## **Electronic Supplementary Information**

## Switching interlayer magnetic order in bilayer CrI<sub>3</sub> by stacking reversal

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Stacking	R3	<i>R</i> 3−r	C2/m	C2/m-r	AA	AA-r
FM	3.44	4.01	3.49	3.48	3.60	4.10
AFM	3.46	4.00	3.48	3.49	3.59	4.06

Table S1. The averaged interlayer distance with the unit of Å in bilayer  $CrI_3$  at different stacking patterns. The values are from the structures relaxed by Liechtenstein's DFT+U approach with  $U=3.9\,\mathrm{eV}$  and  $J=1.1\,\mathrm{eV}$ . The difference of the interlayer distance between the FM and AFM order for each stacking is small. The difference of the interlayer distance between C2/m and C2/m-r is also small. However, it is not the case for stacking patterns of  $R\bar{3}$  and AA: the interlayer distance of  $R\bar{3}$ -r is about 0.54~0.57 Å larger than that of  $R\bar{3}$ ; the interlayer distance of AA-r is about 0.47~0.50 Å larger than that of AA. From the side views of Figure 1 in the main text, we can observe that in  $R\bar{3}$ -r and AA-r stackings, the I atom in the bottom sublayer of the top  $CrI_3$  layer (I2b) sits almost directly above I1t, the I atom in the top sublayer of the bottom  $CrI_3$  layer. Therefore, the orbitals from I2b and I1t atoms in these two stackings tend to repel each other, and push the top and bottom  $CrI_3$  layers farther away, compared to their non-rotated stacking counterparts. This explains their larger interlayer distances (above 4.00 Å), and why their total energies are notably higher in comparison with the corresponding non-rotated stacking patterns  $R\bar{3}$  and AA (Figure 2 in the main text). In contrast, for C2/m-r stacking, the rotation does not lead to I2b over I1t, and thus the interlayer distance barely changes compared to the non-rotated C2/m stacking, which explains why C2/m-r and C2/m share similar total energies.

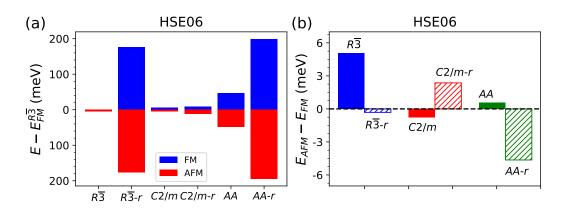


Figure S1. (a) The total energy of bilayer  $CrI_3$  by hybrid functional (HSE06) calculations in all six stacking patterns ( $R\bar{3}$ ,  $R\bar{3}$ -r, C2/m, C2/m-r, AA, and AA-r) with interlayer FM or AFM order.  $R\bar{3}$  stacking with the FM order has the lowest energy and thus was used as the zero energy reference. (b) The energy differences between AFM and FM bilayer  $CrI_3$  at different stacking orders computed by the HSE06 method. The HSE06 results without use of any U and J parameters are similar to those of Liechtenstein's DFT+U approach with U=3.9 eV and J=1.1 eV. This confirms that the  $180^\circ$  stacking rotation can switch the magnetic ground state for all three stacking orders.