

Supplementary information

**Designing Ru-doped Zn₃V₃O₈ Bifunctional OER and HER
Catalyst Through a Unified Computational and Experimental
Approach**

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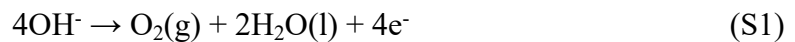
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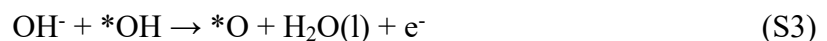
Theoretical Section

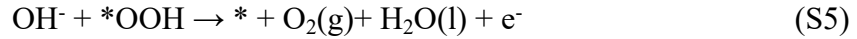
Spin-polarized density functional theory (DFT) calculations were carried out with the Vienna ab initio Simulation Package (VASP)^{1,2} which uses the projector augmented wave (PAW) pseudo-potentials³. For the exchange-correlation functional we used the Perdew-Burke-Ernzerhof (PBE)⁴ within the generalized gradient approximation (GGA). As spinel ferrites are strongly correlated systems, static electronic correlations were taken into account within the GGA+U method⁵, where a U value of 3.25 eV was employed for V⁶. The cutoff energy of 500 eV was adopted. Based on the previous work, Zn₃V₃O₈ can be obtained by partially substituting V atoms by Zn atoms in ZnV₂O₄. The crystallographic data of ZnV₂O₄ can be found in crystallography open database (COD, reference no. 9012331). The [001]-oriented surfaces were simulated using slabs with 4 atomic layers and lattice vectors of $\mathbf{a}_1 = \mathbf{a} + \mathbf{b}$ and $\mathbf{b}_1 = -\mathbf{a} + \mathbf{b}$ (\mathbf{a} , \mathbf{b} are the primitive vectors) for all simulations. A vacuum thickness of 12 Å was inserted to minimize the artificial interactions among the supercell images. All the atomic structures were fully relaxed until the forces on each atom being less than 0.02 eV/Å and the energy variation between two iterations being less than 1×10^{-5} eV. During the structural relaxation, the bottom layer metal atoms were constrained to mimic the structure of a semi-infinite solid. The Brillouin zone of each slab was sampled by a Monkhorst-Pack k-point mesh of $4 \times 4 \times 1$ for geometry optimization and an $8 \times 8 \times 1$ k-mesh for density of states (DOS) calculations, respectively. The Grimme's semiempirical DFT-D3 scheme of the dispersion correction was adopted to describe the van der Waals (vdW) interactions.

Water splitting is considered as two half reactions: OER and HER. Usually, the overall OER reaction is the four-electron reaction pathway.



A widely used approach to model OER considers the formation of four reaction intermediates on the surface:





where * represents the catalyst surface and *OOH, *O and *OH species are oxygenated intermediates. The reaction free energy of each step can be calculated by

$$\Delta G = \Delta E_{\text{DFT}} + \Delta ZPE - T\Delta S - eU \quad (\text{S6})$$

where ΔE_{DFT} , ΔZPE and ΔS are the energy changes in the DFT total energy, zero-point energy and entropy from the initial state to the final state, respectively. ZPE is obtained from vibrational frequency calculation. As for H₂O and H₂ molecules, their entropy values are taken from the NIST-JANAF thermodynamics table⁷. For each adsorbate, their entropy values are computed based on (ZPE - TS) taken from VASPKIT⁸ and ZPE. The theoretical overpotential η is determined by the potential limiting step:

$$\eta = \Delta G_{\text{max}}/e - U_0 \quad (\text{S7})$$

In order to establish trends in reactivity, the overpotential is often related to binding energy differences. The binding energy of the intermediate species to the surface are defined as:

$$\Delta G_{* \text{O}} = E_{* \text{O}} - E^* - E_{\text{H}_2\text{O}} + E_{\text{H}_2} + \Delta ZPE - T\Delta S \quad (\text{S8})$$

$$\Delta G_{* \text{OH}} = E_{* \text{OH}} - E^* - E_{\text{H}_2\text{O}} + (1/2)E_{\text{H}_2} + \Delta ZPE - T\Delta S \quad (\text{S9})$$

$$\Delta G_{* \text{OOH}} = E_{* \text{OOH}} - E^* - 2E_{\text{H}_2\text{O}} + (3/2)E_{\text{H}_2} + \Delta ZPE - T\Delta S \quad (\text{S10})$$

where E^* , $E_{* \text{O}}$, $E_{* \text{OH}}$ and $E_{* \text{OOH}}$ are the DFT total energies of a clean catalyst surface and that absorbed by a O, OH and OOH species, respectively; $E_{\text{H}_2\text{O}}$ and E_{H_2} are the energies of a H₂O and H₂ molecule in a vacuum, respectively.

For HER, the overall reaction is



A widely used approach to model HER considers the formation of the following reaction intermediate on the surface.



The calculated reaction free energy ($\Delta G_{* \text{H}}$) under electrode potential $U = 0$ V can be calculated by:

$$\Delta G_{*H} = E_{*H} - E^* - (1/2)E_{H_2} + \Delta ZPE - T\Delta S \quad (S13)$$

The optimal value for HER is $\Delta G_{*H} = 0$, which means that the smaller the $|\Delta G_{*H}|$, the better HER performance the material.

Experimental Section

Preparation of the precursors: 200 mg V_2O_5 , 300 mg $Zn(NO_3)_2 \cdot 6H_2O$, 280 mg hexamethylenetetramine, and 500 mg sodium sulfate were dissolved in 35 mL distilled water under vigorous stirring for 30 min. The obtained mixture was transferred into 50 mL Teflon-lined stainless steel autoclave which was sealed and treated at 110 °C for 24 h in oven. The obtained sample on the bottom of autoclave was ZnV-LDHs precursor. Similarly, ZnVRu-LDHs was prepared based on the same procedure except for the extra 10 mg $RuCl_3 \cdot 3H_2O$. Then, all the precursors were washed with deionized water and pure ethanol thoroughly, followed by drying overnight in a vacuum oven at 60 °C.

Fabricating hierarchical porous undoped and Ru-doped $Zn_3V_3O_8$: The precursors were put in the middle of the quartz boat which was put in a horizontal quartz tube furnace. A programmed heating process was adopted in the quartz tube furnace under Ar/ H_2 (Ar=40 SCCM; H_2 =10 SCCM) atmosphere (Detailedly, 25 °C to 500 °C with a rate of 5 °C min^{-1} , and then from 500 °C to 600 °C with a rate of 1°C min^{-1} , finally held at 600 °C for 120 min). After dissolving ZnO in 0.1 M NaOH solution, the undoped and Ru-doped $Zn_3V_3O_8$ were collected by centrifugation using deionized water.

Characterizations: Scanning electron microscope (FESEM, JSM-7800F), transmission electron microscopy (TEM, Philips, Tecnai, F30) coupled with energy-dispersive X-ray spectrometry (EDS) analyser and high-angle annular dark-file scanning trans-mission electron microscopy (HAADF-STEM) images were collected on JEOL JEMARM200F microscope incorporated with a spherical aberration correction system for STEM; X-ray photoelectron spectroscopy (XPS, PHI 5000 Versaprobe) and powder X-ray diffraction (XRD, Bruker D8 Advance X-ray

diffractometer with Cu K α radiation) were adopted to characterize the as-prepared samples.

Electrochemical OER and HER tests: The as-synthesized samples were dispersed into a mixed solution of 10 vol.% Nafion (0.5 wt.%) and 90 vol.% ethanol to form a homogeneous slurry which was evenly painted on carbon fiber paper with a catalyst loading of 2 mg cm⁻² as a working electrode. Saturated calomel electrode (SCE), and graphite rod worked as the reference and counter electrodes, respectively. The three electrode cell with 1.0 M KOH electrolyte was tested on a CHI 660D electrochemical work station (CH Instruments, Inc., Shanghai). The potential values were changed to E (vs. RHE) from E (vs. SCE) according to the formula: $E_{\text{RHE}} = E_{\text{SCE}} + 0.059\text{pH} + E_{\text{SCE}}^0$; the overpotential (η) for OER was calculated according to the following formula: η (V) = $E_{\text{RHE}} - 1.23$ V.

Figures

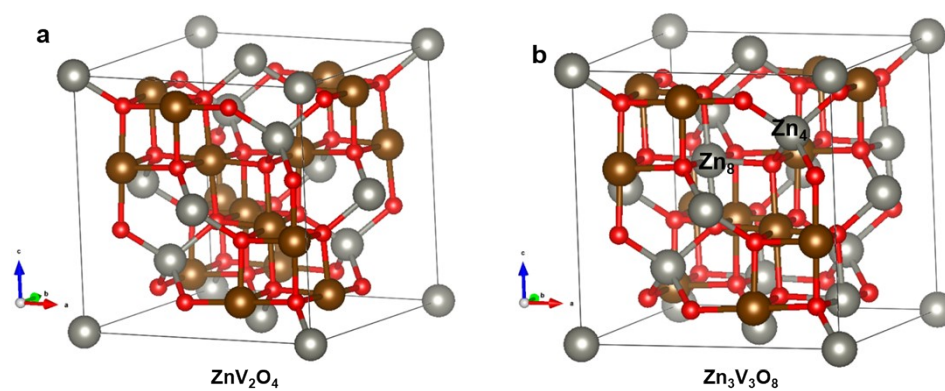


Fig. S1 Structures of ZnV_2O_4 (a) and $\text{Zn}_3\text{V}_3\text{O}_8$ (b). Brown, grey and red balls represent the V, Zn and O atoms, respectively. Meanwhile, Zn atom at a tetrahedral site and a octahedral site are labeled as Zn_4 and Zn_8 , respectively.

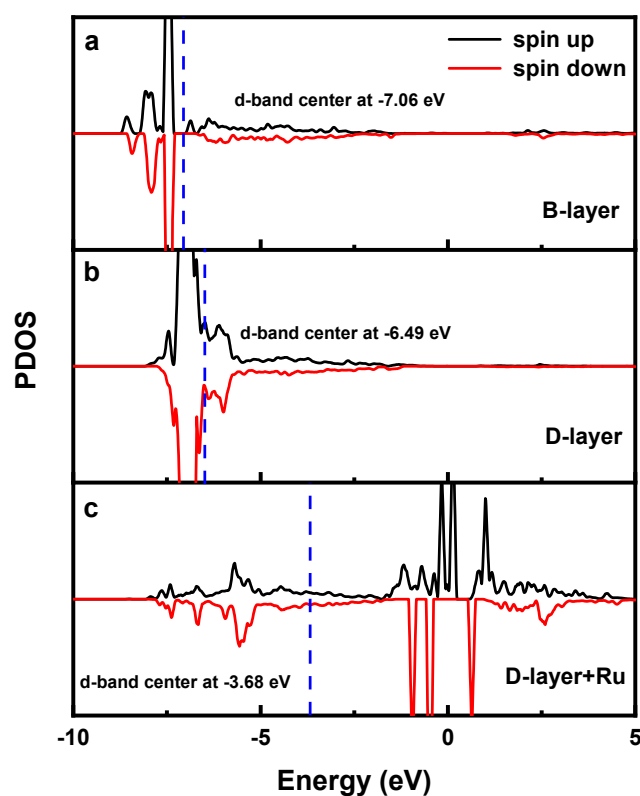


Fig. S2 Projected DOS from d-orbital of Zn_4 at B-layer (a), Zn_4 at D-layer (b) and Ru at Ru-doped D-layer (c).

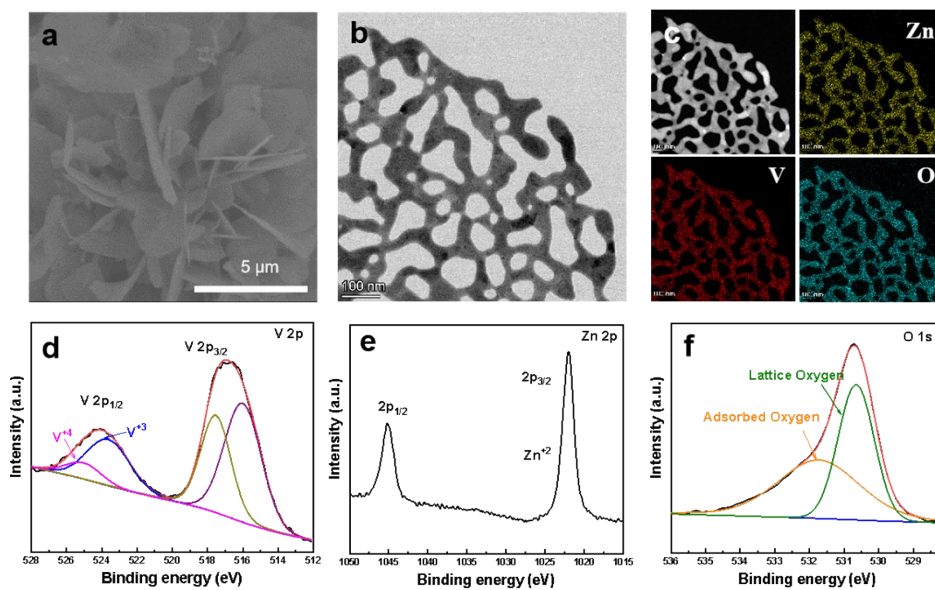


Fig. S3 SEM (a) and TEM (b) and the corresponding elemental mappings (c) of the undoped $\text{Zn}_3\text{V}_3\text{O}_8$ sample. XPS spectra of V 2p (d), Zn 2p (e) and O 1s (f) of the undoped $\text{Zn}_3\text{V}_3\text{O}_8$.

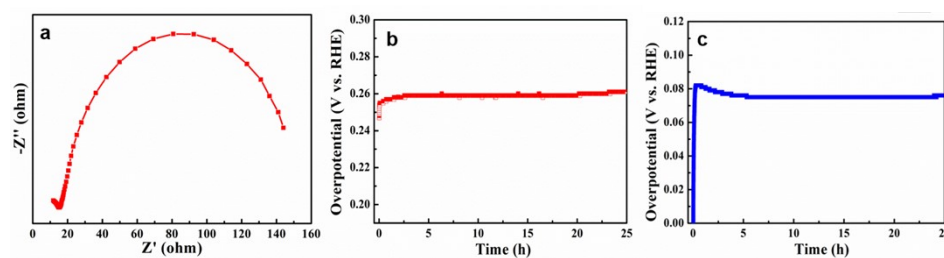


Fig. S4 (a) EIS of Ru-doped $\text{Zn}_3\text{V}_3\text{O}_8$ in 1.0 M KOH; (b) OER durability test for Ru-doped $\text{Zn}_3\text{V}_3\text{O}_8$ at the current density of 10 mA cm^{-2} ; (c) HER durability test for Ru-doped $\text{Zn}_3\text{V}_3\text{O}_8$ at the current density of 10 mA cm^{-2} .

Tables

Table S1 Surface energies (E_{surf}) of four terminations. E_{surf} is calculated by the formula:

$E_{surf} = \frac{E_{slab} - N \times E_{bulk}}{2A}$, where E_{slab} and E_{bulk} are energies of each termination and $Zn_3V_3O_8$ bulk, respectively.

	A-layer	B-layer	C-layer	D-layer
E_{surf} (eV Å ⁻²)	0.103	0.084	0.106	0.086

Table S2 Reaction free energies of each step ($U = 0$) and overpotentials for the Ru-doped C-layer and D-layer terminations. The rate-limiting steps for each reaction site and the lowest overpotential are highlighted in bold font.

Reaction site		ΔG_1 (eV)	ΔG_2 (eV)	ΔG_3 (eV)	ΔG_4 (eV)	η (V)
C-layer+Ru (replace V)	Ru(V)	-0.12	0.37	2.66	2.01	1.43
	V(V)	0.36	0.63	2.56	1.37	1.33
C-layer+Ru (replace Zn ₈)	Ru(Zn ₈)	-0.11	0.51	2.37	2.15	1.14
	V(Zn ₈)	0.30	0.56	2.65	1.41	1.42
D-layer+Ru (replace V)	Ru(V)	0.15	0.64	2.18	1.95	0.95
	V(V)	0.25	0.73	2.44	1.50	1.21
	Zn ₄ (V)	0.33	2.48	0.85	1.26	1.25
D-layer+Ru (replace Zn ₄)	Ru(Zn ₄)	-0.20	0.41	2.46	2.25	1.23
	V(Zn ₄)	0.24	0.62	2.56	1.50	1.33
	Zn ₄ (Zn ₄)	0.08	2.51	0.73	1.60	1.28
D-layer+Ru (replace Zn ₈)	Ru(Zn ₈)	-0.15	0.93	2.02	2.12	0.89
	V(Zn ₈)	0.38	0.69	2.09	1.76	0.86
	Zn ₄ (Zn ₈)	-0.02	2.46	0.74	1.74	1.23

Table S3 Binding energies (E_{bind}) of Ru on B-layer and D-layer. E_{bind} is calculated by: $E_{bind} = E_{total} - E_{sub-Zn/V} - E_{Ru}/n$, where E_{total} , $E_{sub-Zn/V}$ and E_{Ru}/n are energies of Ru doped $Zn_3V_3O_8$, the termination except replacing Zn or V atom and a Ru atom in the bulk, respectively.

	B-layer		D-layer		
	Ru(V)	Ru(Zn ₄)	Ru(V)	Ru(Zn ₄)	Ru(Zn ₈)
E_{bind} (eV)	0.254	3.451	0.580	3.261	0.905

Table S4 Free energies of H adsorption for different reaction sites at the Ru-doped A-layer and B-layer terminations. The small $|\Delta G_{*H}|$ is highlighted in bold font.

Reaction site		ΔG_{*H} (eV)
A-layer+Ru (replace V)	Ru(V)	0.04
	V(V)	1.09
B-layer+Ru (replace V)	Ru(V)	0.50
	V(V)	1.41
	Zn ₄ (V)	0.47
B-layer+Ru (replace Zn ₄)	Ru(Zn ₄)	-0.60
	V(Zn ₄)	1.45
	Zn ₄ (Zn ₄)	0.27
C-layer+Ru (replace V)	Ru(V)	-0.19
	V(V)	1.00
	Zn ₈ (V)	1.34
C-layer+Ru (replace Zn ₈)	Ru(Zn ₈)	-0.23
	V(Zn ₈)	0.70
	Zn ₈ (Zn ₈)	1.04

Table S5 Zero-point energy (ZPE) and entropy correction (TS) at T = 298 K for relevant species.

Species	ZPE (eV)	TS (eV)
H ₂ O	0.56	0.67
H ₂	0.27	0.41
*OOH	0.35	0
*OH	0.31	0.01
*O	0.05	0
*H	0.19	0

Table S6 Comparison of OER catalytic performances.

Catalyst	Tafel slope (mV/dec)	Overpotential at 10 mA cm ⁻² (mV)	Reference
Ru/Zn ₃ V ₃ O ₈	81.9	250	This work
NiCo ₂ O ₄	90	460	<i>J. Mater. Chem. A</i> , 2014, 2 , 20823-20831
Au/NiCo ₂ O ₄	63	360	<i>ChemCatChem</i> , 2014, 6 , 2501- 2506
IrNiO _x	/	320	<i>Angew. Chem. Int. Ed.</i> , 2015, 54 , 2975-2979.
NiC/C	46	316	<i>Adv. Mater.</i> , 2016, 28 , 3326
Zn _x Co _{3-x} O _x	51	320	<i>Chem. Mater.</i> , 2014, 26 , 1889- 1895
NiCoP/C	96	330	<i>Angew. Chem. Int. Ed.</i> , 2017, 129 , 3955-3958
Ni@graphene	66	370	<i>ACS Sustainable Chem. Eng.</i> , 2017, 5 , 4771-4777
VOOH	68	270	<i>Angew. Chem. Int. Ed.</i> , 2017, 56 , 573-577
NiV LDH	50	318	<i>Nat. Commun.</i> , 2016, 7 , 1-9

Table S7 Comparison of HER catalytic performances.

Catalyst	Tafel slope (mV/dec)	Overpotential at 10 mA cm ⁻² (mV)	Reference
Ru/Zn ₃ V ₃ O ₈	50.6	70	This work
NiCo ₂ O ₄	49.7	90	<i>Angew. Chem. Int. Ed.</i> , 2016, 55 , 6290-6294
NiP ₂ NS/CC	51	75	<i>Nanoscale</i> , 2014, 6 , 13440- 13445
MoC _x	59	115	<i>Nat. Commun.</i> , 2015, 6 , 6512
VOOH	104	164	<i>Angew. Chem. Int. Ed.</i> , 2017, 56 , 573-577
NiFe LDH	/	210	<i>Science</i> , 2014, 345 , 1593-1596
CoNi@NC	104	224	<i>Angew. Chem. Int. Ed.</i> , 2015, 54 , 2100-2104
Pt-CoS ₂ /CC	82	24	<i>Adv. Energy Mater.</i> , 2018, 8 , 1800935
MoC _x @C-1	56	79	<i>J. Mater. Chem. A</i> , 2016, 4 , 3947-3954
Ni@graphene	120	240	<i>ACS Sustainable Chem. Eng.</i> , 2017, 5 , 4771–4777

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