Supplementary Information

Bonding Heterogeneity in Mixed-Anion Compounds Realizes Ultralow Lattice Thermal Conductivity

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Figure S1. The total charge density of (a) $MnSbS_2Cl$ and (b) $MnBiS_2Cl$ with isosurface value of 0.05 e bohr⁻³, and the electron localization function (ELF) of (c) $MnSbS_2Cl$ and (d) $MnBiS_2Cl$ with isosurface value of 0.80 for (c) and 0.72 for (d), respectively. The black, red, purple, yellow, and green atoms represent Mn, Sb, Bi, S, and Cl, respectively.



Figure S2. The calculated potential energy of each atomic site as a function of displacements along cartesian x-, y-, and z-directions for MnSbS₂Cl, MnBiS₂Cl, and CuTaS₃ with fitting curves using only quadratic term.



Figure S3. The calculated potential energy of each atomic site as a function of displacements along cartesian x-, y-, and z-directions for MnSbS₂Cl, MnBiS₂Cl, and CuTaS₃.



Figure S4. The calculated mean square displacement as a function of temperature along cartesian x-, y-, and z-directions for MnSbS₂Cl, MnBiS₂Cl, and CuTaS₃.



Figure S5. The calculated phonon group velocity as a function of the phonon frequency for MnSbS₂Cl, MnBiS₂Cl, and CuTaS₃.



Figure S6. The calculated spectral lattice thermal conductivity, κ_{spec} , as a function of the phonon frequency for MnSbS₂Cl, MnBiS₂Cl, and CuTaS₃.



Figure S7. The XRD patterns of the polycrystalline bulk samples prepared by SPS for MnSbS₂Cl, MnBiS₂Cl, and CuTaS₃, together with their simulated patterns. Black arrows denote unknown impurity phases.

Table S1. Lattice parameters of the relaxed primitive cell of MnSbS₂Cl, MnBiS₂Cl, and CuTaS₃.

Material	a (Å)	b (Å)	c (Å)
MnSbS ₂ Cl	9.1800	3.7704	12.039
MnBiS ₂ CI	9.1672	3.8346	12.111
CuTaS₃	9.3918	3.4628	11.688