

Supporting Information

for

Alternate pathway for standard SCR on Cu-Zeolites with gas-phase ammonia

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1. Reaction Mechanism for Site-Specific SCR Model

The site-specific model utilized here builds upon our previous work on a 3-site NH₃ storage model to simulate NH₃ TPD (temperature programmed desorption) as a function of hydrothermal aging [1]. The model structure on Brønsted acid sites and Physisorbed sites is retained with similar rate parameters, while the lumped Copper sites are separated into Z₂Cu and ZCuOH sites. Number densities of Z₂Cu and ZCuOH sites are estimated through NO₂-TPD and NO + NH₃ titration experiments, as reported in [2].

We consider up to 1 NH₃ adsorbed per ZCuOH site, and up to 2 NH₃ to adsorb per Z₂Cu site, consistent with previous quantification of NH₃ adsorbed per Cu site at 200°C in 10% O₂ and 7% H₂O [1, 3]. While DFT calculations and spectroscopic investigations suggest NH₃/Cu ratios of 4 for Z₂Cu sites, and 3 for ZCuOH sites [4-5], this level of NH₃ solvation is likely achieved at temperatures below 200°C. The additional NH₃ adsorption on Cu sites at low temperatures is lumped into the Physisorbed site, which also includes weakly bound NH₃ on Brønsted acid sites and Lewis acidic extra-framework aluminum sites. The desorption activation energies on isolated Cu sites are consistent with DFT estimations in [4]. More details on the identification of adsorption-desorption kinetics and surface coverages on each site are included in [1, 6].

Standard SCR is assumed to occur through the reaction of NO with NH₃-solvated Cu species, consistent with the current state of understanding [7-8]. This is represented globally in the model through reactions R7 and R8 (Table S1). Rate parameters for these SCR reactions are estimated using kinetic regime experimental data on catalysts with different proportions of Z₂Cu and ZCuOH sites. More details on this will be included in a future publication. The overall reaction mechanism is shown in Table S1.

Table S1
Site-Specific NH₃ Storage and Standard SCR Reaction Mechanism on Cu-SSZ-13

Reaction Number	Reaction	Rate Expression
R1	$\text{NH}_3 + \text{ZH} \leftrightarrow \text{ZNH}_4$	$r_{\text{AdsZH}} = k_{\text{AdsZH}} y_{\text{NH}_3,s} \theta_{\text{ZH}} \Omega_{\text{ZH}}$ $r_{\text{DesZH}} = k_{\text{DesZH}} \theta_{\text{ZNH}_4} \Omega_{\text{ZH}}$
R2	$\text{NH}_3 + \text{ZNH}_4 \leftrightarrow \text{ZNH}_4\text{NH}_3$	$r_{\text{AdsZNH}_4} = k_{\text{AdsZNH}_4} y_{\text{NH}_3,s} \theta_{\text{ZNH}_4} \Omega_{\text{ZH}}$ $r_{\text{DesZNH}_4} = k_{\text{DesZNH}_4} \theta_{\text{ZNH}_4\text{NH}_3} \Omega_{\text{ZH}}$
R3	$\text{NH}_3 + \text{P} \leftrightarrow \text{PNH}_3$	$r_{\text{Adsp}} = k_{\text{Adsp}} y_{\text{NH}_3,s} \theta_{\text{P}} \Omega_{\text{P}}$ $r_{\text{Desp}} = k_{\text{Desp}} \theta_{\text{PNH}_3} \Omega_{\text{P}}$
R4	$\text{NH}_3 + \text{ZCuOH} \leftrightarrow \text{ZCuOHNH}_3$	$r_{\text{AdsZCuOH}} = k_{\text{AdsZCuOH}} y_{\text{NH}_3,s} \theta_{\text{ZCuOH}} \Omega_{\text{ZCuOH}}$ $r_{\text{DesZCuOH}} = k_{\text{DesZCuOH}} \theta_{\text{ZCuOHNH}_3} \Omega_{\text{ZCuOH}}$

R5	$\text{NH}_3 + \text{Z}_2\text{Cu} \leftrightarrow \text{Z}_2\text{CuNH}_3$	$r_{\text{Ads}_{\text{Z}_2\text{Cu}}} = k_{\text{Ads}_{\text{Z}_2\text{Cu}}} y_{\text{NH}_3,s} \theta_{\text{Z}_2\text{Cu}} \Omega_{\text{Z}_2\text{Cu}}$ $r_{\text{Des}_{\text{Z}_2\text{Cu}}} = k_{\text{Des}_{\text{Z}_2\text{Cu}}} \theta_{\text{Z}_2\text{CuNH}_3} \Omega_{\text{Z}_2\text{Cu}}$
R6	$\text{NH}_3 + \text{Z}_2\text{CuNH}_3 \leftrightarrow \text{Z}_2\text{Cu}(\text{NH}_3)_2$	$r_{\text{Ads}_{\text{Z}_2\text{CuNH}_3}} = k_{\text{Ads}_{\text{Z}_2\text{CuNH}_3}} y_{\text{NH}_3,s} \theta_{\text{Z}_2\text{CuNH}_3} \Omega_{\text{Z}_2\text{Cu}}$ $r_{\text{Des}_{\text{Z}_2\text{CuNH}_3}} = k_{\text{Des}_{\text{Z}_2\text{CuNH}_3}} \theta_{\text{Z}_2\text{Cu}(\text{NH}_3)_2} \Omega_{\text{Z}_2\text{Cu}}$
R7	$4\text{ZCuOHNH}_3 + 4\text{NO} + \text{O}_2 \rightarrow 4\text{ZCuOH} + 4\text{N}_2 + 6\text{H}_2\text{O}$	$r_{\text{SSCR}_{\text{ZCuOH}}} = k_{\text{SSCR}_{\text{ZCuOH}}} y_{\text{NO},s}^{0.8} y_{\text{O}_2,s}^{0.3} \theta_{\text{ZCuOHNH}_3} \Omega_{\text{ZCuOH}}$
R8	$2\text{Z}_2\text{Cu}(\text{NH}_3)_2 + 4\text{NO} + \text{O}_2 \rightarrow 2\text{Z}_2\text{Cu} + 4\text{N}_2 + 6\text{H}_2\text{O}$	$r_{\text{SSCR}_{\text{Z}_2\text{Cu}}} = k_{\text{SSCR}_{\text{Z}_2\text{Cu}}} y_{\text{NO},s}^{0.8} y_{\text{O}_2,s}^{0.3} \theta_{\text{Z}_2\text{Cu}(\text{NH}_3)_2} \Omega_{\text{Z}_2\text{Cu}}$

2. Dynamic NO_x Conversion as a function of Temperature and NO Feed

Figure S1 shows the initial change in the NO_x conversion vs. NH₃ storage for 200 ppm and 1000 ppm feed NO from 175°C-250°C. The contribution of the initial increase in NO_x conversion to the overall steady-state conversion appears to increase with increasing feed and decreasing temperatures

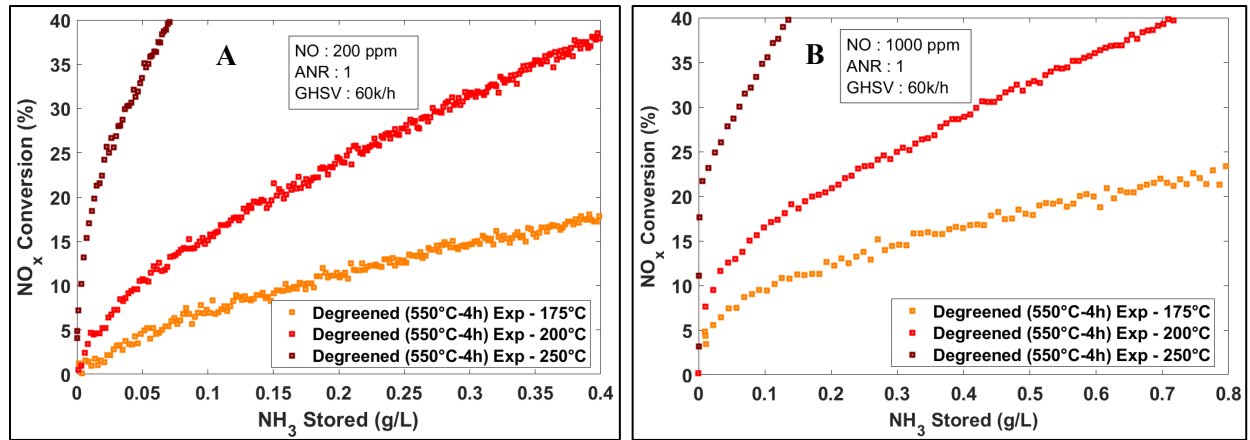


Figure S1. Initial NO_x Conversion as a function of NH₃ storage and catalyst temperature under standard SCR conditions (NO₂/NO_x = 0) at 60k/h GHSV and ANR 1 with **A.** Feed NO : 200 ppm and **B.** Feed NO : 1000 ppm

3. Site-Specific Model for Reduction of Cu²⁺ Sites

3.1 Reaction Mechanism

To model the reduction half cycle of the standard SCR reaction, we utilized the same NH₃ storage model framework shown in Table S1. We included the interaction of NO with NH₃ solvated Cu sites to generate reduced Cu sites, and the subsequent NH₃ solvation of the reduced Cu sites. Activation energies for the reduction of ZCuOH and Z₂Cu sites were set to 71 kJ/mol and 74 kJ/mol respectively, as reported from

theoretical calculations in [4]. Reaction pre-exponentials are estimated from NO + NH₃ titration experiments on catalysts with different proportions of Z₂Cu and ZCuOH sites. More details on this will be included in a future publication. Following the reduction of Cu sites and subsequent NH₃ solvation, a temperature programmed desorption (TPD) experiment was run to desorb the NH₃ from reduced Cu and Bronsted acid sites (similar protocol to NH₃-TPD on oxidized catalysts). This information was utilized to estimate the adsorption-desorption kinetics for the reduced Cu sites. More details on the identification of these kinetics and surface coverages on each site are included in [6]. The overall reaction mechanism is shown in Table S2.

Table S2
Reaction Mechanism for Reduction of ZCuOH and Z₂Cu Sites on Cu-SSZ-13

Reaction Number	Reaction	Rate Expression
R7	$\text{ZCuOHNH}_3 + \text{NO} \rightarrow \text{ZCu} + \text{N}_2 + 2\text{H}_2\text{O}$	$r_{\text{RHCZCuOH}} = k_{\text{RHCZCuOH}} y_{\text{NO},s} \theta_{\text{ZCuOHNH}_3} \Omega_{\text{ZCuOH}}$
R8	$\text{Z}_2\text{CuNH}_3 + \text{NO} \rightarrow \text{ZCu} + \text{ZH} + \text{N}_2 + \text{H}_2\text{O}$	$r_{\text{RHCZ}_2\text{Cu}} = k_{\text{RHCZ}_2\text{Cu}} y_{\text{NO},s} \theta_{\text{Z}_2\text{CuNH}_3} \Omega_{\text{Z}_2\text{Cu}}$
R9	$\text{Z}_2\text{Cu}(\text{NH}_3)_2 + \text{NO} \rightarrow \text{ZCuNH}_3 + \text{ZH} + \text{N}_2 + 2\text{H}_2\text{O}$	$r_{\text{RHCZ}_2\text{Cu}} = k_{\text{RHCZ}_2\text{Cu}} y_{\text{NO},s} \theta_{\text{Z}_2\text{Cu}(\text{NH}_3)_2} \Omega_{\text{Z}_2\text{Cu}}$
R10	$\text{NH}_3 + \text{ZCu} \leftrightarrow \text{ZCuNH}_3$	$r_{\text{AdSZCu}} = k_{\text{AdSZCu}} y_{\text{NH}_3,s} \theta_{\text{ZCu}} \Omega_{\text{ZCu}}$ $r_{\text{DesZCu}} = k_{\text{DesZCu}} \theta_{\text{ZCuNH}_3} \Omega_{\text{ZCu}}$
R11	$\text{NH}_3 + \text{ZCuNH}_3 \leftrightarrow \text{ZCu}(\text{NH}_3)_2$	$r_{\text{AdSZCuNH}_3} = k_{\text{AdSZCuNH}_3} y_{\text{NH}_3,s} \theta_{\text{ZCuNH}_3} \Omega_{\text{ZCu}}$ $r_{\text{DesZCuNH}_3} = k_{\text{DesZCuNH}_3} \theta_{\text{ZCu}(\text{NH}_3)_2} \Omega_{\text{ZCu}}$

3.2 Results

Figure S2 compares the NO consumption experimental data against the model predictions. While the model reasonably predicts the overall qualitative NO consumption rates, the initial NO consumption is significantly underpredicted. This is associated with the requirement for NH₃ solvation of Z₂Cu and ZCuOH sites prior to reduction, inconsistent with observed experimental data.

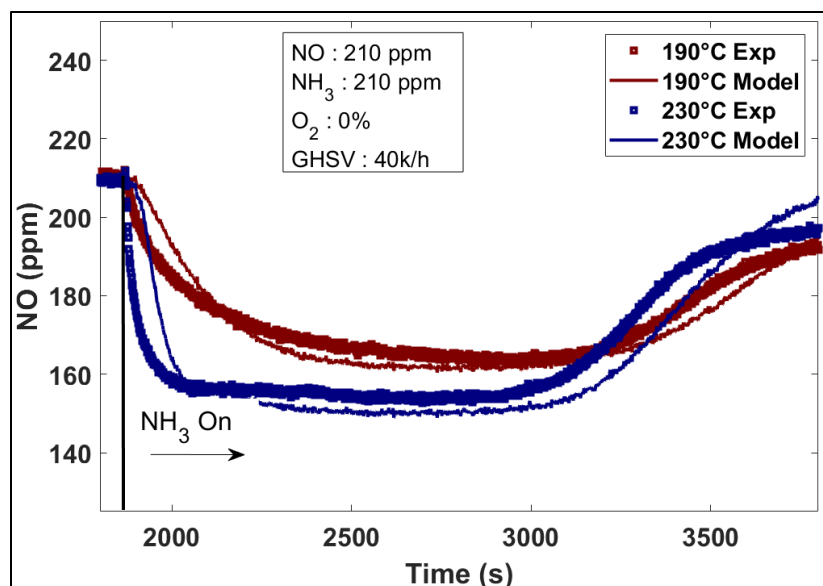


Figure S2. NO Consumption during NO + NH₃ titration of Cu²⁺ sites. Squares represent experimental data and lines represents model results (190°C in dark red, 230°C in dark blue)

4. Influence of SCR reaction with gas-phase NH₃ on Dynamic NO_x Conversion at 200°C and 175°C

Figure S3 plots the complete dynamic NO_x conversion curve at 200°C and 175°C, comparing the two kinetic models with experimental data. The influence of the SCR reaction with gas-phase NH₃ is primarily observed at low NH₃ coverage and the addition of this reaction in the kinetic model leads to accurate representation of the experimental data.

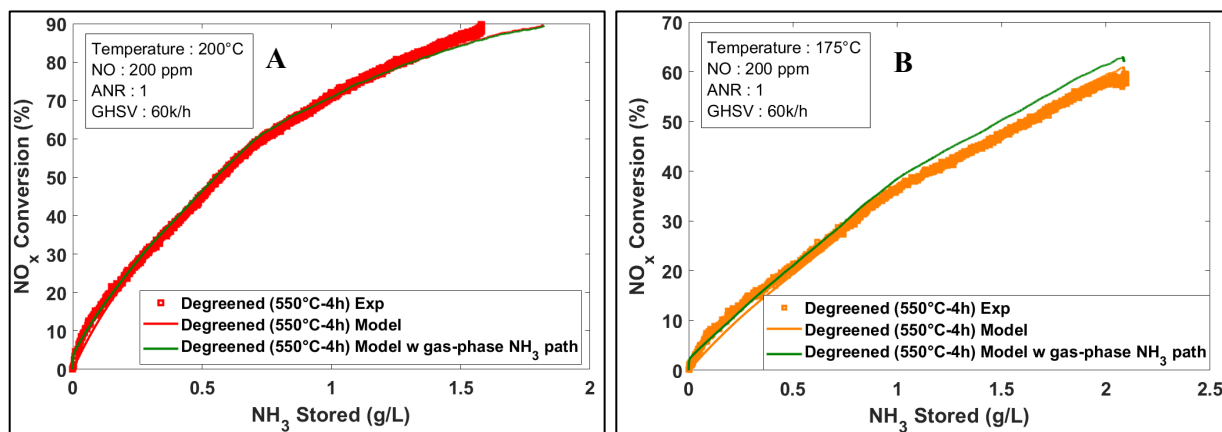


Figure S3. NO_x Conversion as a function of NH₃ storage under standard SCR conditions at **A.** 200°C and **B.** 175°C.

Squares represent experimental data and lines represent model results

5. Standard SCR Reaction Order in NH₃

5.1 Analytical Expression

In general, the NH₃ reaction order for standard SCR can be estimated as:

$$O_{\text{NH}_3} = y_{\text{NH}_3,s} \frac{\partial \ln(r_{\text{sscr}})}{\partial y_{\text{NH}_3,s}} \quad (1)$$

Utilizing the rate expressions for standard SCR with adsorbed-NH₃ and gas-phase NH₃ (Table 1 in main manuscript), we can write the overall SCR rate as:

$$r_{\text{sscr}} = k_{\text{sscr1}} y_{\text{NO},s} y_{\text{O}_2}^{0.32} \theta_{\text{NH}_3\text{S1}} \Omega_1 + \frac{k_{\text{sscr2}} y_{\text{NO}} y_{\text{O}_2}^{0.32} y_{\text{NH}_3,s} \Omega_1}{1 + K_{\text{inh}} y_{\text{NH}_3,s}} \quad (2)$$

The definition of steady state can be used to express the NH₃ surface coverage as a function of the NO and NH₃ surface mole fractions, as shown in equation (4).

$$\frac{\partial \theta_{\text{NH}_3\text{S1}}}{\partial t} = k_{\text{Ads}} y_{\text{NH}_3,s} (1 - \theta_{\text{NH}_3\text{S1}}) - (k_{\text{Des1}} + k_{\text{Des2}}) \theta_{\text{NH}_3\text{S1}} - k_{\text{sscr1}} y_{\text{NO},s} y_{\text{O}_2}^{0.32} \theta_{\text{NH}_3\text{S1}} = 0 \quad (3)$$

$$\Rightarrow \theta_{\text{NH}_3\text{S1}} = \frac{k_{\text{Ads}} y_{\text{NH}_3,s}}{k_{\text{Ads}} y_{\text{NH}_3,s} + (k_{\text{Des1}} + k_{\text{Des2}}) + k_{\text{sscr1}} y_{\text{NO},s} y_{\text{O}_2}^{0.32}} \quad (4)$$

Using the result from equation (4) in equation (2), we have:

$$r_{\text{sscr}} = \frac{k_{\text{sscr1}} y_{\text{NO},s} y_{\text{O}_2}^{0.32} k_{\text{Ads}} y_{\text{NH}_3,s} \Omega_1}{k_{\text{Ads}} y_{\text{NH}_3,s} + (k_{\text{Des1}} + k_{\text{Des2}}) + k_{\text{sscr1}} y_{\text{NO},s} y_{\text{O}_2}^{0.32}} + \frac{k_{\text{sscr2}} y_{\text{NO}} y_{\text{O}_2}^{0.32} y_{\text{NH}_3,s} \Omega_1}{1 + K_{\text{inh}} y_{\text{NH}_3,s}} \quad (5)$$

Multiplying both sides of equation (5) by the natural logarithm, we obtain the following result:

$$\begin{aligned} \ln r_{\text{sscr}} = & \ln(k_{\text{sscr1}} y_{\text{O}_2}^{0.32} \Omega_1) + \ln y_{\text{NO},s} + \ln(k_{\text{Ads}} y_{\text{NH}_3,s}) - \ln(k_{\text{Ads}} y_{\text{NH}_3,s} + (k_{\text{Des1}} + k_{\text{Des2}}) + \\ & k_{\text{sscr1}} y_{\text{NO},s} y_{\text{O}_2}^{0.32}) + \ln(k_{\text{sscr2}} y_{\text{O}_2}^{0.32} \Omega_1) + \ln y_{\text{NO},s} + \ln y_{\text{NH}_3,s} - \ln(1 + K_{\text{inh}} y_{\text{NH}_3,s}) \end{aligned} \quad (6)$$

Differentiating equation (6) in $y_{\text{NH}_3,s}$ and using the result in equation (1) leads to the following expression for NH₃ reaction order

$$\begin{aligned} O_{\text{NH}_3} = y_{\text{NH}_3,s} \frac{\partial \ln(r_{\text{sscr}})}{\partial y_{\text{NH}_3,s}} = & y_{\text{NH}_3,s} \left(\frac{1}{y_{\text{NO},s}} \frac{\partial y_{\text{NO},s}}{\partial y_{\text{NH}_3,s}} + \frac{1}{y_{\text{NH}_3,s}} - \frac{k_{\text{Ads}} + \frac{\partial(k_{\text{Des1}} + k_{\text{Des2}})}{\partial y_{\text{NH}_3,s}} + k_{\text{sscr1}} y_{\text{O}_2}^{0.32} \frac{\partial y_{\text{NO},s}}{\partial y_{\text{NH}_3,s}}}{k_{\text{Ads}} y_{\text{NH}_3,s} + (k_{\text{Des1}} + k_{\text{Des2}}) + k_{\text{sscr1}} y_{\text{NO},s} y_{\text{O}_2}^{0.32}} + \right. \\ & \left. \frac{1}{y_{\text{NO},s}} \frac{\partial y_{\text{NO},s}}{\partial y_{\text{NH}_3,s}} + \frac{1}{y_{\text{NH}_3,s}} - \frac{K_{\text{inh}}}{(1 + K_{\text{inh}} y_{\text{NH}_3,s})} \right) \end{aligned} \quad (7)$$

$$\Rightarrow \theta_{\text{NH}_3} = 2 + 2 \frac{y_{\text{NH}_3,s}}{y_{\text{NO},s}} \frac{\partial y_{\text{NO},s}}{\partial y_{\text{NH}_3,s}} - \frac{y_{\text{NH}_3,s} (k_{\text{Ads}} + \frac{\partial(k_{\text{Des1}} + k_{\text{Des2}})}{\partial y_{\text{NH}_3,s}} + k_{\text{SScr1}} y_{\text{O}_2}^{0.32} \frac{\partial y_{\text{NO},s}}{\partial y_{\text{NH}_3,s}})}{k_{\text{Ads}} y_{\text{NH}_3,s} + (k_{\text{Des1}} + k_{\text{Des2}}) + k_{\text{SScr1}} y_{\text{NO},s} y_{\text{O}_2}^{0.32}} - \frac{K_{\text{inh}} y_{\text{NH}_3,s}}{(1 + K_{\text{inh}} y_{\text{NH}_3,s})} \quad (8)$$

5.2 NH₃ Coverage as a Function of NH₃ Surface Mole Fraction

The model estimated mean NH₃ coverage as a function of the NH₃ surface mole fraction is shown in Figure S4. A linear relationship is observed below an ANR of 0.7, as expected for Langmuir-type adsorption isotherms at low partial pressures.

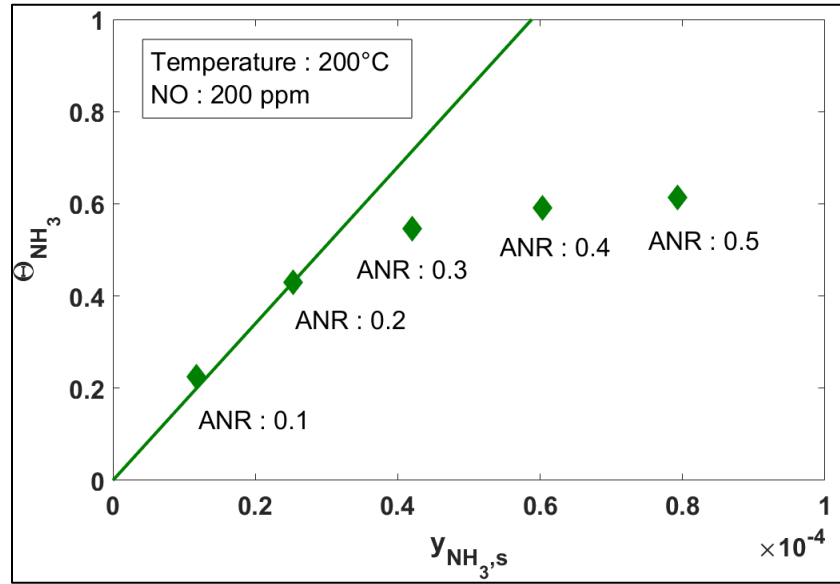


Figure S4. Mean NH₃ surface coverage as a function of NH₃ surface mole fraction. Green diamonds represent model results from ANR sweep at 200°C and solid line represents a linear regression fit

5.3 ANR Sweep Repeatability

ANR sweep experiments were conducted at 200°C to identify the SCR reaction order with NH₃. Each ANR point was repeated three times to establish repeatability, and the results are summarized in Table S3. In general, NO_x conversion and NH₃ storage values were repeatable at all ANRs included in the test, leading to minor deviations in estimated turnover rates and mean NH₃ surface coverages. Turnover rates (TORs) were calculated by normalizing the NO_x consumption rate with the total reducible Cu sites quantified from NO + NH₃ titration experiments.

Table S3
ANR Sweep Test Results at 200°C

NO _x Feed (ppm)	ANR	NH ₃ Feed (ppm)	NH ₃ Conversion (%)	NO _x Conversion (%)	NH ₃ Storage (g/L)	Mean NH ₃ Coverage	ln(Mean NH ₃ Coverage)	NO _x Flow (mol/s)	TOR (mol _{NO} /mol _{Cu} -s)	ln(TOR)
199.89	0.33	66.37	99.42	33.92	0.71	0.25	-1.40	8.53E-08	1.04E-03	-6.87
201.38	0.33	66.82	99.35	33.17	0.70	0.24	-0.35	8.59E-08	1.02E-03	-6.88
202.80	0.33	67.07	99.50	33.66	0.71	0.24	-0.34	8.65E-08	1.05E-03	-6.86
200.85	0.28	56.26	99.35	28.52	0.62	0.21	-0.48	8.57E-08	8.79E-04	-7.04
201.70	0.28	56.43	99.31	28.78	0.63	0.22	-0.46	8.61E-08	8.90E-04	-7.02
202.78	0.28	56.62	99.34	29.14	0.62	0.21	-0.48	8.65E-08	9.06E-04	-7.01
201.76	0.23	45.60	99.33	23.25	0.51	0.17	-0.68	8.61E-08	7.20E-04	-7.24
202.07	0.23	45.96	99.24	23.44	0.50	0.17	-0.69	8.62E-08	7.27E-04	-7.23
202.75	0.23	46.10	99.26	23.26	0.50	0.17	-0.69	8.65E-08	7.24E-04	-7.23
201.63	0.17	35.14	99.20	18.24	0.43	0.15	-0.83	8.60E-08	5.64E-04	-7.48
202.47	0.17	35.29	98.96	18.34	0.40	0.14	-0.92	8.64E-08	5.70E-04	-7.47
202.51	0.17	35.25	99.07	18.10	0.42	0.14	-0.87	8.64E-08	5.62E-04	-7.48
200.70	0.12	24.53	98.90	12.63	0.30	0.10	-1.21	8.56E-08	3.89E-04	-7.85
202.16	0.12	24.54	98.81	12.59	0.32	0.11	-1.15	8.63E-08	3.90E-04	-7.85
202.55	0.12	24.81	98.90	12.71	0.32	0.11	-1.14	8.64E-08	3.95E-04	-7.84

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