

## Multiferroic vanadium phosphide monolayer with ferromagnetic half-metallicity and topological Dirac states

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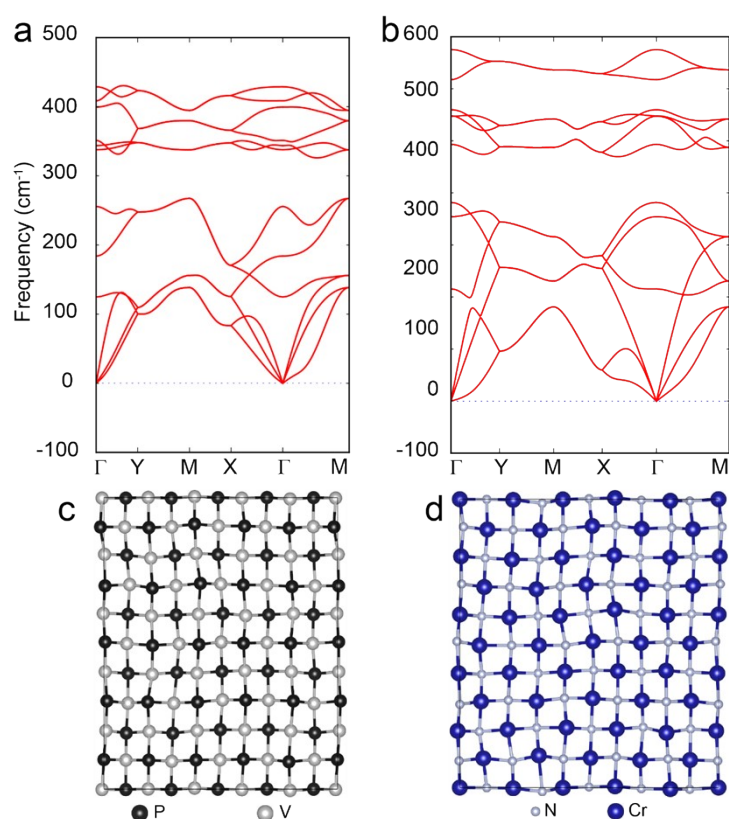


Figure S1. (a, b) Calculated phonon spectra of the t-VP and t-CrN monolayers. (c, d) Snapshots of the two monolayers at the end of 10 ps ab initio molecular dynamics simulations at 500 K.

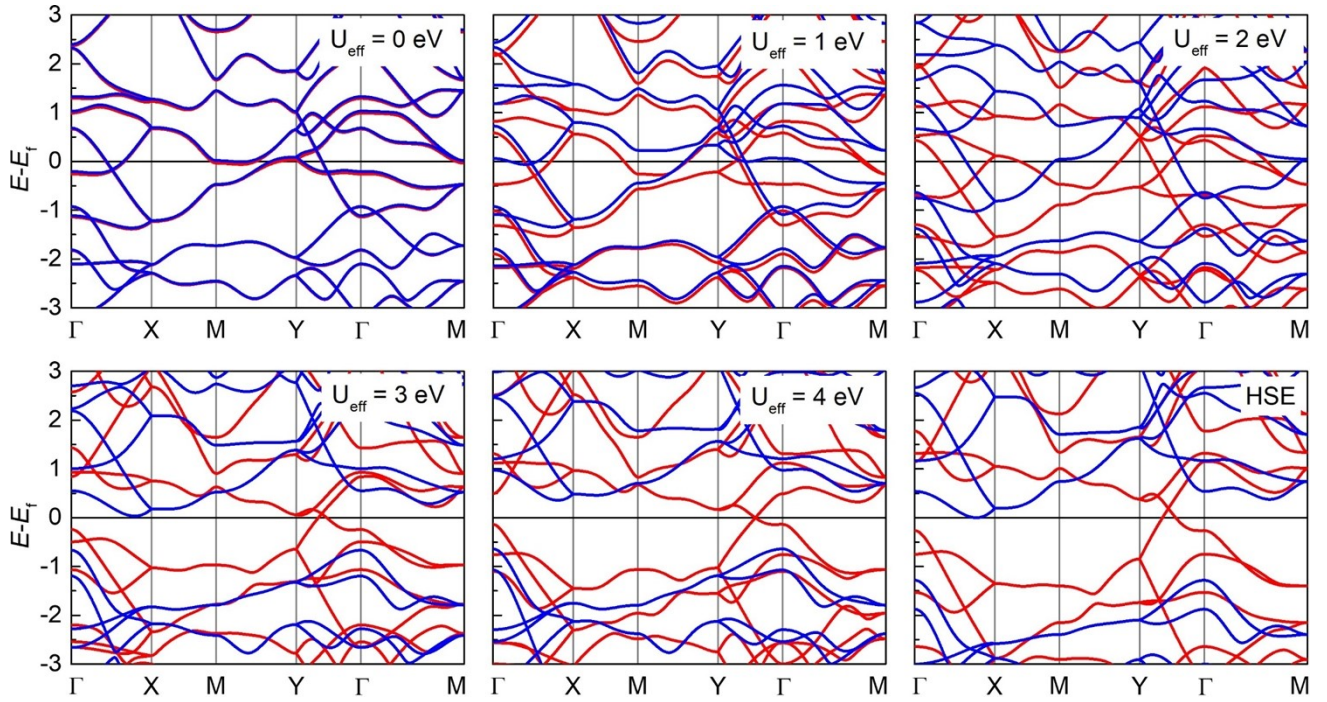


Figure S2. Band structures of the t-VP monolayer without the SOC calculated with the DFT+U method (the values of  $U_{\text{eff}}$  are provided) and HSE06 functional. The red and blue lines present the spin-up and spin-down band structures, respectively.

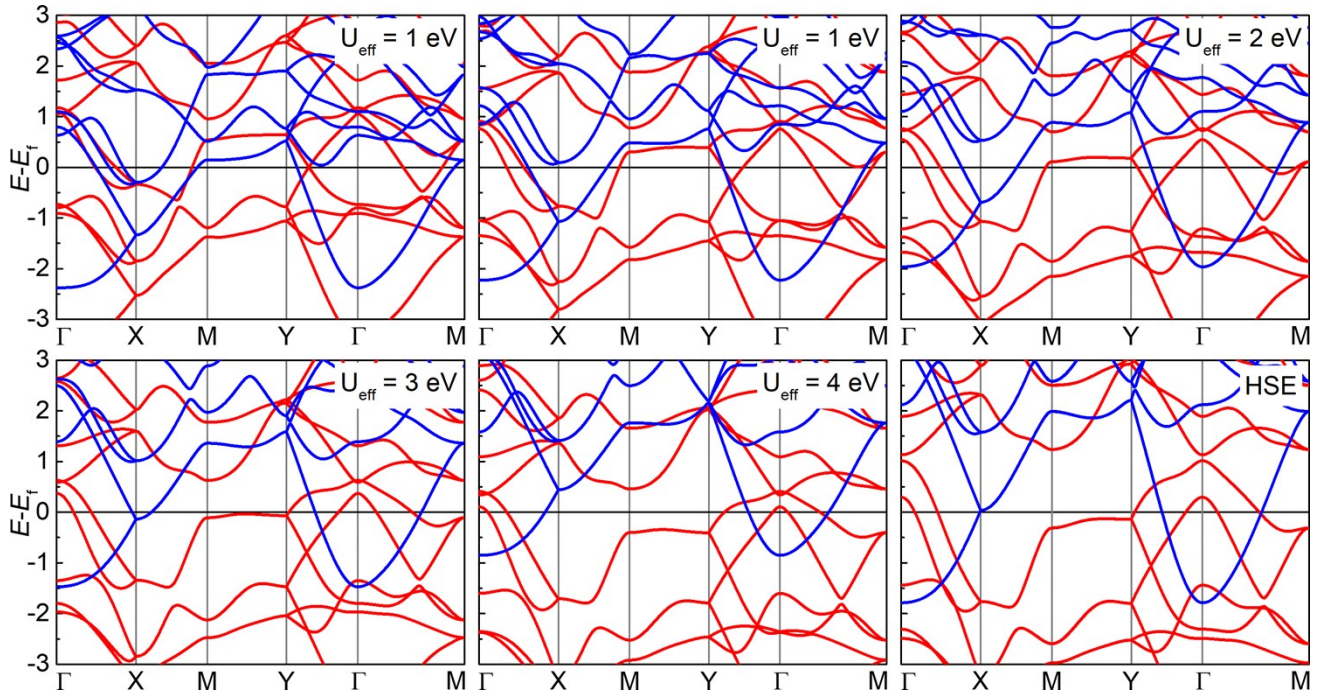


Figure S3. Band structures of the t-CrN monolayer without the SOC calculated with the DFT+U method (the values of  $U_{\text{eff}}$  are provided) and HSE06 functional. The red and blue lines present the spin-up and spin-down band structures, respectively.

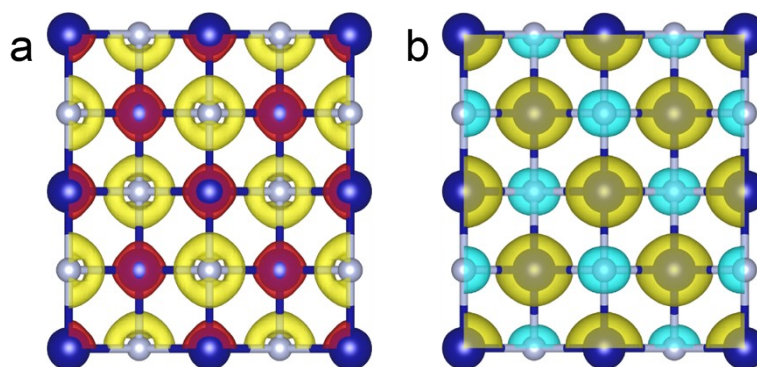


Figure S4. Isosurface plots of deformation electronic density (a,  $0.134 \text{ e}/\text{\AA}^3$ ) and spin polarization distribution (b,  $0.134 \text{ e}/\text{\AA}^3$ ) of the t-CrN monolayer. Bader charge analysis shows that a charge transfer of  $0.60 \text{ e}$  from each Cr atom to N atom (from deep red to yellow). The transferred electrons in the t-CrN monolayer are mainly from  $3 d_{xz,yz}$  orbitals of Cr atoms and delocalize around N atoms in  $3 p_{x,y}$  orbitals.

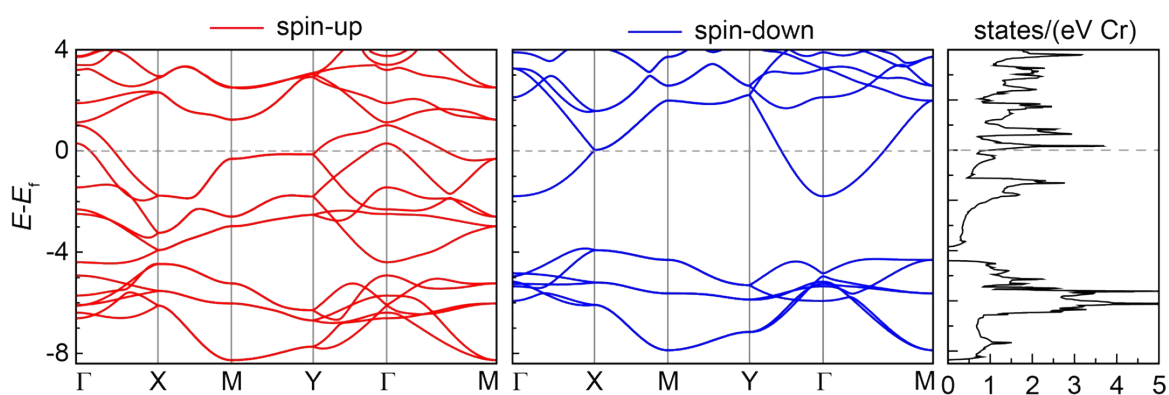


Figure S5. Spin-polarized band structures and density of states of the t-CrN monolayer in its non-magnetic state, calculated with the HSE06 functional.