

**Supporting Information for: Extending Timescale of Molecular Simulations by Using
Time-Temperature Superposition: Rheology of Ionic Liquids**

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Table S1: Simulation run information of the steady shear for viscosity calculation.

| Shear rate, $\dot{\gamma}$ (s ⁻¹) | Simulation run time (ns) |
|---|--------------------------|
| 5×10^6 | 40 |
| 7×10^6 | 40 |
| 1×10^7 | 40 |
| 1.5×10^7 | 40 |
| 2.5×10^7 | 10 |
| 5×10^7 | 10 |
| 1×10^8 | 10 |
| 2.5×10^8 | 10 |
| 1×10^9 | 10 |
| 1×10^{10} | 10 |
| 5×10^{10} | 10 |
| 1×10^{11} | 10 |

Table S2: Simulation run information of the oscillatory shear for moduli calculation.

| Frequency, ω (rad s ⁻¹) | Number of oscillations | simulation run time (ns) |
|--|------------------------|--------------------------|
| 2×10^9 | 24 | 72 |
| 5×10^9 | 70 | 84 |
| 1×10^{10} | 120 | 72 |
| 2×10^{10} | 120 | 36 |
| 5×10^{10} | 120 | 14.4 |
| 1×10^{11} | 120 | 7.2 |

Table S3: Zero shear viscosity at different temperatures

| Temperature (K) | Zero shear viscosity, η_o (Pa s) |
|-----------------|---------------------------------------|
| 300 | 0.7729 ± 0.0428 |
| 340 | 0.0720 ± 0.0014 |
| 380 | 0.0171 ± 0.0004 |
| 420 | 0.0070 ± 0.0008 |
| 460 | 0.0038 ± 0.0004 |

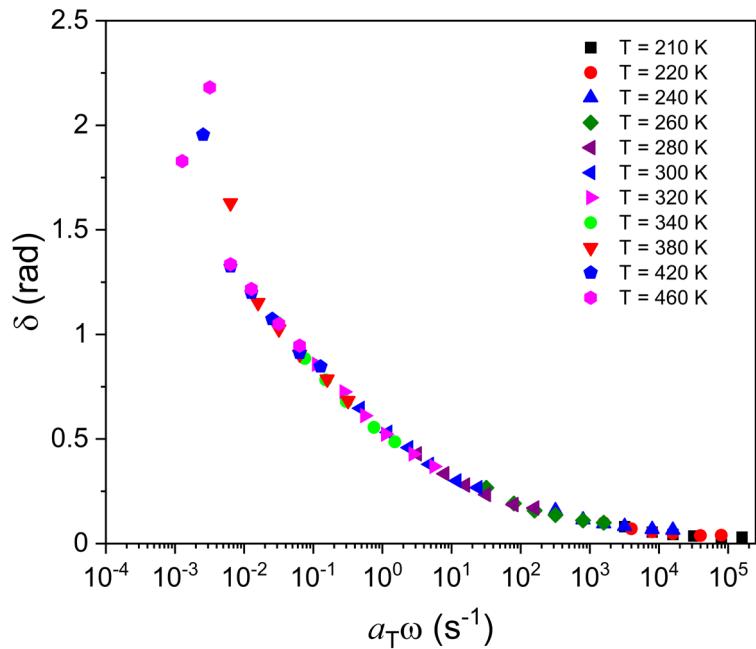


Fig. S1 Master curve of phase angle as a function of the rescaled frequency constructed at a reference temperature of 300 K.

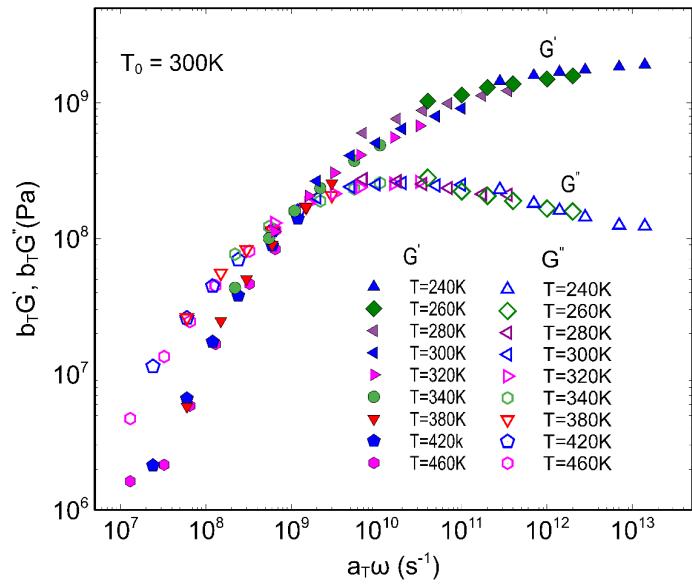


Fig. S2 Master curve of the moduli data using the same shift factors obtained from the MSD master curves at a reference temperature of 300 K.