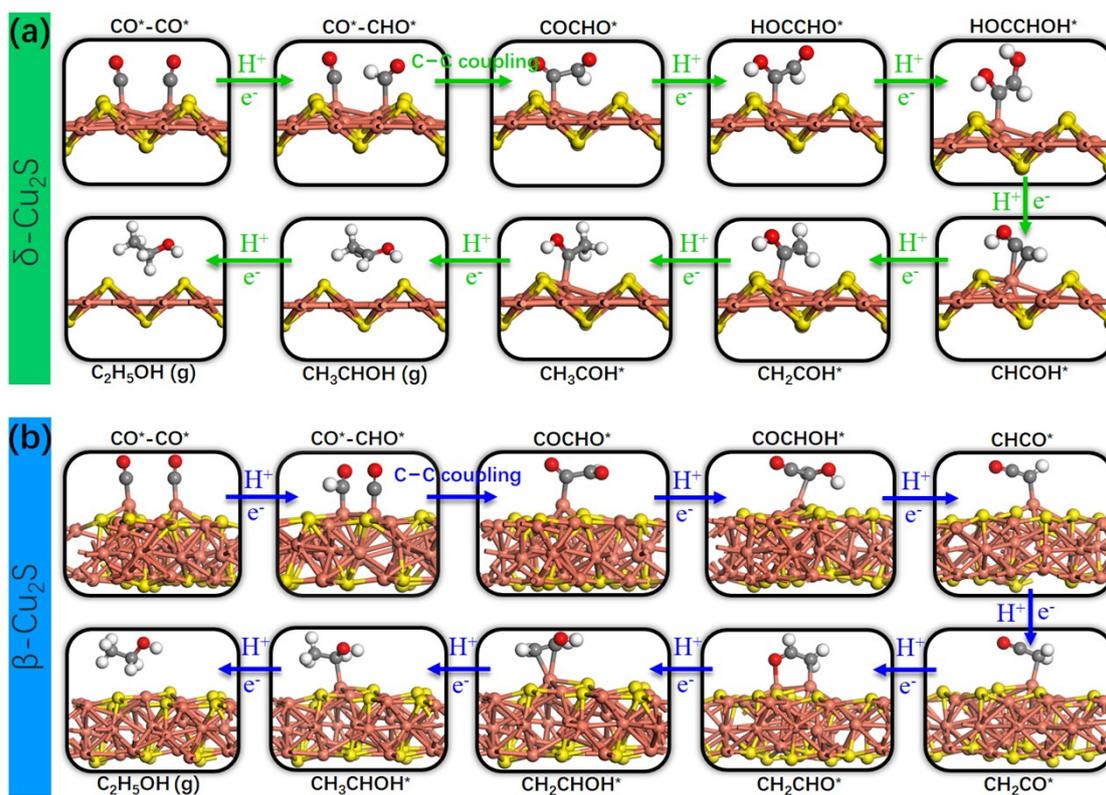


Figure S8. Optimized geometric of various intermediates of CO^{*}-CO^{*}, CO^{*}-CHO^{*}, COCHO^{*}, HOCCHO^{*}, HOCCHOH^{*}, CHCOH^{*}, CH₂COH^{*}, CH₃CHO^{*}, CH₃CHOH and C₂H₅OH on the (a) δ -Cu₂S surface; and CO^{*}-CO^{*}, CO^{*}-CHO^{*}, COCHO^{*}, COCHOH^{*}, CHCO^{*}, CH₂CO^{*}, CH₂CHO^{*}, CH₂CHOH^{*}, CH₃CHOH and C₂H₅OH on the (b) β -Cu₂S surface along the reaction path of CO₂RR proceeded.

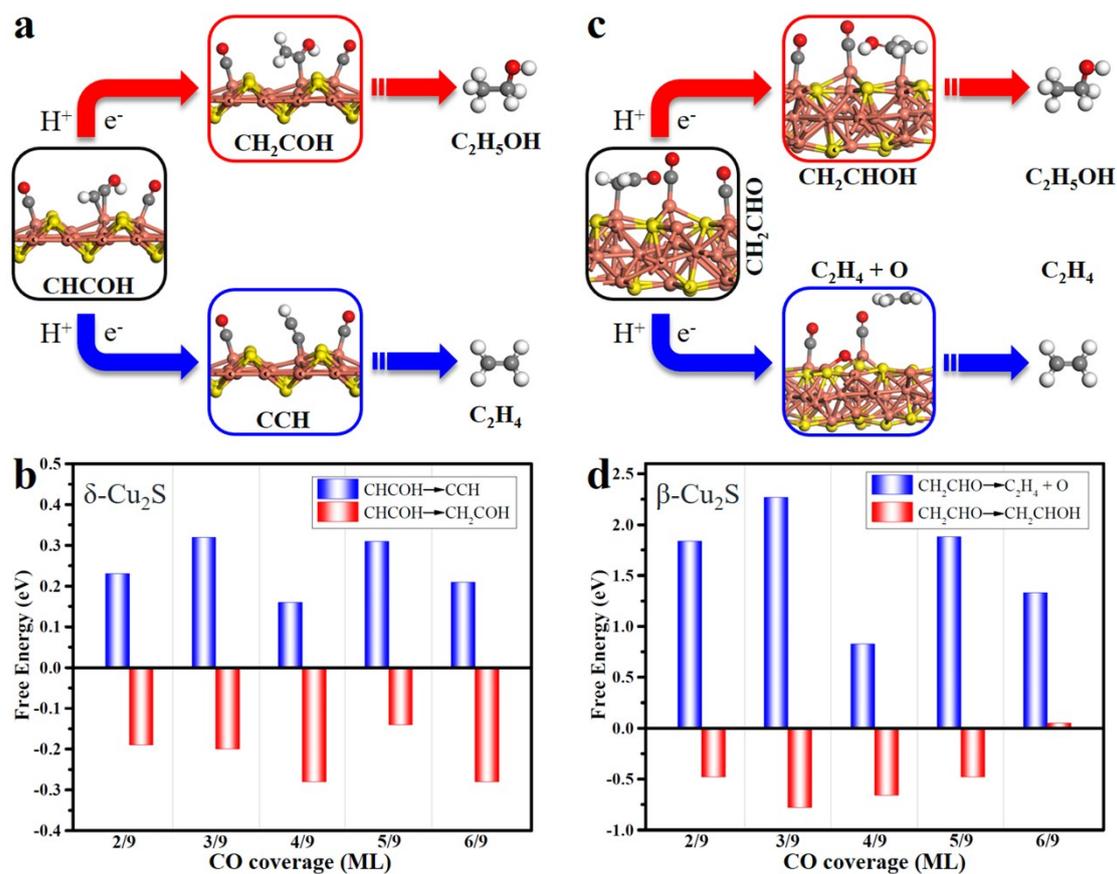


Figure S9. Key reaction pathways for (a) CHCOH* → CH₂COH* (ethanol path) or CHCOH* → CCH* (ethylene path) on $\delta\text{-Cu}_2\text{S}$ surface; (c) CH₂CHO* → CH₂CHOH* (ethanol path) or CH₂CHO* → C₂H₄ (ethylene path) on $\beta\text{-Cu}_2\text{S}$ surface. Reaction free energies of (b) CHCOH* → CH₂COH* or CHCOH* → CCH* on $\delta\text{-Cu}_2\text{S}$ surface; and (d) CH₂CHO* → CH₂CHOH* or CH₂CHO* → C₂H₄ on $\beta\text{-Cu}_2\text{S}$ surface under different CO* coverages ranging from 2/9 to 6/9 monolayer (ML).

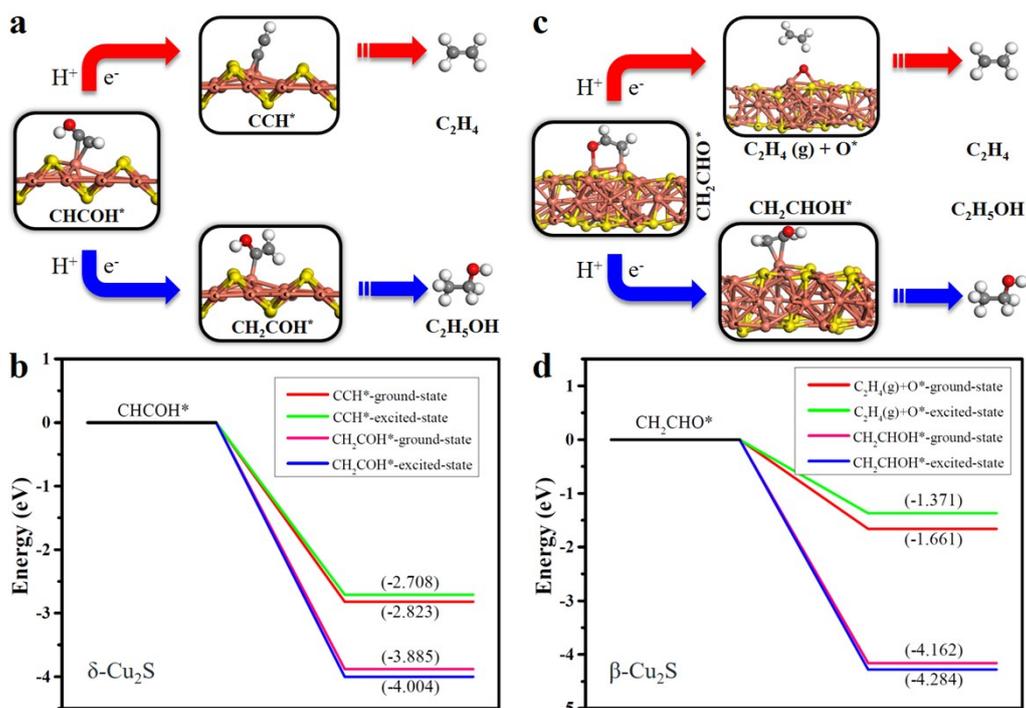


Figure S10. Key reaction pathways for (a) CHCOH* → CH₂COH* (ethanol path) or CHCOH* → CCH* (ethylene path) on δ-Cu₂S surface, (c) CH₂CHO* → CH₂CHOH* (ethanol path) or CH₂CHO* → C₂H₄ (ethylene path) on β-Cu₂S surface. Energy profiles for (b) CHCOH* → CCH* or CHCOH* → CH₂COH* on δ-Cu₂S surface, and (d) CH₂CHO* → C₂H₄ or CH₂CHO* → CH₂CHOH* on β-Cu₂S surface under the electro-driven (ground-state) and photo-driven (excited-state).

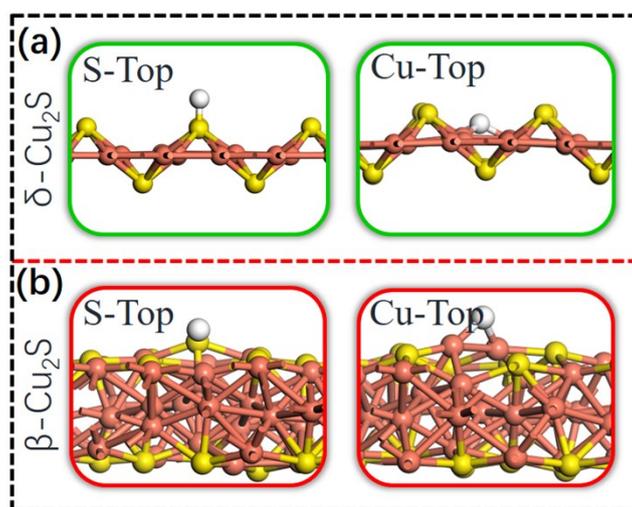


Figure S11. Optimized geometries of H* adsorbed on (a) δ-Cu₂S and (b) β-Cu₂S.

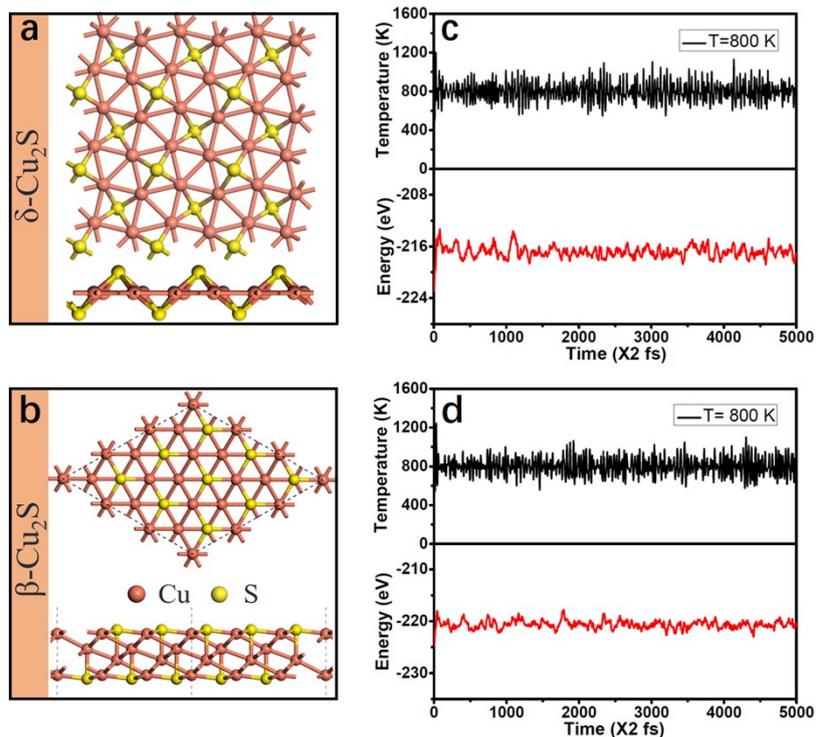


Figure S12. Top and side views of atomic configurations of **(a)** δ -Cu₂S and **(b)** β -Cu₂S in a 3×3 supercell. Color scheme: pink and yellow spheres represent Cu and S atoms, respectively. Variations of temperature and energy fluctuations versus AIMD simulation time progress for **(c)** δ -Cu₂S and **(d)** β -Cu₂S. The simulation lasting for 10 ps with a time step of 2 fs at $T = 800$ K.

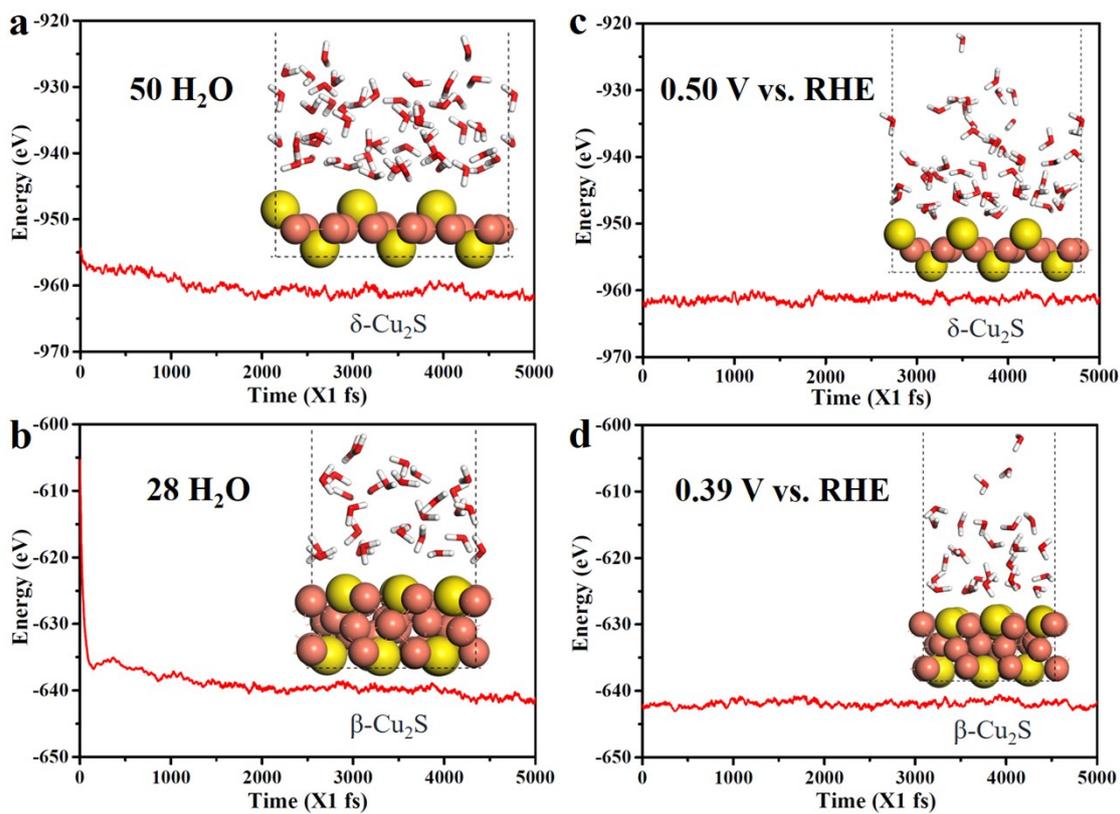


Figure S13. Energy fluctuations versus AIMD simulation time progress under the existence of the solvent on the (a) δ -Cu₂S and (b) β -Cu₂S, and the potential (i.e. limiting potential during the CO₂RR) of (c) -0.50 V (vs reversible hydrogen electrode (RHE)) on the δ -Cu₂S and (d) -0.39 V vs. RHE on β -Cu₂S. The model consists of a $3 \times 3 \times 1$ supercell of δ -Cu₂S with 50 H₂O molecules, and β -Cu₂S with 28 H₂O molecules.