Supporting Information

Magnetic Order-dependent phonon properties in 2D Magnet CrI₃

Ke Wang¹, WuXing Zhou², Yuan Cheng³, Min Zhang¹, Hai Wang^{1*}, and Gang Zhang^{4*}

1. Xidian University, No. 2 Taibai Road, Xi'an, Shaanxi Province 710071, China

2. Hunan Provincial Key Laboratory of Advanced Materials for New Energy Storage and Conversion,

Hunan University of Science and Technology, Xiangtan 411201, China

3. Monash Suzhou Research Institute, Suzhou 215123, P. R. China

4. Institute of High Performance Computing, A*STAR, 138632, Singapore

*Corresponding authors. Email: <u>wanghai@mail.xidian.edu.cn (H.W.)</u>; <u>zhangg@ihpc.a-star.edu.sg</u>

<u>(G.Z.)</u>



Figure S1. Optimization of lattice constant of CrI_3 monolayer with FM (a), AFM (b), and PM (c) phases.

| | FM | | | AFM | | | PM | |
|-------|--------------------|-------|-------|--------------------|--------|-------|--------------------|--------|
| mode | Frequency (THz) | γ | mode | Frequency (THz) | γ | mode | Frequency (THz) | γ |
| 1,2 | 1.371 | 0.943 | 1,2 | 1.364 | 0.767 | 1,2 | 1.275 | -0.535 |
| 3 | 1.535 | 1.894 | 3 | 1.544 | 1.838 | 3 | 1.607 | 1.179 |
| 4 | 2.017 | 1.624 | 4 | 2.0187 | 1.573 | 4 | 2.175 | 1.536 |
| 5,6 | 2.119 | 0.644 | 5,6 | 2.200 | 0.706 | 5,6 | 2.537 | 0.580 |
| 7 | 2.521 | 0.856 | 7 | 2.554 | 0.843 | 7,8 | 2.810 | -1.836 |
| 8,9 | 2.876 | 0.672 | 8,9 | 2.810 | -0.242 | 9 | 2.862 | 0.0903 |
| 10,11 | 2.963 | 0.165 | 10,11 | 2.970 | 0.318 | 10,11 | 3.098 | 0.842 |
| 12,13 | 3.076 | 0.867 | 12,13 | 3.118 | 1.096 | 12,13 | 3.340 | -0.117 |
| 14 | 3.569 | 0.540 | 14 | 3.494 | 0.173 | 14 | 3.781 | -0.311 |
| 15 | 3.591 | 0.622 | 15 | 3.609 | 0.851 | 15 | 4.118 | 0.794 |
| 16 | 5.855 | 0.720 | 16 | 5.967 | 0.484 | 16 | 4.729 | 2.253 |
| 17,18 | 6.151 | 0.825 | 17,18 | 6.256 | 0.756 | 17,18 | 6.215 | -0.526 |
| 19,20 | 6.598 | 0.681 | 19,20 | 6.557 | 0.352 | 19,20 | 6.412 | 0.500 |
| 21 | 7.314 | 0.675 | 21 | 7.247 | 0.664 | 21 | 6.788 | 0.082 |

Table S1. Frequencies and Grüneisen constants of 21 optical modes at Γ point.



Figure S2. The ferromagnetic (FM) (a) and antiferromagnetic (AFM) (b) configurations for CrI_3 monolayer. The spin up and spin down are represented by the red and green arrows, respectively.





Figure S3. Interatomic force constants for CrI_3 with FM phase (a), the differences between the interatomic force constants of AFM and FM (AFM-FM) phases (b) and between PM and FM (PM-FM) phases (c).



Figure S4. Group velocities of longitudinal acoustic (LA), transverse acoustic (TA) and out-of-plane acoustic (ZA) branches for CrI₃ monolayer with FM (a), AFM (b) and PM (c) configurations.



Figure S5. Specific heat capacity of CrI₃ monolayer as a function of temperature for FM, AFM and PM phases, respectively.



Figure S6. Electron density of states (DOS) of CrI_3 monolayer with FM (a), AFM (b), and PM (c) phases.



Figure S7. Phonon dispersion for FM-CrI₃ when lattice constant *a* is 7.00 and 6.99 Å, respectively.