

***In situ* TEM investigation of large crystals formation in lithiated SnO₂ anode assisted by electron beam irradiation**

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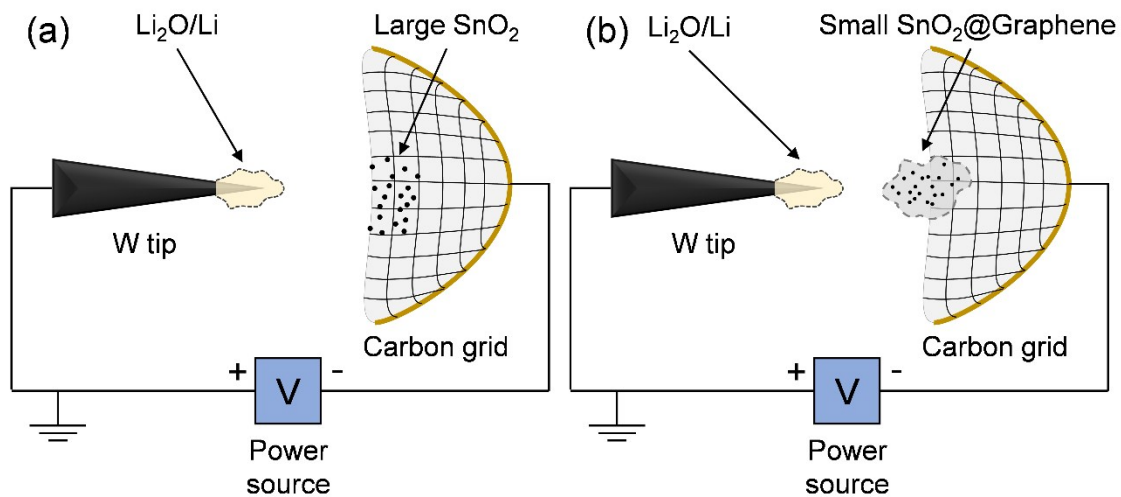


Fig S1. Schematic illustration of the experimental setup for (a) large SnO₂ sample (larger than 50 nm) and (b) small SnO₂ sample (smaller than 50 nm).

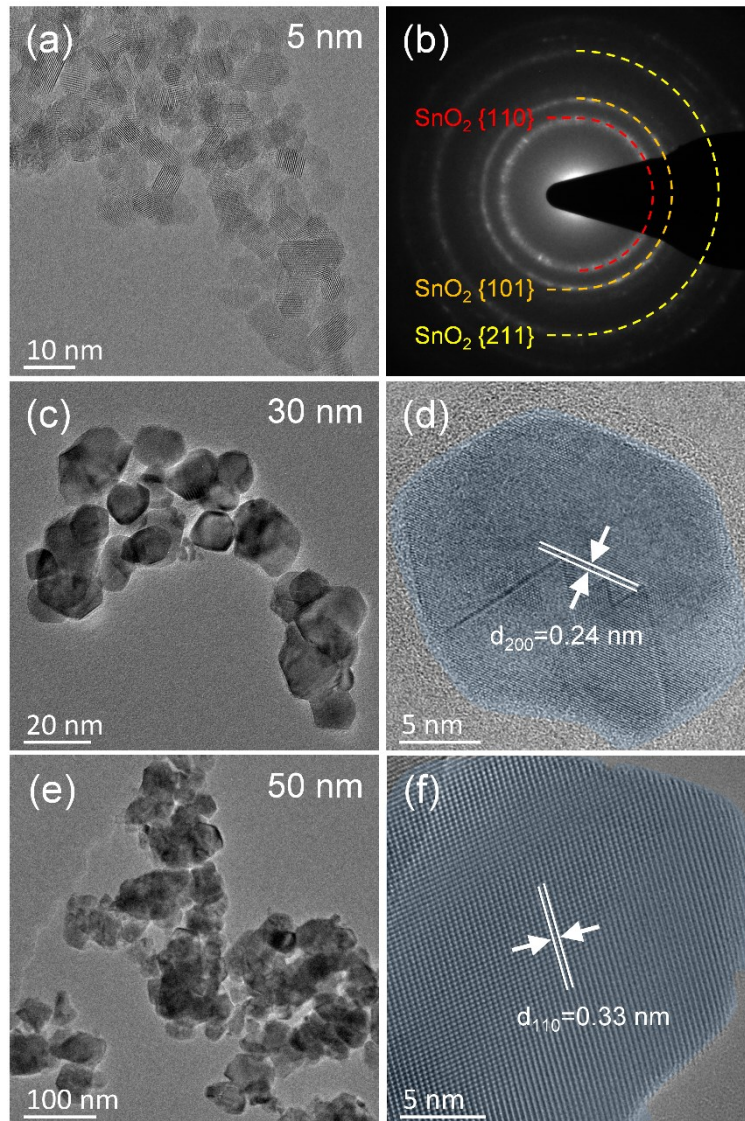


Fig S2. SnO₂ nanoparticles with different size (a, b) 5 nm; (c, d) 30 nm; (e, f) 50 nm.

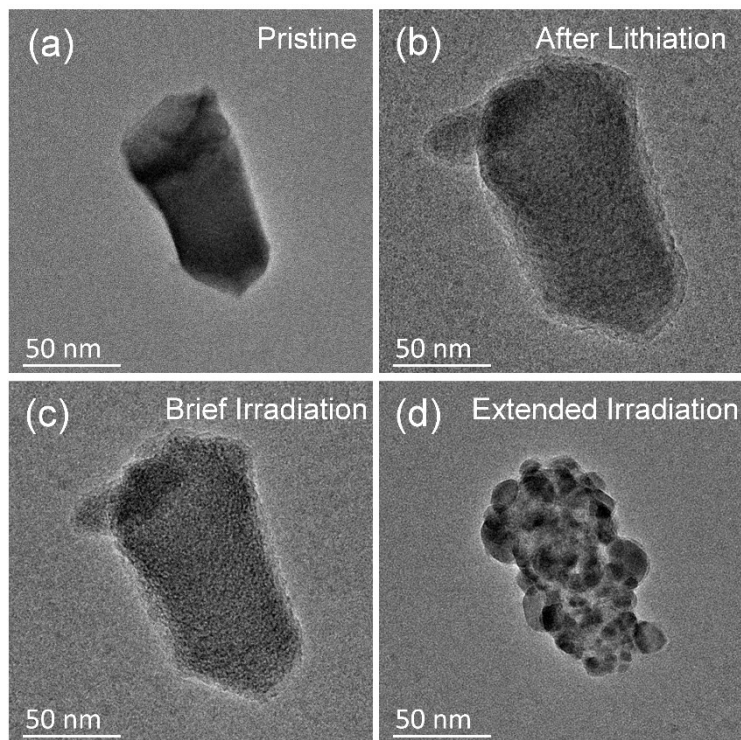


Fig S3. The structural transformation of a SnO₂ particles after lithiation and after irradiation. The pristine crystalline SnO₂ particle (a) was converted to the amorphous phase after lithiation (b). The sample was then be irradiated by electron beam with the lithium source removed. After brief irradiation (c), the amorphous sample shrank, and SEI decomposed. With the irradiation extending (d), numerous large crystals were formed.

Facets Matching Method

For each 2D lattice image, two sets of lattices, d_{1exp} and d_{2exp} and the crossing angle θ_{exp} can be directly measured from the image. In order to check if the certain phase might expose a similar 2D lattice, the following comparison algorithm is applied.

1. Calculate theoretical lattice spacing for each facet. The theoretical interplanar spacing d_{theo} of (h, k, l) plane with crystal constant $(a, b, c, \alpha, \beta, \gamma)$ is calculated according to Eq. 1:

$$d_{theo}^2 = V^2 / ((S_{11}h)^2 + (S_{22}k)^2 + (S_{33}l)^2 + 2(S_{12}hk + S_{13}hl + S_{23}kl)) \quad (\text{Eq.1})$$

where $V = abc(1 - \cos(\alpha)^2 - \cos(\beta)^2 - \cos(\gamma)^2 + 2\cos(\alpha)\cos(\beta)\cos(\gamma))$, $S_{11} = bcsin(\alpha)$, $S_{22} = acsin(\beta)$, $S_{33} = absin(\gamma)$, $S_{12} = abc^2(\cos(\alpha)\cos(\beta) - \cos(\gamma))$, $S_{13} = ab^2c(\cos(\alpha)\cos(\gamma) - \cos(\beta))$, $S_{23} = a^2bc(\cos(\beta)\cos(\gamma) - \cos(\alpha))$.

2. Create comparison list. The comparison list $D_{d1exp}[n]$ and $D_{d2exp}[m]$ of the experimentally observed lattice spacing is secondly created. If $\text{abs}(d_{theo} - d_{exp}) < \delta d$, where δd is the pre-defined accuracy, vector (h, k, l, d_{theo}) will be appended to the $D_{dexp}[n]$.

3. Calculate theoretical crossing angle. After obtaining both the $D_{d1exp}[n]$ and $D_{d2exp}[m]$, the theoretical crossing angle $\theta_{theo}[i, j]$ between $D_{d1exp}[i]$, $i \in n$, and $D_{d2exp}[j]$, $j \in m$, is calculated according to Eq. 2:

$$\theta_{theo}[i, j] = \arccos(d_{1theo}[i] d_{2theo}[j] / (V^2(S_{11}h_1[i]h_2[j] + S_{22}k_1[i]k_2[j] + S_{33}l_1[i]l_2[j] + S_{12}h_1[i]k_2[j] + S_{12}k_1[i]h_2[j] + S_{13}h_1[i]l_2[j] + S_{13}l_1[i]h_2[j] + S_{23}k_1[i]l_2[j] + S_{23}l_1[i]h_2[j]))) \quad (\text{Eq.2})$$

If the theoretical crossing angle is within the permissible error range to the experimental angle, namely $\text{abs}(\theta_{theo}[i, j] - \theta_{exp}) < \delta\theta$, (h_1, k_1, l_1) and (h_2, k_2, l_2) are considered as a set of matching 2D lattice. In this paper, δd is set to 0.05\AA and $\delta\theta$ set to 3° .

Table S1. Matching results for the three facets in Figure 2.

Lattice Phase	$d_{1exp}=0.28\text{nm}$, $d_{2exp}=0.28\text{nm}$, $\theta_{exp}=139^\circ$	$d_{1exp}=0.28\text{nm}$, $d_{2exp}=0.20\text{nm}$, $\theta_{exp}=78^\circ$	$d_{1exp}=0.29\text{nm}$, $d_{2exp}=0.28\text{nm}$, $\theta_{exp}=90^\circ$
Tetragonal Sn	No Match	$d_{101}=0.279\text{nm}$, $d_{211}=0.201\text{nm}$, $\theta_{theo}=77.0^\circ$	$d_{200}=0.291\text{nm}$, $d_{011}=0.279\text{nm}$, $\theta_{theo}=90.0^\circ$
Cubic Sn	No Match	No Match	No Match
LiSn	No Match	No Match	No Match
Li ₅ Sn ₂	No Match	$d_{105}=0.285\text{nm}$, $d_{022}=0.201\text{nm}$, $\theta_{theo}=78.8^\circ$	No Match
Li ₇ Sn ₃	No Match	$d_{221}=0.285\text{nm}$, $d_{122}=0.206\text{nm}$, $\theta_{theo}=80.4^\circ$	No Match
Li ₇ Sn ₂	No Match	$d_{240}=0.282\text{nm}$, $d_{421}=0.208\text{nm}$, $\theta_{theo}=76.0^\circ$	No Match
Li ₁₃ Sn ₅	No Match	$d_{007}=0.283\text{nm}$, $d_{022}=0.201\text{nm}$, $\theta_{theo}=78.0^\circ$	No Match
Li ₂₂ Sn ₅	$d_{107}=0.279\text{nm}$, $d_{345}=0.279\text{nm}$, $\theta_{theo}=139.5^\circ$	$d_{700}=0.283\text{nm}$, $d_{293}=0.204\text{nm}$, $\theta_{theo}=78.1^\circ$	$d_{603}=0.295\text{nm}$, $d_{700}=0.283\text{nm}$, $\theta_{theo}=90.0^\circ$

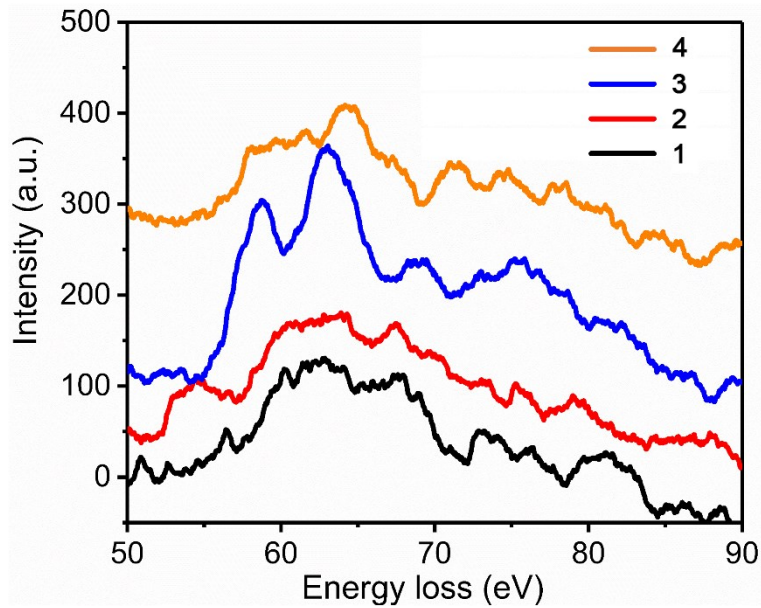


Fig S4. EELS spectra of the Li-K edge of the carbon support with different treatments: (1) 30 mins' placement with 0 min's irradiation; (2) 30 mins' placement with 15 mins' irradiation; (3) 0 min's placement with 0 min's irradiation; (4) 0 min's placement with 25 mins' irradiation.

The spectra were collected in the same carbon support area (~150 nm apart from the sample) under an imaging mode. For spectrum 1 (black line), it was collected when the freshly lithiated SnO₂ particle (~70 nm) was placed for 30 min. Subsequently, the entire area with a diameter about 1 μm, including the employed carbon area and the lithiated SnO₂, was irradiated under an electron beam dose of $1.19 \times 10^5 \text{ A m}^{-2}$. When the irradiation time reached to 15 minutes, the EELS spectrum was then collected in the carbon support area (red line, 2). After that, the SnO₂ sample was re-lithiated and the EELS spectrum was immediately acquired without placement and irradiation (blue line, 3). Finally, the entire area was irradiated for 25 minutes and the EELS spectrum was obtained (orange line, 4).

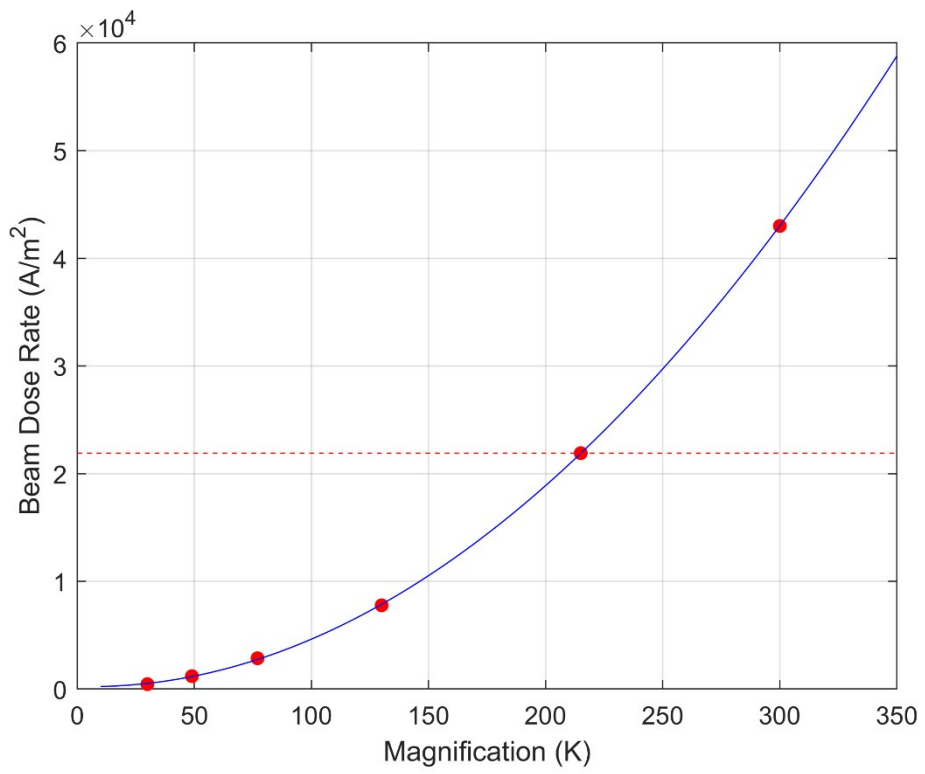


Fig S5. The quadric dependency between the Beam Dose Rate and TEM Magnification. Electron beam with dose rate beyond 21940 A m⁻² can result in large crystal formation in a lithiated SnO₂ particle.

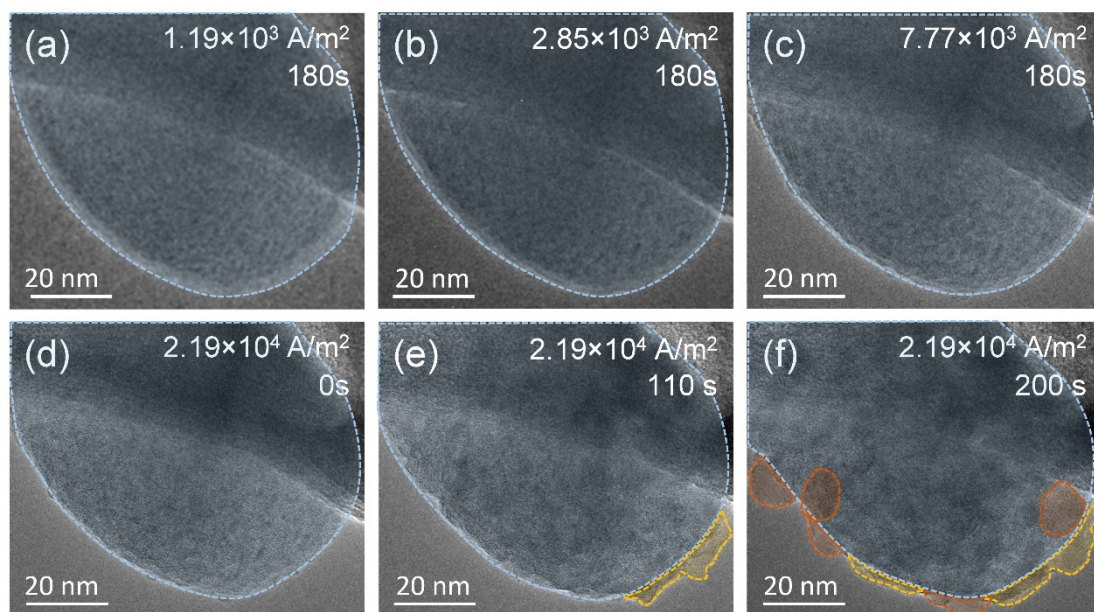


Figure S6. The effect of electron beam irradiation on the amorphous lithiated SnO₂ particle. The amorphous particle was irradiated by an electron beam for 180 s under a sequentially increasing dose rate of (a) 1190 A m^{-2} , (b) 2850 A m^{-2} , (c) 7770 A m^{-2} , and (d-f) 21900 A m^{-2} . The formation of large crystal (marked in orange) was observed after the amorphous sample being irradiated for 200 s under the dose rate of 21900 A m^{-2} .

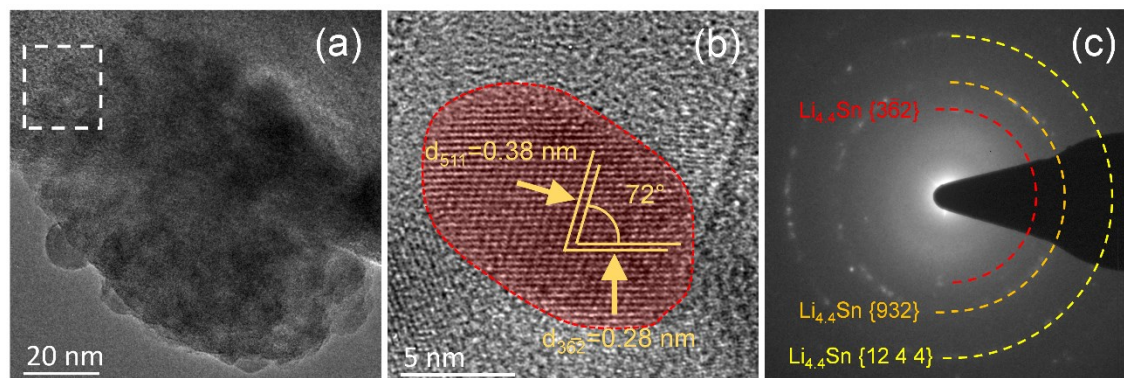


Figure S7. Identification of the phase of formed large crystal in the irradiated sample. (a) TEM image of the sample after 200s' irradiation at $2.19 \times 10^4 \text{ A m}^{-2}$. (b) HRTEM of one nanocrystal. (c) SAED image of the sample.

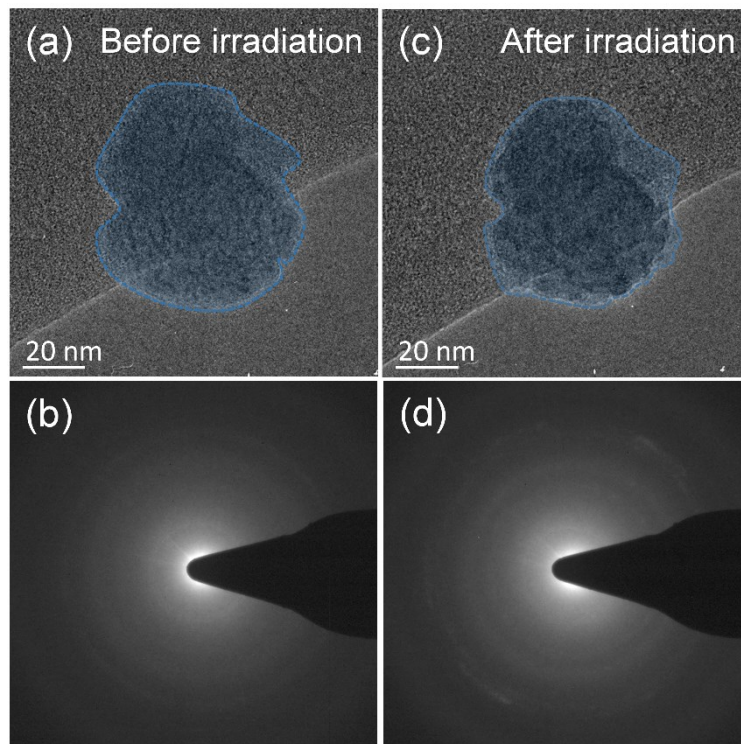


Fig S8. Extending irradiation experiment of lithiated SnO₂ particle with a moderate dose rate. (a, b) TEM and SAED image of the amorphous sample before irradiation. (c, d) TEM and SAED image of the sample after irradiation. Beam dose: $6.13 \times 10^3 \text{ A m}^{-2}$, Duration: 30 mins.

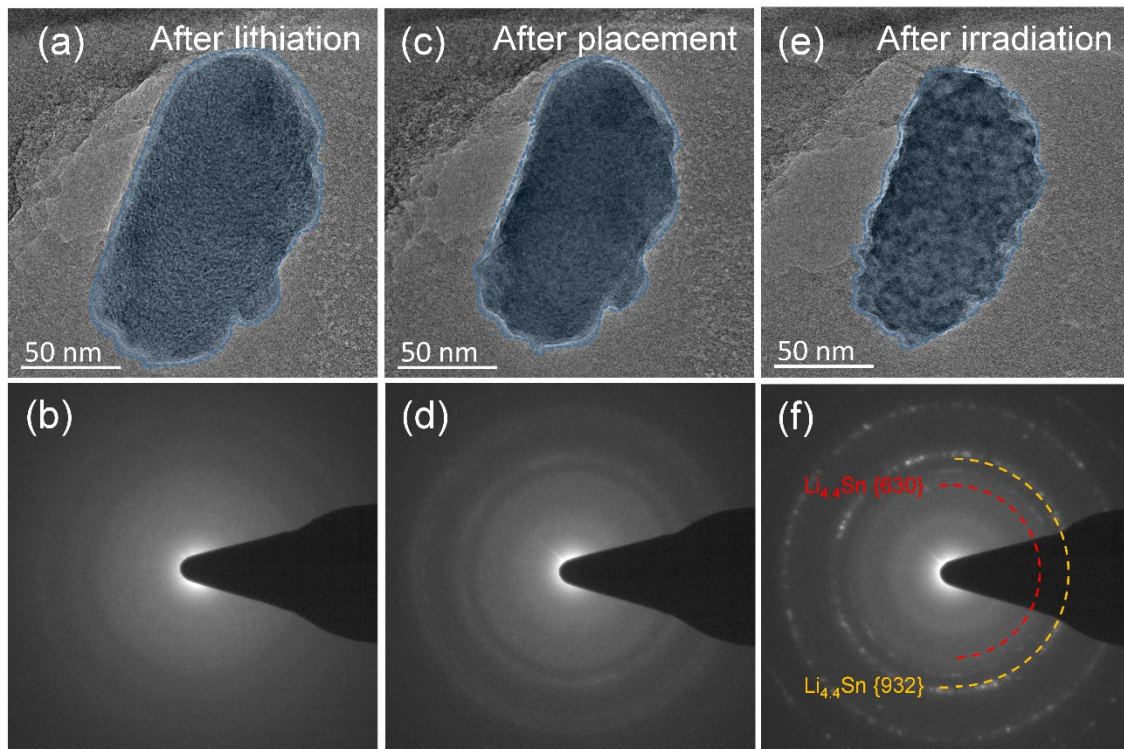


Fig S9. Phase transition of lithiated SnO_2 particle after placement and after irradiation. TEM and SAED image of the (a, b) freshly lithiated amorphous sample, (c, d) amorphous sample after placement, and (e, f) nanocrystalline sample after irradiation.

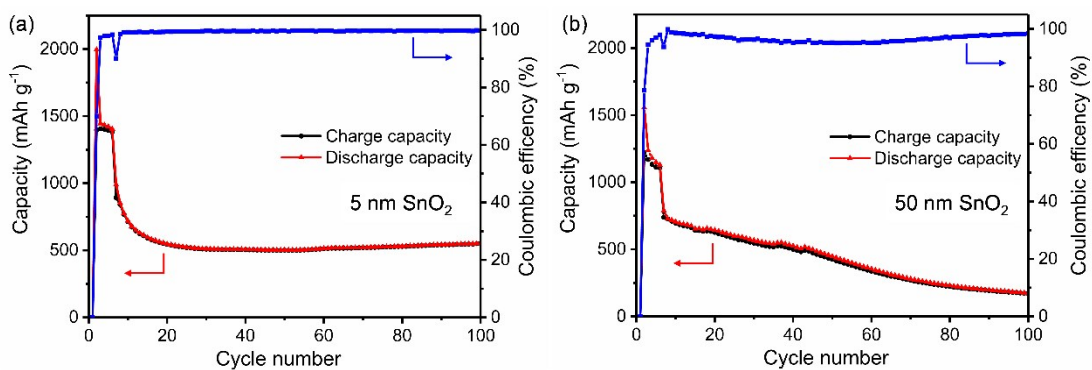


Figure S10. The cycling performance of (a) 5 nm SnO₂ and (b) 50 nm SnO₂ under a current density of 1000 mA g⁻¹ between the voltage range of 0.01 V and 3 V vs Li⁺/Li. The cell was first discharged/charged under a small current density of 50 mA g⁻¹ during the initial 5 cycles to activate the anode materials. The small-sized SnO₂ showed superior cycling stability and reversibility compared with large SnO₂.

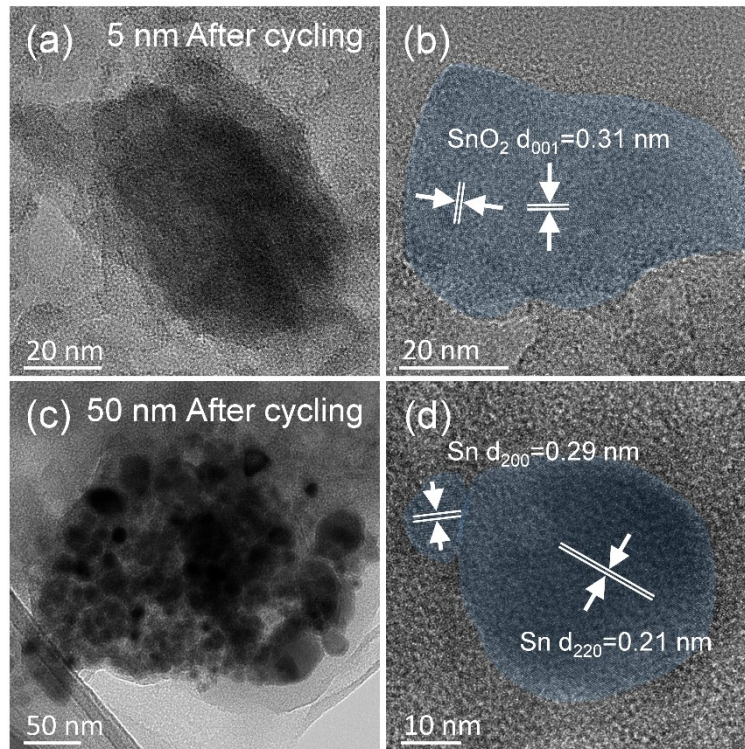


Fig S11. TEM and HRTEM images of the cycled anode in charged state. (a, b) 5 nm SnO₂ anode; (c, d) 50 nm SnO₂ anode.

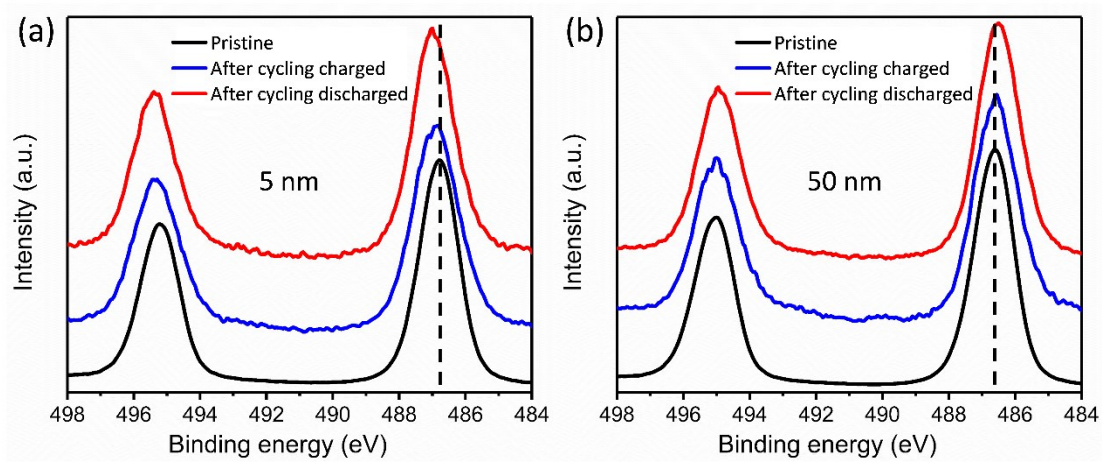


Fig S12. Sn 3d XPS spectra for the SnO₂ anode. (a) The pristine 5 nm SnO₂ anode, 5 nm SnO₂ anode after 100 cycles in charged and discharged state; (b) The pristine 50 nm SnO₂ anode, 50 nm SnO₂.