

## Inorganic Chemistry Frontiers

### Supporting Information

**$\text{ACs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$  (A = K, Rb and Cs) with two kinds of isolated**

**P–O groups designed by dimensional reduction theory**

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**Table S1.** Crystal data and structure refinement for  $\text{ACs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$  (A = K, Rb and Cs).

|                                                    | $\text{KCs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$ | $\text{RbCs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$ | $\text{Cs}_6\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$ |
|----------------------------------------------------|------------------------------------------------------------------|-------------------------------------------------------------------|-----------------------------------------------------------------|
| Formula weight                                     | 2251.33                                                          | 2297.70                                                           | 2345.14                                                         |
| Temperature / K                                    | 298(2)                                                           | 299(2)                                                            | 299(2)                                                          |
| Wavelength / Å                                     | 0.71073                                                          | 0.71073                                                           | 0.71073                                                         |
| Crystal system                                     | Monoclinic                                                       | Monoclinic                                                        | Monoclinic                                                      |
| Space group, Z                                     | $P2_1/c$ , 4                                                     | $P2_1/c$ , 4                                                      | $P2_1/c$ , 4                                                    |
| $a$ / Å                                            | 9.1435(4)                                                        | 9.1839(9)                                                         | 9.1860(7)                                                       |
| $b$ / Å                                            | 9.3581(4)                                                        | 9.3584(9)                                                         | 9.3662(8)                                                       |
| $c$ / Å                                            | 36.4405(18)                                                      | 36.724(3)                                                         | 37.368(3)                                                       |
| $\beta$ / °                                        | 95.9210(10)                                                      | 96.100(3)                                                         | 96.677(2)                                                       |
| Volume / Å <sup>3</sup>                            | 3101.4(2)                                                        | 3138.5(5)                                                         | 3193.3(4)                                                       |
| $\rho$ / Mg/m <sup>3</sup>                         | 4.822                                                            | 4.863                                                             | 4.878                                                           |
| $\mu$ / mm <sup>-1</sup>                           | 29.067                                                           | 30.132                                                            | 29.224                                                          |
| $F(000)$                                           | 3912                                                             | 3984                                                              | 4056                                                            |
| Crystal size / mm <sup>3</sup>                     | 0.090x0.083x0.075                                                | 0.082x0.080x0.063                                                 | 0.120x0.068x0.077                                               |
| $\Theta$ range for data collection / °             | 2.24 to 27.54                                                    | 2.23 to 27.50                                                     | 2.19 to 27.53                                                   |
| Limiting indices                                   | $-11 \leq h \leq 11, -12 \leq k \leq 12, -47 \leq l \leq 47$     | $-11 \leq h \leq 11, -12 \leq k \leq 12, -47 \leq l \leq 35$      | $-11 \leq h \leq 11, -12 \leq k \leq 12, -48 \leq l \leq 48$    |
| Reflections collected / unique                     | 39188 / 7124 [ $R(\text{int}) = 0.0578$ ]                        | 32088 / 7181 [ $R(\text{int}) = 0.0815$ ]                         | 35551 / 7318 [ $R(\text{int}) = 0.0952$ ]                       |
| Completeness                                       | 99.8%                                                            | 99.9 %                                                            | 99.7 %                                                          |
| Refinement method                                  | Full-matrix least-squares on $F^2$                               | Full-matrix least-squares on $F^2$                                | Full-matrix least-squares on $F^2$                              |
| Data / restraints / parameters                     | 7124 / 0 / 425                                                   | 7181 / 0 / 279                                                    | 7318 / 0 / 279                                                  |
| Goodness-of-fit on $F^2$                           | 1.042                                                            | 1.057                                                             | 1.080                                                           |
| Final $R$ indices [ $F_o^2 > 2\sigma(F_o^2)$ ] [a] | $R_1 = 0.0361, wR_2 = 0.0787$                                    | $R_1 = 0.0508, wR_2 = 0.1021$                                     | $R_1 = 0.0489, wR_2 = 0.0893$                                   |
| $R$ indices (all data) [a]                         | $R_1 = 0.0481, wR_2 = 0.0854$                                    | $R_1 = 0.0818, wR_2 = 0.1187$                                     | $R_1 = 0.0838, wR_2 = 0.1051$                                   |
| Largest diff. peak and hole / e·Å <sup>-3</sup>    | 1.579 and -4.415                                                 | 2.499 and -4.728                                                  | 2.362 and -2.539                                                |

[a]  $R_1 = \Sigma||F_o| - |F_c|| / \Sigma|F_o|$  and  $wR_2 = [\Sigma w(F_o^2 - F_c^2)^2 / \Sigma wF_o^4]^{1/2}$  for  $F_o^2 > 2\sigma(F_o^2)$

**Table S2.** Atomic coordinates and equivalent isotropic displacement parameters ( $\text{\AA}^2$ ) for  $\text{KCs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$ .

| Atom  | x           | y          | z          | U(eq) <sup>[a]</sup> | BVS  |
|-------|-------------|------------|------------|----------------------|------|
| Bi(1) | -0.3231(1)  | 1.1217(1)  | 0.0516(1)  | 0.012(1)             | 2.95 |
| Bi(2) | -0.0724(1)  | 0.6221(1)  | 0.1892(1)  | 0.015(1)             | 3.29 |
| Bi(3) | 0.5579(1)   | 0.7927(1)  | 0.1228(1)  | 0.012(1)             | 2.86 |
| Bi(4) | -0.1338(1)  | 1.5913(1)  | 0.0542(1)  | 0.014(1)             | 2.98 |
| K(1)  | 0.0539(3)   | 1.2926(3)  | 0.1239(1)  | 0.019(1)             | 1.14 |
| Cs(1) | 0.1775(1)   | 0.9975(1)  | 0.0496(1)  | 0.022(1)             | 1.07 |
| Cs(2) | 0.4017(1)   | 0.4559(1)  | 0.1889(1)  | 0.027(1)             | 1.14 |
| Cs(3) | -0.6421(1)  | 1.4815(1)  | 0.0506(1)  | 0.037(1)             | 1.37 |
| Cs(4) | 0.2334(1)   | 0.6359(1)  | 0.3007(1)  | 0.034(1)             | 1.13 |
| Cs(5) | 0.2665(1)   | 0.9759(1)  | 0.2001(1)  | 0.031(1)             | 0.98 |
| P(1)  | 0.5599(3)   | 0.7972(3)  | 0.0247(1)  | 0.011(1)             | 5.03 |
| P(2)  | -0.0950(3)  | 0.8948(3)  | 0.1205(1)  | 0.014(1)             | 5.21 |
| P(3)  | 0.6207(3)   | 0.7357(3)  | 0.2248(1)  | 0.016(1)             | 4.96 |
| P(4)  | 0.4591(3)   | 1.1677(3)  | 0.1190(1)  | 0.012(1)             | 5.04 |
| P(5)  | -0.0435(3)  | 1.3046(3)  | 0.0178(1)  | 0.013(1)             | 4.98 |
| P(6)  | 0.1680(3)   | 0.7074(3)  | 0.1268(1)  | 0.018(1)             | 5.31 |
| P(7)  | 0.6804(3)   | 0.4064(3)  | 0.1203(1)  | 0.016(1)             | 4.95 |
| P(8)  | 0.9025(3)   | 0.8410(3)  | 0.2610(1)  | 0.019(1)             | 5.03 |
| O(1)  | 0.1038(15)  | 0.5983(14) | 0.1021(5)  | 0.081(5)             | 2.00 |
| O(2)  | 0.5822(9)   | 0.2824(8)  | 0.1357(2)  | 0.019(2)             | 2.34 |
| O(3)  | 0.6538(8)   | 0.6613(8)  | 0.0276(2)  | 0.015(2)             | 2.27 |
| O(4)  | 0.4450(8)   | 1.1832(8)  | 0.0775(2)  | 0.019(2)             | 2.04 |
| O(5)  | 0.4350(8)   | 0.7640(8)  | -0.0058(2) | 0.015(2)             | 2.20 |
| O(6)  | -0.1278(8)  | 1.1646(8)  | 0.0237(2)  | 0.018(2)             | 2.28 |
| O(7)  | -0.1521(8)  | 1.4304(8)  | 0.0103(2)  | 0.018(2)             | 2.27 |
| O(8)  | 0.4931(9)   | 0.8250(9)  | 0.0609(2)  | 0.022(2)             | 2.00 |
| O(9)  | 0.6485(9)   | 0.9264(8)  | 0.0144(2)  | 0.020(2)             | 2.09 |
| O(10) | 0.0292(9)   | 1.2724(8)  | -0.0180(3) | 0.025(2)             | 2.21 |
| O(11) | 0.7225(10)  | 0.3594(10) | 0.0825(2)  | 0.028(2)             | 2.00 |
| O(12) | 0.7184(9)   | 0.6072(9)  | 0.2178(3)  | 0.025(2)             | 2.08 |
| O(13) | 0.7370(9)   | 0.8572(8)  | 0.2412(3)  | 0.024(2)             | 2.31 |
| O(14) | 0.0627(10)  | 1.3389(10) | 0.0508(2)  | 0.030(2)             | 1.86 |
| O(15) | 0.5310(11)  | 1.0274(9)  | 0.1319(3)  | 0.037(2)             | 2.11 |
| O(16) | 0.0752(9)   | 0.8250(10) | 0.1200(3)  | 0.033(2)             | 2.27 |
| O(17) | 0.5170(10)  | 0.7078(10) | 0.2530(3)  | 0.029(2)             | 1.80 |
| O(18) | -0.0068(9)  | 0.7793(9)  | 0.2319(2)  | 0.024(2)             | 2.20 |
| O(19) | 0.5495(9)   | 0.7962(10) | 0.1889(2)  | 0.028(2)             | 1.95 |
| O(20) | 0.8103(10)  | 0.4181(11) | 0.1491(3)  | 0.037(2)             | 1.91 |
| O(21) | -0.1828(12) | 0.8190(14) | 0.0897(3)  | 0.058(4)             | 1.86 |
| O(22) | 0.3201(9)   | 0.7545(12) | 0.2955(3)  | 0.036(2)             | 2.20 |
| O(23) | 0.3255(10)  | 1.1998(12) | 0.1375(3)  | 0.037(2)             | 1.98 |

|       |             |            |           |          |      |
|-------|-------------|------------|-----------|----------|------|
| O(24) | 0.9039(10)  | 0.7567(12) | 0.2955(3) | 0.036(2) | 1.90 |
| O(25) | 0.5829(13)  | 0.5382(9)  | 0.1172(3) | 0.043(3) | 2.00 |
| O(26) | 0.9455(11)  | 0.9965(10) | 0.2673(3) | 0.039(3) | 2.20 |
| O(27) | 0.1596(11)  | 0.6762(12) | 0.1676(3) | 0.045(3) | 2.17 |
| O(28) | -0.1008(11) | 1.0528(10) | 0.1162(4) | 0.049(3) | 1.84 |
| O(29) | -0.1443(12) | 0.8386(13) | 0.1560(3) | 0.052(3) | 1.96 |

[a] U(eq) is defined as one third of the trace of the orthogonalized  $U_{ij}$  tensor.

**Table S3.** Atomic coordinates and equivalent isotropic displacement parameters ( $\text{\AA}^2$ ) for  $\text{RbCs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$ .

| Atom  | x          | y          | z         | U(eq) <sup>[a]</sup> | BVS  |
|-------|------------|------------|-----------|----------------------|------|
| Bi(1) | 0.6772(1)  | 0.8739(1)  | 1.0514(1) | 0.012(1)             | 2.83 |
| Bi(2) | 1.0735(1)  | 0.6306(1)  | 0.8109(1) | 0.016(1)             | 3.24 |
| Bi(3) | 0.4407(1)  | 0.7895(1)  | 0.8776(1) | 0.012(1)             | 3.15 |
| Bi(4) | 0.1283(1)  | 0.5881(1)  | 0.9455(1) | 0.014(1)             | 3.16 |
| Rb(1) | 1.0605(2)  | 0.7077(2)  | 1.1244(1) | 0.020(1)             | 1.15 |
| Cs(1) | 0.5953(1)  | 0.4560(1)  | 0.8108(1) | 0.028(1)             | 0.97 |
| Cs(2) | 0.8179(1)  | 0.9999(1)  | 0.9510(1) | 0.025(1)             | 1.09 |
| Cs(3) | 0.3596(1)  | 0.5210(1)  | 1.0490(1) | 0.036(1)             | 1.44 |
| Cs(4) | 0.7309(1)  | 0.9701(1)  | 0.7991(1) | 0.033(1)             | 0.96 |
| Cs(5) | 0.2336(2)  | 1.1330(1)  | 0.8000(1) | 0.038(1)             | 1.08 |
| P(1)  | 0.9036(5)  | 0.3400(5)  | 0.7621(1) | 0.021(1)             | 4.93 |
| P(2)  | 0.9554(5)  | 0.6973(4)  | 1.0166(1) | 0.013(1)             | 4.97 |
| P(3)  | 0.3762(5)  | 0.7373(5)  | 0.7749(1) | 0.017(1)             | 5.08 |
| P(4)  | 0.5315(5)  | 0.1645(4)  | 0.8798(1) | 0.014(1)             | 5.07 |
| P(5)  | 1.0944(5)  | 0.8938(4)  | 0.8801(1) | 0.014(1)             | 5.10 |
| P(6)  | 0.8303(5)  | 0.7111(5)  | 0.8745(1) | 0.017(1)             | 5.39 |
| P(7)  | 0.3232(5)  | 0.4112(4)  | 0.8797(1) | 0.015(1)             | 5.01 |
| P(8)  | 0.4364(5)  | 0.7956(4)  | 0.9741(1) | 0.013(1)             | 4.96 |
| O(1)  | 0.8703(12) | 0.8369(12) | 1.0232(3) | 0.016(2)             | 2.26 |
| O(2)  | 0.3411(12) | 0.6609(12) | 0.9718(3) | 0.017(2)             | 2.24 |
| O(3)  | 0.5595(12) | 0.7644(12) | 1.0054(3) | 0.020(3)             | 2.15 |
| O(4)  | 0.8487(12) | 0.5716(12) | 1.0104(3) | 0.017(2)             | 2.30 |
| O(5)  | 0.2807(14) | 0.6089(13) | 0.7813(3) | 0.027(3)             | 2.08 |
| O(6)  | 0.2623(13) | 0.8565(13) | 0.7580(3) | 0.025(3)             | 2.34 |
| O(7)  | 0.4063(12) | 0.2784(12) | 0.8641(3) | 0.020(3)             | 2.34 |
| O(8)  | 0.2764(13) | 0.3676(13) | 0.9166(3) | 0.026(3)             | 1.84 |
| O(9)  | 1.0663(14) | 0.6629(14) | 1.0482(3) | 0.030(3)             | 1.89 |
| O(10) | 0.3471(13) | 0.9262(13) | 0.9832(3) | 0.022(3)             | 2.08 |
| O(11) | 0.1938(14) | 0.4364(14) | 0.8516(3) | 0.032(3)             | 1.88 |
| O(12) | 0.5586(14) | 0.1873(14) | 0.9204(3) | 0.028(3)             | 2.01 |
| O(13) | 0.9259(14) | 0.8545(14) | 0.8828(3) | 0.030(3)             | 2.24 |
| O(14) | 0.5049(13) | 0.8208(13) | 0.9382(3) | 0.026(3)             | 2.02 |
| O(15) | 0.4830(14) | 0.7098(14) | 0.7480(3) | 0.029(3)             | 1.81 |
| O(16) | 0.6790(15) | 0.7670(15) | 0.8779(4) | 0.034(3)             | 2.27 |
| O(17) | 0.4315(15) | 0.5338(14) | 0.8828(4) | 0.033(3)             | 2.04 |
| O(18) | 1.0246(13) | 0.7293(13) | 0.9802(3) | 0.024(3)             | 2.17 |
| O(19) | 0.6593(15) | 0.1897(15) | 0.8592(4) | 0.038(3)             | 1.85 |
| O(20) | 1.1327(18) | 0.8561(17) | 0.8425(4) | 0.050(4)             | 1.87 |
| O(21) | 0.9960(13) | 0.2860(13) | 0.7325(3) | 0.022(3)             | 2.18 |
| O(22) | 0.9054(15) | 0.2500(15) | 0.7950(4) | 0.035(3)             | 1.96 |
| O(23) | 0.4440(14) | 0.8000(14) | 0.8107(4) | 0.033(3)             | 1.93 |

|       |            |            |           |          |      |
|-------|------------|------------|-----------|----------|------|
| O(24) | 0.8460(15) | 0.6706(15) | 0.8360(4) | 0.037(3) | 2.11 |
| O(25) | 0.4529(16) | 0.0236(15) | 0.8708(4) | 0.039(4) | 2.12 |
| O(26) | 0.8815(18) | 0.6063(17) | 0.9017(4) | 0.051(4) | 2.03 |
| O(27) | 1.1116(18) | 1.0452(18) | 0.8920(4) | 0.054(4) | 1.82 |
| O(28) | 1.1863(19) | 0.7940(19) | 0.9062(5) | 0.058(5) | 1.83 |
| O(29) | 0.9458(16) | 0.4965(16) | 0.7705(4) | 0.043(4) | 2.14 |

[a]  $U(eq)$  is defined as one third of the trace of the orthogonalized  $U_{ij}$  tensor.

**Table S4.** Atomic coordinates and equivalent isotropic displacement parameters ( $\text{\AA}^2$ ) for  $\text{Cs}_6\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$ .

| Atom  | x           | y          | z          | U(eq) <sup>[a]</sup> | BVS  |
|-------|-------------|------------|------------|----------------------|------|
| Bi(1) | -0.0767(1)  | 0.6434(1)  | 0.1889(1)  | 0.013(1)             | 3.08 |
| Bi(2) | -0.3155(1)  | 0.1294(1)  | 0.0519(1)  | 0.013(1)             | 2.98 |
| Bi(3) | -0.1209(1)  | 0.5835(1)  | 0.0553(1)  | 0.012(1)             | 3.05 |
| Bi(4) | 0.5636(1)   | 0.7922(1)  | 0.1229(1)  | 0.011(1)             | 3.21 |
| Cs(1) | 0.4086(1)   | 0.4615(1)  | 0.1894(1)  | 0.024(1)             | 0.92 |
| Cs(2) | -0.6324(1)  | 0.4799(1)  | 0.0484(1)  | 0.023(1)             | 1.31 |
| Cs(3) | 0.0713(1)   | 0.2818(1)  | 0.1248(1)  | 0.029(1)             | 1.21 |
| Cs(4) | -0.8091(1)  | 0.0019(1)  | 0.0478(1)  | 0.023(1)             | 1.03 |
| Cs(5) | 0.2685(1)   | 0.9659(1)  | 0.2021(1)  | 0.028(1)             | 0.97 |
| Cs(6) | 0.2390(1)   | 0.6341(1)  | 0.2972(1)  | 0.030(1)             | 1.14 |
| P(1)  | -0.0925(4)  | -0.1055(4) | 0.1182(1)  | 0.014(1)             | 5.04 |
| P(2)  | -0.0471(4)  | 0.3032(4)  | 0.0160(1)  | 0.013(1)             | 4.90 |
| P(3)  | 0.6871(4)   | 0.4203(4)  | 0.1228(1)  | 0.013(1)             | 5.01 |
| P(4)  | 0.6295(4)   | 0.7446(5)  | 0.2256(1)  | 0.017(1)             | 5.01 |
| P(5)  | 0.0898(4)   | 0.3411(4)  | 0.2357(1)  | 0.016(1)             | 4.86 |
| P(6)  | 0.1730(4)   | 0.7130(4)  | 0.1249(1)  | 0.016(1)             | 5.09 |
| P(7)  | -0.4288(4)  | 0.7978(4)  | 0.0284(1)  | 0.012(1)             | 4.92 |
| P(8)  | 0.4835(4)   | 0.1663(4)  | 0.1219(1)  | 0.015(1)             | 5.17 |
| O(1)  | -0.1295(10) | 0.1612(11) | 0.0230(3)  | 0.017(2)             | 2.28 |
| O(2)  | 0.0004(10)  | 0.2941(11) | 0.2658(3)  | 0.018(2)             | 2.07 |
| O(3)  | -0.3340(10) | 0.6618(11) | 0.0305(3)  | 0.016(2)             | 2.19 |
| O(4)  | -0.3323(11) | 0.9277(12) | 0.0223(3)  | 0.023(3)             | 2.17 |
| O(5)  | 0.7357(11)  | 0.3841(11) | 0.0863(3)  | 0.023(2)             | 1.82 |
| O(6)  | 0.0643(11)  | 0.3402(12) | 0.0475(3)  | 0.026(3)             | 1.83 |
| O(7)  | 0.0522(11)  | 0.4975(12) | 0.2251(3)  | 0.024(3)             | 2.12 |
| O(8)  | -0.1592(10) | 0.4264(11) | 0.0114(3)  | 0.019(2)             | 2.24 |
| O(9)  | -0.5049(10) | 0.8167(11) | 0.0634(3)  | 0.018(2)             | 1.98 |
| O(10) | 0.2582(11)  | 0.3620(11) | 0.2546(3)  | 0.023(3)             | 2.29 |
| O(11) | -0.5491(11) | 0.7807(11) | -0.0030(3) | 0.023(3)             | 2.04 |
| O(12) | 0.0169(11)  | 0.2750(11) | -0.0200(3) | 0.023(3)             | 2.10 |
| O(13) | 0.5716(11)  | 0.5341(12) | 0.1205(3)  | 0.024(3)             | 2.05 |
| O(14) | 0.5136(11)  | 0.7187(12) | 0.2494(3)  | 0.027(3)             | 1.79 |
| O(15) | 0.8136(12)  | 0.4474(13) | 0.1516(3)  | 0.032(3)             | 1.92 |
| O(16) | 0.0858(11)  | 0.2417(12) | 0.2048(3)  | 0.030(3)             | 1.96 |
| O(17) | -0.1170(11) | 0.0310(12) | 0.0975(3)  | 0.028(3)             | 1.93 |
| O(18) | 0.6107(11)  | 0.2800(12) | 0.1374(3)  | 0.024(3)             | 2.17 |
| O(19) | 0.1451(11)  | 0.6724(13) | 0.1632(3)  | 0.030(3)             | 1.97 |
| O(20) | 0.3268(12)  | 0.7727(13) | 0.1249(3)  | 0.032(3)             | 2.15 |
| O(21) | 0.8143(12)  | 0.7713(13) | 0.1011(3)  | 0.035(3)             | 1.84 |
| O(22) | 0.0756(11)  | 0.8534(12) | 0.1137(3)  | 0.024(3)             | 2.17 |
| O(23) | 0.1326(13)  | 0.6025(14) | 0.0980(3)  | 0.044(3)             | 1.96 |



|       |             |             |           |          |      |
|-------|-------------|-------------|-----------|----------|------|
| O(24) | 0.7247(11)  | 0.6137(12)  | 0.2212(3) | 0.029(3) | 2.04 |
| O(25) | 0.5722(13)  | 0.0281(13)  | 0.1253(3) | 0.038(3) | 2.08 |
| O(26) | -0.1085(14) | -0.1014(14) | 0.1574(4) | 0.046(4) | 1.77 |
| O(27) | 0.3742(14)  | 0.1755(16)  | 0.1468(4) | 0.054(4) | 2.10 |
| O(28) | 0.4388(12)  | 0.1955(14)  | 0.0827(3) | 0.038(3) | 1.94 |
| O(29) | 0.5777(12)  | 0.8122(13)  | 0.1895(3) | 0.038(3) | 1.87 |

[a] U(eq) is defined as one third of the trace of the orthogonalized  $U_{ij}$  tensor.

**Table S5.** Bond lengths (Å) and angles (°) for  $\text{KCs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$ .

|               |           |                |           |
|---------------|-----------|----------------|-----------|
| K(1)-O(23)    | 2.630(10) | Cs(4)-O(2)#7   | 3.047(8)  |
| K(1)-O(28)    | 2.653(10) | Cs(4)-O(13)#4  | 3.050(9)  |
| K(1)-O(14)    | 2.709(9)  | Cs(4)-O(26)#4  | 3.113(11) |
| K(1)-O(20)#3  | 2.757(10) | Cs(4)-O(24)#2  | 3.205(9)  |
| K(1)-O(24)#7  | 2.943(10) | Cs(4)-O(15)#4  | 3.258(10) |
| K(1)-O(1)#9   | 3.016(15) | Cs(4)-O(20)#7  | 3.260(11) |
| K(1)-O(11)#3  | 3.302(10) | Cs(4)-O(17)    | 3.336(9)  |
| Cs(1)-O(9)#12 | 3.041(8)  | Cs(4)-O(29)#13 | 3.341(12) |
| Cs(1)-O(6)#1  | 3.066(8)  | Cs(4)-O(18)    | 3.432(9)  |
| Cs(1)-O(4)    | 3.086(8)  | Cs(4)-O(28)#13 | 3.465(13) |
| Cs(1)-O(16)   | 3.133(10) | Cs(5)-O(24)#7  | 3.068(10) |
| Cs(1)-O(6)    | 3.254(8)  | Cs(5)-O(19)    | 3.147(9)  |
| Cs(1)-O(10)#1 | 3.291(8)  | Cs(5)-O(27)    | 3.159(13) |
| Cs(1)-O(8)    | 3.295(8)  | Cs(5)-O(23)    | 3.185(11) |
| Cs(1)-O(14)   | 3.365(10) | Cs(5)-O(12)#7  | 3.223(9)  |
| Cs(1)-O(22)   | 3.606(10) | Cs(5)-O(17)#7  | 3.293(9)  |
| Cs(2)-O(27)   | 3.066(10) | Cs(5)-O(18)    | 3.402(9)  |
| Cs(2)-O(23)#5 | 3.078(10) | Cs(5)-O(16)    | 3.444(10) |
| Cs(2)-O(13)#4 | 3.099(9)  | Cs(5)-O(22)    | 3.615(11) |
| Cs(2)-O(2)    | 3.127(8)  | Cs(5)-O(15)    | 3.675(12) |
| Cs(2)-O(17)#4 | 3.176(10) | Bi(1)-O(5)#1   | 2.149(7)  |
| Cs(2)-O(12)   | 3.297(8)  | Bi(1)-O(6)     | 2.179(7)  |
| Cs(2)-O(25)   | 3.327(11) | Bi(1)-O(9)#2   | 2.273(8)  |
| Cs(2)-O(17)   | 3.409(10) | Bi(1)-O(4)#2   | 2.478(8)  |
| Cs(2)-O(24)#4 | 3.455(10) | Bi(1)-O(11)#3  | 2.508(9)  |
| Cs(2)-O(19)   | 3.459(10) | Bi(3)-O(22)    | 2.198(9)  |
| Cs(3)-O(7)#10 | 2.879(8)  | Bi(3)-O(15)    | 2.239(8)  |
| Cs(3)-O(14)#2 | 3.012(9)  | Bi(3)-O(8)     | 2.292(8)  |
| Cs(3)-O(4)#2  | 3.038(8)  | Bi(3)-O(25)    | 2.403(9)  |
| Cs(3)-O(25)#3 | 3.061(12) | Bi(3)-O(19)    | 2.421(9)  |
| Cs(3)-O(3)#1  | 3.141(8)  | Bi(4)-O(10)#8  | 2.132(8)  |
| Cs(3)-O(1)#3  | 3.320(16) | Bi(4)-O(3)#3   | 2.180(7)  |
| Cs(3)-O(3)#3  | 3.364(8)  | Bi(4)-O(7)     | 2.192(8)  |
| Cs(3)-O(8)#3  | 3.450(9)  | Bi(4)-O(21)#9  | 2.556(11) |
| Cs(3)-O(5)#3  | 3.466(8)  | Bi(4)-O(1)#9   | 2.643(13) |
| Cs(3)-O(5)#1  | 3.487(8)  | P(1)-O(9)      | 1.523(8)  |
| Cs(3)-O(11)#3 | 3.602(9)  | P(1)-O(8)      | 1.531(8)  |
| Bi(2)-O(18)   | 2.180(8)  | P(1)-O(3)      | 1.532(8)  |
| Bi(2)-O(26)#4 | 2.204(9)  | P(1)-O(5)      | 1.542(7)  |
| Bi(2)-O(12)#2 | 2.275(9)  | P(2)-O(28)     | 1.487(10) |
| Bi(2)-O(27)   | 2.392(10) | P(2)-O(21)     | 1.489(10) |
| Bi(2)-O(29)   | 2.417(10) | P(2)-O(29)     | 1.506(10) |
| Bi(2)-O(20)#2 | 2.571(9)  | P(2)-O(16)     | 1.609(8)  |

|                       |           |                       |           |
|-----------------------|-----------|-----------------------|-----------|
| P(3)-O(17)            | 1.492(9)  | P(4)-O(23)            | 1.485(9)  |
| P(3)-O(19)            | 1.508(9)  | P(4)-O(4)             | 1.510(8)  |
| P(3)-O(12)            | 1.535(9)  | P(4)-O(15)            | 1.520(9)  |
| P(3)-O(13)            | 1.629(8)  | P(4)-O(2)#9           | 1.627(8)  |
| P(5)-O(14)            | 1.499(9)  | P(6)-O(1)             | 1.444(13) |
| P(5)-O(7)             | 1.546(8)  | P(6)-O(22)            | 1.492(9)  |
| P(5)-O(6)             | 1.547(8)  | P(6)-O(27)            | 1.526(10) |
| P(5)-O(10)            | 1.554(9)  | P(6)-O(16)            | 1.603(9)  |
| P(7)-O(20)            | 1.506(10) | P(8)-O(24)            | 1.482(10) |
| P(7)-O(25)            | 1.519(9)  | P(8)-O(26)            | 1.519(9)  |
| P(7)-O(11)            | 1.532(9)  | P(8)-O(18)#11         | 1.526(9)  |
| P(7)-O(2)             | 1.604(8)  | P(8)-O(13)            | 1.615(8)  |
|                       |           |                       |           |
| O(23)-K(1)-O(28)      | 102.9(3)  | O(9)#12-Cs(1)-O(6)#1  | 59.3(2)   |
| O(23)-K(1)-O(14)      | 96.6(3)   | O(9)#12-Cs(1)-O(4)    | 70.2(2)   |
| O(28)-K(1)-O(14)      | 95.8(4)   | O(6)#1-Cs(1)-O(4)     | 127.4(2)  |
| O(23)-K(1)-O(20)#3    | 149.0(3)  | O(9)#12-Cs(1)-O(16)   | 162.7(2)  |
| O(28)-K(1)-O(20)#3    | 87.5(3)   | O(6)#1-Cs(1)-O(16)    | 118.0(2)  |
| O(14)-K(1)-O(20)#3    | 111.5(3)  | O(4)-Cs(1)-O(16)      | 105.5(2)  |
| O(23)-K(1)-O(24)#7    | 75.5(3)   | O(9)#12-Cs(1)-O(6)    | 99.6(2)   |
| O(28)-K(1)-O(24)#7    | 91.3(4)   | O(6)#1-Cs(1)-O(6)     | 86.6(2)   |
| O(14)-K(1)-O(24)#7    | 170.5(3)  | O(4)-Cs(1)-O(6)       | 116.9(2)  |
| O(20)#3-K(1)-O(24)#7  | 75.1(3)   | O(16)-Cs(1)-O(6)      | 97.2(2)   |
| O(23)-K(1)-O(1)#9     | 101.4(4)  | O(9)#12-Cs(1)-O(10)#1 | 103.8(2)  |
| O(28)-K(1)-O(1)#9     | 150.3(4)  | O(6)#1-Cs(1)-O(10)#1  | 44.5(2)   |
| O(14)-K(1)-O(1)#9     | 64.5(4)   | O(4)-Cs(1)-O(10)#1    | 162.7(2)  |
| O(20)#3-K(1)-O(1)#9   | 80.4(4)   | O(16)-Cs(1)-O(10)#1   | 75.2(2)   |
| O(24)#7-K(1)-O(1)#9   | 111.3(4)  | O(6)-Cs(1)-O(10)#1    | 79.8(2)   |
| O(23)-K(1)-O(11)#3    | 162.3(3)  | O(9)#12-Cs(1)-O(8)    | 71.9(2)   |
| O(28)-K(1)-O(11)#3    | 70.0(3)   | O(6)#1-Cs(1)-O(8)     | 85.1(2)   |
| O(14)-K(1)-O(11)#3    | 68.8(3)   | O(4)-Cs(1)-O(8)       | 65.2(2)   |
| O(20)#3-K(1)-O(11)#3  | 48.5(3)   | O(16)-Cs(1)-O(8)      | 91.0(2)   |
| O(24)#7-K(1)-O(11)#3  | 119.8(2)  | O(6)-Cs(1)-O(8)       | 170.4(2)  |
| O(1)#9-K(1)-O(11)#3   | 81.8(3)   | O(10)#1-Cs(1)-O(8)    | 97.6(2)   |
| O(27)-Cs(2)-O(23)#5   | 104.9(3)  | O(9)#12-Cs(1)-O(14)   | 88.6(2)   |
| O(27)-Cs(2)-O(13)#4   | 93.6(2)   | O(6)#1-Cs(1)-O(14)    | 117.6(2)  |
| O(23)#5-Cs(2)-O(13)#4 | 100.5(2)  | O(4)-Cs(1)-O(14)      | 72.5(2)   |
| O(27)-Cs(2)-O(2)      | 127.3(3)  | O(16)-Cs(1)-O(14)     | 106.4(2)  |
| O(23)#5-Cs(2)-O(2)    | 47.1(2)   | O(6)-Cs(1)-O(14)      | 44.58(19) |
| O(13)#4-Cs(2)-O(2)    | 129.9(2)  | O(10)#1-Cs(1)-O(14)   | 124.4(2)  |
| O(27)-Cs(2)-O(17)#4   | 140.6(2)  | O(8)-Cs(1)-O(14)      | 137.2(2)  |
| O(23)#5-Cs(2)-O(17)#4 | 81.9(3)   | O(9)#12-Cs(1)-O(22)   | 121.7(2)  |
| O(13)#4-Cs(2)-O(17)#4 | 47.4(2)   | O(6)#1-Cs(1)-O(22)    | 109.2(2)  |
| O(2)-Cs(2)-O(17)#4    | 86.1(2)   | O(4)-Cs(1)-O(22)      | 84.3(2)   |

|                       |          |                       |            |
|-----------------------|----------|-----------------------|------------|
| O(27)-Cs(2)-O(12)     | 112.3(3) | O(16)-Cs(1)-O(22)     | 41.3(2)    |
| O(23)#5-Cs(2)-O(12)   | 131.7(2) | O(6)-Cs(1)-O(22)      | 138.4(2)   |
| O(13)#4-Cs(2)-O(12)   | 106.6(2) | O(10)#1-Cs(1)-O(22)   | 85.5(2)    |
| O(2)-Cs(2)-O(12)      | 85.3(2)  | O(8)-Cs(1)-O(22)      | 49.8(2)    |
| O(17)#4-Cs(2)-O(12)   | 87.9(2)  | O(14)-Cs(1)-O(22)     | 132.8(2)   |
| O(27)-Cs(2)-O(25)     | 92.9(2)  | O(7)#10-Cs(3)-O(14)#2 | 67.3(2)    |
| O(23)#5-Cs(2)-O(25)   | 78.6(3)  | O(7)#10-Cs(3)-O(4)#2  | 129.9(2)   |
| O(13)#4-Cs(2)-O(25)   | 173.5(2) | O(14)#2-Cs(3)-O(4)#2  | 78.3(2)    |
| O(2)-Cs(2)-O(25)      | 45.2(2)  | O(7)#10-Cs(3)-O(25)#3 | 153.4(2)   |
| O(17)#4-Cs(2)-O(25)   | 126.2(2) | O(14)#2-Cs(3)-O(25)#3 | 127.2(3)   |
| O(12)-Cs(2)-O(25)     | 70.1(3)  | O(4)#2-Cs(3)-O(25)#3  | 76.8(2)    |
| O(27)-Cs(2)-O(17)     | 82.7(3)  | O(7)#10-Cs(3)-O(3)#1  | 57.6(2)    |
| O(23)#5-Cs(2)-O(17)   | 172.1(3) | O(14)#2-Cs(3)-O(3)#1  | 82.3(2)    |
| O(13)#4-Cs(2)-O(17)   | 76.5(2)  | O(4)#2-Cs(3)-O(3)#1   | 83.4(2)    |
| O(2)-Cs(2)-O(17)      | 129.7(2) | O(25)#3-Cs(3)-O(3)#1  | 138.6(2)   |
| O(17)#4-Cs(2)-O(17)   | 90.83(3) | O(7)#10-Cs(3)-O(1)#3  | 84.4(3)    |
| O(12)-Cs(2)-O(17)     | 44.3(2)  | O(14)#2-Cs(3)-O(1)#3  | 57.7(3)    |
| O(25)-Cs(2)-O(17)     | 103.6(2) | O(4)#2-Cs(3)-O(1)#3   | 107.2(3)   |
| O(27)-Cs(2)-O(24)#4   | 80.2(3)  | O(25)#3-Cs(3)-O(1)#3  | 87.0(3)    |
| O(23)#5-Cs(2)-O(24)#4 | 62.9(2)  | O(3)#1-Cs(3)-O(1)#3   | 133.9(3)   |
| O(13)#4-Cs(2)-O(24)#4 | 45.4(2)  | O(7)#10-Cs(3)-O(3)#3  | 98.3(2)    |
| O(2)-Cs(2)-O(24)#4    | 108.0(2) | O(14)#2-Cs(3)-O(3)#3  | 165.0(2)   |
| O(17)#4-Cs(2)-O(24)#4 | 68.5(2)  | O(4)#2-Cs(3)-O(3)#3   | 110.4(2)   |
| O(12)-Cs(2)-O(24)#4   | 151.4(2) | O(25)#3-Cs(3)-O(3)#3  | 67.6(2)    |
| O(25)-Cs(2)-O(24)#4   | 137.0(3) | O(3)#1-Cs(3)-O(3)#3   | 86.56(19)  |
| O(17)-Cs(2)-O(24)#4   | 117.3(2) | O(1)#3-Cs(3)-O(3)#3   | 127.1(3)   |
| O(27)-Cs(2)-O(19)     | 69.7(3)  | O(7)#10-Cs(3)-O(8)#3  | 90.9(2)    |
| O(2)#7-Cs(4)-O(13)#4  | 134.1(2) | O(14)#2-Cs(3)-O(8)#3  | 136.4(2)   |
| O(2)#7-Cs(4)-O(26)#4  | 176.7(2) | O(4)#2-Cs(3)-O(8)#3   | 137.92(19) |
| O(13)#4-Cs(4)-O(26)#4 | 46.2(2)  | O(25)#3-Cs(3)-O(8)#3  | 63.2(2)    |
| O(2)#7-Cs(4)-O(24)#2  | 109.3(2) | O(3)#1-Cs(3)-O(8)#3   | 118.24(19) |
| O(13)#4-Cs(4)-O(24)#2 | 113.8(2) | O(1)#3-Cs(3)-O(8)#3   | 84.0(3)    |
| O(26)#4-Cs(4)-O(24)#2 | 71.7(3)  | O(3)#3-Cs(3)-O(8)#3   | 43.34(18)  |
| O(2)#7-Cs(4)-O(15)#4  | 45.3(2)  | O(7)#10-Cs(3)-O(5)#3  | 58.72(19)  |
| O(13)#4-Cs(4)-O(15)#4 | 91.5(2)  | O(14)#2-Cs(3)-O(5)#3  | 125.2(2)   |
| O(26)#4-Cs(4)-O(15)#4 | 136.2(2) | O(4)#2-Cs(3)-O(5)#3   | 146.1(2)   |
| O(24)#2-Cs(4)-O(15)#4 | 134.4(3) | O(25)#3-Cs(3)-O(5)#3  | 100.2(2)   |
| O(2)#7-Cs(4)-O(20)#7  | 45.5(2)  | O(3)#1-Cs(3)-O(5)#3   | 77.04(19)  |
| O(13)#4-Cs(4)-O(20)#7 | 175.1(2) | O(1)#3-Cs(3)-O(5)#3   | 106.4(3)   |
| O(26)#4-Cs(4)-O(20)#7 | 134.6(2) | O(3)#3-Cs(3)-O(5)#3   | 41.67(17)  |
| O(24)#2-Cs(4)-O(20)#7 | 65.1(2)  | O(8)#3-Cs(3)-O(5)#3   | 42.38(18)  |
| O(15)#4-Cs(4)-O(20)#7 | 86.5(2)  | O(7)#10-Cs(3)-O(5)#1  | 99.88(19)  |
| O(2)#7-Cs(4)-O(17)    | 84.6(2)  | O(14)#2-Cs(3)-O(5)#1  | 103.8(2)   |
| O(2)#7-Cs(4)-O(13)#4  | 134.1(2) | O(4)#2-Cs(3)-O(5)#1   | 53.8(2)    |

|                         |          |                       |            |
|-------------------------|----------|-----------------------|------------|
| O(2)#7-Cs(4)-O(26)#4    | 176.7(2) | O(25)#3-Cs(3)-O(5)#1  | 97.6(2)    |
| O(13)#4-Cs(4)-O(26)#4   | 46.2(2)  | O(3)#1-Cs(3)-O(5)#1   | 42.63(17)  |
| O(2)#7-Cs(4)-O(24)#2    | 109.3(2) | O(1)#3-Cs(3)-O(5)#1   | 158.0(3)   |
| O(13)#4-Cs(4)-O(24)#2   | 113.8(2) | O(3)#3-Cs(3)-O(5)#1   | 73.97(18)  |
| O(26)#4-Cs(4)-O(24)#2   | 71.7(3)  | O(8)#3-Cs(3)-O(5)#1   | 117.31(18) |
| O(2)#7-Cs(4)-O(15)#4    | 45.3(2)  | O(5)#3-Cs(3)-O(5)#1   | 94.10(17)  |
| O(13)#4-Cs(4)-O(15)#4   | 91.5(2)  | O(7)#10-Cs(3)-O(11)#3 | 148.1(2)   |
| O(26)#4-Cs(4)-O(15)#4   | 136.2(2) | O(14)#2-Cs(3)-O(11)#3 | 131.2(2)   |
| O(24)#2-Cs(4)-O(15)#4   | 134.4(3) | O(4)#2-Cs(3)-O(11)#3  | 53.2(2)    |
| O(13)#4-Cs(4)-O(17)     | 78.3(2)  | O(25)#3-Cs(3)-O(11)#3 | 43.6(2)    |
| O(26)#4-Cs(4)-O(17)     | 92.4(3)  | O(3)#1-Cs(3)-O(11)#3  | 95.82(19)  |
| O(24)#2-Cs(4)-O(17)     | 132.4(2) | O(1)#3-Cs(3)-O(11)#3  | 126.9(3)   |
| O(15)#4-Cs(4)-O(17)     | 88.1(3)  | O(3)#3-Cs(3)-O(11)#3  | 59.83(18)  |
| O(20)#7-Cs(4)-O(17)     | 106.0(2) | O(8)#3-Cs(3)-O(11)#3  | 87.22(19)  |
| O(2)#7-Cs(4)-O(29)#13   | 99.1(2)  | O(5)#3-Cs(3)-O(11)#3  | 101.26(18) |
| O(13)#4-Cs(4)-O(29)#13  | 64.1(2)  | O(5)#1-Cs(3)-O(11)#3  | 54.02(18)  |
| O(26)#4-Cs(4)-O(29)#13  | 83.9(3)  | O(24)#7-Cs(5)-O(19)   | 153.3(3)   |
| O(24)#2-Cs(4)-O(29)#13  | 92.8(3)  | O(24)#7-Cs(5)-O(27)   | 129.8(3)   |
| O(15)#4-Cs(4)-O(29)#13  | 63.8(3)  | O(19)-Cs(5)-O(27)     | 72.8(2)    |
| O(20)#7-Cs(4)-O(29)#13  | 111.1(2) | O(24)#7-Cs(5)-O(23)   | 66.3(3)    |
| O(17)-Cs(4)-O(29)#13    | 130.9(3) | O(19)-Cs(5)-O(23)     | 93.2(2)    |
| O(2)#7-Cs(4)-O(18)      | 129.9(2) | O(27)-Cs(5)-O(23)     | 112.6(3)   |
| O(13)#4-Cs(4)-O(18)     | 92.9(2)  | O(24)#7-Cs(5)-O(12)#7 | 66.3(2)    |
| O(26)#4-Cs(4)-O(18)     | 48.5(2)  | O(19)-Cs(5)-O(12)#7   | 111.5(2)   |
| O(24)#2-Cs(4)-O(18)     | 44.9(2)  | O(27)-Cs(5)-O(12)#7   | 131.9(2)   |
| O(15)#4-Cs(4)-O(18)     | 175.2(2) | O(23)-Cs(5)-O(12)#7   | 114.8(2)   |
| O(20)#7-Cs(4)-O(18)     | 89.3(2)  | O(24)#7-Cs(5)-O(17)#7 | 71.9(2)    |
| O(17)-Cs(4)-O(18)       | 90.8(2)  | O(19)-Cs(5)-O(17)#7   | 87.8(2)    |
| O(29)#13-Cs(4)-O(18)    | 120.1(2) | O(27)-Cs(5)-O(17)#7   | 157.7(2)   |
| O(2)#7-Cs(4)-O(28)#13   | 69.7(2)  | O(23)-Cs(5)-O(17)#7   | 78.5(2)    |
| O(13)#4-Cs(4)-O(28)#13  | 107.7(2) | O(12)#7-Cs(5)-O(17)#7 | 45.7(2)    |
| O(26)#4-Cs(4)-O(28)#13  | 113.6(3) | O(24)#7-Cs(5)-O(18)   | 92.9(2)    |
| O(24)#2-Cs(4)-O(28)#13  | 73.7(2)  | O(19)-Cs(5)-O(18)     | 113.5(2)   |
| O(15)#4-Cs(4)-O(28)#13  | 62.3(3)  | O(27)-Cs(5)-O(18)     | 55.8(2)    |
| O(20)#7-Cs(4)-O(28)#13  | 67.5(2)  | O(23)-Cs(5)-O(18)     | 141.7(2)   |
| O(17)-Cs(4)-O(28)#13    | 149.5(2) | O(12)#7-Cs(5)-O(18)   | 81.5(2)    |
| O(29)#13-Cs(4)-O(28)#13 | 43.6(2)  | O(17)#7-Cs(5)-O(18)   | 127.1(2)   |
| O(18)-Cs(4)-O(28)#13    | 118.1(2) | O(24)#7-Cs(5)-O(16)   | 96.7(2)    |
| O(5)#1-Bi(1)-O(6)       | 84.0(3)  | O(19)-Cs(5)-O(16)     | 93.6(2)    |
| O(5)#1-Bi(1)-O(9)#2     | 85.5(3)  | O(27)-Cs(5)-O(16)     | 43.4(2)    |
| O(6)-Bi(1)-O(9)#2       | 85.4(3)  | O(23)-Cs(5)-O(16)     | 73.9(2)    |
| O(5)#1-Bi(1)-O(4)#2     | 79.8(3)  | O(12)#7-Cs(5)-O(16)   | 152.1(2)   |
| O(6)-Bi(1)-O(4)#2       | 155.4(3) | O(17)#7-Cs(5)-O(16)   | 152.4(2)   |
| O(9)#2-Bi(1)-O(4)#2     | 111.4(3) | O(18)-Cs(5)-O(16)     | 77.3(2)    |

|                       |          |                     |          |
|-----------------------|----------|---------------------|----------|
| O(5)#1-Bi(1)-O(11)#3  | 87.2(3)  | O(24)#7-Cs(5)-O(22) | 130.1(2) |
| O(6)-Bi(1)-O(11)#3    | 86.5(3)  | O(19)-Cs(5)-O(22)   | 53.9(2)  |
| O(9)#2-Bi(1)-O(11)#3  | 169.6(3) | O(27)-Cs(5)-O(22)   | 41.9(2)  |
| O(4)#2-Bi(1)-O(11)#3  | 74.4(3)  | O(23)-Cs(5)-O(22)   | 76.2(2)  |
| O(18)-Bi(2)-O(26)#4   | 76.2(4)  | O(12)#7-Cs(5)-O(22) | 163.6(2) |
| O(18)-Bi(2)-O(12)#2   | 84.1(3)  | O(17)#7-Cs(5)-O(22) | 131.8(2) |
| O(26)#4-Bi(2)-O(12)#2 | 92.5(4)  | O(18)-Cs(5)-O(22)   | 97.2(2)  |
| O(18)-Bi(2)-O(27)     | 84.5(4)  | O(16)-Cs(5)-O(22)   | 39.9(2)  |
| O(26)#4-Bi(2)-O(27)   | 86.0(4)  | O(24)#7-Cs(5)-O(15) | 107.2(2) |
| O(12)#2-Bi(2)-O(27)   | 168.5(4) | O(19)-Cs(5)-O(15)   | 51.4(2)  |
| O(18)-Bi(2)-O(29)     | 80.4(4)  | O(27)-Cs(5)-O(15)   | 93.6(2)  |
| O(26)#4-Bi(2)-O(29)   | 154.6(4) | O(23)-Cs(5)-O(15)   | 42.0(2)  |
| O(12)#2-Bi(2)-O(29)   | 94.8(3)  | O(12)#7-Cs(5)-O(15) | 127.6(2) |
| O(27)-Bi(2)-O(29)     | 82.1(3)  | O(17)#7-Cs(5)-O(15) | 82.1(2)  |
| O(18)-Bi(2)-O(20)#2   | 167.2(3) | O(18)-Cs(5)-O(15)   | 149.3(2) |
| O(26)#4-Bi(2)-O(20)#2 | 99.8(4)  | O(16)-Cs(5)-O(15)   | 77.5(2)  |
| O(12)#2-Bi(2)-O(20)#2 | 83.9(3)  | O(22)-Cs(5)-O(15)   | 52.1(2)  |
| O(27)-Bi(2)-O(20)#2   | 107.6(4) | O(9)-P(1)-O(8)      | 110.3(5) |
| O(29)-Bi(2)-O(20)#2   | 105.2(4) | O(9)-P(1)-O(3)      | 111.6(4) |
| O(26)#4-Bi(2)-O(12)#2 | 92.5(4)  | O(8)-P(1)-O(3)      | 110.6(5) |
| O(22)-Bi(3)-O(15)     | 92.3(4)  | O(9)-P(1)-O(5)      | 110.8(5) |
| O(22)-Bi(3)-O(8)      | 81.0(3)  | O(8)-P(1)-O(5)      | 108.9(4) |
| O(15)-Bi(3)-O(8)      | 89.7(3)  | O(3)-P(1)-O(5)      | 104.5(4) |
| O(22)-Bi(3)-O(25)     | 86.5(4)  | O(28)-P(2)-O(21)    | 112.5(7) |
| O(15)-Bi(3)-O(25)     | 176.1(4) | O(28)-P(2)-O(29)    | 115.4(7) |
| O(8)-Bi(3)-O(25)      | 93.7(3)  | O(21)-P(2)-O(29)    | 107.1(8) |
| O(22)-Bi(3)-O(19)     | 83.9(3)  | O(28)-P(2)-O(16)    | 105.7(5) |
| O(15)-Bi(3)-O(19)     | 79.9(4)  | O(21)-P(2)-O(16)    | 108.7(6) |
| O(8)-Bi(3)-O(19)      | 161.3(3) | O(29)-P(2)-O(16)    | 107.3(6) |
| O(25)-Bi(3)-O(19)     | 96.4(3)  | O(17)-P(3)-O(19)    | 114.5(5) |
| O(10)#8-Bi(4)-O(3)#3  | 88.9(3)  | O(17)-P(3)-O(12)    | 113.5(5) |
| O(10)#8-Bi(4)-O(7)    | 87.9(3)  | O(19)-P(3)-O(12)    | 110.9(5) |
| O(3)#3-Bi(4)-O(7)     | 83.4(3)  | O(17)-P(3)-O(13)    | 107.8(5) |
| O(10)#8-Bi(4)-O(21)#9 | 85.9(4)  | O(19)-P(3)-O(13)    | 105.3(5) |
| O(3)#3-Bi(4)-O(21)#9  | 77.3(3)  | O(12)-P(3)-O(13)    | 103.8(4) |
| O(7)-Bi(4)-O(21)#9    | 159.8(3) | O(23)-P(4)-O(4)     | 116.4(5) |
| O(10)#8-Bi(4)-O(1)#9  | 90.2(5)  | O(23)-P(4)-O(15)    | 112.6(6) |
| O(3)#3-Bi(4)-O(1)#9   | 156.9(3) | O(4)-P(4)-O(15)     | 112.4(5) |
| O(7)-Bi(4)-O(1)#9     | 119.7(4) | O(23)-P(4)-O(2)#9   | 105.4(5) |
| O(21)#9-Bi(4)-O(1)#9  | 79.6(4)  | O(4)-P(4)-O(2)#9    | 107.1(4) |
| O(1)-P(6)-O(22)       | 116.7(8) | O(15)-P(4)-O(2)#9   | 101.2(5) |
| O(1)-P(6)-O(27)       | 114.4(9) | O(14)-P(5)-O(7)     | 109.3(5) |
| O(22)-P(6)-O(27)      | 109.2(6) | O(14)-P(5)-O(6)     | 111.1(5) |
| O(1)-P(6)-O(16)       | 109.0(7) | O(7)-P(5)-O(6)      | 110.4(4) |

|                  |          |                     |          |
|------------------|----------|---------------------|----------|
| O(22)-P(6)-O(16) | 102.5(5) | O(14)-P(5)-O(10)    | 114.6(5) |
| O(27)-P(6)-O(16) | 103.4(6) | O(7)-P(5)-O(10)     | 108.8(5) |
| O(20)-P(7)-O(25) | 114.0(6) | O(6)-P(5)-O(10)     | 102.4(4) |
| O(20)-P(7)-O(11) | 113.2(5) | O(24)-P(8)-O(26)    | 113.8(6) |
| O(25)-P(7)-O(11) | 111.5(6) | O(24)-P(8)-O(18)#11 | 115.5(6) |
| O(20)-P(7)-O(2)  | 103.8(5) | O(26)-P(8)-O(18)#11 | 108.5(6) |
| O(25)-P(7)-O(2)  | 105.5(5) | O(24)-P(8)-O(13)    | 110.8(5) |
| O(11)-P(7)-O(2)  | 108.0(5) | O(26)-P(8)-O(13)    | 101.1(5) |
|                  |          | O(18)#11-P(8)-O(13) | 106.0(5) |

Symmetry transformations used to generate equivalent atoms:

#1 -x, -y+2, -z    #2 x-1, y, z    #3 x-1, y+1, z  
 #4 -x+1, y-1/2, -z+1/2    #5 x, y-1, z    #6 x+1, y-1, z  
 #7 -x+1, y+1/2, -z+1/2    #8 -x, -y+3, -z  
 #9 x, y+1, z    #10 -x-1, -y+3, -z    #11 x+1, y, z  
 #12 -x+1, -y+2, -z    #13 -x, y-1/2, -z+1/2  
 #14 -x, y+1/2, -z+1/2

**Table S6.** Bond lengths (Å) and angles (°) for RbCs<sub>5</sub>Bi<sub>4</sub>(PO<sub>4</sub>)<sub>2</sub>(P<sub>2</sub>O<sub>7</sub>)<sub>3</sub>.

|                |           |                |           |
|----------------|-----------|----------------|-----------|
| Bi(1)-O(3)     | 2.164(11) | Cs(1)-O(19)    | 3.080(14) |
| Bi(1)-O(1)     | 2.174(11) | Cs(1)-O(6)#6   | 3.110(12) |
| Bi(1)-O(10)#1  | 2.260(12) | Cs(1)-O(24)    | 3.120(14) |
| Bi(1)-O(8)#2   | 2.562(12) | Cs(1)-O(15)#6  | 3.188(13) |
| Bi(1)-O(12)#2  | 2.564(13) | Cs(1)-O(7)     | 3.214(12) |
| Bi(2)-O(29)    | 2.187(15) | Cs(1)-O(17)    | 3.260(13) |
| Bi(2)-O(21)#3  | 2.201(12) | Cs(1)-O(5)     | 3.302(12) |
| Bi(2)-O(5)#4   | 2.297(13) | Cs(1)-O(15)    | 3.394(13) |
| Bi(2)-O(24)    | 2.401(14) | Cs(2)-O(1)     | 3.051(11) |
| Bi(2)-O(20)    | 2.442(16) | Cs(2)-O(10)#1  | 3.062(12) |
| Bi(2)-O(11)#4  | 2.532(13) | Cs(2)-O(12)#7  | 3.073(13) |
| Bi(3)-O(16)    | 2.198(14) | Cs(2)-O(13)    | 3.105(13) |
| Bi(3)-O(25)#7  | 2.208(15) | Cs(2)-O(18)    | 3.277(12) |
| Bi(3)-O(14)    | 2.261(12) | Cs(2)-O(1)#10  | 3.294(11) |
| Bi(3)-O(17)    | 2.403(14) | Cs(2)-O(14)    | 3.318(13) |
| Bi(3)-O(23)    | 2.461(13) | Cs(2)-O(9)#10  | 3.329(13) |
| Bi(3)-O(28)#8  | 2.662(17) | Cs(2)-O(16)    | 3.588(13) |
| Bi(4)-O(18)#8  | 2.130(12) | Cs(3)-O(4)#2   | 2.878(11) |
| Bi(4)-O(2)     | 2.195(11) | Cs(3)-O(9)#8   | 3.001(13) |
| Bi(4)-O(4)#2   | 2.198(11) | Cs(3)-O(12)#2  | 3.017(13) |
| Bi(4)-O(28)#8  | 2.498(18) | Cs(3)-O(17)#2  | 3.033(13) |
| Bi(4)-O(26)#8  | 2.641(16) | Cs(3)-O(2)     | 3.109(11) |
| Bi(4)-O(8)     | 2.745(12) | Cs(3)-O(26)#2  | 3.234(16) |
| Rb(1)-O(19)#5  | 2.753(15) | Cs(3)-O(2)#2   | 3.389(11) |
| Rb(1)-O(27)#10 | 2.830(17) | Cs(3)-O(3)     | 3.427(12) |
| Rb(1)-O(9)     | 2.836(13) | Cs(3)-O(14)#2  | 3.446(12) |
| Rb(1)-O(11)#2  | 2.914(14) | Cs(3)-O(3)#2   | 3.463(12) |
| Rb(1)-O(22)#5  | 2.968(13) | Cs(3)-O(8)#2   | 3.600(13) |
| Rb(1)-O(26)#5  | 3.154(16) | Cs(4)-O(22)#7  | 3.083(14) |
| Rb(1)-O(8)#2   | 3.369(13) | Cs(4)-O(19)#7  | 3.136(14) |
| P(1)-O(22)     | 1.474(14) | Cs(4)-O(23)    | 3.147(14) |
| P(1)-O(21)     | 1.533(12) | Cs(4)-O(5)#11  | 3.217(12) |
| P(1)-O(29)     | 1.538(16) | Cs(4)-O(24)    | 3.242(14) |
| P(1)-O(6)#6    | 1.628(13) | Cs(4)-O(15)#11 | 3.341(13) |
| P(2)-O(9)      | 1.495(13) | Cs(4)-O(21)#3  | 3.350(12) |
| P(2)-O(4)      | 1.532(12) | Cs(4)-O(16)    | 3.537(13) |
| P(2)-O(1)      | 1.555(11) | Cs(4)-O(13)    | 3.560(13) |
| P(2)-O(18)     | 1.568(12) | Cs(4)-O(15)    | 3.704(13) |
| P(3)-O(15)     | 1.486(14) | Cs(5)-O(7)#7   | 3.021(11) |
| P(3)-O(23)     | 1.511(14) | Cs(5)-O(6)     | 3.037(12) |
| P(3)-O(5)      | 1.521(13) | Cs(5)-O(29)#11 | 3.183(15) |
| P(3)-O(6)      | 1.608(13) | Cs(5)-O(22)#12 | 3.194(14) |
| P(4)-O(19)     | 1.481(15) | Cs(5)-O(20)#8  | 3.213(16) |



|                        |           |                       |           |
|------------------------|-----------|-----------------------|-----------|
| P(4)-O(12)             | 1.502(13) | Cs(5)-O(25)#7         | 3.280(14) |
| P(4)-O(25)             | 1.523(15) | Cs(5)-O(15)#11        | 3.373(13) |
| P(4)-O(7)              | 1.627(12) | Cs(5)-O(21)#12        | 3.435(12) |
| P(5)-O(27)             | 1.485(17) | Cs(5)-O(11)#7         | 3.455(13) |
| P(5)-O(20)             | 1.503(16) | Cs(5)-O(23)           | 3.666(13) |
| P(5)-O(28)             | 1.526(17) | P(7)-O(11)            | 1.507(14) |
| P(5)-O(13)             | 1.604(14) | P(7)-O(17)            | 1.515(14) |
| P(6)-O(26)             | 1.442(16) | P(7)-O(8)             | 1.522(13) |
| P(6)-O(24)             | 1.487(14) | P(7)-O(7)             | 1.596(12) |
| P(6)-O(16)             | 1.502(14) | P(8)-O(10)            | 1.528(12) |
| P(6)-O(13)             | 1.615(14) | P(8)-O(2)             | 1.533(12) |
|                        |           | P(8)-O(14)            | 1.539(13) |
| O(3)-Bi(1)-O(1)        | 85.3(4)   | P(8)-O(3)             | 1.551(12) |
| O(3)-Bi(1)-O(10)#1     | 86.7(4)   | O(29)-Bi(2)-O(21)#3   | 78.2(5)   |
| O(1)-Bi(1)-O(10)#1     | 84.3(4)   | O(29)-Bi(2)-O(5)#4    | 92.3(5)   |
| O(3)-Bi(1)-O(8)#2      | 89.1(4)   | O(21)#3-Bi(2)-O(5)#4  | 84.7(4)   |
| O(1)-Bi(1)-O(8)#2      | 88.5(4)   | O(29)-Bi(2)-O(24)     | 85.6(5)   |
| O(10)#1-Bi(1)-O(8)#2   | 171.9(4)  | O(21)#3-Bi(2)-O(24)   | 88.7(5)   |
| O(3)-Bi(1)-O(12)#2     | 80.6(4)   | O(5)#4-Bi(2)-O(24)    | 173.4(5)  |
| O(1)-Bi(1)-O(12)#2     | 157.5(4)  | O(29)-Bi(2)-O(20)     | 153.5(5)  |
| O(10)#1-Bi(1)-O(12)#2  | 112.0(4)  | O(21)#3-Bi(2)-O(20)   | 78.8(5)   |
| O(8)#2-Bi(1)-O(12)#2   | 74.0(4)   | O(5)#4-Bi(2)-O(20)    | 98.5(5)   |
| O(16)-Bi(3)-O(25)#7    | 91.9(5)   | O(24)-Bi(2)-O(20)     | 80.9(5)   |
| O(16)-Bi(3)-O(14)      | 81.5(5)   | O(29)-Bi(2)-O(11)#4   | 99.1(5)   |
| O(25)#7-Bi(3)-O(14)    | 88.4(5)   | O(21)#3-Bi(2)-O(11)#4 | 167.6(4)  |
| O(16)-Bi(3)-O(17)      | 87.0(5)   | O(5)#4-Bi(2)-O(11)#4  | 83.3(4)   |
| O(25)#7-Bi(3)-O(17)    | 177.8(5)  | O(24)-Bi(2)-O(11)#4   | 103.2(4)  |
| O(14)-Bi(3)-O(17)      | 93.3(4)   | O(20)-Bi(2)-O(11)#4   | 106.1(5)  |
| O(16)-Bi(3)-O(23)      | 83.7(5)   | O(18)#8-Bi(4)-O(2)    | 88.7(4)   |
| O(25)#7-Bi(3)-O(23)    | 80.9(5)   | O(18)#8-Bi(4)-O(4)#2  | 89.7(4)   |
| O(14)-Bi(3)-O(23)      | 161.4(5)  | O(2)-Bi(4)-O(4)#2     | 82.8(4)   |
| O(17)-Bi(3)-O(23)      | 97.1(4)   | O(18)#8-Bi(4)-O(28)#8 | 90.2(5)   |
| O(16)-Bi(3)-O(28)#8    | 156.2(5)  | O(2)-Bi(4)-O(28)#8    | 77.3(5)   |
| O(25)#7-Bi(3)-O(28)#8  | 95.0(5)   | O(4)#2-Bi(4)-O(28)#8  | 160.1(5)  |
| O(14)-Bi(3)-O(28)#8    | 75.9(5)   | O(18)#8-Bi(4)-O(26)#8 | 85.2(5)   |
| O(17)-Bi(3)-O(28)#8    | 86.8(5)   | O(2)-Bi(4)-O(26)#8    | 156.1(5)  |
| O(23)-Bi(3)-O(28)#8    | 119.9(5)  | O(4)#2-Bi(4)-O(26)#8  | 120.1(5)  |
| O(19)#5-Rb(1)-O(27)#10 | 104.5(5)  | O(28)#8-Bi(4)-O(26)#8 | 79.7(5)   |
| O(19)#5-Rb(1)-O(9)     | 98.8(4)   | O(18)#8-Bi(4)-O(8)    | 165.6(4)  |
| O(27)#10-Rb(1)-O(9)    | 88.8(4)   | O(2)-Bi(4)-O(8)       | 87.1(4)   |
| O(19)#5-Rb(1)-O(11)#2  | 148.9(4)  | O(4)#2-Bi(4)-O(8)     | 76.1(4)   |
| O(27)#10-Rb(1)-O(11)#2 | 89.7(4)   | O(28)#8-Bi(4)-O(8)    | 102.2(5)  |
| O(9)-Rb(1)-O(11)#2     | 109.3(4)  | O(26)#8-Bi(4)-O(8)    | 104.0(4)  |
| O(19)#5-Rb(1)-O(22)#5  | 74.8(4)   | O(19)-Cs(1)-O(6)#6    | 98.9(3)   |

|                        |          |                       |          |
|------------------------|----------|-----------------------|----------|
| O(27)#10-Rb(1)-O(22)#5 | 95.8(4)  | O(19)-Cs(1)-O(24)     | 105.1(4) |
| O(9)-Rb(1)-O(22)#5     | 172.9(4) | O(6)#6-Cs(1)-O(24)    | 94.2(3)  |
| O(11)#2-Rb(1)-O(22)#5  | 76.3(4)  | O(19)-Cs(1)-O(15)#6   | 79.7(4)  |
| O(19)#5-Rb(1)-O(26)#5  | 102.0(4) | O(6)#6-Cs(1)-O(15)#6  | 46.9(3)  |
| O(27)#10-Rb(1)-O(26)#5 | 143.7(5) | O(24)-Cs(1)-O(15)#6   | 140.5(4) |
| O(9)-Rb(1)-O(26)#5     | 62.7(4)  | O(19)-Cs(1)-O(7)      | 46.6(3)  |
| O(11)#2-Rb(1)-O(26)#5  | 80.0(4)  | O(6)#6-Cs(1)-O(7)     | 129.9(3) |
| O(22)#5-Rb(1)-O(26)#5  | 115.1(4) | O(24)-Cs(1)-O(7)      | 125.6(3) |
| O(19)#5-Rb(1)-O(8)#2   | 164.5(4) | O(15)#6-Cs(1)-O(7)    | 86.7(3)  |
| O(27)#10-Rb(1)-O(8)#2  | 67.1(4)  | O(19)-Cs(1)-O(17)     | 77.9(4)  |
| O(9)-Rb(1)-O(8)#2      | 68.9(3)  | O(6)#6-Cs(1)-O(17)    | 175.1(3) |
| O(11)#2-Rb(1)-O(8)#2   | 46.4(3)  | O(24)-Cs(1)-O(17)     | 90.3(4)  |
| O(22)#5-Rb(1)-O(8)#2   | 117.9(3) | O(15)#6-Cs(1)-O(17)   | 128.4(3) |
| O(26)#5-Rb(1)-O(8)#2   | 81.1(4)  | O(7)-Cs(1)-O(17)      | 45.2(3)  |
| O(1)-Cs(2)-O(10)#1     | 58.3(3)  | O(19)-Cs(1)-O(5)      | 130.3(4) |
| O(1)-Cs(2)-O(12)#7     | 130.4(3) | O(6)#6-Cs(1)-O(5)     | 107.0(3) |
| O(10)#1-Cs(2)-O(12)#7  | 74.4(3)  | O(24)-Cs(1)-O(5)      | 114.2(3) |
| O(1)-Cs(2)-O(13)       | 116.6(3) | O(15)#6-Cs(1)-O(5)    | 88.0(3)  |
| O(10)#1-Cs(2)-O(13)    | 164.2(3) | O(7)-Cs(1)-O(5)       | 85.0(3)  |
| O(12)#7-Cs(2)-O(13)    | 104.8(3) | O(17)-Cs(1)-O(5)      | 72.9(3)  |
| O(1)-Cs(2)-O(18)       | 45.3(3)  | O(19)-Cs(1)-O(15)     | 169.6(4) |
| O(10)#1-Cs(2)-O(18)    | 103.6(3) | O(6)#6-Cs(1)-O(15)    | 77.4(3)  |
| O(12)#7-Cs(2)-O(18)    | 163.8(3) | O(24)-Cs(1)-O(15)     | 85.0(3)  |
| O(13)-Cs(2)-O(18)      | 72.6(3)  | O(15)#6-Cs(1)-O(15)   | 90.85(4) |
| O(1)-Cs(2)-O(1)#10     | 86.0(3)  | O(7)-Cs(1)-O(15)      | 129.1(3) |
| O(10)#1-Cs(2)-O(1)#10  | 99.0(3)  | O(17)-Cs(1)-O(15)     | 105.1(3) |
| O(12)#7-Cs(2)-O(1)#10  | 117.2(3) | O(5)-Cs(1)-O(15)      | 44.1(3)  |
| O(13)-Cs(2)-O(1)#10    | 95.3(3)  | O(4)#2-Cs(3)-O(9)#8   | 66.5(3)  |
| O(18)-Cs(2)-O(1)#10    | 79.0(3)  | O(4)#2-Cs(3)-O(12)#2  | 132.4(3) |
| O(1)-Cs(2)-O(14)       | 85.7(3)  | O(9)#8-Cs(3)-O(12)#2  | 77.9(4)  |
| O(10)#1-Cs(2)-O(14)    | 74.5(3)  | O(4)#2-Cs(3)-O(17)#2  | 152.4(3) |
| O(12)#7-Cs(2)-O(14)    | 67.1(3)  | O(9)#8-Cs(3)-O(17)#2  | 124.8(4) |
| O(13)-Cs(2)-O(14)      | 90.6(3)  | O(12)#2-Cs(3)-O(17)#2 | 74.6(4)  |
| O(18)-Cs(2)-O(14)      | 96.8(3)  | O(4)#2-Cs(3)-O(2)     | 57.9(3)  |
| O(1)#10-Cs(2)-O(14)    | 171.3(3) | O(9)#8-Cs(3)-O(2)     | 80.9(3)  |
| O(1)-Cs(2)-O(9)#10     | 116.5(3) | O(12)#2-Cs(3)-O(2)    | 86.9(3)  |
| O(10)#1-Cs(2)-O(9)#10  | 87.9(3)  | O(17)#2-Cs(3)-O(2)    | 142.4(3) |
| O(12)#7-Cs(2)-O(9)#10  | 72.3(3)  | O(4)#2-Cs(3)-O(26)#2  | 82.8(4)  |
| O(13)-Cs(2)-O(9)#10    | 107.1(3) | O(9)#8-Cs(3)-O(26)#2  | 60.1(4)  |
| O(18)-Cs(2)-O(9)#10    | 123.8(3) | O(12)#2-Cs(3)-O(26)#2 | 106.4(4) |
| O(1)#10-Cs(2)-O(9)#10  | 44.9(3)  | O(17)#2-Cs(3)-O(26)#2 | 83.4(4)  |
| O(14)-Cs(2)-O(9)#10    | 138.7(3) | O(2)-Cs(3)-O(26)#2    | 133.7(4) |
| O(1)-Cs(2)-O(16)       | 110.9(3) | O(4)#2-Cs(3)-O(2)#2   | 99.6(3)  |
| O(10)#1-Cs(2)-O(16)    | 124.1(3) | O(9)#8-Cs(3)-O(2)#2   | 165.7(3) |

|                        |          |                         |          |
|------------------------|----------|-------------------------|----------|
| O(12)#7-Cs(2)-O(16)    | 82.7(3)  | O(12)#2-Cs(3)-O(2)#2    | 111.3(3) |
| O(13)-Cs(2)-O(16)      | 41.2(3)  | O(17)#2-Cs(3)-O(2)#2    | 69.2(3)  |
| O(18)-Cs(2)-O(16)      | 85.6(3)  | O(2)-Cs(3)-O(2)#2       | 88.5(3)  |
| O(1)#10-Cs(2)-O(16)    | 136.6(3) | O(26)#2-Cs(3)-O(2)#2    | 124.2(3) |
| O(14)-Cs(2)-O(16)      | 49.7(3)  | O(4)#2-Cs(3)-O(3)       | 101.1(3) |
| O(9)#10-Cs(2)-O(16)    | 132.1(3) | O(9)#8-Cs(3)-O(3)       | 103.1(3) |
| O(22)#7-Cs(4)-O(19)#7  | 68.0(4)  | O(12)#2-Cs(3)-O(3)      | 56.5(3)  |
| O(22)#7-Cs(4)-O(23)    | 152.1(4) | O(17)#2-Cs(3)-O(3)      | 100.1(3) |
| O(19)#7-Cs(4)-O(23)    | 89.7(4)  | O(2)-Cs(3)-O(3)         | 43.5(3)  |
| O(22)#7-Cs(4)-O(5)#11  | 65.1(3)  | O(26)#2-Cs(3)-O(3)      | 159.9(4) |
| O(19)#7-Cs(4)-O(5)#11  | 113.1(3) | O(2)#2-Cs(3)-O(3)       | 75.0(3)  |
| O(23)-Cs(4)-O(5)#11    | 112.5(3) | O(4)#2-Cs(3)-O(14)#2    | 91.4(3)  |
| O(22)#7-Cs(4)-O(24)    | 127.4(4) | O(9)#8-Cs(3)-O(14)#2    | 136.3(3) |
| O(19)#7-Cs(4)-O(24)    | 110.8(4) | O(12)#2-Cs(3)-O(14)#2   | 135.8(3) |
| O(23)-Cs(4)-O(24)      | 75.3(4)  | O(17)#2-Cs(3)-O(14)#2   | 62.8(3)  |
| O(5)#11-Cs(4)-O(24)    | 135.3(3) | O(2)-Cs(3)-O(14)#2      | 120.0(3) |
| O(22)#7-Cs(4)-O(15)#11 | 71.6(3)  | O(26)#2-Cs(3)-O(14)#2   | 80.8(4)  |
| O(19)#7-Cs(4)-O(15)#11 | 76.6(3)  | O(2)#2-Cs(3)-O(14)#2    | 43.5(3)  |
| O(23)-Cs(4)-O(15)#11   | 87.4(3)  | O(3)-Cs(3)-O(14)#2      | 118.5(3) |
| O(5)#11-Cs(4)-O(15)#11 | 45.0(3)  | O(4)#2-Cs(3)-O(3)#2     | 59.8(3)  |
| O(24)-Cs(4)-O(15)#11   | 160.9(3) | O(9)#8-Cs(3)-O(3)#2     | 125.7(3) |
| O(22)#7-Cs(4)-O(21)#3  | 90.5(3)  | O(12)#2-Cs(3)-O(3)#2    | 148.5(3) |
| O(19)#7-Cs(4)-O(21)#3  | 143.2(3) | O(17)#2-Cs(3)-O(3)#2    | 101.0(3) |
| O(23)-Cs(4)-O(21)#3    | 117.1(3) | O(2)-Cs(3)-O(3)#2       | 78.1(3)  |
| O(5)#11-Cs(4)-O(21)#3  | 81.0(3)  | O(26)#2-Cs(3)-O(3)#2    | 103.9(4) |
| O(24)-Cs(4)-O(21)#3    | 58.5(3)  | O(2)#2-Cs(3)-O(3)#2     | 41.7(3)  |
| O(15)#11-Cs(4)-O(21)#3 | 125.9(3) | O(3)-Cs(3)-O(3)#2       | 94.9(3)  |
| O(22)#7-Cs(4)-O(16)    | 127.7(3) | O(14)#2-Cs(3)-O(3)#2    | 42.8(3)  |
| O(19)#7-Cs(4)-O(16)    | 73.7(3)  | O(4)#2-Cs(3)-O(8)#2     | 150.5(3) |
| O(23)-Cs(4)-O(16)      | 55.2(3)  | O(9)#8-Cs(3)-O(8)#2     | 132.4(3) |
| O(5)#11-Cs(4)-O(16)    | 166.8(3) | O(12)#2-Cs(3)-O(8)#2    | 54.7(3)  |
| O(24)-Cs(4)-O(16)      | 42.2(3)  | O(17)#2-Cs(3)-O(8)#2    | 43.7(3)  |
| O(15)#11-Cs(4)-O(16)   | 131.4(3) | O(2)-Cs(3)-O(8)#2       | 99.0(3)  |
| O(21)#3-Cs(4)-O(16)    | 100.2(3) | O(26)#2-Cs(3)-O(8)#2    | 125.2(4) |
| O(22)#7-Cs(4)-O(13)    | 94.8(3)  | O(2)#2-Cs(3)-O(8)#2     | 58.6(3)  |
| O(19)#7-Cs(4)-O(13)    | 73.4(3)  | O(3)-Cs(3)-O(8)#2       | 56.5(3)  |
| O(23)-Cs(4)-O(13)      | 94.6(3)  | O(14)#2-Cs(3)-O(8)#2    | 85.0(3)  |
| O(5)#11-Cs(4)-O(13)    | 151.7(3) | O(3)#2-Cs(3)-O(8)#2     | 100.2(3) |
| O(24)-Cs(4)-O(13)      | 42.6(3)  | O(7)#7-Cs(5)-O(6)       | 135.5(3) |
| O(15)#11-Cs(4)-O(13)   | 150.0(3) | O(7)#7-Cs(5)-O(29)#11   | 176.6(4) |
| O(21)#3-Cs(4)-O(13)    | 79.4(3)  | O(6)-Cs(5)-O(29)#11     | 46.5(4)  |
| O(16)-Cs(4)-O(13)      | 39.5(3)  | O(7)#7-Cs(5)-O(22)#12   | 107.7(3) |
| O(22)#7-Cs(4)-O(15)    | 146.0(3) | O(6)-Cs(5)-O(22)#12     | 113.3(3) |
| O(19)#7-Cs(4)-O(15)    | 128.6(3) | O(29)#11-Cs(5)-O(22)#12 | 71.8(4)  |

|                      |          |                         |          |
|----------------------|----------|-------------------------|----------|
| O(23)-Cs(4)-O(15)    | 42.0(3)  | O(7)#7-Cs(5)-O(20)#8    | 98.0(4)  |
| O(5)#11-Cs(4)-O(15)  | 80.9(3)  | O(6)-Cs(5)-O(20)#8      | 66.7(4)  |
| O(24)-Cs(4)-O(15)    | 78.4(3)  | O(29)#11-Cs(5)-O(20)#8  | 85.4(4)  |
| O(15)#11-Cs(4)-O(15) | 83.32(4) | O(22)#12-Cs(5)-O(20)#8  | 89.1(4)  |
| O(21)#3-Cs(4)-O(15)  | 86.0(3)  | O(7)#7-Cs(5)-O(25)#7    | 45.2(3)  |
| O(16)-Cs(4)-O(15)    | 86.1(3)  | O(6)-Cs(5)-O(25)#7      | 93.3(3)  |
| O(13)-Cs(4)-O(15)    | 117.6(3) | O(29)#11-Cs(5)-O(25)#7  | 137.8(4) |
| O(22)-P(1)-O(21)     | 115.8(8) | O(22)#12-Cs(5)-O(25)#7  | 130.4(3) |
| O(22)-P(1)-O(29)     | 113.5(8) | O(20)#8-Cs(5)-O(25)#7   | 63.1(4)  |
| O(21)-P(1)-O(29)     | 108.0(8) | O(7)#7-Cs(5)-O(15)#11   | 86.6(3)  |
| O(22)-P(1)-O(6)#6    | 110.8(7) | O(6)-Cs(5)-O(15)#11     | 78.6(3)  |
| O(21)-P(1)-O(6)#6    | 105.8(7) | O(29)#11-Cs(5)-O(15)#11 | 91.3(3)  |
| O(29)-P(1)-O(6)#6    | 101.8(8) | O(22)#12-Cs(5)-O(15)#11 | 132.3(3) |
| O(9)-P(2)-O(4)       | 108.8(7) | O(20)#8-Cs(5)-O(15)#11  | 134.8(4) |
| O(9)-P(2)-O(1)       | 111.9(7) | O(25)#7-Cs(5)-O(15)#11  | 92.2(3)  |
| O(4)-P(2)-O(1)       | 110.1(6) | O(7)#7-Cs(5)-O(21)#12   | 128.0(3) |
| O(9)-P(2)-O(18)      | 113.4(7) | O(6)-Cs(5)-O(21)#12     | 94.1(3)  |
| O(4)-P(2)-O(18)      | 109.3(6) | O(29)#11-Cs(5)-O(21)#12 | 49.2(3)  |
| O(1)-P(2)-O(18)      | 103.2(6) | O(22)#12-Cs(5)-O(21)#12 | 45.0(3)  |
| O(15)-P(3)-O(23)     | 113.9(8) | O(20)#8-Cs(5)-O(21)#12  | 119.5(4) |
| O(15)-P(3)-O(5)      | 113.5(7) | O(25)#7-Cs(5)-O(21)#12  | 172.5(3) |
| O(23)-P(3)-O(5)      | 111.3(7) | O(15)#11-Cs(5)-O(21)#12 | 90.0(3)  |
| O(15)-P(3)-O(6)      | 108.1(7) | O(7)#7-Cs(5)-O(11)#7    | 43.9(3)  |
| O(23)-P(3)-O(6)      | 104.9(7) | O(6)-Cs(5)-O(11)#7      | 176.8(3) |
| O(5)-P(3)-O(6)       | 104.2(7) | O(29)#11-Cs(5)-O(11)#7  | 134.4(3) |
| O(19)-P(4)-O(12)     | 115.3(8) | O(22)#12-Cs(5)-O(11)#7  | 66.1(3)  |
| O(19)-P(4)-O(25)     | 114.2(8) | O(20)#8-Cs(5)-O(11)#7   | 110.1(4) |
| O(12)-P(4)-O(25)     | 111.2(8) | O(25)#7-Cs(5)-O(11)#7   | 85.0(3)  |
| O(19)-P(4)-O(7)      | 106.6(7) | O(15)#11-Cs(5)-O(11)#7  | 104.1(3) |
| O(12)-P(4)-O(7)      | 107.1(7) | O(21)#12-Cs(5)-O(11)#7  | 87.5(3)  |
| O(25)-P(4)-O(7)      | 101.0(7) | O(7)#7-Cs(5)-O(23)      | 94.1(3)  |
| O(27)-P(5)-O(20)     | 117.7(9) | O(6)-Cs(5)-O(23)        | 42.0(3)  |
| O(27)-P(5)-O(28)     | 111.5(9) | O(29)#11-Cs(5)-O(23)    | 88.1(3)  |
| O(20)-P(5)-O(28)     | 105.4(9) | O(22)#12-Cs(5)-O(23)    | 141.4(3) |
| O(27)-P(5)-O(13)     | 105.9(8) | O(20)#8-Cs(5)-O(23)     | 55.8(4)  |
| O(20)-P(5)-O(13)     | 108.9(8) | O(25)#7-Cs(5)-O(23)     | 51.5(3)  |
| O(28)-P(5)-O(13)     | 107.1(9) | O(15)#11-Cs(5)-O(23)    | 79.1(3)  |
| O(26)-P(6)-O(24)     | 115.3(9) | O(21)#12-Cs(5)-O(23)    | 136.0(3) |
| O(26)-P(6)-O(16)     | 114.6(9) | O(11)#7-Cs(5)-O(23)     | 136.5(3) |
| O(24)-P(6)-O(16)     | 110.6(8) | O(11)-P(7)-O(17)        | 113.3(8) |
| O(26)-P(6)-O(13)     | 107.7(8) | O(11)-P(7)-O(8)         | 112.1(7) |
| O(24)-P(6)-O(13)     | 106.6(8) | O(17)-P(7)-O(8)         | 112.4(7) |
| O(16)-P(6)-O(13)     | 100.7(8) | O(11)-P(7)-O(7)         | 104.4(7) |
| O(10)-P(8)-O(2)      | 110.7(7) | O(17)-P(7)-O(7)         | 106.3(7) |

|                  |          |                 |          |
|------------------|----------|-----------------|----------|
| O(10)-P(8)-O(14) | 110.0(7) | O(8)-P(7)-O(7)  | 107.6(7) |
| O(2)-P(8)-O(14)  | 111.2(7) | O(2)-P(8)-O(3)  | 104.6(6) |
| O(10)-P(8)-O(3)  | 110.8(7) | O(14)-P(8)-O(3) | 109.4(7) |

Symmetry transformations used to generate equivalent atoms:

#1  $-x+1, -y+2, -z+2$     #2  $-x+1, -y+1, -z+2$   
 #3  $-x+2, y+1/2, -z+3/2$     #4  $x+1, y, z$     #5  $-x+2, -y+1, -z+2$   
 #6  $-x+1, y-1/2, -z+3/2$     #7  $x, y+1, z$     #8  $x-1, y, z$   
 #9  $-x, -y+1, -z+2$     #10  $-x+2, -y+2, -z+2$   
 #11  $-x+1, y+1/2, -z+3/2$     #12  $x-1, y+1, z$   
 #13  $x+1, y-1, z$     #14  $x, y-1, z$     #15  $-x+2, y-1/2, -z+3/2$

**Table S7.** Bond lengths (Å) and angles (°) for Cs<sub>6</sub>Bi<sub>4</sub>(PO<sub>4</sub>)<sub>2</sub>(P<sub>2</sub>O<sub>7</sub>)<sub>3</sub>.

|               |           |                |           |
|---------------|-----------|----------------|-----------|
| Bi(1)-O(7)    | 2.174(10) | Cs(1)-O(10)    | 3.083(11) |
| Bi(1)-O(2)#1  | 2.252(10) | Cs(1)-O(27)    | 3.112(15) |
| Bi(1)-O(24)#2 | 2.319(11) | Cs(1)-O(19)    | 3.188(11) |
| Bi(1)-O(19)   | 2.368(11) | Cs(1)-O(13)    | 3.197(11) |
| Bi(1)-O(15)#2 | 2.449(12) | Cs(1)-O(14)#11 | 3.247(11) |
| Bi(1)-O(26)#3 | 2.665(13) | Cs(1)-O(18)    | 3.309(11) |
| Bi(2)-O(1)    | 2.145(10) | Cs(1)-O(24)    | 3.329(11) |
| Bi(2)-O(4)#4  | 2.186(11) | Cs(1)-O(14)    | 3.356(11) |
| Bi(2)-O(11)#5 | 2.252(10) | Cs(2)-O(8)#5   | 2.904(10) |
| Bi(2)-O(17)   | 2.521(11) | Cs(2)-O(28)#2  | 2.995(13) |
| Bi(2)-O(28)#2 | 2.722(12) | Cs(2)-O(6)#2   | 3.075(10) |
| Bi(2)-O(5)#2  | 2.725(11) | Cs(2)-O(13)#2  | 3.139(10) |
| Bi(3)-O(12)#7 | 2.169(11) | Cs(2)-O(23)#2  | 3.214(13) |
| Bi(3)-O(3)    | 2.192(9)  | Cs(2)-O(3)#5   | 3.218(10) |
| Bi(3)-O(8)    | 2.201(10) | Cs(2)-O(3)     | 3.360(10) |
| Bi(3)-O(21)#2 | 2.573(12) | Cs(2)-O(9)     | 3.389(10) |
| Bi(3)-O(5)#2  | 2.631(11) | Cs(2)-O(11)#5  | 3.505(11) |
| Bi(3)-O(23)   | 2.671(12) | Cs(2)-O(11)    | 3.543(11) |
| Bi(4)-O(20)   | 2.192(11) | Cs(2)-O(5)#2   | 3.624(10) |
| Bi(4)-O(25)#3 | 2.213(13) | Cs(4)-O(1)#6   | 3.052(10) |
| Bi(4)-O(9)#8  | 2.250(10) | Cs(4)-O(28)#2  | 3.079(12) |
| Bi(4)-O(13)   | 2.420(11) | Cs(4)-O(22)#12 | 3.118(11) |
| Bi(4)-O(29)   | 2.487(12) | Cs(4)-O(4)#5   | 3.128(11) |
| Bi(4)-O(21)   | 2.538(11) | Cs(4)-O(9)#4   | 3.283(9)  |
| Cs(3)-O(6)    | 2.933(11) | Cs(4)-O(12)#6  | 3.316(10) |
| Cs(3)-O(27)   | 2.979(13) | Cs(4)-O(1)#2   | 3.334(9)  |
| Cs(3)-O(16)   | 3.001(11) | Cs(4)-O(6)#2   | 3.374(11) |
| Cs(3)-O(17)   | 3.024(11) | Cs(4)-O(17)#2  | 3.568(11) |
| Cs(3)-O(15)#2 | 3.093(11) | Cs(5)-O(16)#3  | 3.088(11) |
| Cs(3)-O(23)   | 3.237(13) | Cs(5)-O(27)#3  | 3.087(14) |
| Cs(3)-O(5)#2  | 3.385(10) | Cs(5)-O(24)#10 | 3.175(11) |
| P(1)-O(26)    | 1.489(13) | Cs(5)-O(19)    | 3.252(12) |
| P(1)-O(17)    | 1.499(12) | Cs(5)-O(29)    | 3.267(12) |
| P(1)-O(21)#12 | 1.531(12) | Cs(5)-O(2)#1   | 3.288(10) |
| P(1)-O(22)#4  | 1.619(11) | Cs(5)-O(14)#10 | 3.471(11) |
| P(2)-O(6)     | 1.508(11) | Cs(5)-O(20)    | 3.501(12) |
| P(2)-O(8)     | 1.542(10) | Cs(5)-O(14)    | 3.553(11) |
| P(2)-O(12)    | 1.552(11) | Cs(5)-O(22)    | 3.715(10) |
| P(2)-O(1)     | 1.567(10) | Cs(5)-O(26)#3  | 3.720(13) |
| P(3)-O(13)    | 1.499(11) | Cs(6)-O(18)#10 | 2.995(10) |
| P(3)-O(15)    | 1.510(11) | Cs(6)-O(10)    | 3.019(11) |
| P(3)-O(5)     | 1.522(11) | Cs(6)-O(26)#1  | 3.108(13) |
| P(3)-O(18)    | 1.613(11) | Cs(6)-O(16)#1  | 3.142(11) |

|                       |           |                       |           |
|-----------------------|-----------|-----------------------|-----------|
| P(4)-O(14)            | 1.486(11) | Cs(6)-O(7)            | 3.281(10) |
| P(4)-O(29)            | 1.512(12) | Cs(6)-O(25)#10        | 3.349(12) |
| P(4)-O(24)            | 1.526(12) | Cs(6)-O(14)           | 3.350(11) |
| P(4)-O(10)#10         | 1.626(11) | Cs(6)-O(2)#1          | 3.379(9)  |
| P(5)-O(16)            | 1.480(12) | Cs(6)-O(29)#11        | 3.461(12) |
| P(5)-O(2)             | 1.534(10) | Cs(6)-O(15)#10        | 3.567(12) |
| P(5)-O(7)             | 1.545(11) | P(7)-O(11)            | 1.522(10) |
| P(5)-O(10)            | 1.636(10) | P(7)-O(4)             | 1.537(11) |
| P(6)-O(23)            | 1.460(13) | P(7)-O(3)             | 1.540(10) |
| P(6)-O(20)            | 1.520(11) | P(7)-O(9)             | 1.564(10) |
| P(6)-O(19)            | 1.531(12) | P(8)-O(27)            | 1.450(14) |
| P(6)-O(22)            | 1.618(11) | P(8)-O(28)            | 1.498(12) |
| O(7)-Bi(1)-O(2)#1     | 80.0(4)   | P(8)-O(25)            | 1.527(13) |
| O(7)-Bi(1)-O(24)#2    | 90.3(4)   | P(8)-O(18)            | 1.637(11) |
| O(2)#1-Bi(1)-O(24)#2  | 83.0(4)   |                       |           |
| O(7)-Bi(1)-O(19)      | 83.8(4)   | O(1)-Bi(2)-O(4)#4     | 83.1(4)   |
| O(2)#1-Bi(1)-O(19)    | 91.4(4)   | O(1)-Bi(2)-O(11)#5    | 86.4(4)   |
| O(24)#2-Bi(1)-O(19)   | 172.6(4)  | O(4)#4-Bi(2)-O(11)#5  | 85.0(4)   |
| O(7)-Bi(1)-O(15)#2    | 92.4(4)   | O(1)-Bi(2)-O(17)      | 80.5(4)   |
| O(2)#1-Bi(1)-O(15)#2  | 165.6(4)  | O(4)#4-Bi(2)-O(17)    | 91.6(4)   |
| O(24)#2-Bi(1)-O(15)#2 | 84.8(4)   | O(11)#5-Bi(2)-O(17)   | 166.7(4)  |
| O(19)-Bi(1)-O(15)#2   | 99.9(4)   | O(1)-Bi(2)-O(28)#2    | 158.4(4)  |
| O(7)-Bi(1)-O(26)#3    | 149.5(4)  | O(4)#4-Bi(2)-O(28)#2  | 113.4(4)  |
| O(2)#1-Bi(1)-O(26)#3  | 77.2(4)   | O(11)#5-Bi(2)-O(28)#2 | 81.5(4)   |
| O(24)#2-Bi(1)-O(26)#3 | 106.6(4)  | O(17)-Bi(2)-O(28)#2   | 111.6(4)  |
| O(19)-Bi(1)-O(26)#3   | 76.9(4)   | O(1)-Bi(2)-O(5)#2     | 90.7(3)   |
| O(15)#2-Bi(1)-O(26)#3 | 113.8(4)  | O(4)#4-Bi(2)-O(5)#2   | 173.6(3)  |
| O(12)#7-Bi(3)-O(3)    | 88.5(4)   | O(11)#5-Bi(2)-O(5)#2  | 96.0(3)   |
| O(12)#7-Bi(3)-O(8)    | 89.9(4)   | O(17)-Bi(2)-O(5)#2    | 85.9(3)   |
| O(3)-Bi(3)-O(8)       | 81.5(4)   | O(28)#2-Bi(2)-O(5)#2  | 73.0(3)   |
| O(12)#7-Bi(3)-O(21)#2 | 98.0(4)   | O(20)-Bi(4)-O(25)#3   | 96.5(4)   |
| O(3)-Bi(3)-O(21)#2    | 77.8(4)   | O(20)-Bi(4)-O(9)#8    | 83.0(4)   |
| O(8)-Bi(3)-O(21)#2    | 157.5(3)  | O(25)#3-Bi(4)-O(9)#8  | 86.7(4)   |
| O(12)#7-Bi(3)-O(5)#2  | 168.7(4)  | O(20)-Bi(4)-O(13)     | 87.3(4)   |
| O(3)-Bi(3)-O(5)#2     | 87.4(3)   | O(25)#3-Bi(4)-O(13)   | 176.2(4)  |
| O(8)-Bi(3)-O(5)#2     | 79.0(3)   | O(9)#8-Bi(4)-O(13)    | 94.1(4)   |
| O(21)#2-Bi(3)-O(5)#2  | 91.4(3)   | O(20)-Bi(4)-O(29)     | 84.8(4)   |
| O(12)#7-Bi(3)-O(23)   | 84.7(4)   | O(25)#3-Bi(4)-O(29)   | 83.5(4)   |
| O(3)-Bi(3)-O(23)      | 154.6(4)  | O(9)#8-Bi(4)-O(29)    | 163.3(4)  |
| O(8)-Bi(3)-O(23)      | 122.9(4)  | O(13)-Bi(4)-O(29)     | 96.5(4)   |
| O(21)#2-Bi(3)-O(23)   | 79.0(4)   | O(20)-Bi(4)-O(21)     | 161.0(4)  |
| O(5)#2-Bi(3)-O(23)    | 103.3(4)  | O(25)#3-Bi(4)-O(21)   | 93.5(4)   |
| O(10)-Cs(1)-O(27)     | 96.6(3)   | O(9)#8-Bi(4)-O(21)    | 81.4(4)   |
| O(10)-Cs(1)-O(19)     | 92.1(3)   | O(13)-Bi(4)-O(21)     | 83.0(4)   |

|                      |          |                       |          |
|----------------------|----------|-----------------------|----------|
| O(27)-Cs(1)-O(19)    | 110.4(3) | O(29)-Bi(4)-O(21)     | 112.5(4) |
| O(10)-Cs(1)-O(13)    | 174.7(3) | O(8)#5-Cs(2)-O(28)#2  | 133.6(3) |
| O(27)-Cs(1)-O(13)    | 78.5(3)  | O(8)#5-Cs(2)-O(6)#2   | 66.7(3)  |
| O(19)-Cs(1)-O(13)    | 91.8(3)  | O(28)#2-Cs(2)-O(6)#2  | 77.2(3)  |
| O(10)-Cs(1)-O(14)#11 | 46.6(3)  | O(8)#5-Cs(2)-O(13)#2  | 152.4(3) |
| O(27)-Cs(1)-O(14)#11 | 76.0(3)  | O(28)#2-Cs(2)-O(13)#2 | 72.4(3)  |
| O(19)-Cs(1)-O(14)#11 | 138.4(3) | O(6)#2-Cs(2)-O(13)#2  | 121.9(3) |
| O(13)-Cs(1)-O(14)#11 | 129.1(3) | O(8)#5-Cs(2)-O(23)#2  | 84.8(3)  |
| O(10)-Cs(1)-O(18)    | 130.0(3) | O(28)#2-Cs(2)-O(23)#2 | 101.5(3) |
| O(27)-Cs(1)-O(18)    | 44.6(3)  | O(6)#2-Cs(2)-O(23)#2  | 59.3(3)  |
| O(19)-Cs(1)-O(18)    | 126.6(3) | O(13)#2-Cs(2)-O(23)#2 | 79.8(3)  |
| O(13)-Cs(1)-O(18)    | 44.7(3)  | O(8)#5-Cs(2)-O(3)#5   | 55.6(3)  |
| O(14)#11-Cs(1)-O(18) | 87.8(3)  | O(28)#2-Cs(2)-O(3)#5  | 91.0(3)  |
| O(10)-Cs(1)-O(24)    | 107.4(3) | O(6)#2-Cs(2)-O(3)#5   | 79.9(3)  |
| O(27)-Cs(1)-O(24)    | 125.7(3) | O(13)#2-Cs(2)-O(3)#5  | 146.9(3) |
| O(19)-Cs(1)-O(24)    | 116.4(3) | O(23)#2-Cs(2)-O(3)#5  | 132.6(3) |
| O(13)-Cs(1)-O(24)    | 74.1(3)  | O(8)#5-Cs(2)-O(3)     | 100.0(3) |
| O(14)#11-Cs(1)-O(24) | 86.3(3)  | O(28)#2-Cs(2)-O(3)    | 113.2(3) |
| O(18)-Cs(1)-O(24)    | 84.5(3)  | O(6)#2-Cs(2)-O(3)     | 166.6(3) |
| O(10)-Cs(1)-O(14)    | 79.0(3)  | O(13)#2-Cs(2)-O(3)    | 70.7(3)  |
| O(27)-Cs(1)-O(14)    | 164.5(3) | O(23)#2-Cs(2)-O(3)    | 123.5(3) |
| O(19)-Cs(1)-O(14)    | 84.8(3)  | O(3)#5-Cs(2)-O(3)     | 91.1(2)  |
| O(13)-Cs(1)-O(14)    | 105.1(3) | O(8)#5-Cs(2)-O(9)     | 91.7(3)  |
| O(14)#11-Cs(1)-O(14) | 90.52(3) | O(28)#2-Cs(2)-O(9)    | 134.7(3) |
| O(18)-Cs(1)-O(14)    | 128.6(3) | O(6)#2-Cs(2)-O(9)     | 133.9(3) |
| O(24)-Cs(1)-O(14)    | 44.1(3)  | O(13)#2-Cs(2)-O(9)    | 63.1(3)  |
| O(6)-Cs(3)-O(27)     | 104.3(3) | O(23)#2-Cs(2)-O(9)    | 79.3(3)  |
| O(6)-Cs(3)-O(16)     | 176.2(3) | O(3)#5-Cs(2)-O(9)     | 122.0(2) |
| O(27)-Cs(3)-O(16)    | 75.6(3)  | O(3)-Cs(2)-O(9)       | 44.5(2)  |
| O(6)-Cs(3)-O(17)     | 82.3(3)  | O(8)#5-Cs(2)-O(11)#5  | 98.4(3)  |
| O(27)-Cs(3)-O(17)    | 108.2(3) | O(28)#2-Cs(2)-O(11)#5 | 59.7(3)  |
| O(16)-Cs(3)-O(17)    | 101.3(3) | O(6)#2-Cs(2)-O(11)#5  | 100.4(3) |
| O(6)-Cs(3)-O(15)#2   | 107.2(3) | O(13)#2-Cs(2)-O(11)#5 | 105.0(3) |
| O(27)-Cs(3)-O(15)#2  | 143.5(3) | O(23)#2-Cs(2)-O(11)#5 | 156.5(3) |
| O(16)-Cs(3)-O(15)#2  | 71.8(3)  | O(3)#5-Cs(2)-O(11)#5  | 43.0(2)  |
| O(17)-Cs(3)-O(15)#2  | 94.0(3)  | O(3)-Cs(2)-O(11)#5    | 79.1(2)  |
| O(6)-Cs(3)-O(23)     | 60.4(3)  | O(9)-Cs(2)-O(11)#5    | 123.6(2) |
| O(27)-Cs(3)-O(23)    | 101.8(4) | O(8)#5-Cs(2)-O(11)    | 60.5(3)  |
| O(16)-Cs(3)-O(23)    | 115.9(3) | O(28)#2-Cs(2)-O(11)   | 152.7(3) |
| O(17)-Cs(3)-O(23)    | 136.8(3) | O(6)#2-Cs(2)-O(11)    | 125.8(3) |
| O(15)#2-Cs(3)-O(23)  | 78.6(3)  | O(13)#2-Cs(2)-O(11)   | 101.0(3) |
| O(6)-Cs(3)-O(5)#2    | 67.3(3)  | O(23)#2-Cs(2)-O(11)   | 103.3(3) |
| O(27)-Cs(3)-O(5)#2   | 170.7(3) | O(3)#5-Cs(2)-O(11)    | 80.5(2)  |
| O(16)-Cs(3)-O(5)#2   | 113.0(3) | O(3)-Cs(2)-O(11)      | 42.0(2)  |



|                         |          |                        |          |
|-------------------------|----------|------------------------|----------|
| O(17)-Cs(3)-O(5)#2      | 67.6(3)  | O(9)-Cs(2)-O(11)       | 42.0(2)  |
| O(15)#2-Cs(3)-O(5)#2    | 45.7(3)  | O(11)#5-Cs(2)-O(11)    | 98.4(2)  |
| O(23)-Cs(3)-O(5)#2      | 77.8(3)  | O(8)#5-Cs(2)-O(5)#2    | 151.3(3) |
| O(16)#3-Cs(5)-O(27)#3   | 72.8(3)  | O(28)#2-Cs(2)-O(5)#2   | 57.7(3)  |
| O(16)#3-Cs(5)-O(24)#10  | 63.9(3)  | O(6)#2-Cs(2)-O(5)#2    | 134.6(3) |
| O(27)#3-Cs(5)-O(24)#10  | 110.6(3) | O(13)#2-Cs(2)-O(5)#2   | 42.9(3)  |
| O(16)#3-Cs(5)-O(19)     | 124.0(3) | O(23)#2-Cs(2)-O(5)#2   | 121.5(3) |
| O(27)#3-Cs(5)-O(19)     | 111.0(3) | O(3)#5-Cs(2)-O(5)#2    | 104.0(2) |
| O(24)#10-Cs(5)-O(19)    | 137.8(3) | O(3)-Cs(2)-O(5)#2      | 57.2(2)  |
| O(16)#3-Cs(5)-O(29)     | 149.1(3) | O(9)-Cs(2)-O(5)#2      | 82.9(2)  |
| O(27)#3-Cs(5)-O(29)     | 80.7(3)  | O(11)#5-Cs(2)-O(5)#2   | 62.7(2)  |
| O(24)#10-Cs(5)-O(29)    | 113.3(3) | O(11)-Cs(2)-O(5)#2     | 99.1(2)  |
| O(19)-Cs(5)-O(29)       | 80.0(3)  | O(1)#6-Cs(4)-O(28)#2   | 135.6(3) |
| O(16)#3-Cs(5)-O(2)#1    | 87.9(3)  | O(1)#6-Cs(4)-O(22)#12  | 114.6(3) |
| O(27)#3-Cs(5)-O(2)#1    | 149.6(3) | O(28)#2-Cs(4)-O(22)#12 | 103.4(3) |
| O(24)#10-Cs(5)-O(2)#1   | 79.7(3)  | O(1)#6-Cs(4)-O(4)#5    | 55.4(3)  |
| O(19)-Cs(5)-O(2)#1      | 60.8(3)  | O(28)#2-Cs(4)-O(4)#5   | 82.6(3)  |
| O(29)-Cs(5)-O(2)#1      | 122.6(3) | O(22)#12-Cs(4)-O(4)#5  | 165.4(3) |
| O(16)#3-Cs(5)-O(14)#10  | 72.2(3)  | O(1)#6-Cs(4)-O(9)#4    | 87.5(2)  |
| O(27)#3-Cs(5)-O(14)#10  | 73.1(3)  | O(28)#2-Cs(4)-O(9)#4   | 70.4(3)  |
| O(24)#10-Cs(5)-O(14)#10 | 44.1(3)  | O(22)#12-Cs(4)-O(9)#4  | 89.1(3)  |
| O(19)-Cs(5)-O(14)#10    | 163.7(3) | O(4)#5-Cs(4)-O(9)#4    | 80.3(3)  |
| O(29)-Cs(5)-O(14)#10    | 85.3(3)  | O(1)#6-Cs(4)-O(12)#6   | 45.1(3)  |
| O(2)#1-Cs(5)-O(14)#10   | 123.8(3) | O(28)#2-Cs(4)-O(12)#6  | 164.6(3) |
| O(16)#3-Cs(5)-O(20)     | 126.5(3) | O(22)#12-Cs(4)-O(12)#6 | 70.3(3)  |
| O(27)#3-Cs(5)-O(20)     | 71.7(3)  | O(4)#5-Cs(4)-O(12)#6   | 100.5(3) |
| O(24)#10-Cs(5)-O(20)    | 168.6(3) | O(9)#4-Cs(4)-O(12)#6   | 95.1(2)  |
| O(19)-Cs(5)-O(20)       | 43.4(3)  | O(1)#6-Cs(4)-O(1)#2    | 85.1(3)  |
| O(29)-Cs(5)-O(20)       | 55.6(3)  | O(28)#2-Cs(4)-O(1)#2   | 116.1(3) |
| O(2)#1-Cs(5)-O(20)      | 103.9(3) | O(22)#12-Cs(4)-O(1)#2  | 92.8(3)  |
| O(14)#10-Cs(5)-O(20)    | 130.4(3) | O(4)#5-Cs(4)-O(1)#2    | 96.4(2)  |
| O(16)#3-Cs(5)-O(14)     | 147.6(3) | O(9)#4-Cs(4)-O(1)#2    | 172.5(2) |
| O(27)#3-Cs(5)-O(14)     | 121.1(3) | O(12)#6-Cs(4)-O(1)#2   | 78.8(2)  |
| O(24)#10-Cs(5)-O(14)    | 83.7(3)  | O(1)#6-Cs(4)-O(6)#2    | 116.0(3) |
| O(19)-Cs(5)-O(14)       | 80.8(3)  | O(28)#2-Cs(4)-O(6)#2   | 71.7(3)  |
| O(29)-Cs(5)-O(14)       | 43.4(3)  | O(22)#12-Cs(4)-O(6)#2  | 105.8(3) |
| O(2)#1-Cs(5)-O(14)      | 87.7(2)  | O(4)#5-Cs(4)-O(6)#2    | 88.6(3)  |
| O(14)#10-Cs(5)-O(14)    | 83.77(3) | O(9)#4-Cs(4)-O(6)#2    | 141.5(2) |
| O(20)-Cs(5)-O(14)       | 85.7(3)  | O(12)#6-Cs(4)-O(6)#2   | 123.2(2) |
| O(16)#3-Cs(5)-O(22)     | 93.5(3)  | O(1)#2-Cs(4)-O(6)#2    | 44.5(2)  |
| O(27)#3-Cs(5)-O(22)     | 74.9(3)  | O(1)#6-Cs(4)-O(17)#2   | 114.3(2) |
| O(24)#10-Cs(5)-O(22)    | 152.0(3) | O(28)#2-Cs(4)-O(17)#2  | 109.1(3) |
| O(19)-Cs(5)-O(22)       | 42.0(3)  | O(22)#12-Cs(4)-O(17)#2 | 42.4(3)  |
| O(29)-Cs(5)-O(22)       | 94.6(3)  | O(4)#5-Cs(4)-O(17)#2   | 148.3(3) |

|                        |          |                         |          |
|------------------------|----------|-------------------------|----------|
| O(2)#1-Cs(5)-O(22)     | 83.3(2)  | O(9)#4-Cs(4)-O(17)#2    | 131.2(2) |
| O(14)#10-Cs(5)-O(22)   | 147.6(3) | O(12)#6-Cs(4)-O(17)#2   | 76.2(3)  |
| O(20)-Cs(5)-O(22)      | 39.0(2)  | O(1)#2-Cs(4)-O(17)#2    | 51.9(2)  |
| O(14)-Cs(5)-O(22)      | 117.8(2) | O(6)#2-Cs(4)-O(17)#2    | 68.7(3)  |
| O(16)#3-Cs(5)-O(26)#3  | 71.1(3)  | O(17)#2-Cs(4)-O(20)#12  | 81.7(2)  |
| O(27)#3-Cs(5)-O(26)#3  | 99.0(3)  | O(18)#10-Cs(6)-O(10)    | 140.0(3) |
| O(24)#10-Cs(5)-O(26)#3 | 113.5(3) | O(18)#10-Cs(6)-O(26)#1  | 92.8(3)  |
| O(19)-Cs(5)-O(26)#3    | 53.0(3)  | O(10)-Cs(6)-O(26)#1     | 74.8(3)  |
| O(29)-Cs(5)-O(26)#3    | 129.8(3) | O(18)#10-Cs(6)-O(16)#1  | 102.7(3) |
| O(2)#1-Cs(5)-O(26)#3   | 51.8(3)  | O(10)-Cs(6)-O(16)#1     | 111.8(3) |
| O(14)#10-Cs(5)-O(26)#3 | 143.2(3) | O(26)#1-Cs(6)-O(16)#1   | 79.3(3)  |
| O(20)-Cs(5)-O(26)#3    | 76.4(3)  | O(18)#10-Cs(6)-O(7)     | 174.8(3) |
| O(14)-Cs(5)-O(26)#3    | 128.0(3) | O(10)-Cs(6)-O(7)        | 45.2(3)  |
| O(22)-Cs(5)-O(26)#3    | 39.6(3)  | O(26)#1-Cs(6)-O(7)      | 88.5(3)  |
| O(26)-P(1)-O(17)       | 117.4(7) | O(16)#1-Cs(6)-O(7)      | 72.6(3)  |
| O(26)-P(1)-O(21)#12    | 108.4(7) | O(18)#10-Cs(6)-O(25)#10 | 44.4(3)  |
| O(17)-P(1)-O(21)#12    | 112.6(7) | O(10)-Cs(6)-O(25)#10    | 98.6(3)  |
| O(26)-P(1)-O(22)#4     | 108.2(7) | O(26)#1-Cs(6)-O(25)#10  | 60.7(3)  |
| O(17)-P(1)-O(22)#4     | 103.7(6) | O(16)#1-Cs(6)-O(25)#10  | 120.7(3) |
| O(21)#12-P(1)-O(22)#4  | 105.7(6) | O(7)-Cs(6)-O(25)#10     | 139.8(3) |
| O(6)-P(2)-O(8)         | 107.5(6) | O(18)#10-Cs(6)-O(14)    | 91.3(3)  |
| O(6)-P(2)-O(12)        | 115.1(6) | O(10)-Cs(6)-O(14)       | 79.9(3)  |
| O(8)-P(2)-O(12)        | 110.2(6) | O(26)#1-Cs(6)-O(14)     | 145.2(3) |
| O(6)-P(2)-O(1)         | 111.2(6) | O(16)#1-Cs(6)-O(14)     | 133.1(3) |
| O(8)-P(2)-O(1)         | 108.9(6) | O(7)-Cs(6)-O(14)        | 90.5(3)  |
| O(12)-P(2)-O(1)        | 103.8(6) | O(25)#10-Cs(6)-O(14)    | 100.6(3) |
| O(13)-P(3)-O(15)       | 113.7(6) | O(18)#10-Cs(6)-O(2)#1   | 124.6(3) |
| O(13)-P(3)-O(5)        | 112.7(6) | O(10)-Cs(6)-O(2)#1      | 94.6(3)  |
| O(15)-P(3)-O(5)        | 113.2(6) | O(26)#1-Cs(6)-O(2)#1    | 115.7(3) |
| O(13)-P(3)-O(18)       | 105.4(6) | O(16)#1-Cs(6)-O(2)#1    | 45.7(3)  |
| O(15)-P(3)-O(18)       | 103.1(6) | O(7)-Cs(6)-O(2)#1       | 50.6(3)  |
| O(5)-P(3)-O(18)        | 107.7(6) | O(25)#10-Cs(6)-O(2)#1   | 164.5(3) |
| O(14)-P(4)-O(29)       | 115.4(6) | O(14)-Cs(6)-O(2)#1      | 89.6(2)  |
| O(14)-P(4)-O(24)       | 113.1(7) | O(18)#10-Cs(6)-O(29)#11 | 96.3(3)  |
| O(29)-P(4)-O(24)       | 111.5(7) | O(10)-Cs(6)-O(29)#11    | 44.2(3)  |
| O(14)-P(4)-O(10)#10    | 107.3(6) | O(26)#1-Cs(6)-O(29)#11  | 61.0(3)  |
| O(29)-P(4)-O(10)#10    | 103.9(6) | O(16)#1-Cs(6)-O(29)#11  | 136.7(3) |
| O(24)-P(4)-O(10)#10    | 104.5(6) | O(7)-Cs(6)-O(29)#11     | 88.7(3)  |
| O(16)-P(5)-O(2)        | 115.1(6) | O(25)#10-Cs(6)-O(29)#11 | 54.8(3)  |
| O(16)-P(5)-O(7)        | 114.3(6) | O(14)-Cs(6)-O(29)#11    | 84.2(3)  |
| O(2)-P(5)-O(7)         | 109.7(6) | O(2)#1-Cs(6)-O(29)#11   | 138.8(3) |
| O(16)-P(5)-O(10)       | 110.4(6) | O(18)#10-Cs(6)-O(15)#10 | 42.7(3)  |
| O(2)-P(5)-O(10)        | 106.1(6) | O(10)-Cs(6)-O(15)#10    | 175.3(3) |
| O(7)-P(5)-O(10)        | 99.8(6)  | O(26)#1-Cs(6)-O(15)#10  | 101.9(3) |

|                  |          |                         |          |
|------------------|----------|-------------------------|----------|
| O(23)-P(6)-O(20) | 115.0(7) | O(16)#1-Cs(6)-O(15)#10  | 64.0(3)  |
| O(23)-P(6)-O(19) | 114.3(7) | O(7)-Cs(6)-O(15)#10     | 132.1(3) |
| O(20)-P(6)-O(19) | 110.4(6) | O(25)#10-Cs(6)-O(15)#10 | 82.5(3)  |
| O(23)-P(6)-O(22) | 108.1(7) | O(14)-Cs(6)-O(15)#10    | 104.4(3) |
| O(20)-P(6)-O(22) | 100.8(6) | O(2)#1-Cs(6)-O(15)#10   | 83.8(2)  |
| O(19)-P(6)-O(22) | 107.1(6) | O(29)#11-Cs(6)-O(15)#10 | 137.2(3) |
| O(11)-P(7)-O(4)  | 110.5(6) | O(27)-P(8)-O(28)        | 119.1(7) |
| O(11)-P(7)-O(3)  | 108.0(6) | O(27)-P(8)-O(25)        | 113.5(8) |
| O(4)-P(7)-O(3)   | 109.3(6) | O(28)-P(8)-O(25)        | 108.7(7) |
| O(11)-P(7)-O(9)  | 107.5(6) | O(27)-P(8)-O(18)        | 104.6(7) |
| O(4)-P(7)-O(9)   | 110.8(6) | O(28)-P(8)-O(18)        | 109.3(6) |
| O(3)-P(7)-O(9)   | 110.8(6) | O(25)-P(8)-O(18)        | 99.8(6)  |

Symmetry transformations used to generate equivalent atoms:

#1 -x, y+1/2, -z+1/2    #2 x-1, y, z    #3 x, y+1, z  
#4 x, y-1, z    #5 -x-1, -y+1, -z    #6 -x-1, -y, -z  
#7 -x, -y+1, -z    #8 x+1, y, z    #9 x+1, y+1, z  
#10 -x+1, y+1/2, -z+1/2    #11 -x+1, y-1/2, -z+1/2  
#12 x-1, y-1, z    #13 -x, y-1/2, -z+1/2

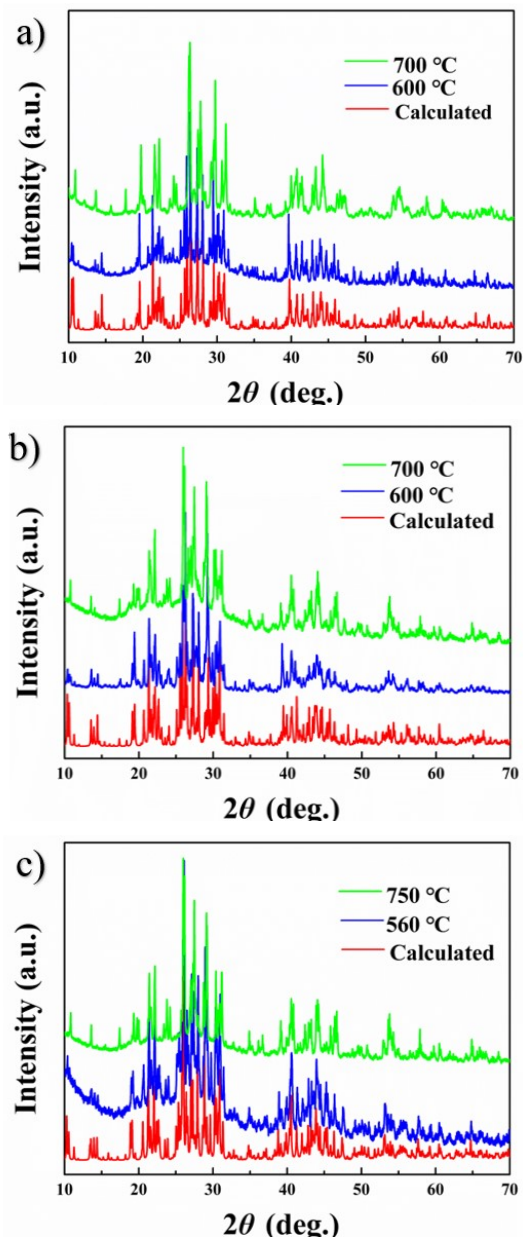
**Table S8.** Some reported bismuth phosphates containing alkali metals or alkaline earth metals cations.

| Compounds                                                                           | Space Group                | Dimension | Reference          |
|-------------------------------------------------------------------------------------|----------------------------|-----------|--------------------|
| $\text{Li}_2\text{KBi}(\text{PO}_4)_2$                                              | $P2_1$                     | 1D        | 1                  |
| $\text{Li}_2\text{RbBi}(\text{PO}_4)_2$                                             | $C2$                       | 1D        | 1                  |
| $\text{Li}_2\text{CsBi}(\text{PO}_4)_2$                                             | $C2$                       | 1D        | 1                  |
| $\text{K}_3\text{SrBi}(\text{P}_2\text{O}_7)_2$                                     | $P2_1$                     | 2D        | 2                  |
| $\text{Rb}_3\text{SrBi}(\text{P}_2\text{O}_7)_2$                                    | $P2_1$                     | 2D        | 2                  |
| $\text{Rb}_3\text{PbBi}(\text{P}_2\text{O}_7)_2$                                    | $P2_1$                     | 2D        | 3                  |
| $\text{Cs}_3\text{PbBi}(\text{P}_2\text{O}_7)_2$                                    | $P2_12_12_1$               | 2D        | 3                  |
| $\text{Rb}_3\text{BaBi}(\text{P}_2\text{O}_7)_2$                                    | $P2_1$                     | 2D        | 4                  |
| $\text{Cs}_3\text{BaBi}(\text{P}_2\text{O}_7)_2$                                    | $P2_12_12_1$               | 2D        | 4                  |
| $\text{Cs}_3\text{SrBi}(\text{P}_2\text{O}_7)_2$                                    | $P2_12_12_1$               | 2D        | 5                  |
| $\text{Cs}_3\text{CaBi}(\text{P}_2\text{O}_7)_2$                                    | $P2_12_12_1$               | 2D        | 5                  |
| $\text{Rb}_2\text{PbBi}_2(\text{PO}_4)_2(\text{P}_2\text{O}_7)$                     | $Pnma$                     | 3D        | 6                  |
| $\text{Cs}_2\text{PbBi}_2(\text{PO}_4)_2(\text{P}_2\text{O}_7)$                     | $Pnma$                     | 3D        | 6                  |
| $\text{Rb}_6\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$                     | $P2_1/c$                   | 3D        | 7                  |
| <b><math>\text{Cs}_6\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3</math></b>   | <b><math>P2_1/c</math></b> | <b>3D</b> | <b>The Article</b> |
| <b><math>\text{RbCs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3</math></b> | <b><math>P2_1/c</math></b> | <b>3D</b> | <b>The Article</b> |
| <b><math>\text{KCs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3</math></b>  | <b><math>P2_1/c</math></b> | <b>3D</b> | <b>The Article</b> |

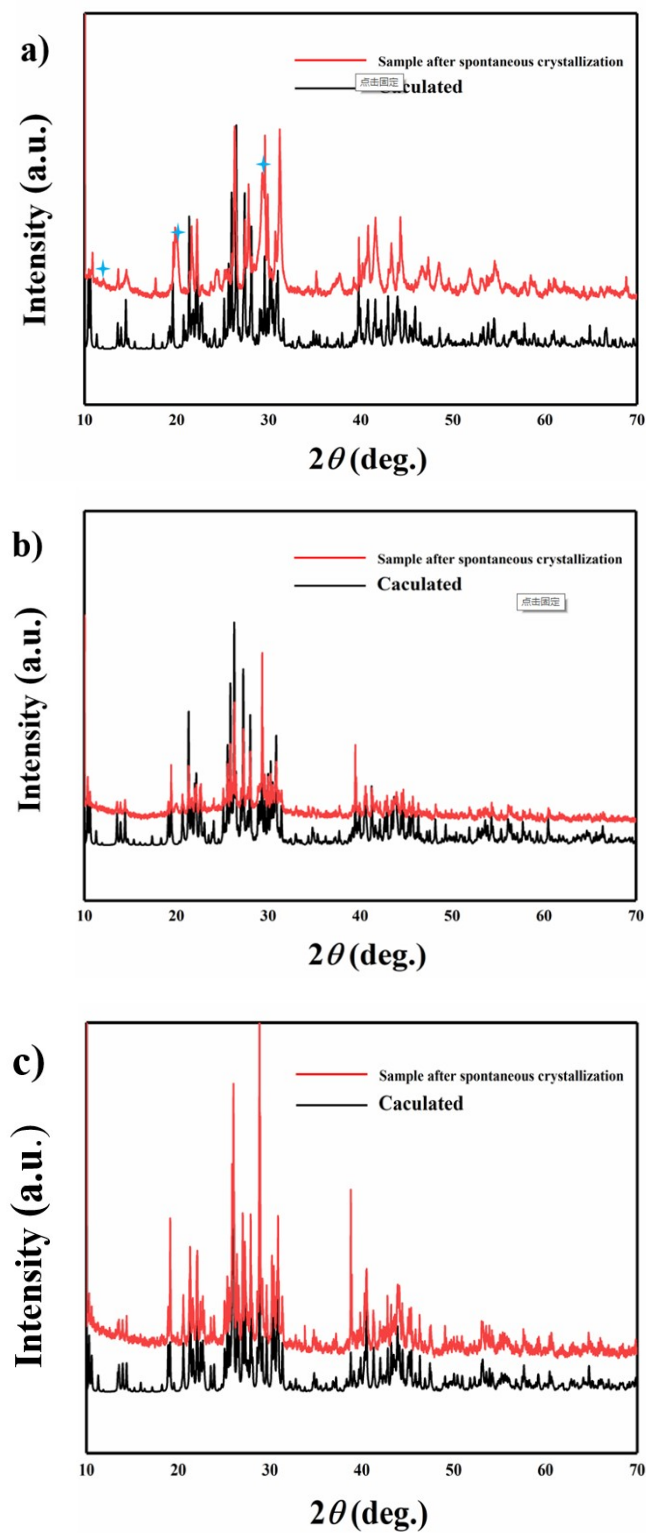
**Table S9.** Some reported phosphates designed by dimensional reduction theory.

| Compounds                                                                                                    | Parents <sup>[a]</sup>               | Dimensional<br>reduction agents <sup>[a]</sup>  | Equivalent |
|--------------------------------------------------------------------------------------------------------------|--------------------------------------|-------------------------------------------------|------------|
| $\text{Cs}_2\text{PbBi}_2(\text{PO}_4)_2(\text{P}_2\text{O}_7)^6$                                            | $\text{CsBiP}_2\text{O}_7$           | PbO                                             | 1/2        |
| $\text{Rb}_2\text{PbBi}_2(\text{PO}_4)_2(\text{P}_2\text{O}_7)^6$                                            | $\text{Bi}_2\text{P}_4\text{O}_{13}$ | PbO, $\text{Rb}_2\text{O}$                      | 1, 1       |
| $\text{Pb}_9[\text{Li}_2(\text{P}_2\text{O}_7)_2(\text{P}_4\text{O}_{13})_2]^8$                              | $\text{Pb}_3\text{P}_4\text{O}_{13}$ | $\text{Li}_2\text{O}$                           | 1/3        |
| $\text{Pb}_{12}[\text{Li}_2(\text{P}_2\text{O}_7)_2(\text{P}_4\text{O}_{13})_2](\text{P}_4\text{O}_{13})^9$  | $\text{Pb}_3\text{P}_4\text{O}_{13}$ | $\text{Li}_2\text{O}$                           | 1/4        |
| $\text{Rb}_6\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3^7$                                            | $\text{Bi}_2\text{P}_4\text{O}_{13}$ | $\text{Rb}_2\text{O}$                           | 3/2        |
| <b><math>\text{Cs}_6\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3</math></b>                            | $\text{CsBiP}_2\text{O}_7$           | $\text{Cs}_2\text{O}$                           | 1/4        |
| <b><math>\text{RbCs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3</math></b>                          | $\text{CsBiP}_2\text{O}_7$           | $\text{Cs}_2\text{O}$ , $\text{Rb}_2\text{O}$   | 1/8, 1/8   |
| <b><math>\text{KCs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3</math></b>                           | $\text{CsBiP}_2\text{O}_7$           | $\text{Cs}_2\text{O}$ , $\text{K}_2\text{O}$    | 1/8, 1/8   |
| $\text{Th}_4(\text{PO}_4)_4(\text{P}_2\text{O}_7)^{10}$                                                      | $\text{ThP}_2\text{O}_7$             | $\text{ThO}_2$                                  | 1/3        |
| $\text{U}_2(\text{PO}_4)(\text{P}_3\text{O}_{10})^{11}$                                                      | $\text{U}(\text{PO}_3)_4$            | $\text{UO}_2$                                   | 1          |
| $\text{Na}_4\text{Ni}_5(\text{PO}_4)_2(\text{P}_2\text{O}_7)^{12}$                                           | $\text{NaNi}(\text{PO}_3)_3$         | $\text{Na}_2\text{O}$ , $\text{NiO}$            | 1/2, 3/2   |
| $\text{Na}_4\text{A}_3(\text{PO}_4)_2(\text{P}_2\text{O}_7)$ (A = Mg, Mn, Fe,<br>Co and Ni) <sup>13,14</sup> | $\text{A}_2\text{P}_4\text{O}_{12}$  | $\text{Na}_2\text{O}$ , AO                      | 2, 1       |
| $\text{Ni}_4\text{M}_2(\text{PO}_4)_2(\text{P}_2\text{O}_7)$ (M = K, Tl) <sup>15</sup>                       | $\text{Ni}_2\text{P}_2\text{O}_7$    | $\text{M}_2\text{O}$                            | 1/2        |
| $\text{Li}_9\text{Al}_3(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3^{16}$                                         | $\text{LiAl}(\text{PO}_3)_4$         | $\text{Li}_2\text{O}$ , $\text{Al}_2\text{O}_3$ | 7/2, 1/4   |
| $\text{LiMg}_3(\text{PO}_4)(\text{P}_2\text{O}_7)^{17}$                                                      | $\text{Mg}_2\text{P}_2\text{O}_7$    | $\text{Li}_2\text{O}$                           | 1/3        |
| $\text{KNi}_3(\text{PO}_4)(\text{P}_2\text{O}_7)^{18}$                                                       | $\text{Ni}_2\text{P}_2\text{O}_7$    | $\text{K}_2\text{O}$                            | 1/3        |
| $\text{Eu}_2\text{Si}(\text{PO}_4)_2(\text{P}_2\text{O}_7)^{19}$                                             | $\text{EuP}_5\text{O}_{14}$          | $\text{Eu}_2\text{O}_3$ , $\text{SiO}_2$        | 3/5, 1     |
| $\text{MnSr}_2(\text{PO}_4)(\text{P}_2\text{O}_7)^{20}$                                                      | $\text{Sr}(\text{PO}_3)_2$           | $\text{Mn}_2\text{O}_3$ , $\text{SrO}$          | 1/2, 1/3   |
| $\text{VCa}_2(\text{PO}_4)(\text{P}_2\text{O}_7)^{21}$                                                       | $\text{Ca}(\text{PO}_3)_2$           | $\text{V}_2\text{O}_3$ , $\text{CaO}$           | 1/2, 1/3   |
| $\text{MoPb}_2(\text{PO}_4)(\text{P}_2\text{O}_7)^{22}$                                                      | $\text{Pb}(\text{PO}_3)_2$           | $\text{Mo}_2\text{O}_3$ , $\text{PbO}$          | 1/2, 1/3   |
| $\text{AgN}_2(\text{PO}_4)(\text{P}_2\text{O}_7)$ (N = V, Cr) <sup>23</sup>                                  | $\text{N}(\text{PO}_3)_3$            | $\text{N}_2\text{O}_3$ , $\text{Ag}_2\text{O}$  | 1/2, 1/2   |
| $\text{KX}_6(\text{P}_2\text{O}_7)_2(\text{P}_3\text{O}_{10})$ (M = Cd, Mg) <sup>24,25</sup>                 | $\text{X}(\text{PO}_3)_2$            | XO, $\text{K}_2\text{O}$                        | 5/7, 1/2   |
| $\text{AMn}_6(\text{P}_2\text{O}_7)_2(\text{P}_3\text{O}_{10})$ (A = Na, Ag,<br>K) <sup>25,26</sup>          | $\text{Mn}(\text{PO}_3)_2$           | $\text{MnO}$ , $\text{A}_2\text{O}$             | 5/7, 1/2   |
| $\text{Na}_7\text{Y}_2(\text{P}_2\text{O}_7)_2(\text{P}_3\text{O}_{10})^{27}$                                | $\text{NaPO}_3$                      | $\text{Y}_2\text{O}_3$                          | 1/7        |

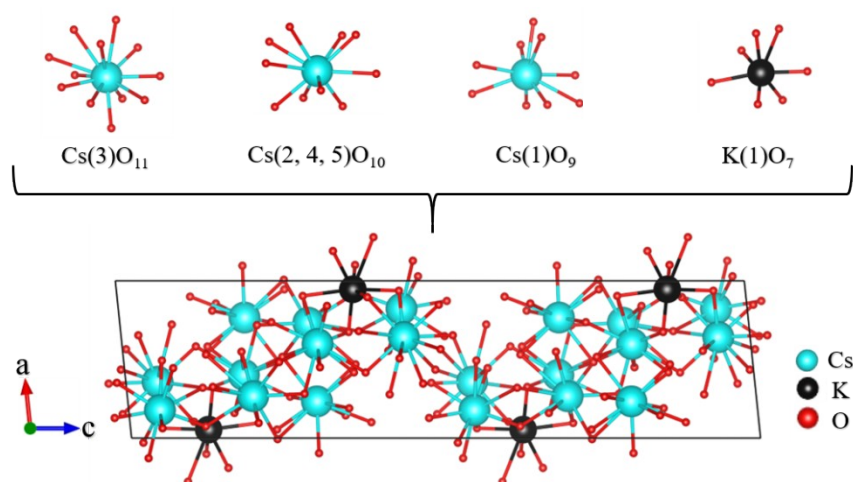
[a] A compounds can possess different parents when different agents are selected as dimensional reduction agents. For example, in  $\text{Cs}_2\text{PbBi}_2(\text{PO}_4)_2(\text{P}_2\text{O}_7)$ , when selecting PbO as dimensional reduction agent,  $\text{CsBiP}_2\text{O}_7$  is regard as parent; when selecting  $\text{Cs}_2\text{O}$  and PbO as dimensional reduction agent,  $\text{Bi}_2\text{P}_4\text{O}_{13}$  is regard as parent.



**Figure S1.** PXRD spectra of a)  $\text{KCs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$ , b)  $\text{RbCs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$  and c)  $\text{Cs}_6\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$ .

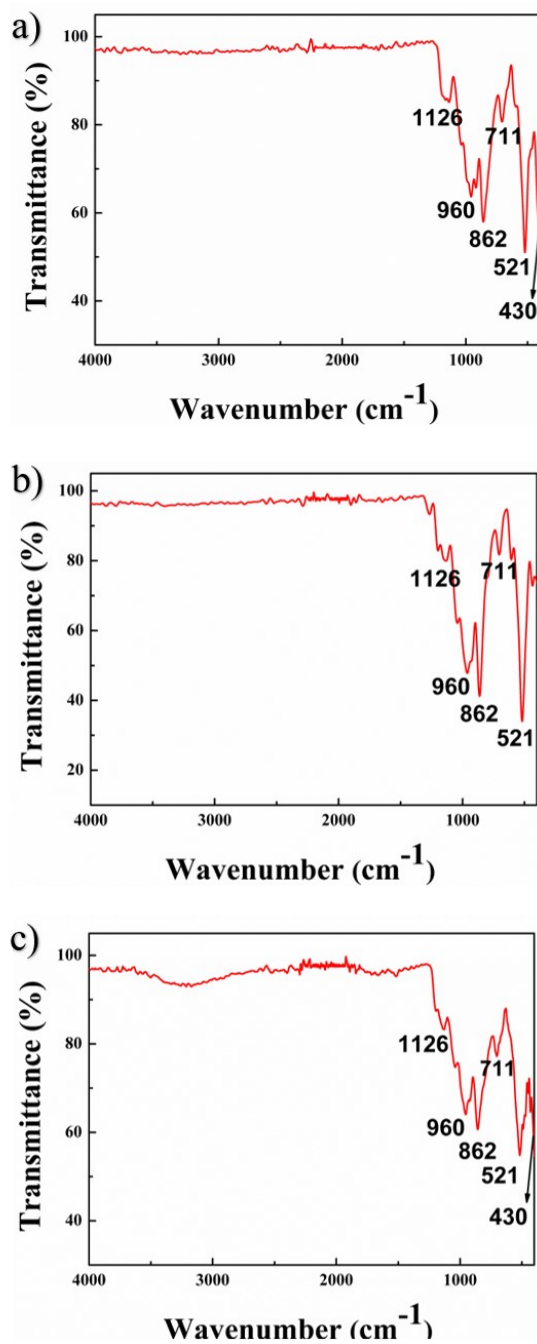


**Figure S2.** PXRD of a)  $\text{KCs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$ , b)  $\text{RbCs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$  and c)  $\text{Cs}_6\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$  after spontaneous crystallization

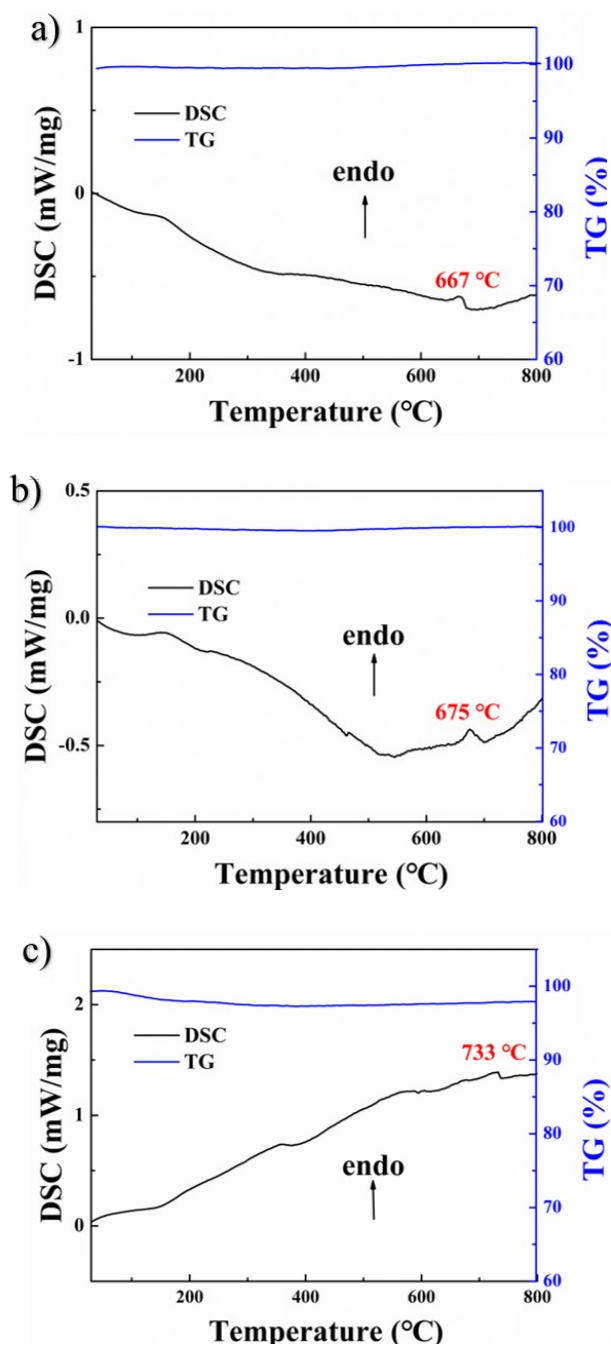


**Figure S3.** Coordination environment of  $\text{K}^+$  and  $\text{Cs}^+$  cations in  $\text{KCs}_5\text{Bi}_4(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2$ .

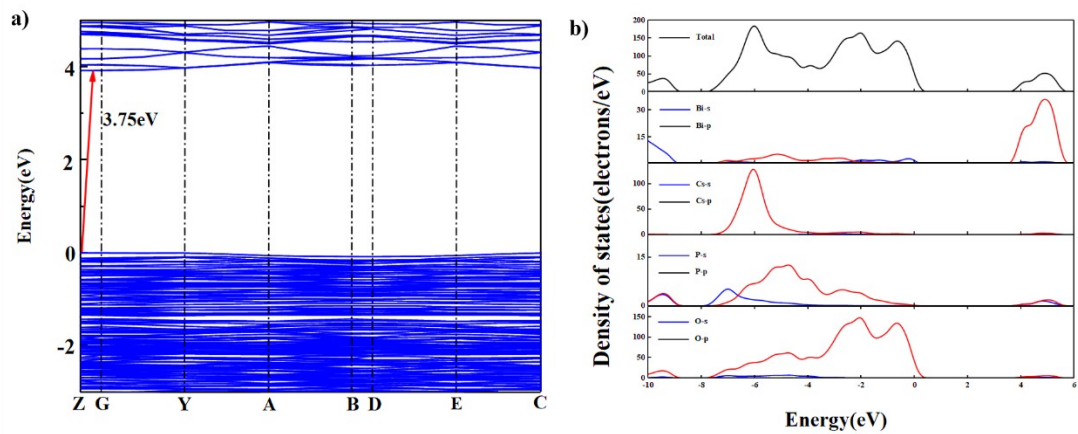




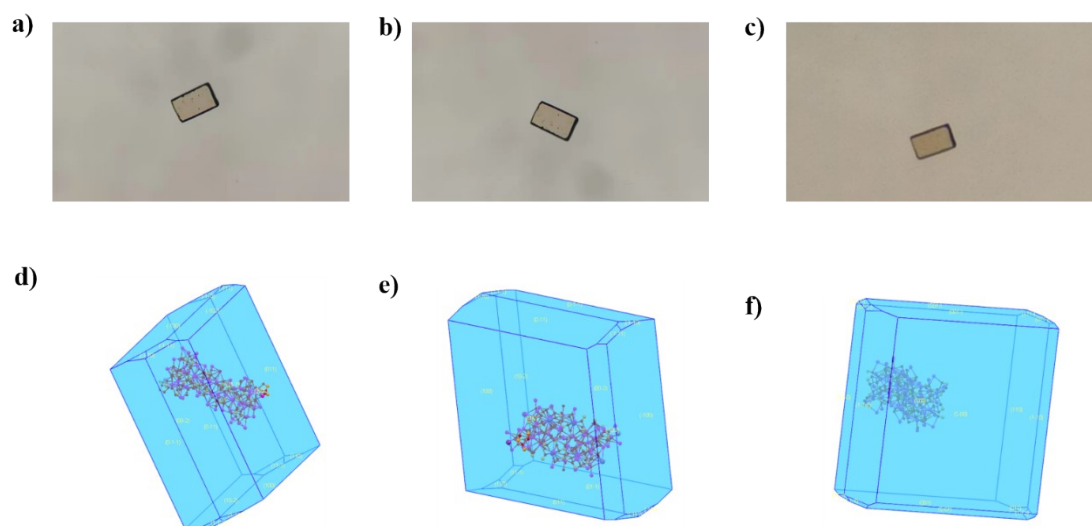
**Figure S4.** IR spectra of a)  $\text{KCs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$ , b)  $\text{RbCs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$  and c)  $\text{Cs}_6\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$ .



**Figure S5.** TG and DSC curves of a)  $\text{KCs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$ , b)  $\text{RbCs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$  and c)  $\text{Cs}_6\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$ .



**Figure S6.** a) Band structure b) DOSs and total DOSs of  $\text{Cs}_6\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$ .



**Figure S7.** a-c) crystal photo and d-f) theoretical crystal morphology of  $\text{KCs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$ ,  $\text{RbCs}_5\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$  and  $\text{Cs}_6\text{Bi}_4(\text{PO}_4)_2(\text{P}_2\text{O}_7)_3$ , respectively.

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