## **Supplementary Information**

## Discovery of intrinsic two-dimensional antiferromagnets from transition-metal borides

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**Fig. S1** Top view of eleven collinear magnetic configurations of a 2-D monolayer MBs. FM and AFM-i (i= 0, 1, 2, 3, 4, 5, 6, 7, 8, 9) respectively means ferromagnetic and antiferromagnetic state.  $J_1$ ,  $J_2$ ,  $J_3$ ,  $J_4$ , and  $J_5$  are nearest- (1<sup>st</sup>), second-nearest- (2<sup>nd</sup>), third-nearest- (3<sup>rd</sup>), fourth-nearest- (4<sup>th</sup>), and fifth-nearest-neighbor (5<sup>th</sup>) magnetic coupling parameters, respectively. The up-arrow and down-arrow respectively represent the spin-up and spin-down state.



**Fig. S2** (a) the plane along (001) direction. (b) calculated electron localization function ELF of 2-D MnB on (001) plane. The isosurface is set to 0.65 e/Å<sup>3</sup>. The blue and green balls are respectively Mn and B atoms.

The topological analysis of electron localization function ELF is a very useful tool

for the determination of chemical bonding type.<sup>S1</sup> The values of ELF vary between 0 and 1, in which 1 represents the completely localized character of electrons, while 0 stands for the delocalization of electrons. ELF = 0.5 is corresponding to the electron-gas like pair probability. According to the ELF results in Fig. S2, we can see that the ELF between B and B atoms in 2-D MnB is close to 1.0, indicating a strong covalent bonding character.



Fig. S3 Calculated phonon spectra of 2-D monolayer MBs using GGA-PBE.



Fig. S4 Snapshots of 2-D monolayer MBs after 5 ps AIMD simulations at 600 K.



Fig. S5 Simulated normalized |S| (black data) and specific heat  $C_V$  (blue data) as a function of temperature for monolayer  $CrI_3$ .

For monolayer CrI<sub>3</sub>, the energy difference between FM and AFM state per unit-cell is 58.0 meV. The J is obtained by  $(E_{AFM}-EFM)/6S^2$ , where S is the spin vector of each Cr atom. Using the normalized |S|=1, J is 9.6 meV, which agrees with the value of 9.1 meV in same approach<sup>S2</sup>. The Curie temperature is about 50 K in Fig. S5.



**Fig. S6** Calculated band structure of 2-D (a) CrB, (b) MnB, and (c) FeB in their magnetic ground state by employing GGA+U ( $U_{eff}$  = 2.0 eV). The solid and dash lines respectively mean spin-up and spin-down channel. The contribution of DOS for each 2-D MB around the Fermi level are from transition-metal M atoms. Calculated band structure of 2-D (d) CrB, (e) MnB, and (f) FeB in their magnetic ground state by employing hybrid HSE06. The Fermi levels are set to zero. For the band structures of 2-D MnB and FeB, only the spin-up state is shown here. The figures (a), (b), and (c) are plotted by pymatgen.<sup>[S3]</sup>



**Fig. S7** Projected density of state (PDOS) of  $d_{xy}, d_{yz}, d_{z^2}, d_{xz}$ , and  $d_{x^2-y^2}$  of 2-D (a)

CrB, (b) MnB, (c) FeB using GGA+U. (U<sub>eff</sub> =2.0 eV). The Fermi levels are set to zero.



Fig. S8 Adsorption energies of different configurations of 2-D (a) CrBT and (b)

MnBT. T is O, OH, and F respectively.



Fig. S9 Calculated specific heat C<sub>V</sub> as functions of temperature T for 2-D (a) CrBO, (b)

CrBOH, and (c) CrBF. Calculated spin-spin correlations of 1st, 2nd, 3rd, 4th, and 5th neighboring magnetic atoms by Monte Carlo simulation at T=10 K for 2-D (d) CrBO, (e) CrBOH, and (f) CrBF.



**Fig. S10** Calculated specific heat  $C_V$  as functions of temperature T for 2-D (a) MnBO, (b) MnBOH, and (c) MnBF. Calculated spin-spin correlations of 1st, 2nd, 3rd, 4th, and 5th neighboring magnetic atoms by Monte Carlo simulation at T=10 K for 2-D (d) MnBO, (e) MnBOH, and (f) MnBF.



Fig. S11 Band structures and density of states (DOS) projected on each element for 2-D (a) FeBO, (b) FeBOH, and (c) FeBF, respectively both in most stable adsorption configuration and in magnetic ground state using GGA+U. The solid and dash line are respectively spin-up and spin-down state ( $U_{eff} = 2.0 \text{ eV}$ ). These figures are plotted by pymatgen.<sup>[S3]</sup>



Fig. S12 Band structures and density of states (DOS) projected on each element for 2-D (a) CrBO, (b) CrBOH, and (c) CrBF, respectively both in most stable adsorption configuration and in magnetic ground state using GGA+U. The solid and dash line are respectively spin-up and spin-down state ( $U_{eff} = 2.0 \text{ eV}$ ). These figures are plotted by pymatgen.<sup>[S3]</sup>



**Fig. S13** Band structures and density of states (DOS) projected on each element for 2-D (a) MnBO, (b) MnBOH, and (c) MnBF, respectively both in most stable adsorption configuration and in magnetic ground state using GGA+U. The solid and dash line are respectively spin-up and spin-down state ( $U_{eff} = 2.0 \text{ eV}$ ). These figures are plotted by pymatgen.<sup>[S3]</sup>

From Fig. S11, S12, and S13, it is found that most of functionalized 2-D MBT (M = Fe, Mn, Cr; T = O, OH, F) are metallic with the Fermi energy falling into a continuum of energy states. However, for FeBOH and CrBO, the functionalized MBT are semiconductors with a small band gap of 0.26 or 0.19 eV, respectively.

	by using m	SE00.				
2-D Pmma	а	b	11	$l_2$	h	М
ScB	3.342	3.108	2.421	2.478	2.720	0.16
TiB	3.178	2.965	2.284	2.300	2.396	0.52
VB	3.264	2.901	2.206	2.223	1.906	1.94
CrB	2.948	2.879	2.211	2.157	2.290	3.20
MnB	2.928	2.881	2.172	2.116	2.118	3.50
FeB	2.803	2.832	2.147	2.052	2.119	2.75
СоВ	2.644	2.911	2.102	2.034	2.156	1.59
NiB	2.584	2.917	2.170	2.053	2.393	0
YB	3.548	3.206	2.596	2.686	3.120	0.25
ZrB	3.291	3.089	2.434	2.481	2.825	0.12
NbB	3.208	3.001	2.351	2.356	2.573	0
MoB	3.052	3.045	2.274	2.252	2.338	0.68
TcB	3.019	3.015	2.295	2.196	2.250	1.29
RuB	2.911	2.971	2.298	2.177	2.425	1.05
RhB	2.761	2.976	2.345	2.192	2.724	0
PdB	2.919	2.996	2.362	2.246	2.678	0
HfB	3.242	3.068	2.404	2.441	2.765	0
TaB	3.183	2.969	2.353	2.339	2.593	0
WB	3.040	3.042	2.298	2.244	2.367	0.66
ReB	2.999	2.881	3.153	2.137	2.280	0
OsB	2.958	2.920	2.399	2.158	2.473	1
IrB	2.759	2.906	2.489	2.175	2.918	0
PtB	2.853	3.029	2.470	2.213	2.771	0
OsB IrB PtB	2.958 2.759 2.853	2.920 2.906 3.029	2.399 2.489 2.470	2.158 2.175 2.213	2.473 2.918 2.771	1 0 0

**Table S1.** a and b (in Å) are lattice constant.  $l_1$  and  $l_2$  (in Å) are bond length between M and B atom. h (in Å) is layer height. M (in  $\mu$ B/f.u.) is the total magnetic moment per formula unit by using HSE06

**Table S2.** Calculated elastic constants C (in GPa) of MBs, graphene,  $MoS_2$  and  $Ti_2C$  monolayers. The data from other calculations<sup>S4, S5, S6</sup> are listed in parentheses for comparison. The cohesive energies  $E_{coh}$  (in eV) of 2-D MBs were obtained by using GGA.

2-D	C <sub>11</sub>	C <sub>22</sub>	C <sub>44</sub>	C <sub>12</sub>	$E_{coh}$	
CrB	119.3	75.0	52.7	31.4	4.79	
MnB	118.0	82.1	47.2	27.1	4.83	
FeB	111.4	92.4	47.4	33.7	4.72	
CoB	80.9	48.1	53.8	42.4	5.50	
RuB	67.9	99.0	30.5	23.4	6.03	
Graphene	351.6 (352.7) <sup>4</sup>	351.6 (352.7)4	145.4 (145.9)4	60.9 (60.9) <sup>4</sup>	/	
$MoS_2$	131.1 (130)5	131.1 (130)5	49.3 (45)5	32.6 (40) <sup>5</sup>	/	
Ti <sub>2</sub> C	145.4 (137) <sup>6</sup>	145.4 (137)6	57.1 (53)6	31.2 (31.2)6	/	

Table S3.  $E_{FM}$  and  $E_{AFM-i}$  (in eV) are total energies of FM and AFM-i of 2-D MB (i=0,

1, 2, ...,9) by using GGA+U ( $U_{eff} = 2.0 \text{ eV}$ ) and HSE06.

GGA+U	$\mathrm{E}_{\mathrm{FM}}$	E <sub>AFM-0</sub>	E <sub>AFM-1</sub>	E <sub>AFM-2</sub>	E <sub>AFM-3</sub>	E <sub>AFM-4</sub>	E <sub>AFM-5</sub>	E <sub>AFM-6</sub>	E <sub>AFM-7</sub>	E <sub>AFM-8</sub>	E <sub>AFM-9</sub>
FeB	-100.770	-101.330	-101.360	-101.420	-101.190	-101.399	-101.820	-101.460	-101.460	-101.380	-100.970
MnB	-108.634	-108.144	-108.667	-108.455	-108.370	-108.563	-109.043	-108.715	-108.571	-108.130	-107.795
CrB	-109.780	-109.400	-109.070	-108.730	-108.770	-109.141	-108.58	-108.500	-109.050	-109.190	-107.840
HSE06	$E_{\text{FM}}$	E <sub>AFM-0</sub>	E <sub>AFM-1</sub>	E <sub>AFM-2</sub>	E <sub>AFM-3</sub>	E <sub>AFM-4</sub>	E <sub>AFM-5</sub>	E <sub>AFM-6</sub>	E <sub>AFM-7</sub>	E <sub>AFM-8</sub>	E <sub>AFM-9</sub>
FeB	-147.220	-148.340	-148.500	-148.550	-148.480	-148.436	-149.460	-148.670	-148.540	-149.060	-148.510
MnB	-159.655	-158.300	-159.484	-159.031	-159.084	-158.839	-160.174	-159.588	-159.153	-159.133	-158.498
CrB	-156.920	-156.870	-156.100	-155.500	-155.600	-156.279	-155.160	-155.100	-156.460	-155.940	-154.050

FeB	$E_{\text{FM}}$	E <sub>AFM-0</sub>	E <sub>AFM-1</sub>	E <sub>AFM-2</sub>	E <sub>AFM-3</sub>	E <sub>AFM-4</sub>	E <sub>AFM-5</sub>	E <sub>AFM-6</sub>	E <sub>AFM-7</sub>	E <sub>AFM-8</sub>	E <sub>AFM-9</sub>
U <sub>eff</sub> =1	-108.020	-108.230	-108.210	-108.240	-107.940	-108.192	-108.670	-108.190	-108.190	-107.830	-107.630
U <sub>eff</sub> =2	-100.770	-101.330	-101.360	-101.420	-101.190	-101.399	-101.820	-101.460	-101.460	-101.380	-100.970
U <sub>eff</sub> =3	-94.558	-95.201	-95.207	-95.082	-95.256	-95.2687	-95.635	-95.071	-95.363	-95.602	-95.238
U <sub>eff</sub> =4	-88.749	-89.748	-89.711	-89.326	-89.645	-89.8401	-89.974	-89.606	-90.055	-90.381	-90.147
U <sub>eff</sub> =5	-83.776	-84.887	-84.871	-84.554	-84.969	-85.0853	-84.888	-84.838	-84.876	-85.634	-85.546
MnB	$E_{FM}$	E <sub>AFM-0</sub>	E <sub>AFM-1</sub>	E <sub>AFM-2</sub>	E <sub>AFM-3</sub>	E <sub>AFM-4</sub>	E <sub>AFM-5</sub>	E <sub>AFM-6</sub>	E <sub>AFM-7</sub>	E <sub>AFM-8</sub>	E <sub>AFM-9</sub>
U <sub>eff</sub> =1	-114.960	-114.636	-114.792	-114.778	-114.570	-114.945	-114.937	-114.750	-114.754	-114.147	-113.949
U <sub>eff</sub> =2	-108.634	-108.144	-108.667	-108.455	-108.370	-108.563	-109.043	-108.715	-108.571	-108.130	-107.795
U <sub>eff</sub> =3	-103.126	-102.382	-102.210	-102.835	-102.862	-102.828	-103.740	-103.294	-103.088	-102.827	-102.332
U <sub>eff</sub> =4	-98.223	-97.226	-98.297	-97.804	-97.942	-97.709	-98.940	-98.386	-98.169	-98.090	-97.452
U <sub>eff</sub> =5	-93.841	-92.634	-93.848	-93.268	-93.510	-93.155	-94.583	-93.935	-93.702	-93.823	-93.078
CrB	$E_{\text{FM}}$	E <sub>AFM-0</sub>	E <sub>AFM-1</sub>	E <sub>AFM-2</sub>	E <sub>AFM-3</sub>	E <sub>AFM-4</sub>	E <sub>AFM-5</sub>	E <sub>AFM-6</sub>	E <sub>AFM-7</sub>	E <sub>AFM-8</sub>	E <sub>AFM-9</sub>
U <sub>eff</sub> =1	-116.530	-116.000	-115.730	-115.490	-115.690	-115.698	-115.460	-115.490	-115.620	-115.930	-115.150
U <sub>eff</sub> =2	-109.780	-109.400	-109.070	-108.730	-108.770	-109.141	-108.580	-108.500	-109.050	-109.190	-107.840
U <sub>eff</sub> =3	-103.850	-103.670	-103.200	-102.710	-102.740	-103.365	-102.380	-102.370	-103.470	-103.230	-101.320
U <sub>eff</sub> =4	-98.518	-98.590	-97.953	-97.380	-97.492	-98.247	-96.921	-97.103	-98.455	-97.946	-95.600
U <sub>eff</sub> =5	-93.628	-94.028	-93.234	-92.652	-92.800	-93.6865	-91.971	-92.455	-93.936	-93.212	-90.820

Table S4.  $E_{FM}$  and  $E_{AFMi}(\text{in eV})$  are total energies of FM and AFM-i by using different

 $U_{eff}$  values for MnB, FeB, and CrB monolayers (i=0, 1, 2, ..., 9).

Table S5. Calculated magnetic couple constants of  $J_1$ ,  $J_2$ ,  $J_3$ ,  $J_4$ ,  $J_5$  (in meV) and the

 $T_{c} \\$ 

320

300

440

2-D	Ground state	$\mathbf{J}_1$	$J_2$	<b>J</b> <sub>3</sub>	$J_4$	$J_5$	
FeB	AFM-5	8.7	-10.0	-14.3	-21.9	-3.7	
MnB	AFM-5	53.0	-2.6	-16.5	-12.4	5.7	
CrB	FM	42.5	-21.5	52.4	-2.7	14.6	

critical temperature of T by using GGA+U.

To obtain the strength of magnetic coupling of monolayer MB based on 2-D Heisenberg model, the energy in FM and collinear AFM-i (i=0, 1, ..., 9) states were used to compute  $J_1$ ,  $J_2$ ,  $J_3$ ,  $J_4$ , and  $J_5$  using least-squares method. The equation (2) can be further written as:

$$\begin{split} E_{FM} &= E_0 - 8J_1 |S|^2 - 8J_2 |S|^2 - 8J_3 |S|^2 - 16J_4 |S|^2 - 16J_5 |S|^2 - A|S|^2 \\ E_{AFM-0} &= E_0 + 0J_1 |S|^2 + 8J_2 |S|^2 - 8J_3 |S|^2 + 0J_4 |S|^2 + 16J_5 |S|^2 - A|S|^2 \\ E_{AFM-1} &= E_0 + 0J_1 |S|^2 + 0J_2 |S|^2 + 0J_3 |S|^2 + 8J_4 |S|^2 + 0J_5 |S|^2 - A|S|^2 \\ E_{AFM-2} &= E_0 + 0J_1 |S|^2 + 0J_2 |S|^2 + 0J_3 |S|^2 + 0J_4 |S|^2 + 16J_5 |S|^2 - A|S|^2 \\ E_{AFM-3} &= E_0 + 4J_1 |S|^2 + 0J_2 |S|^2 + 0J_3 |S|^2 + 0J_4 |S|^2 + 0J_5 |S|^2 - A|S|^2 \\ E_{AFM-4} &= E_0 + 0J_1 |S|^2 + 8J_2 |S|^2 + 0J_3 |S|^2 + 0J_4 |S|^2 + 0J_5 |S|^2 - A|S|^2 \\ E_{AFM-5} &= E_0 - 8J_1 |S|^2 - 8J_2 |S|^2 + 8J_3 |S|^2 + 16J_4 |S|^2 + 16J_5 |S|^2 - A|S|^2 \\ E_{AFM-6} &= E_0 + 0J_1 |S|^2 + 8J_2 |S|^2 + 8J_3 |S|^2 + 0J_4 |S|^2 - 16J_5 |S|^2 - A|S|^2 \\ E_{AFM-7} &= E_0 + 0J_1 |S|^2 + 8J_2 |S|^2 + 8J_3 |S|^2 + 0J_4 |S|^2 - 16J_5 |S|^2 - A|S|^2 \\ E_{AFM-8} &= E_0 + 8J_1 |S|^2 - 8J_2 |S|^2 + 8J_3 |S|^2 + 16J_4 |S|^2 - 16J_5 |S|^2 - A|S|^2 \\ E_{AFM-8} &= E_0 + 8J_1 |S|^2 - 8J_2 |S|^2 + 8J_3 |S|^2 - 16J_4 |S|^2 - 16J_5 |S|^2 - A|S|^2 \\ E_{AFM-9} &= E_0 + 8J_1 |S|^2 - 8J_2 |S|^2 + 8J_3 |S|^2 - 16J_4 |S|^2 - 16J_5 |S|^2 - A|S|^2 \\ E_{AFM-9} &= E_0 + 8J_1 |S|^2 - 8J_2 |S|^2 + 8J_3 |S|^2 - 16J_4 |S|^2 - 16J_5 |S|^2 - A|S|^2 \\ E_{AFM-9} &= E_0 + 8J_1 |S|^2 - 8J_2 |S|^2 + 8J_3 |S|^2 - 16J_4 |S|^2 - 16J_5 |S|^2 - A|S|^2 \\ E_{AFM-9} &= E_0 + 8J_1 |S|^2 - 8J_2 |S|^2 + 8J_3 |S|^2 - 16J_4 |S|^2 - 16J_5 |S|^2 - A|S|^2 \\ E_{AFM-9} &= E_0 + 8J_1 |S|^2 - 8J_2 |S|^2 + 8J_3 |S|^2 - 16J_4 |S|^2 - 16J_5 |S|^2 - A|S|^2 \\ E_{AFM-9} &= E_0 + 8J_1 |S|^2 - 8J_2 |S|^2 + 8J_3 |S|^2 - 16J_4 |S|^2 - 16J_5 |S|^2 - A|S|^2 \\ E_{AFM-9} &= E_0 + 8J_1 |S|^2 - 8J_2 |S|^2 + 8J_3 |S|^2 - 16J_4 |S|^2 - 16J_5 |S|^2 - A|S|^2 \\ E_{AFM-9} &= E_0 + 8J_1 |S|^2 - 8J_2 |S|^2 + 8J_3 |S|^2 - 16J_4 |S|^2 - 16J_5 |S|^2 - A|S|^2 \\ E_{AFM-9} &= E_0 + 8J_1 |S|^2 - 8J_2 |S|^2 + 8J_3 |S|^2 - 16J_4 |S|^2 - 16J_5 |S|^2 - A|S|^2 \\ E_{AFM-9} &= E_0 + 8J_1 |S|^2 - 8J_2 |S|^2 + 8J_3 |S|^2 - 16J_4 |S|^2 - 16J_5 |S|^2 - A|S|^2 \\ E_{AFM-9} &= E_0 + 8J_1 |S|^2 - 8J_2 |S|^2 + 8J_3 |S|^2 - 16$$

where  $E_0$  is the energy of the nonmagnetic state,  $J_1$ ,  $J_2$ ,  $J_3$ ,  $J_4$ , and  $J_5$  are the 1<sup>st</sup>, 2<sup>nd</sup>, 3<sup>rd</sup>, 4<sup>th</sup>, and 5<sup>th</sup> neighbor exchange coupling parameters, respectively. *A* is anisotropy energy parameter, which is obtained by using the magnetic anisotropy energy as:

$$A = \frac{E_{hard}(axis) - E_{easy}(axis)}{\left|S\right|^2}$$

**Table S6.** Magnetic anisotropy energy (MAE) is defined as the energy difference

 between the system with spin direction along the magnetic hard axis and the system

2-D	MAE	K <sub>1(a-c)</sub>	K <sub>2(a-c)</sub>	K <sub>1(b-c)</sub>	K <sub>2(b-c)</sub>	Easy axis
FeB	482.2	482.2	3.3	230.1	-0.1	с
MnB	222.7	222.7	-0.1	187.9	-0.3	c
CrB	23.6	20.2	-2.9	-6.5	0.04	b

with spin parallel to the magnetic easy axis.  $K_1$  and  $K_2$  are anisotropy constants.

**Table S7.**  $E_{FM}$  and  $E_{AFMi}$  (in eV) are total energies of FM and AFM-i of 2-D MBT (M= Fe, Mn, Cr; T= O, OH, F; i= 0, 1, 2, ...,9) by using the GGA+U (U<sub>eff</sub> = 2.0 eV). The slash means that the AFM configuration could not be retained and turns out to be nonmagnetic configuration after DFT calculations.

MBT	$\mathrm{E}_{\mathrm{FM}}$	E <sub>AFM-0</sub>	E <sub>AFM-1</sub>	E <sub>AFM-2</sub>	E <sub>AFM-3</sub>	E <sub>AFM-4</sub>	E <sub>AFM-5</sub>	E <sub>AFM-6</sub>	E <sub>AFM-7</sub>	E <sub>AFM-8</sub>	E <sub>AFM-9</sub>
FeBO	-160.997	-158.882	-159.697	/	-158.858	-159.498	-161.605	-159.860	-159.615	-157.854	-158.296
FeBOH	-186.145	-184.189	/	/	-185.729	/	-186.020	-185.917	-185.424	-185.782	-187.076
FeBF	-138.292	-138.043	-138.368	-138.649	-138.333	-138.460	-139.036	-138.912	-138.722	-137.449	-139.173
MnBO	-173.38	-172.45	-172.35	-172.68	-172.12	-172.35	-173.50	-172.42	-171.96	-171.39	-172.37
MnBOH	-196.16	-195.56	-195.71	-195.92	-195.84	-195.41	-196.16	-195.52	-195.15	-196.09	-196.32
MnBF	-150.59	-149.94	-149.94	-150.17	-150.06	-149.76	-150.31	-149.68	-149.3	-150.23	-150.37
CrBO	-174.061	-173.987	-174.448	/	-174.194	-174.315	-173.822	-174.103	-174.942	-175.056	-172.775
CrBOH	-199.573	-199.182	-199.028	/	-198.876	-199.323	-198.552	-198.929	-199.128	-198.430	-197.985
CrBF	-152.141	-151.772	-151.515	/	-151.338	-151.954	-151.042	-151.459	-151.880	-150.849	-150.334

**Table S8.** Magnetic couple constants  $J_1$ ,  $J_2$ ,  $J_3$ ,  $J_4$ ,  $J_5$  (in meV), magnetic anisotropyenergy MAE ( $\mu$ eV/atom), magnetic easy axis, and critical temperature  $T_c$  (in K) of 2-D

MBT	$J_1$	J <sub>2</sub>	J <sub>3</sub>	$J_4$	J <sub>5</sub>	MAE	Ground state	Magnetic easy axis	T <sub>c</sub>
FeBO	199.9	21.6	-39.3	-3.6	3.3	80.6	AFM-5	с	910
FeBOH	-21.7	75.9	-40.6	22.2	2.4	568.4	AFM-9	c	930
FeBF	22.5	4.8	-59.1	15.0	-9.3	720.6	AFM-9	с	420
MnBO	96.6	25.3	-1.0	13.4	-16.1	128.3	AFM-5	b	370
MnBOH	-3.8	50.8	12.7	3.8	-8.9	184.4	AFM-9	а	280
MnBF	8.1	44.4	25.3	6.7	-9.5	285.5	FM	с	330
CrBO	1.3	-30.5	9.5	-32.0	34.6	214.6	AFM-8	а	560
CrBOH	51.7	-36.9	21.6	8.1	11.1	37.3	FM	а	280
CrBF	61.4	-49.2	19.5	8.6	14.7	67.2	FM	а	250

MBT by employing GGA+U ( $U_{eff} = 2.0 \text{ eV}$ ).

The code for calculating J by using least-square method is as follow. Here, we take 2-D MnBO as an example.

Y= [-173.3776239 -172.4498714 -172.3529803 -172.683568 -172.1228168 -172.3525338 -173.4971323 -172.4150622 -171.9597934 -171.3890329 -

172.3670717]';

X= [1 -8 -8 -8 -16 -16;1 0 8 -8 0 16;1 0 0 0 8 0;1 0 0 0 0 16;1 4 0 0 0 0;1 0 8 0 0 0;1 -8 -8 8 16 16;1 0 0 8 0 0;1 0 8 8 0 -16; 1 8 -8 -8 16 -16;1 8 -8 8 -16 16];

 $B1_3 = pinv(X'*X)*X'*Y;$ 

 $B2_3 = (X'*X)^{-1}X'*Y;$ 

 $B3_3 = [B1_3 B2_3]$ 

$$Yp = X*B2_3;$$

err = [abs(Y-Yp)./Y]'

Ym = mean(Y);

 $SStot = sum((Y-Ym).^2);$ 

 $SSreg = sum((Yp-Ym).^2);$ 

 $SSres = sum((Yp-Y).^2);$ 

R2 = 1-SSres/SStot

plot(Yp,Y,'o');

hold on

plot([min(Yp) max(Yp)],[min(Yp) max(Yp)])

hold off

The calculated results are as follow.



Therefore, the values of  $J_1$ ,  $J_2$ ,  $J_3$ ,  $J_4$ , and  $J_5$  of MnBO are respectively 96.6 meV, 25.3 meV, -1.0 meV, 13.4 meV, and -16.1 meV.

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