

— **Supplementary Information** —

**Defect Chemistry and Doping of BiCuSeO**

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## Pristine and Interstitial Structures

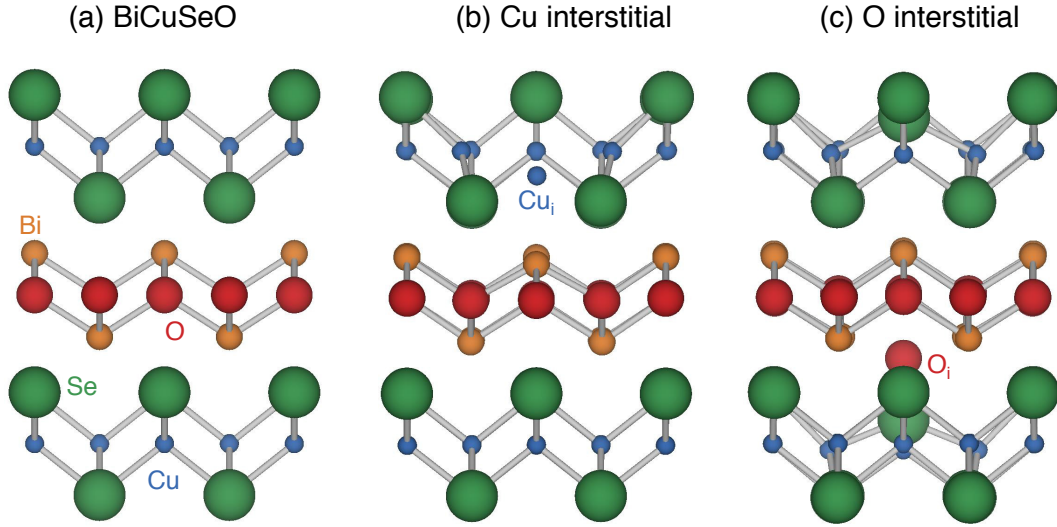


Figure S1: (a) Crystal structure of BiCuSeO, (b) Structure of copper interstitial ( $\text{Cu}_i^{+1}$ ), and (c) Structure of oxygen interstitial ( $\text{O}_i^0$ ).

## Calculated Lattice Parameters

Method	$a$ ( $\text{\AA}$ )	$c$ ( $\text{\AA}$ )	$a$ Error (%)	$c$ Error (%)
PBE + $U$	3.949	9.062	0.52	1.49
vdW + $U$	3.926	8.927	0.08	0.02
Experiment <sup>1</sup>	3.929	8.929		

Table S1: Lattice constants calculated using different functionals and compared to experimental values.<sup>1</sup> The experimental lattice constants are better reproduced with the van der Waals-corrected functional with Hubbard  $U$  correction (vdW+ $U$ ).

## Electronic Structure of BiCuSeO

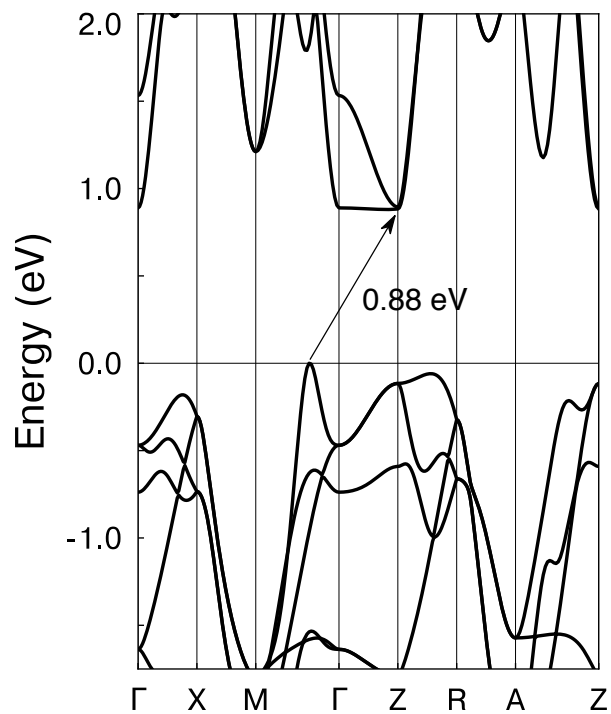


Figure S2: Computed electronic band structure of BiCuSeO along the special  $k$ -point paths of the Brillouin zone. The band edge positions are rigidly shifted to according to GW and spin-orbit coupling calculations.

## Elemental Reference Chemical Potentials

Element	$\mu^0$ (eV)
Bi	-4.42
Cu	-1.65
Se	-3.63
O	-4.76
Li	-1.64
Zn	-0.80
Mg	-1.00
Ca	-1.60
Sr	-1.15
Ba	-1.34
Al	-2.81
Ga	-2.30
In	-2.27
Tl	-2.35
Si	-4.74
Ge	-4.07
Sn	-3.65
Pb	-3.79
Sc	-4.49
Y	-4.81
Ti	-5.39
Zr	-5.97
Hf	-7.51
F	-1.52
Cl	-1.73
Br	-1.74
I	-1.67

Table S2: Elemental reference chemical potentials  $\mu^0$ , fitted to experimental formation enthalpies.<sup>2,3</sup> GGA+U functional is used to calculate the total energy of the compounds used in the fitting.

## Phase Equilibria of BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$p - n$ ( $\text{cm}^{-3}$ )
Se, $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{Se}_3$	-0.378	-0.62	-1.923	0.0	$7.36 \times 10^{19}$
Se, $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{O}_3$	-0.602	-0.708	-1.61	0.0	$1.26 \times 10^{20}$
Se, $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{Se}_3$	-0.378	-0.708	-1.835	0.0	$1.25 \times 10^{20}$
Se, $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_3$	-0.865	-0.62	-1.435	0.0	$7.48 \times 10^{19}$
$\text{Cu}_2\text{O}$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_3$	-0.603	-0.445	-1.61	-0.262	$2.6 \times 10^{19}$
$\text{Cu}_2\text{Se}$ , $\text{Cu}_2\text{O}$ , $\text{Cu}_3\text{Se}_2$	-0.285	-0.318	-1.864	-0.453	$1.13 \times 10^{19}$
Bi, $\text{Cu}_2\text{O}$ , $\text{Bi}_2\text{O}_3$	0.0	-0.244	-2.012	-0.664	$5.61 \times 10^{18}$
Bi, $\text{Cu}_2\text{Se}$ , $\text{Cu}_2\text{O}$	0.0	-0.223	-2.054	-0.643	$5.11 \times 10^{18}$
Bi, $\text{Cu}_2\text{Se}$ , $\text{Cu}_3\text{Se}_2$	0.0	-0.318	-2.149	-0.453	$1.1 \times 10^{19}$
Bi, $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{Se}_3$	0.0	-0.452	-2.216	-0.252	$2.33 \times 10^{19}$
Bi, $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{O}_3$	0.0	-0.507	-2.012	-0.402	$3.44 \times 10^{19}$
Bi, $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{Se}_3$	0.0	-0.582	-2.087	-0.252	$5.4 \times 10^{19}$

Table S3: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quaternary Bi-Cu-Se-O phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## Native Defects in BiCuSeO

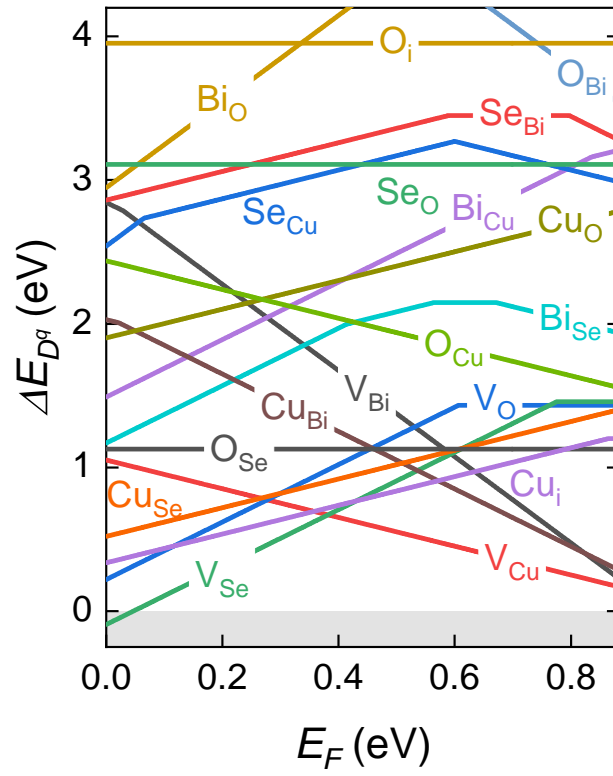


Figure S3: Formation energy ( $\Delta E_{Dq}$ ) as a function of Fermi energy ( $E_F$ ) of all native defects in BiCuSeO under the most Cu-rich condition where BiCuSeO is in equilibrium with Bi,  $Cu_2Se$ , and  $Cu_2O$ .

## Group-2 Doping: Mg, Ca, Sr, Ba

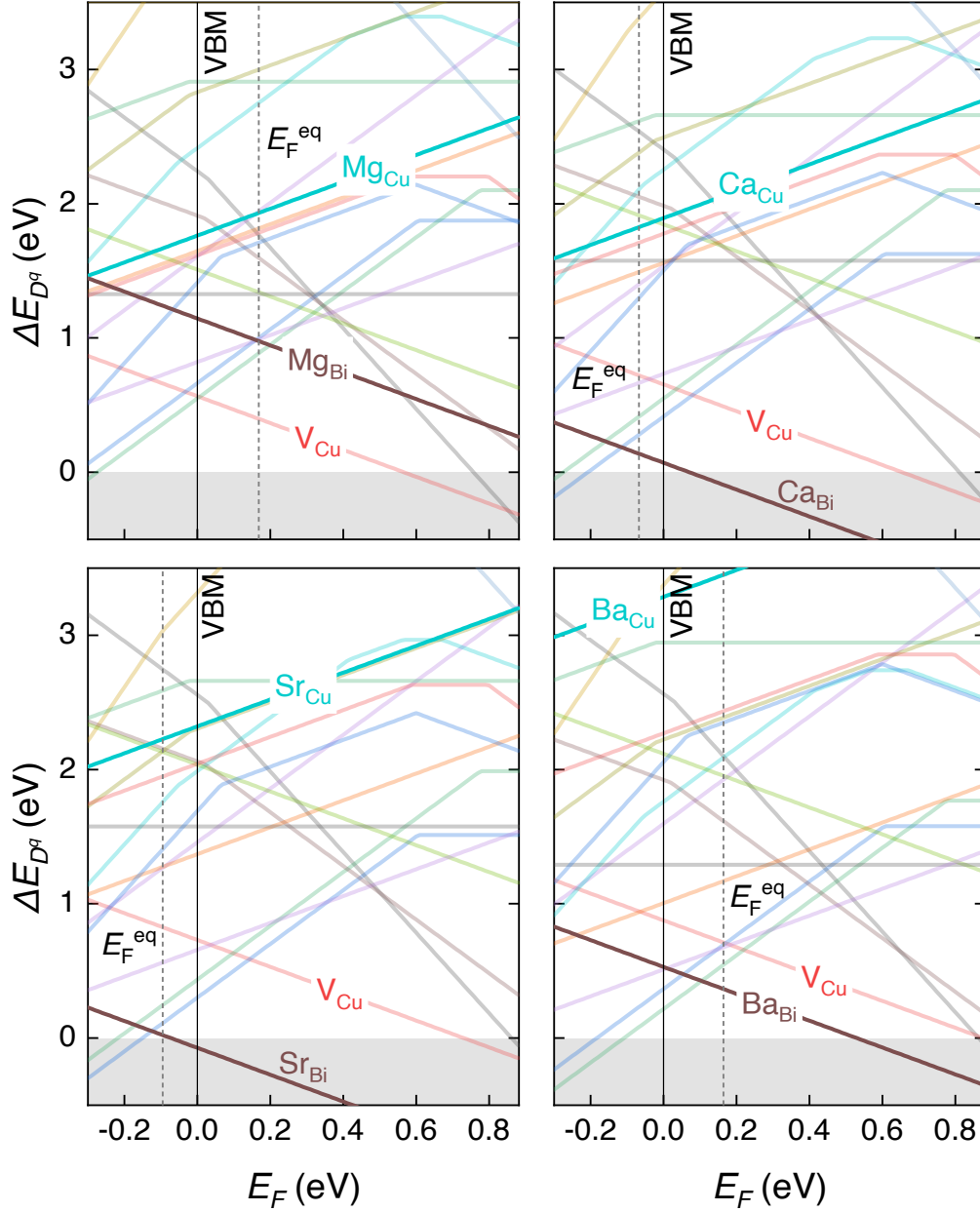


Figure S4: Formation energy of defects associated with (a) Mg, (b) Ca, (c) Sr, and (d) Ba doping under the most Cu-poor and dopant-rich conditions i.e., phase regions that yield the highest hole concentrations. BiCuSeO is in equilibrium with the following phases: (a) Se, MgO,  $\text{Bi}_2\text{O}_2\text{Se}$ , and  $\text{Bi}_2\text{O}_3$ , (b) Se, CaO,  $\text{Cu}_3\text{Se}_2$ , and  $\text{CaSeO}_3$ , (c)  $\text{SrSeO}_3$ , SrSe,  $\text{Bi}_2\text{O}_5\text{Sr}_2$ , and  $\text{Cu}_3\text{Se}_2$ , and (d)  $\text{BaCu}_2\text{Se}_2$ ,  $\text{BaSeO}_3$ ,  $\text{Cu}_3\text{Se}_2$ , and  $\text{Ba}_2\text{Bi}_4\text{O}_8$ . Native defects of BiCuSeO (Figure 2 in the main text) are shown in lighter colors. The valence band maximum (VBM) is shown as the vertical solid line at  $E_F = 0$ . The equilibrium Fermi energy ( $E_F^{\text{eq}}$ ) is shown as the dotted vertical line.

## Group-17 Doping: F

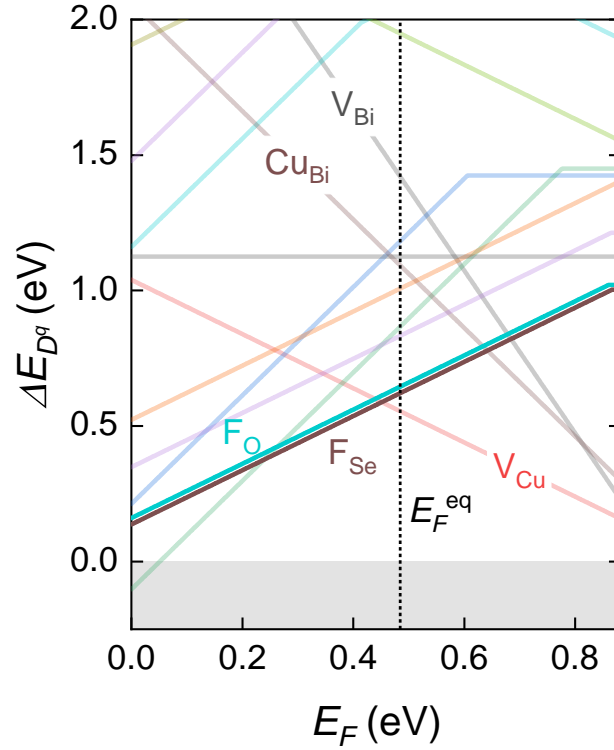


Figure S5: Formation energy of defects associated with F doping under the most Cu-rich condition, where BiCuSeO is in equilibrium with Bi, Cu<sub>2</sub>O, Cu<sub>2</sub>Se, and BiFO. Native defects of BiCuSeO (Figure 2 in main text) are shown in lighter colors. The equilibrium Fermi energy ( $E_F^{eq}$ ), as determined by charge neutrality at 973 K, is marked with a dotted vertical line.



## Group-1 Doping: Li

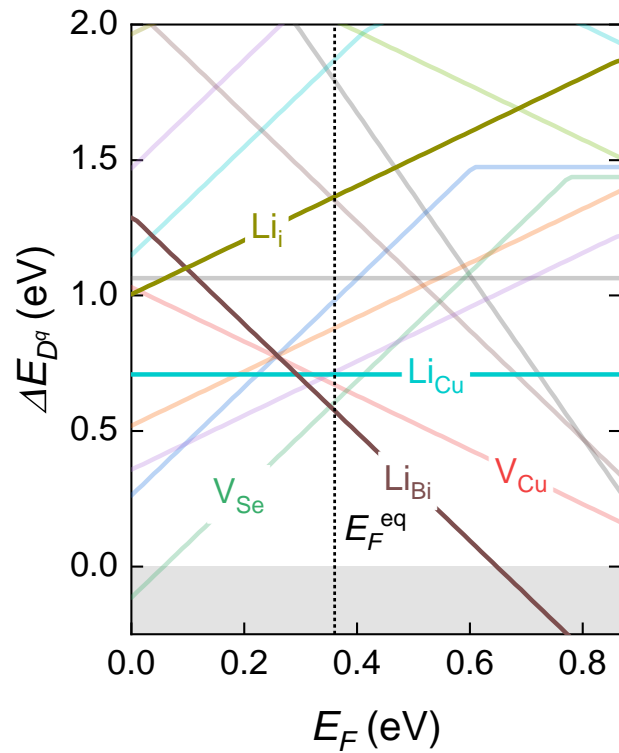


Figure S6: Formation energy of defects associated with Li doping in BiCuSeO under the most Cu-rich condition where BiCuSeO is in equilibrium with Bi, Cu<sub>2</sub>O, Bi<sub>2</sub>O<sub>3</sub>, and Cu<sub>8</sub>Li<sub>8</sub>O<sub>8</sub>. Native defects of BiCuSeO (Figure 2 in main text) are shown in lighter colors. The equilibrium Fermi energy ( $E_F^{eq}$ ), as determined by charge neutrality at 973 K, is marked with a dotted vertical line.

## Group-12 Doping: Zn

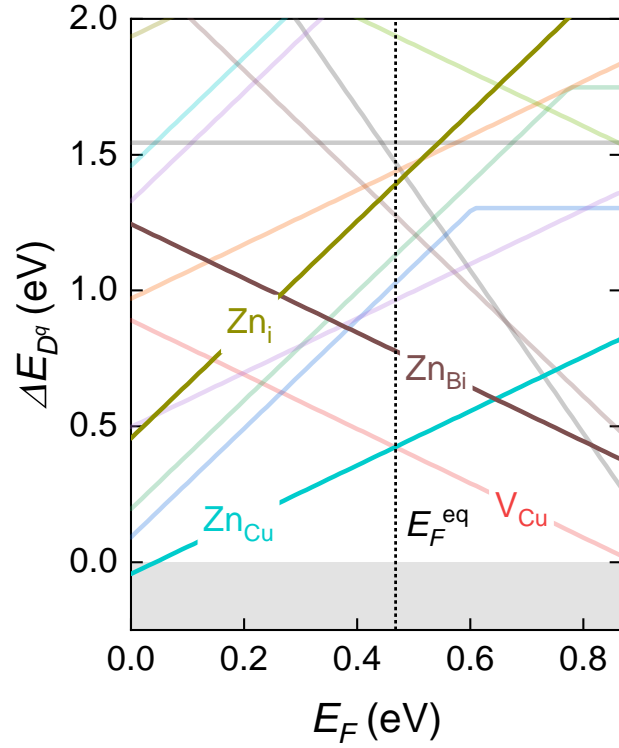


Figure S7: Formation energy of defects associated with Zn doping in BiCuSeO under the thermodynamic conditions where BiCuSeO is in equilibrium with Bi,  $\text{Cu}_3\text{Se}_2$ , ZnSe, and ZnO. Native defects of BiCuSeO (Figure 2 in main text) are shown in lighter colors. The equilibrium Fermi energy ( $E_F^{\text{eq}}$ ), as determined by charge neutrality at 973 K, is marked with a dotted vertical line.

## Group-3 Doping: Sc, Y

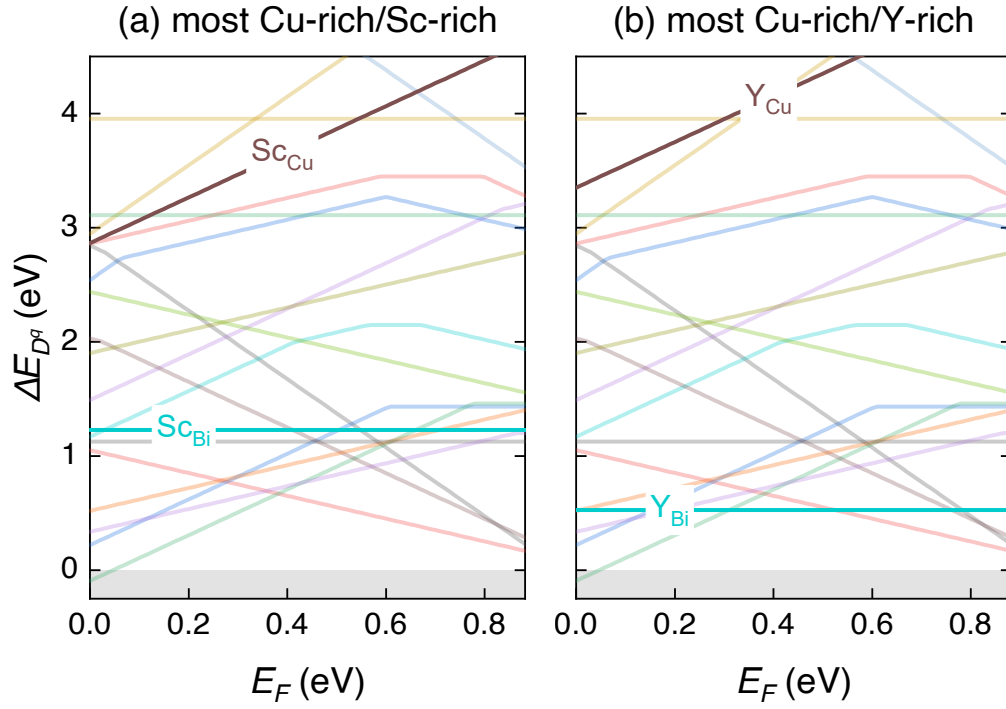


Figure S8: Formation energy of defects associated with (a) Sc, and (b) Y doping in BiCuSeO under the most Cu-rich conditions where BiCuSeO is in equilibrium with (a) Bi, Cu<sub>2</sub>Se, Cu<sub>2</sub>O, and CuO<sub>2</sub>Sc, and (b) Bi, Cu<sub>2</sub>Se, Cu<sub>2</sub>O, and Y<sub>2</sub>O<sub>3</sub>. Native defects of BiCuSeO (Figure 2 in main text) are shown in lighter colors. The equilibrium Fermi energy ( $E_F^{\text{eq}}$ ), as determined by charge neutrality at 973 K, is marked with a dotted vertical line.

## Group-4 Doping: Ti, Zr, Hf

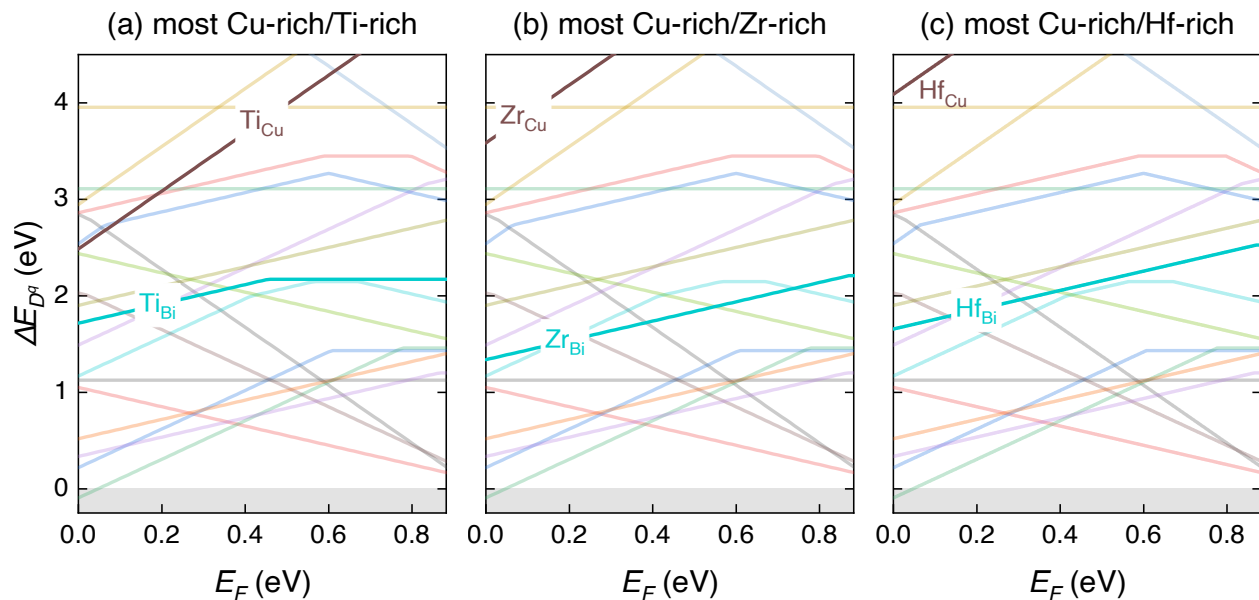


Figure S9: Formation energy of defects associated with (a) Ti, (b) Zr, and (c) Hf doping in BiCuSeO under Cu-rich conditions where BiCuSeO is in equilibrium with (a) Bi, Cu<sub>2</sub>Se, Cu<sub>2</sub>O, and Bi<sub>2</sub>O<sub>7</sub>Ti<sub>2</sub>, (b) Bi, Cu<sub>2</sub>Se, Cu<sub>2</sub>O, and ZrO<sub>2</sub>, and (c) Bi, Cu<sub>2</sub>Se, Cu<sub>2</sub>O, and HfO<sub>2</sub>. Native defects of BiCuSeO (Figure 2 in main text) are shown in lighter colors. The equilibrium Fermi energy ( $E_F^{\text{eq}}$ ), as determined by charge neutrality at 973 K, is marked with a dotted vertical line.

## Group-13 Doping: Al, Ga, In, and Tl

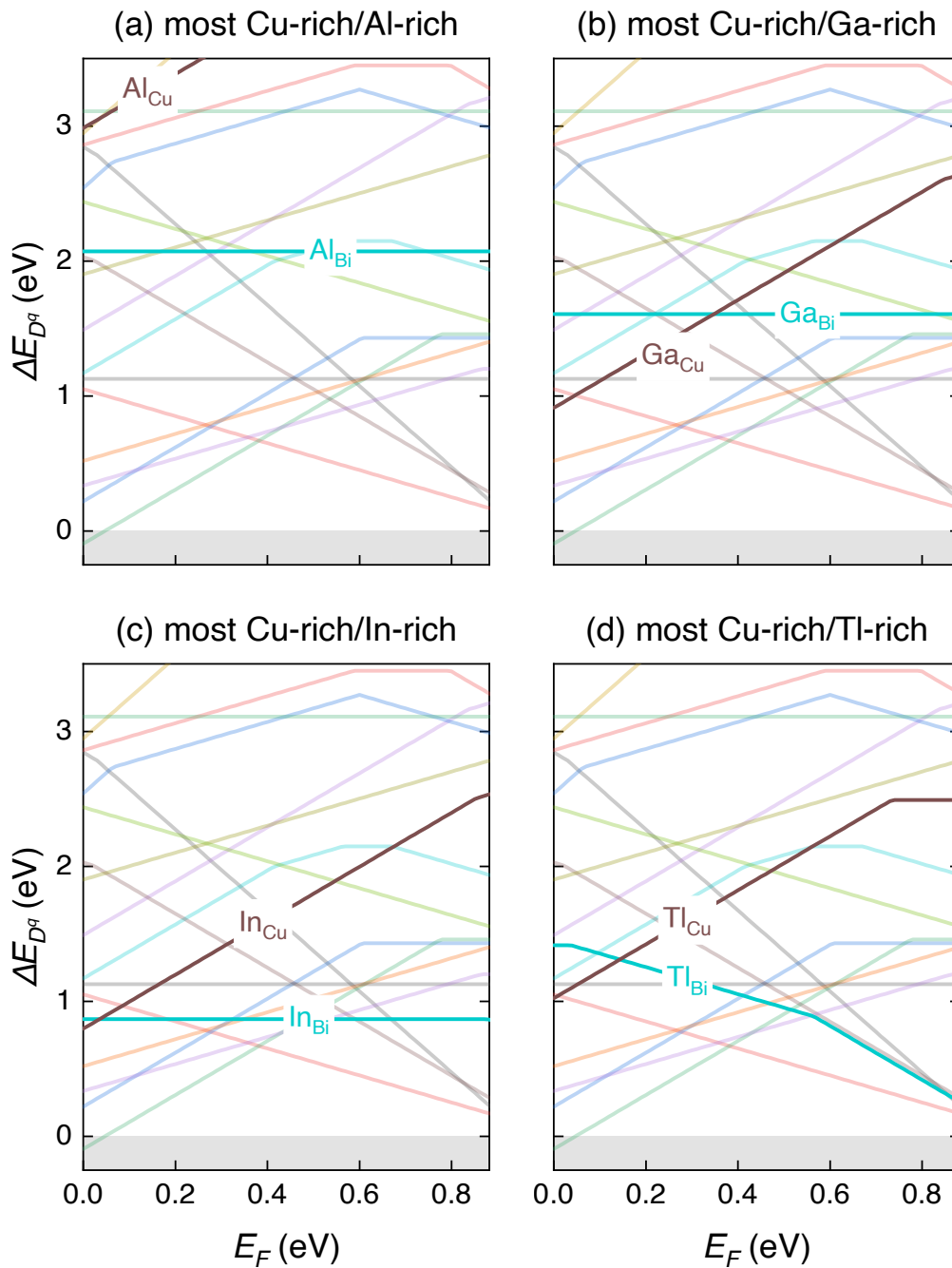


Figure S10: Formation energy of defects associated with (a) Al, (b) Ga, (c) In, and (d) Tl doping in BiCuSeO under Cu-rich conditions where BiCuSeO is in equilibrium with (a) Bi,  $\text{Cu}_2\text{Se}$ ,  $\text{Cu}_2\text{O}$ , and  $\text{AlCuO}_2$ , (b) Bi,  $\text{Cu}_2\text{Se}$ ,  $\text{Cu}_2\text{O}$ , and  $\text{CuGaO}_2$ , (c) Bi,  $\text{Cu}_2\text{Se}$ ,  $\text{Cu}_2\text{O}$ , and  $\text{CuInO}_2$ , and (d) Bi,  $\text{Cu}_2\text{Se}$ ,  $\text{Cu}_2\text{O}$ , and  $\text{Cu}_2\text{Se}_2\text{Tl}$ . Native defects of BiCuSeO (Figure 2 in main text) are shown in lighter colors. The equilibrium Fermi energy ( $E_F^{\text{eq}}$ ), as determined by charge neutrality at 973 K, is marked with a dotted vertical line.

## Group-14 Doping: Si, Ge, Sn, Pb

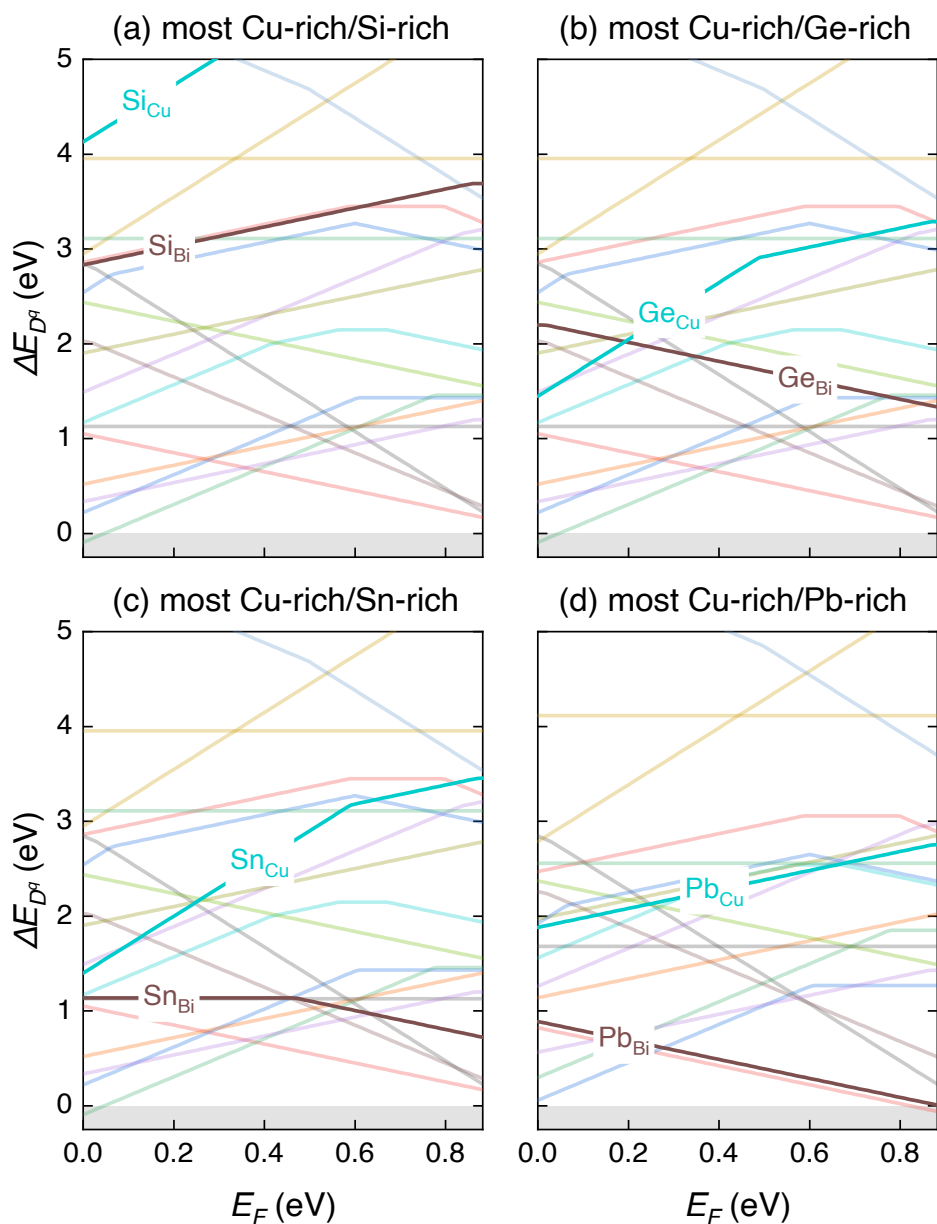


Figure S11: Formation energy of defects associated with (a) Si, (b) Ge, (c) Sn, and (d) Pb doping in BiCuSeO under Cu-rich conditions where BiCuSeO is in equilibrium with a) Bi, Cu<sub>2</sub>Se, Cu<sub>2</sub>O, and Bi<sub>4</sub>O<sub>12</sub>Si<sub>3</sub>, (b) Bi, Cu<sub>2</sub>Se, Cu<sub>2</sub>O, and Bi<sub>4</sub>Ge<sub>3</sub>O<sub>12</sub>, (c) Bi, Cu<sub>2</sub>O, Bi<sub>2</sub>O<sub>7</sub>Sn<sub>2</sub>, and Cu<sub>2</sub>Se, and (d) Bi, PbSe, Cu<sub>3</sub>Se<sub>2</sub>, and Bi<sub>2</sub>Se<sub>3</sub>. Native defects of BiCuSeO (Figure 2 in main text) are shown in lighter colors. The equilibrium Fermi energy ( $E_F^{\text{eq}}$ ), as determined by charge neutrality at 973 K, is marked with a dotted vertical line.

## Phase Equilibria of Mg-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{Mg}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$p - n$ ( $\text{cm}^{-3}$ )
Se, MgO, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.62	-4.323	-1.923	0.0	$7.39 \times 10^{19}$
Se, MgO, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub>	-0.602	-0.708	-4.636	-1.61	0.0	$1.26 \times 10^{20}$
Se, MgO, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.708	-4.411	-1.835	0.0	$1.25 \times 10^{20}$
Se, MgO, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-0.865	-0.62	-4.811	-1.435	0.0	$7.53 \times 10^{19}$
Bi, MgO, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.582	-4.159	-2.087	-0.252	$5.39 \times 10^{19}$
Bi, Cu <sub>2</sub> Se, MgO, Cu <sub>2</sub> O	0.0	-0.223	-4.192	-2.054	-0.643	$5.24 \times 10^{18}$
Bi, MgO, Cu <sub>2</sub> O, Bi <sub>2</sub> O <sub>3</sub>	0.0	-0.244	-4.234	-2.012	-0.664	$5.67 \times 10^{18}$
Bi, MgO, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub>	0.0	-0.507	-4.234	-2.012	-0.402	$3.45 \times 10^{19}$
Bi, MgO, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.452	-4.03	-2.216	-0.252	$2.36 \times 10^{19}$
Bi, Cu <sub>2</sub> Se, MgO, Cu <sub>3</sub> Se <sub>2</sub>	0.0	-0.318	-4.097	-2.149	-0.453	$1.12 \times 10^{19}$
MgO, Cu <sub>3</sub> Se <sub>2</sub> , Cu <sub>2</sub> O, Bi <sub>2</sub> O <sub>3</sub>	-0.603	-0.445	-4.636	-1.61	-0.262	$2.63 \times 10^{19}$
Cu <sub>2</sub> Se, MgO, Cu <sub>3</sub> Se <sub>2</sub> , Cu <sub>2</sub> O	-0.285	-0.318	-4.382	-1.864	-0.453	$1.16 \times 10^{19}$

Table S4: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-Mg phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## Phase Equilibria of Ca-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Ca}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$p - n$ ( $\text{cm}^{-3}$ )
Se, CaO, $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{Se}_3$	-0.378	-4.659	-0.62	-1.923	0.0	$1.38 \times 10^{21}$
Se, CaO, $\text{CaO}_3\text{Se}$ , $\text{Bi}_2\text{Se}_3$	-0.378	-4.723	-0.684	-1.859	0.0	$1.19 \times 10^{21}$
Se, $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{CaO}_3\text{Se}$ , $\text{Bi}_2\text{Se}_3$	-0.378	-4.795	-0.708	-1.835	0.0	$8.89 \times 10^{20}$
Se, CaO, $\text{Cu}_3\text{Se}_2$ , $\text{CaO}_3\text{Se}$	-0.441	-4.723	-0.62	-1.859	0.0	$1.53 \times 10^{21}$
Se, $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_3$ , $\text{CaO}_3\text{Se}$	-0.865	-5.995	-0.62	-1.435	0.0	$7.65 \times 10^{19}$
Se, $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{O}_3$ , $\text{CaO}_3\text{Se}$	-0.602	-5.47	-0.708	-1.61	0.0	$1.45 \times 10^{20}$
Bi, CaO, $\text{Cu}_2\text{O}$ , $\text{Bi}_2\text{O}_3$	0.0	-4.57	-0.244	-2.012	-0.664	$1.11 \times 10^{20}$
Bi, CaO, $\text{Cu}_2\text{Se}$ , $\text{Cu}_2\text{O}$	0.0	-4.528	-0.223	-2.054	-0.643	$1.41 \times 10^{20}$
Bi, CaO, $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{Se}_3$	0.0	-4.495	-0.582	-2.087	-0.252	$3.88 \times 10^{20}$
Bi, CaO, $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{O}_3$	0.0	-4.57	-0.507	-2.012	-0.402	$2.53 \times 10^{20}$
Bi, CaO, $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{Se}_3$	0.0	-4.366	-0.452	-2.216	-0.252	$4.48 \times 10^{20}$
Bi, CaO, $\text{Cu}_2\text{Se}$ , $\text{Cu}_3\text{Se}_2$	0.0	-4.433	-0.318	-2.149	-0.453	$3.44 \times 10^{20}$
CaO, $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{CaO}_3\text{Se}$ , $\text{Bi}_2\text{Se}_3$	-0.354	-4.731	-0.7	-1.851	-0.016	$1.05 \times 10^{21}$
CaO, $\text{Cu}_2\text{Se}$ , $\text{Cu}_2\text{O}$ , $\text{Cu}_3\text{Se}_2$	-0.285	-4.718	-0.318	-1.864	-0.453	$3.95 \times 10^{20}$
CaO, $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{O}_3$ , $\text{CaO}_3\text{Se}$	-0.353	-4.806	-0.625	-1.776	-0.166	$7 \times 10^{20}$
CaO, $\text{Cu}_2\text{O}$ , $\text{Bi}_2\text{O}_3$ , $\text{CaO}_3\text{Se}$	-0.485	-4.894	-0.406	-1.688	-0.341	$6.1 \times 10^{20}$
$\text{Cu}_2\text{O}$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_3$ , $\text{CaO}_3\text{Se}$	-0.603	-5.208	-0.445	-1.61	-0.262	$2.97 \times 10^{20}$
CaO, $\text{Cu}_2\text{O}$ , $\text{Cu}_3\text{Se}_2$ , $\text{CaO}_3\text{Se}$	-0.496	-4.886	-0.402	-1.696	-0.327	$6.81 \times 10^{20}$

Table S5: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-Ca phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.



## Phase Equilibria of Sr-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$\Delta\mu_{\text{Sr}}$	$p - n$ ( $\text{cm}^{-3}$ )
Bi, SeSr, $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{Se}_3$	0.0	-0.452	-2.216	-0.252	-4.274	$5.95 \times 10^{20}$
Bi, $\text{Cu}_2\text{O}$ , $\text{Bi}_2\text{O}_3$ , $\text{Bi}_2\text{O}_4\text{Sr}$	0.0	-0.244	-2.012	-0.664	-4.72	$5.66 \times 10^{19}$
Bi, $\text{Cu}_2\text{Se}$ , $\text{Cu}_2\text{O}$ , $\text{Bi}_2\text{O}_4\text{Sr}$	0.0	-0.223	-2.054	-0.643	-4.551	$1.2 \times 10^{20}$
Bi, $\text{Cu}_2\text{Se}$ , $\text{Bi}_2\text{O}_5\text{Sr}_2$ , $\text{Bi}_2\text{O}_4\text{Sr}$	0.0	-0.258	-2.089	-0.573	-4.411	$2.66 \times 10^{20}$
Bi, $\text{Cu}_2\text{Se}$ , $\text{Bi}_2\text{O}_5\text{Sr}_2$ , $\text{Cu}_3\text{Se}_2$	0.0	-0.318	-2.149	-0.453	-4.261	$6.19 \times 10^{20}$
Bi, SeSr, $\text{Bi}_2\text{O}_5\text{Sr}_2$ , $\text{Cu}_3\text{Se}_2$	0.0	-0.386	-2.183	-0.351	-4.175	$8.91 \times 10^{20}$
$\text{O}_3\text{SeSr}$ , SeSr, $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{Se}_3$	-0.313	-0.591	-1.973	-0.043	-4.483	$1.7 \times 10^{21}$
$\text{O}_3\text{SeSr}$ , SeSr, $\text{Bi}_2\text{O}_5\text{Sr}_2$ , $\text{Bi}_2\text{Se}_3$	-0.256	-0.61	-1.973	-0.081	-4.445	$1.59 \times 10^{21}$
$\text{O}_3\text{SeSr}$ , $\text{Bi}_2\text{O}_5\text{Sr}_2$ , $\text{Bi}_2\text{O}_4\text{Sr}$ , $\text{Bi}_2\text{Se}_3$	-0.242	-0.66	-1.927	-0.09	-4.573	$1.05 \times 10^{21}$
$\text{O}_3\text{SeSr}$ , $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{O}_4\text{Sr}$ , $\text{Bi}_2\text{Se}_3$	-0.244	-0.663	-1.924	-0.089	-4.583	$1.02 \times 10^{21}$
$\text{O}_3\text{SeSr}$ , $\text{Cu}_2\text{O}$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_4\text{Sr}$	-0.474	-0.394	-1.712	-0.339	-4.968	$4.02 \times 10^{20}$
$\text{O}_3\text{SeSr}$ , $\text{Bi}_2\text{O}_5\text{Sr}_2$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_4\text{Sr}$	-0.371	-0.445	-1.842	-0.262	-4.658	$1.09 \times 10^{21}$
$\text{O}_3\text{SeSr}$ , $\text{Cu}_2\text{O}$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_3$	-0.603	-0.445	-1.61	-0.262	-5.353	$1.29 \times 10^{20}$
$\text{O}_3\text{SeSr}$ , SeSr, $\text{Bi}_2\text{O}_5\text{Sr}_2$ , $\text{Cu}_3\text{Se}_2$	-0.289	-0.544	-1.973	-0.114	-4.412	$1.92 \times 10^{21}$
$\text{O}_3\text{SeSr}$ , $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{O}_3$ , $\text{Bi}_2\text{O}_4\text{Sr}$	-0.356	-0.625	-1.774	-0.164	-4.958	$3.1 \times 10^{20}$
$\text{O}_3\text{SeSr}$ , $\text{Cu}_2\text{O}$ , $\text{Bi}_2\text{O}_3$ , $\text{Bi}_2\text{O}_4\text{Sr}$	-0.487	-0.407	-1.687	-0.339	-5.045	$3.03 \times 10^{20}$
$\text{Cu}_2\text{Se}$ , $\text{Bi}_2\text{O}_5\text{Sr}_2$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_4\text{Sr}$	-0.18	-0.318	-1.969	-0.453	-4.531	$5.04 \times 10^{20}$
$\text{Cu}_2\text{Se}$ , $\text{Cu}_2\text{O}$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_4\text{Sr}$	-0.285	-0.318	-1.864	-0.453	-4.741	$3.4 \times 10^{20}$
Se, $\text{O}_3\text{SeSr}$ , $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{O}_3$	-0.603	-0.708	-1.61	0.0	-5.615	$1.29 \times 10^{20}$
Se, $\text{O}_3\text{SeSr}$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_3$	-0.865	-0.62	-1.435	0.0	-6.14	$7.53 \times 10^{19}$
Se, $\text{O}_3\text{SeSr}$ , $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{Se}_3$	-0.378	-0.708	-1.835	0.0	-4.94	$4.03 \times 10^{20}$
Se, $\text{O}_3\text{SeSr}$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{Se}_3$	-0.378	-0.62	-1.923	0.0	-4.677	$1.22 \times 10^{21}$

Table S6: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-Sr phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## Phase Equilibria of Ba-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Ba}}$	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$p - n$ (cm <sup>-3</sup> )
Se, Bi <sub>2</sub> Se <sub>3</sub> , BaO <sub>3</sub> Se, Cu <sub>3</sub> Se <sub>2</sub>	-4.722	-0.378	-0.62	-1.923	0.0	$8.82 \times 10^{19}$
Se, Bi <sub>2</sub> Se <sub>3</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, BaO <sub>3</sub> Se	-4.985	-0.378	-0.708	-1.835	0.0	$1.25 \times 10^{20}$
Se, BaO <sub>3</sub> Se, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-6.185	-0.865	-0.62	-1.435	0.0	$7.5 \times 10^{19}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, BaO <sub>3</sub> Se, Bi <sub>2</sub> O <sub>3</sub>	-5.66	-0.603	-0.708	-1.61	0.0	$1.26 \times 10^{20}$
Bi <sub>2</sub> Se <sub>3</sub> , BaSe, BaBiSe <sub>3</sub> , BaCu <sub>2</sub> Se <sub>2</sub>	-4.399	-0.169	-0.609	-2.003	-0.139	$1.12 \times 10^{20}$
Bi <sub>2</sub> Se <sub>3</sub> , BaCu <sub>2</sub> Se <sub>2</sub> , BaO <sub>3</sub> Se, Cu <sub>3</sub> Se <sub>2</sub>	-4.643	-0.351	-0.608	-1.943	-0.018	$9.45 \times 10^{19}$
Bi <sub>2</sub> Se <sub>3</sub> , BaBiSe <sub>3</sub> , BaCu <sub>2</sub> Se <sub>2</sub> , BaO <sub>3</sub> Se	-4.448	-0.218	-0.617	-1.979	-0.106	$1.16 \times 10^{20}$
Bi <sub>2</sub> Se <sub>3</sub> , BaSe, Bi <sub>2</sub> O <sub>2</sub> Se, BaO <sub>3</sub> Se	-4.389	-0.154	-0.633	-1.984	-0.149	$1.17 \times 10^{20}$
Bi <sub>2</sub> Se <sub>3</sub> , BaSe, BaBiSe <sub>3</sub> , BaO <sub>3</sub> Se	-4.399	-0.169	-0.628	-1.984	-0.139	$1.18 \times 10^{20}$
Cu <sub>2</sub> O, BaO <sub>3</sub> Se, Cu <sub>3</sub> Se <sub>2</sub> , Ba <sub>2</sub> Bi <sub>4</sub> O <sub>8</sub>	-4.706	-0.372	-0.353	-1.795	-0.401	$4.84 \times 10^{19}$
BaCu <sub>2</sub> Se <sub>2</sub> , BaO <sub>3</sub> Se, Cu <sub>3</sub> Se <sub>2</sub> , Ba <sub>2</sub> Bi <sub>4</sub> O <sub>8</sub>	-4.433	-0.281	-0.398	-1.908	-0.333	$1.33 \times 10^{20}$
Cu <sub>2</sub> O, BaO <sub>3</sub> Se, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-5.398	-0.603	-0.445	-1.61	-0.262	$2.62 \times 10^{19}$
Cu <sub>2</sub> O, BaO <sub>3</sub> Se, Bi <sub>2</sub> O <sub>3</sub> , Ba <sub>2</sub> Bi <sub>4</sub> O <sub>8</sub>	-4.844	-0.395	-0.376	-1.748	-0.401	$2.94 \times 10^{19}$
Bi <sub>2</sub> O <sub>2</sub> Se, BaO <sub>3</sub> Se, Bi <sub>2</sub> O <sub>3</sub> , Ba <sub>2</sub> Bi <sub>4</sub> O <sub>8</sub>	-4.757	-0.264	-0.595	-1.836	-0.226	$6.61 \times 10^{19}$
BaSe, Bi <sub>2</sub> O <sub>2</sub> Se, BaO <sub>3</sub> Se, Ba <sub>2</sub> Bi <sub>4</sub> O <sub>8</sub>	-4.386	-0.153	-0.632	-1.984	-0.152	$1.17 \times 10^{20}$
BaSe, BaCu <sub>2</sub> Se <sub>2</sub> , BaO <sub>3</sub> Se, Ba <sub>2</sub> Bi <sub>4</sub> O <sub>8</sub>	-4.357	-0.167	-0.588	-1.984	-0.181	$1.28 \times 10^{20}$
BaSe, BaBiSe <sub>3</sub> , BaCu <sub>2</sub> Se <sub>2</sub> , BaO <sub>3</sub> Se	-4.412	-0.194	-0.615	-1.984	-0.126	$1.2 \times 10^{20}$
BaCu <sub>2</sub> Se <sub>2</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Cu <sub>2</sub> Se, Ba <sub>2</sub> Bi <sub>4</sub> O <sub>8</sub>	-4.353	-0.161	-0.318	-1.988	-0.453	$8.68 \times 10^{19}$
Cu <sub>2</sub> O, Cu <sub>3</sub> Se <sub>2</sub> , Cu <sub>2</sub> Se, Ba <sub>2</sub> Bi <sub>4</sub> O <sub>8</sub>	-4.601	-0.285	-0.318	-1.864	-0.453	$4.84 \times 10^{19}$
Bi, Cu <sub>2</sub> O, Cu <sub>2</sub> Se, Ba <sub>2</sub> Bi <sub>4</sub> O <sub>8</sub>	-4.411	0.0	-0.223	-2.054	-0.643	$1.93 \times 10^{19}$
Bi, BaCu <sub>2</sub> Se <sub>2</sub> , Cu <sub>2</sub> Se, Ba <sub>2</sub> Bi <sub>4</sub> O <sub>8</sub>	-4.246	0.0	-0.264	-2.095	-0.56	$5.07 \times 10^{19}$
Bi, Cu <sub>2</sub> O, Bi <sub>2</sub> O <sub>3</sub> , Ba <sub>2</sub> Bi <sub>4</sub> O <sub>8</sub>	-4.581	0.0	-0.244	-2.012	-0.664	$9.38 \times 10^{18}$
Bi, BaCu <sub>2</sub> Se <sub>2</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Cu <sub>2</sub> Se	-4.353	0.0	-0.318	-2.149	-0.453	$3.76 \times 10^{19}$
Bi, Bi <sub>2</sub> Se <sub>3</sub> , BaCu <sub>2</sub> Se <sub>2</sub> , Cu <sub>3</sub> Se <sub>2</sub>	-4.487	0.0	-0.452	-2.216	-0.252	$2.87 \times 10^{19}$
Bi, BaSe, BaCu <sub>2</sub> Se <sub>2</sub> , Ba <sub>2</sub> Bi <sub>4</sub> O <sub>8</sub>	-4.246	0.0	-0.532	-2.095	-0.292	$8.36 \times 10^{19}$
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub> , Ba <sub>2</sub> Bi <sub>4</sub> O <sub>8</sub>	-4.581	0.0	-0.507	-2.012	-0.402	$3.6 \times 10^{19}$
Bi, BaSe, Bi <sub>2</sub> O <sub>2</sub> Se, Ba <sub>2</sub> Bi <sub>4</sub> O <sub>8</sub>	-4.284	0.0	-0.581	-2.086	-0.254	$8.02 \times 10^{19}$
Bi, Bi <sub>2</sub> Se <sub>3</sub> , BaSe, Bi <sub>2</sub> O <sub>2</sub> Se	-4.286	0.0	-0.582	-2.087	-0.252	$8 \times 10^{19}$
Bi, Bi <sub>2</sub> Se <sub>3</sub> , BaSe, BaCu <sub>2</sub> Se <sub>2</sub>	-4.286	0.0	-0.553	-2.116	-0.252	$7.29 \times 10^{19}$

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Table S7: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-Ba phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## Phase Equilibria of Li-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{Li}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$p - n$ (cm <sup>-3</sup> )
Se, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub> , Bi <sub>8</sub> Li <sub>24</sub> O <sub>24</sub>	-0.378	-0.62	-2.217	-1.923	0.0	$1.12 \times 10^{20}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub> , BiLiO <sub>2</sub>	-0.603	-0.708	-2.509	-1.61	0.0	$1.44 \times 10^{20}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, BiLiO <sub>2</sub> , Bi <sub>8</sub> Li <sub>24</sub> O <sub>24</sub>	-0.438	-0.708	-2.345	-1.775	0.0	$1.22 \times 10^{20}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> Se <sub>3</sub> , Bi <sub>8</sub> Li <sub>24</sub> O <sub>24</sub>	-0.378	-0.708	-2.305	-1.835	0.0	$1.09 \times 10^{20}$
Se, Li <sub>4</sub> O <sub>5</sub> Se, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>8</sub> Li <sub>24</sub> O <sub>24</sub>	-0.609	-0.62	-2.372	-1.691	0.0	$1.75 \times 10^{20}$
Se, Li <sub>4</sub> O <sub>5</sub> Se, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-0.865	-0.62	-2.691	-1.435	0.0	$1.48 \times 10^{20}$
Se, Li <sub>4</sub> O <sub>5</sub> Se, BiLiO <sub>2</sub> , Bi <sub>8</sub> Li <sub>24</sub> O <sub>24</sub>	-0.594	-0.655	-2.397	-1.671	0.0	$1.57 \times 10^{20}$
Se, Li <sub>4</sub> O <sub>5</sub> Se, Bi <sub>2</sub> O <sub>3</sub> , BiLiO <sub>2</sub>	-0.676	-0.683	-2.534	-1.561	0.0	$1.48 \times 10^{20}$
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> Se <sub>3</sub> , Bi <sub>8</sub> Li <sub>24</sub> O <sub>24</sub>	0.0	-0.582	-2.179	-2.087	-0.252	$4.61 \times 10^{19}$
Bi, BiLiO <sub>2</sub> , Cu <sub>8</sub> Li <sub>8</sub> O <sub>8</sub> , Bi <sub>8</sub> Li <sub>24</sub> O <sub>24</sub>	0.0	-0.329	-2.199	-2.067	-0.525	$2.62 \times 10^{19}$
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, BiLiO <sub>2</sub> , Bi <sub>8</sub> Li <sub>24</sub> O <sub>24</sub>	0.0	-0.562	-2.199	-2.067	-0.292	$4.48 \times 10^{19}$
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub> , BiLiO <sub>2</sub>	0.0	-0.507	-2.309	-2.012	-0.402	$3.57 \times 10^{19}$
Bi, Bi <sub>2</sub> O <sub>3</sub> , BiLiO <sub>2</sub> , Cu <sub>8</sub> Li <sub>8</sub> O <sub>8</sub>	0.0	-0.274	-2.309	-2.012	-0.634	$1.53 \times 10^{19}$
Bi, Cu <sub>2</sub> O, Bi <sub>2</sub> O <sub>3</sub> , Cu <sub>8</sub> Li <sub>8</sub> O <sub>8</sub>	0.0	-0.244	-2.338	-2.012	-0.664	$1.28 \times 10^{19}$
Bi, Cu <sub>2</sub> Se, Cu <sub>2</sub> O, Cu <sub>8</sub> Li <sub>8</sub> O <sub>8</sub>	0.0	-0.223	-2.317	-2.054	-0.643	$1.41 \times 10^{19}$
Bi, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub> , Bi <sub>8</sub> Li <sub>24</sub> O <sub>24</sub>	0.0	-0.452	-2.049	-2.216	-0.252	$4.26 \times 10^{19}$
Bi, Cu <sub>2</sub> Se, Cu <sub>3</sub> Se <sub>2</sub> , Cu <sub>8</sub> Li <sub>8</sub> O <sub>8</sub>	0.0	-0.318	-2.127	-2.149	-0.453	$3.45 \times 10^{19}$
Bi, Cu <sub>3</sub> Se <sub>2</sub> , Cu <sub>8</sub> Li <sub>8</sub> O <sub>8</sub> , Bi <sub>8</sub> Li <sub>24</sub> O <sub>24</sub>	0.0	-0.329	-2.111	-2.155	-0.437	$3.66 \times 10^{19}$
Cu <sub>3</sub> Se <sub>2</sub> , BiLiO <sub>2</sub> , Cu <sub>8</sub> Li <sub>8</sub> O <sub>8</sub> , Bi <sub>8</sub> Li <sub>24</sub> O <sub>24</sub>	-0.527	-0.505	-2.375	-1.715	-0.173	$1.23 \times 10^{20}$
Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , BiLiO <sub>2</sub> , Cu <sub>8</sub> Li <sub>8</sub> O <sub>8</sub>	-0.692	-0.505	-2.539	-1.55	-0.173	$1.25 \times 10^{20}$
Cu <sub>2</sub> O, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , Cu <sub>8</sub> Li <sub>8</sub> O <sub>8</sub>	-0.603	-0.445	-2.539	-1.61	-0.262	$8.63 \times 10^{19}$
Li <sub>4</sub> O <sub>5</sub> Se, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , BiLiO <sub>2</sub>	-0.739	-0.536	-2.555	-1.519	-0.126	$1.43 \times 10^{20}$
Li <sub>4</sub> O <sub>5</sub> Se, Cu <sub>3</sub> Se <sub>2</sub> , BiLiO <sub>2</sub> , Bi <sub>8</sub> Li <sub>24</sub> O <sub>24</sub>	-0.63	-0.573	-2.409	-1.647	-0.071	$1.65 \times 10^{20}$
Cu <sub>2</sub> Se, Cu <sub>2</sub> O, Cu <sub>3</sub> Se <sub>2</sub> , Cu <sub>8</sub> Li <sub>8</sub> O <sub>8</sub>	-0.285	-0.318	-2.412	-1.864	-0.453	$3.66 \times 10^{19}$

Table S8: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-Li phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## Phase Equilibria of Zn-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$\Delta\mu_{\text{Zn}}$	$p - n$ ( $\text{cm}^{-3}$ )
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> Se <sub>3</sub> , SeZn	0.0	-0.582	-2.087	-0.252	-1.496	$6.54 \times 10^{18}$
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, SeZn, OZn	0.0	-0.579	-2.084	-0.256	-1.492	$6.37 \times 10^{18}$
Bi, Cu <sub>2</sub> Se, Cu <sub>2</sub> O, OZn	0.0	-0.223	-2.054	-0.643	-1.522	$4.3 \times 10^{18}$
Bi, Cu <sub>2</sub> O, Bi <sub>2</sub> O <sub>3</sub> , OZn	0.0	-0.244	-2.012	-0.664	-1.564	$4.94 \times 10^{18}$
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub> , OZn	0.0	-0.507	-2.012	-0.402	-1.564	$9.63 \times 10^{18}$
Bi, Bi <sub>2</sub> Se <sub>3</sub> , Cu <sub>3</sub> Se <sub>2</sub> , SeZn	0.0	-0.452	-2.216	-0.252	-1.496	$6.37 \times 10^{18}$
Bi, Cu <sub>3</sub> Se <sub>2</sub> , SeZn, OZn	0.0	-0.384	-2.182	-0.354	-1.394	$3.33 \times 10^{18}$
Bi, Cu <sub>2</sub> Se, Cu <sub>3</sub> Se <sub>2</sub> , OZn	0.0	-0.318	-2.149	-0.453	-1.427	$3.99 \times 10^{18}$
Cu <sub>2</sub> Se, Cu <sub>2</sub> O, Cu <sub>3</sub> Se <sub>2</sub> , OZn	-0.285	-0.318	-1.864	-0.453	-1.712	$1.04 \times 10^{19}$
Cu <sub>2</sub> O, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , OZn	-0.603	-0.445	-1.61	-0.262	-1.966	$2.55 \times 10^{19}$
Se, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , OZn	-0.865	-0.62	-1.435	0.0	-2.141	$7.29 \times 10^{19}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> Se <sub>3</sub> , SeZn	-0.378	-0.708	-1.835	0.0	-1.748	$2.89 \times 10^{19}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, SeZn, OZn	-0.385	-0.708	-1.828	0.0	-1.748	$2.89 \times 10^{19}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub> , OZn	-0.603	-0.708	-1.61	0.0	-1.966	$8.07 \times 10^{19}$
Se, Bi <sub>2</sub> Se <sub>3</sub> , Cu <sub>3</sub> Se <sub>2</sub> , SeZn	-0.378	-0.62	-1.923	0.0	-1.748	$2.76 \times 10^{19}$
Se, Cu <sub>3</sub> Se <sub>2</sub> , SeZn, OZn	-0.472	-0.62	-1.828	0.0	-1.748	$2.77 \times 10^{19}$

Table S9: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-Zn phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## Phase Equilibria of Al-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Al}}$	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$p - n$ ( $\text{cm}^{-3}$ )
Se, Al <sub>2</sub> O <sub>3</sub> , Bi <sub>2</sub> Se <sub>3</sub> , Cu <sub>3</sub> Se <sub>2</sub>	-5.916	-0.378	-0.62	-1.923	0.0	$7.36 \times 10^{19}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub> , Al <sub>4</sub> Bi <sub>2</sub> O <sub>9</sub>	-6.484	-0.602	-0.708	-1.61	0.0	$1.26 \times 10^{20}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> Se <sub>3</sub> , Al <sub>4</sub> Bi <sub>2</sub> O <sub>9</sub>	-6.09	-0.378	-0.708	-1.835	0.0	$1.25 \times 10^{20}$
Se, Al <sub>2</sub> O <sub>3</sub> , Bi <sub>2</sub> Se <sub>3</sub> , Al <sub>4</sub> Bi <sub>2</sub> O <sub>9</sub>	-5.962	-0.378	-0.651	-1.892	0.0	$8.88 \times 10^{19}$
Se, Al <sub>2</sub> O <sub>3</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Al <sub>4</sub> Bi <sub>2</sub> O <sub>9</sub>	-6.055	-0.47	-0.62	-1.83	0.0	$7.46 \times 10^{19}$
Se, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , Al <sub>4</sub> Bi <sub>2</sub> O <sub>9</sub>	-6.746	-0.865	-0.62	-1.435	0.0	$7.5 \times 10^{19}$
Cu <sub>2</sub> O, Cu <sub>3</sub> Se <sub>2</sub> , AlCuO <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-6.523	-0.603	-0.445	-1.61	-0.262	$2.61 \times 10^{19}$
Cu <sub>3</sub> Se <sub>2</sub> , AlCuO <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , Al <sub>4</sub> Bi <sub>2</sub> O <sub>9</sub>	-6.602	-0.721	-0.524	-1.531	-0.145	$4.22 \times 10^{19}$
Al <sub>2</sub> O <sub>3</sub> , Cu <sub>3</sub> Se <sub>2</sub> , AlCuO <sub>2</sub> , Al <sub>4</sub> Bi <sub>2</sub> O <sub>9</sub>	-5.614	-0.029	-0.326	-2.124	-0.441	$1.17 \times 10^{19}$
Cu <sub>2</sub> Se, Cu <sub>2</sub> O, Cu <sub>3</sub> Se <sub>2</sub> , AlCuO <sub>2</sub>	-6.142	-0.285	-0.318	-1.864	-0.453	$1.13 \times 10^{19}$
Cu <sub>2</sub> Se, Al <sub>2</sub> O <sub>3</sub> , Cu <sub>3</sub> Se <sub>2</sub> , AlCuO <sub>2</sub>	-5.59	-0.009	-0.318	-2.14	-0.453	$1.1 \times 10^{19}$
Bi, Cu <sub>2</sub> Se, Al <sub>2</sub> O <sub>3</sub> , Cu <sub>3</sub> Se <sub>2</sub>	-5.576	0.0	-0.318	-2.149	-0.453	$1.1 \times 10^{19}$
Bi, Al <sub>2</sub> O <sub>3</sub> , Bi <sub>2</sub> Se <sub>3</sub> , Cu <sub>3</sub> Se <sub>2</sub>	-5.476	0.0	-0.452	-2.216	-0.252	$2.34 \times 10^{19}$
Bi, Cu <sub>2</sub> Se, Cu <sub>2</sub> O, AlCuO <sub>2</sub>	-5.857	0.0	-0.223	-2.054	-0.643	$5.11 \times 10^{18}$
Bi, Cu <sub>2</sub> Se, Al <sub>2</sub> O <sub>3</sub> , AlCuO <sub>2</sub>	-5.581	0.0	-0.315	-2.146	-0.459	$1.08 \times 10^{19}$
Bi, Al <sub>2</sub> O <sub>3</sub> , AlCuO <sub>2</sub> , Al <sub>4</sub> Bi <sub>2</sub> O <sub>9</sub>	-5.585	0.0	-0.316	-2.143	-0.46	$1.08 \times 10^{19}$
Bi, AlCuO <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , Al <sub>4</sub> Bi <sub>2</sub> O <sub>9</sub>	-5.881	0.0	-0.283	-2.012	-0.625	$7.59 \times 10^{18}$
Bi, Cu <sub>2</sub> O, AlCuO <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-5.92	0.0	-0.244	-2.012	-0.664	$5.61 \times 10^{18}$
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub> , Al <sub>4</sub> Bi <sub>2</sub> O <sub>9</sub>	-5.881	0.0	-0.507	-2.012	-0.402	$3.45 \times 10^{19}$
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> Se <sub>3</sub> , Al <sub>4</sub> Bi <sub>2</sub> O <sub>9</sub>	-5.712	0.0	-0.582	-2.087	-0.252	$5.39 \times 10^{19}$
Bi, Al <sub>2</sub> O <sub>3</sub> , Bi <sub>2</sub> Se <sub>3</sub> , Al <sub>4</sub> Bi <sub>2</sub> O <sub>9</sub>	-5.585	0.0	-0.525	-2.143	-0.252	$3.77 \times 10^{19}$

Table S10: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-Al phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## Phase Equilibria of Ga-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{Ga}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$p - n$ ( $\text{cm}^{-3}$ )
Se, $\text{Cu}_3\text{Se}_2$ , $\text{Ga}_2\text{O}_3$ , $\text{Bi}_2\text{Se}_3$	-0.378	-0.62	-2.811	-1.923	0.0	$7.36 \times 10^{19}$
Se, $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{Ga}_4\text{O}_9$ , $\text{Bi}_2\text{O}_3$	-0.602	-0.708	-3.341	-1.61	0.0	$1.26 \times 10^{20}$
Se, $\text{Bi}_2\text{Ga}_4\text{O}_9$ , $\text{Ga}_2\text{O}_3$ , $\text{Bi}_2\text{Se}_3$	-0.378	-0.701	-2.933	-1.842	0.0	$1.19 \times 10^{20}$
Se, $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{Ga}_4\text{O}_9$ , $\text{Bi}_2\text{Se}_3$	-0.378	-0.708	-2.948	-1.835	0.0	$1.24 \times 10^{20}$
Se, $\text{Bi}_2\text{Ga}_4\text{O}_9$ , $\text{Cu}_3\text{Se}_2$ , $\text{Ga}_2\text{O}_3$	-0.62	-0.62	-3.175	-1.68	0.0	$7.48 \times 10^{19}$
Se, $\text{Bi}_2\text{Ga}_4\text{O}_9$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_3$	-0.865	-0.62	-3.604	-1.435	0.0	$7.5 \times 10^{19}$
Bi, $\text{Cu}_2\text{O}$ , $\text{CuGaO}_2$ , $\text{Bi}_2\text{O}_3$	0.0	-0.244	-2.754	-2.012	-0.664	$5.61 \times 10^{18}$
Bi, $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{Ga}_4\text{O}_9$ , $\text{Bi}_2\text{Se}_3$	0.0	-0.582	-2.57	-2.087	-0.252	$5.37 \times 10^{19}$
Bi, $\text{Bi}_2\text{Ga}_4\text{O}_9$ , $\text{Ga}_2\text{O}_3$ , $\text{Bi}_2\text{Se}_3$	0.0	-0.575	-2.555	-2.093	-0.252	$5.14 \times 10^{19}$
Bi, $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{Ga}_4\text{O}_9$ , $\text{Bi}_2\text{O}_3$	0.0	-0.507	-2.739	-2.012	-0.402	$3.45 \times 10^{19}$
Bi, $\text{CuGaO}_2$ , $\text{Bi}_2\text{Ga}_4\text{O}_9$ , $\text{Ga}_2\text{O}_3$	0.0	-0.28	-2.555	-2.093	-0.546	$8.27 \times 10^{18}$
Bi, $\text{CuGaO}_2$ , $\text{Bi}_2\text{Ga}_4\text{O}_9$ , $\text{Bi}_2\text{O}_3$	0.0	-0.26	-2.739	-2.012	-0.648	$6.37 \times 10^{18}$
Bi, $\text{Cu}_2\text{Se}$ , $\text{CuGaO}_2$ , $\text{Ga}_2\text{O}_3$	0.0	-0.274	-2.537	-2.105	-0.54	$8 \times 10^{18}$
Bi, $\text{Cu}_2\text{Se}$ , $\text{Cu}_2\text{O}$ , $\text{CuGaO}_2$	0.0	-0.223	-2.691	-2.054	-0.643	$5.11 \times 10^{18}$
Bi, $\text{Cu}_3\text{Se}_2$ , $\text{Ga}_2\text{O}_3$ , $\text{Bi}_2\text{Se}_3$	0.0	-0.452	-2.371	-2.216	-0.252	$2.33 \times 10^{19}$
Bi, $\text{Cu}_2\text{Se}$ , $\text{Cu}_3\text{Se}_2$ , $\text{Ga}_2\text{O}_3$	0.0	-0.318	-2.471	-2.149	-0.453	$1.1 \times 10^{19}$
$\text{CuGaO}_2$ , $\text{Bi}_2\text{Ga}_4\text{O}_9$ , $\text{Cu}_3\text{Se}_2$ , $\text{Ga}_2\text{O}_3$	-0.221	-0.354	-2.776	-1.946	-0.399	$1.44 \times 10^{19}$
$\text{CuGaO}_2$ , $\text{Bi}_2\text{Ga}_4\text{O}_9$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_3$	-0.65	-0.477	-3.389	-1.578	-0.215	$3.17 \times 10^{19}$
$\text{Cu}_2\text{O}$ , $\text{CuGaO}_2$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_3$	-0.603	-0.445	-3.357	-1.61	-0.262	$2.61 \times 10^{19}$
$\text{Cu}_2\text{Se}$ , $\text{Cu}_2\text{O}$ , $\text{CuGaO}_2$ , $\text{Cu}_3\text{Se}_2$	-0.285	-0.318	-2.976	-1.864	-0.453	$1.13 \times 10^{19}$
$\text{Cu}_2\text{Se}$ , $\text{CuGaO}_2$ , $\text{Cu}_3\text{Se}_2$ , $\text{Ga}_2\text{O}_3$	-0.131	-0.318	-2.668	-2.018	-0.453	$1.13 \times 10^{19}$

Table S11: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-Ga phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## Phase Equilibria of In-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{In}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$p - n$ ( $\text{cm}^{-3}$ )
Se, $\text{In}_2\text{O}_3$ , $\text{Cu}_3\text{Se}_2$ , $\text{CuInSe}_2$	-0.379	-0.62	-1.896	-1.921	0.0	$7.34 \times 10^{19}$
Se, $\text{Cu}_3\text{Se}_2$ , $\text{CuInSe}_2$ , $\text{Bi}_2\text{Se}_3$	-0.378	-0.62	-1.896	-1.923	0.0	$7.34 \times 10^{19}$
Se, $\text{In}_2\text{O}_3$ , $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{O}_3$	-0.602	-0.708	-2.362	-1.61	0.0	$1.26 \times 10^{20}$
Se, $\text{In}_2\text{O}_3$ , $\text{CuInSe}_2$ , $\text{Bi}_2\text{Se}_3$	-0.378	-0.621	-1.895	-1.922	0.0	$7.39 \times 10^{19}$
Se, $\text{In}_2\text{O}_3$ , $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{Se}_3$	-0.378	-0.708	-2.025	-1.835	0.0	$1.24 \times 10^{20}$
Se, $\text{In}_2\text{O}_3$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_3$	-0.865	-0.62	-2.625	-1.435	0.0	$7.48 \times 10^{19}$
Bi, $\text{In}_2\text{O}_3$ , $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{Se}_3$	0.0	-0.582	-1.648	-2.087	-0.252	$5.36 \times 10^{19}$
Bi, $\text{In}_2\text{O}_3$ , $\text{CuInSe}_2$ , $\text{Bi}_2\text{Se}_3$	0.0	-0.495	-1.518	-2.173	-0.252	$3.08 \times 10^{19}$
Bi, $\text{In}_2\text{O}_3$ , $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{O}_3$	0.0	-0.507	-1.76	-2.012	-0.402	$3.45 \times 10^{19}$
Bi, $\text{Cu}_2\text{Se}$ , $\text{In}_2\text{O}_3$ , $\text{CuInO}_2$	0.0	-0.223	-1.696	-2.054	-0.642	$5.13 \times 10^{18}$
Bi, $\text{Cu}_2\text{Se}$ , $\text{Cu}_2\text{O}$ , $\text{CuInO}_2$	0.0	-0.223	-1.697	-2.054	-0.643	$5.11 \times 10^{18}$
Bi, $\text{Cu}_2\text{O}$ , $\text{CuInO}_2$ , $\text{Bi}_2\text{O}_3$	0.0	-0.244	-1.76	-2.012	-0.664	$5.61 \times 10^{18}$
Bi, $\text{In}_2\text{O}_3$ , $\text{CuInO}_2$ , $\text{Bi}_2\text{O}_3$	0.0	-0.245	-1.76	-2.012	-0.664	$5.65 \times 10^{18}$
Bi, $\text{Cu}_3\text{Se}_2$ , $\text{CuInSe}_2$ , $\text{Bi}_2\text{Se}_3$	0.0	-0.452	-1.56	-2.216	-0.252	$2.33 \times 10^{19}$
Bi, $\text{In}_2\text{O}_3$ , $\text{Cu}_3\text{Se}_2$ , $\text{CuInSe}_2$	0.0	-0.413	-1.482	-2.197	-0.31	$1.91 \times 10^{19}$
Bi, $\text{Cu}_2\text{Se}$ , $\text{In}_2\text{O}_3$ , $\text{Cu}_3\text{Se}_2$	0.0	-0.318	-1.554	-2.149	-0.453	$1.1 \times 10^{19}$
$\text{In}_2\text{O}_3$ , $\text{CuInO}_2$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_3$	-0.604	-0.446	-2.364	-1.609	-0.261	$2.62 \times 10^{19}$
$\text{Cu}_2\text{O}$ , $\text{CuInO}_2$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_3$	-0.603	-0.445	-2.363	-1.61	-0.262	$2.6 \times 10^{19}$
$\text{Cu}_2\text{Se}$ , $\text{In}_2\text{O}_3$ , $\text{CuInO}_2$ , $\text{Cu}_3\text{Se}_2$	-0.284	-0.318	-1.98	-1.865	-0.453	$1.13 \times 10^{19}$
$\text{Cu}_2\text{Se}$ , $\text{Cu}_2\text{O}$ , $\text{CuInO}_2$ , $\text{Cu}_3\text{Se}_2$	-0.285	-0.318	-1.982	-1.864	-0.453	$1.13 \times 10^{19}$

Table S12: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-In phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.



## Phase Equilibria of Tl-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$\Delta\mu_{\text{Tl}}$	$p - n$ ( $\text{cm}^{-3}$ )
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, BiSe <sub>2</sub> Tl, Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.582	-2.087	-0.252	-0.659	$5.39 \times 10^{19}$
Bi, BiSe <sub>2</sub> Tl, Bi <sub>2</sub> O <sub>3</sub> , Se <sub>12</sub> Tl <sub>20</sub>	0.0	-0.41	-2.012	-0.498	-0.166	$1.85 \times 10^{19}$
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, BiSe <sub>2</sub> Tl, Bi <sub>2</sub> O <sub>3</sub>	0.0	-0.507	-2.012	-0.402	-0.359	$3.45 \times 10^{19}$
Bi, BiSe <sub>2</sub> Tl, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.452	-2.216	-0.252	-0.659	$2.34 \times 10^{19}$
Bi, BiSe <sub>2</sub> Tl, Se <sub>12</sub> Tl <sub>20</sub> , Cu <sub>2</sub> Se <sub>2</sub> Tl	0.0	-0.399	-2.023	-0.498	-0.166	$1.74 \times 10^{19}$
Bi, Bi <sub>2</sub> O <sub>3</sub> , Se <sub>12</sub> Tl <sub>20</sub> , Cu <sub>2</sub> Se <sub>2</sub> Tl	0.0	-0.372	-2.012	-0.537	-0.142	$1.43 \times 10^{19}$
Bi, Cu <sub>2</sub> O, Bi <sub>2</sub> O <sub>3</sub> , Cu <sub>2</sub> Se <sub>2</sub> Tl	0.0	-0.244	-2.012	-0.664	-0.142	$5.67 \times 10^{18}$
Bi, Cu <sub>2</sub> Se, Cu <sub>2</sub> O, Cu <sub>2</sub> Se <sub>2</sub> Tl	0.0	-0.223	-2.054	-0.643	-0.227	$5.15 \times 10^{18}$
Bi, BiSe <sub>2</sub> Tl, Cu <sub>3</sub> Se <sub>2</sub> , Cu <sub>2</sub> Se <sub>2</sub> Tl	0.0	-0.399	-2.189	-0.332	-0.498	$1.78 \times 10^{19}$
Bi, Cu <sub>2</sub> Se, Cu <sub>3</sub> Se <sub>2</sub> , Cu <sub>2</sub> Se <sub>2</sub> Tl	0.0	-0.318	-2.149	-0.453	-0.417	$1.1 \times 10^{19}$
BiSe <sub>2</sub> Tl, Bi <sub>2</sub> O <sub>3</sub> , Se <sub>12</sub> Tl <sub>20</sub> , Cu <sub>2</sub> Se <sub>2</sub> Tl	-0.097	-0.447	-1.947	-0.429	-0.207	$2.44 \times 10^{19}$
Cu <sub>2</sub> Se, Cu <sub>2</sub> O, Cu <sub>3</sub> Se <sub>2</sub> , Cu <sub>2</sub> Se <sub>2</sub> Tl	-0.285	-0.318	-1.864	-0.453	-0.417	$1.14 \times 10^{19}$
Cu <sub>2</sub> O, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , Cu <sub>2</sub> Se <sub>2</sub> Tl	-0.603	-0.445	-1.61	-0.262	-0.544	$2.62 \times 10^{19}$
Se, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , Cu <sub>2</sub> Se <sub>2</sub> Tl	-0.865	-0.62	-1.435	0.0	-0.719	$7.53 \times 10^{19}$
Se, BiSe <sub>2</sub> Tl, Bi <sub>2</sub> O <sub>3</sub> , Cu <sub>2</sub> Se <sub>2</sub> Tl	-0.612	-0.704	-1.604	0.0	-0.55	$1.23 \times 10^{20}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, BiSe <sub>2</sub> Tl, Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.708	-1.835	0.0	-0.784	$1.25 \times 10^{20}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, BiSe <sub>2</sub> Tl, Bi <sub>2</sub> O <sub>3</sub>	-0.602	-0.708	-1.61	0.0	-0.56	$1.26 \times 10^{20}$
Se, BiSe <sub>2</sub> Tl, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.62	-1.923	0.0	-0.784	$7.36 \times 10^{19}$
Se, BiSe <sub>2</sub> Tl, Cu <sub>3</sub> Se <sub>2</sub> , Cu <sub>2</sub> Se <sub>2</sub> Tl	-0.443	-0.62	-1.857	0.0	-0.719	$7.43 \times 10^{19}$

Table S13: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-Tl phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## Phase Equilibria of Si-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$\Delta\mu_{\text{Si}}$	$p - n$ ( $\text{cm}^{-3}$ )
Bi, Bi <sub>4</sub> O <sub>12</sub> Si <sub>3</sub> , Bi <sub>2</sub> Se <sub>3</sub> , O <sub>2</sub> Si	0.0	-0.491	-2.177	-0.252	-5.116	$3.02 \times 10^{19}$
Bi, Bi <sub>4</sub> O <sub>12</sub> Si <sub>3</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.582	-2.087	-0.252	-5.477	$5.39 \times 10^{19}$
Bi, Cu <sub>2</sub> O, Bi <sub>4</sub> O <sub>12</sub> Si <sub>3</sub> , Bi <sub>2</sub> O <sub>3</sub>	0.0	-0.244	-2.012	-0.664	-5.777	$5.61 \times 10^{18}$
Bi, Bi <sub>4</sub> O <sub>12</sub> Si <sub>3</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub>	0.0	-0.507	-2.012	-0.402	-5.777	$3.45 \times 10^{19}$
Bi, Cu <sub>2</sub> Se, Cu <sub>2</sub> O, Bi <sub>4</sub> O <sub>12</sub> Si <sub>3</sub>	0.0	-0.223	-2.054	-0.643	-5.608	$5.11 \times 10^{18}$
Bi, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub> , O <sub>2</sub> Si	0.0	-0.452	-2.216	-0.252	-5.038	$2.34 \times 10^{19}$
Bi, Bi <sub>4</sub> O <sub>12</sub> Si <sub>3</sub> , Cu <sub>3</sub> Se <sub>2</sub> , O <sub>2</sub> Si	0.0	-0.374	-2.177	-0.369	-5.116	$1.55 \times 10^{19}$
Bi, Cu <sub>2</sub> Se, Bi <sub>4</sub> O <sub>12</sub> Si <sub>3</sub> , Cu <sub>3</sub> Se <sub>2</sub>	0.0	-0.318	-2.149	-0.453	-5.228	$1.1 \times 10^{19}$
Bi <sub>4</sub> O <sub>12</sub> Si <sub>3</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub> , O <sub>2</sub> Si	-0.352	-0.609	-1.942	-0.017	-5.586	$6.87 \times 10^{19}$
Cu <sub>2</sub> Se, Cu <sub>2</sub> O, Bi <sub>4</sub> O <sub>12</sub> Si <sub>3</sub> , Cu <sub>3</sub> Se <sub>2</sub>	-0.285	-0.318	-1.864	-0.453	-5.988	$1.13 \times 10^{19}$
Cu <sub>2</sub> O, Bi <sub>4</sub> O <sub>12</sub> Si <sub>3</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-0.603	-0.445	-1.61	-0.262	-6.581	$2.61 \times 10^{19}$
Se, Bi <sub>4</sub> O <sub>12</sub> Si <sub>3</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-0.865	-0.62	-1.435	0.0	-6.931	$7.5 \times 10^{19}$
Se, Bi <sub>4</sub> O <sub>12</sub> Si <sub>3</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.62	-1.923	0.0	-5.63	$7.36 \times 10^{19}$
Se, Bi <sub>4</sub> O <sub>12</sub> Si <sub>3</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.708	-1.835	0.0	-5.981	$1.25 \times 10^{20}$
Se, Bi <sub>4</sub> O <sub>12</sub> Si <sub>3</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub>	-0.603	-0.708	-1.61	0.0	-6.581	$1.26 \times 10^{20}$

Table S14: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-Si phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## Phase Equilibria of Ge-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{Ge}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$p - n$ (cm <sup>-3</sup> )
Se, Bi <sub>4</sub> Ge <sub>3</sub> O <sub>12</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.62	-2.165	-1.923	0.0	$7.36 \times 10^{19}$
Se, Bi <sub>12</sub> GeO <sub>20</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>4</sub> Ge <sub>3</sub> O <sub>12</sub>	-0.582	-0.708	-3.061	-1.63	0.0	$1.26 \times 10^{20}$
Se, Bi <sub>12</sub> GeO <sub>20</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub>	-0.603	-0.708	-3.224	-1.61	0.0	$1.26 \times 10^{20}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>4</sub> Ge <sub>3</sub> O <sub>12</sub> , Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.708	-2.515	-1.835	0.0	$1.25 \times 10^{20}$
Se, Bi <sub>12</sub> GeO <sub>20</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-0.865	-0.62	-3.574	-1.435	0.0	$7.5 \times 10^{19}$
Se, Bi <sub>12</sub> GeO <sub>20</sub> , Bi <sub>4</sub> Ge <sub>3</sub> O <sub>12</sub> , Cu <sub>3</sub> Se <sub>2</sub>	-0.845	-0.62	-3.411	-1.455	0.0	$7.48 \times 10^{19}$
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>4</sub> Ge <sub>3</sub> O <sub>12</sub> , Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.582	-2.012	-2.087	-0.252	$5.39 \times 10^{19}$
Bi, Bi <sub>12</sub> GeO <sub>20</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub>	0.0	-0.507	-2.421	-2.012	-0.402	$3.45 \times 10^{19}$
Bi, Bi <sub>12</sub> GeO <sub>20</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>4</sub> Ge <sub>3</sub> O <sub>12</sub>	0.0	-0.514	-2.284	-2.018	-0.388	$3.62 \times 10^{19}$
Bi, Bi <sub>4</sub> Ge <sub>3</sub> O <sub>12</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.452	-1.494	-2.216	-0.252	$2.34 \times 10^{19}$
Bi, Cu <sub>2</sub> Se, Bi <sub>4</sub> Ge <sub>3</sub> O <sub>12</sub> , Cu <sub>3</sub> Se <sub>2</sub>	0.0	-0.318	-1.762	-2.149	-0.453	$1.1 \times 10^{19}$
Bi, Cu <sub>2</sub> Se, Cu <sub>2</sub> O, Bi <sub>4</sub> Ge <sub>3</sub> O <sub>12</sub>	0.0	-0.223	-2.142	-2.054	-0.643	$5.11 \times 10^{18}$
Bi, Bi <sub>12</sub> GeO <sub>20</sub> , Cu <sub>2</sub> O, Bi <sub>2</sub> O <sub>3</sub>	0.0	-0.244	-2.421	-2.012	-0.664	$5.61 \times 10^{18}$
Bi, Bi <sub>12</sub> GeO <sub>20</sub> , Cu <sub>2</sub> O, Bi <sub>4</sub> Ge <sub>3</sub> O <sub>12</sub>	0.0	-0.241	-2.284	-2.018	-0.661	$5.54 \times 10^{18}$
Cu <sub>2</sub> Se, Cu <sub>2</sub> O, Bi <sub>4</sub> Ge <sub>3</sub> O <sub>12</sub> , Cu <sub>3</sub> Se <sub>2</sub>	-0.285	-0.318	-2.522	-1.864	-0.453	$1.13 \times 10^{19}$
Bi <sub>12</sub> GeO <sub>20</sub> , Cu <sub>2</sub> O, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-0.603	-0.445	-3.224	-1.61	-0.262	$2.61 \times 10^{19}$
Bi <sub>12</sub> GeO <sub>20</sub> , Cu <sub>2</sub> O, Bi <sub>4</sub> Ge <sub>3</sub> O <sub>12</sub> , Cu <sub>3</sub> Se <sub>2</sub>	-0.552	-0.425	-3.02	-1.651	-0.293	$2.3 \times 10^{19}$

Table S15: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-Ge phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## Phase Equilibria of Sn-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$\Delta\mu_{\text{Sn}}$	$p - n$ (cm <sup>-3</sup> )
Se, O <sub>2</sub> Sn, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.62	-1.923	0.0	-1.897	$7.36 \times 10^{19}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>7</sub> Sn <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-0.603	-0.708	-1.61	0.0	-2.676	$1.26 \times 10^{20}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>7</sub> Sn <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.708	-1.835	0.0	-2.113	$1.25 \times 10^{20}$
Se, O <sub>2</sub> Sn, Bi <sub>2</sub> O <sub>7</sub> Sn <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.68	-1.863	0.0	-2.017	$1.06 \times 10^{20}$
Se, O <sub>2</sub> Sn, Bi <sub>2</sub> O <sub>7</sub> Sn <sub>2</sub> , Cu <sub>3</sub> Se <sub>2</sub>	-0.557	-0.62	-1.743	0.0	-2.256	$7.48 \times 10^{19}$
Se, Bi <sub>2</sub> O <sub>7</sub> Sn <sub>2</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-0.865	-0.62	-1.435	0.0	-3.026	$7.5 \times 10^{19}$
Cu <sub>2</sub> O, Bi <sub>2</sub> O <sub>7</sub> Sn <sub>2</sub> , Cu <sub>2</sub> Se, Cu <sub>3</sub> Se <sub>2</sub>	-0.285	-0.318	-1.864	-0.453	-2.104	$1.13 \times 10^{19}$
O <sub>2</sub> Sn, Bi <sub>2</sub> O <sub>7</sub> Sn <sub>2</sub> , Cu <sub>2</sub> Se, Cu <sub>3</sub> Se <sub>2</sub>	-0.104	-0.318	-2.045	-0.453	-1.652	$1.13 \times 10^{19}$
Cu <sub>2</sub> O, Bi <sub>2</sub> O <sub>7</sub> Sn <sub>2</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-0.603	-0.445	-1.61	-0.262	-2.676	$2.61 \times 10^{19}$
Bi, Cu <sub>2</sub> O, Bi <sub>2</sub> O <sub>7</sub> Sn <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	0.0	-0.244	-2.012	-0.664	-1.873	$5.61 \times 10^{18}$
Bi, O <sub>2</sub> Sn, Bi <sub>2</sub> O <sub>7</sub> Sn <sub>2</sub> , Cu <sub>2</sub> Se	0.0	-0.283	-2.114	-0.522	-1.513	$8.61 \times 10^{18}$
Bi, Cu <sub>2</sub> O, Bi <sub>2</sub> O <sub>7</sub> Sn <sub>2</sub> , Cu <sub>2</sub> Se	0.0	-0.223	-2.054	-0.643	-1.724	$5.11 \times 10^{18}$
Bi, O <sub>2</sub> Sn, Cu <sub>2</sub> Se, Cu <sub>3</sub> Se <sub>2</sub>	0.0	-0.318	-2.149	-0.453	-1.444	$1.11 \times 10^{19}$
Bi, O <sub>2</sub> Sn, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.452	-2.216	-0.252	-1.31	$2.34 \times 10^{19}$
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>7</sub> Sn <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	0.0	-0.507	-2.012	-0.402	-1.873	$3.45 \times 10^{19}$
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>7</sub> Sn <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.582	-2.087	-0.252	-1.61	$5.39 \times 10^{19}$
Bi, O <sub>2</sub> Sn, Bi <sub>2</sub> O <sub>7</sub> Sn <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.554	-2.114	-0.252	-1.513	$4.52 \times 10^{19}$

Table S16: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-Sn phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## Phase Equilibria of Pb-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Pb}}$	$\Delta\mu_{\text{Se}}$	$p - n$ ( $\text{cm}^{-3}$ )
Se, PbSe, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.62	-1.923	-0.942	0.0	$8.28 \times 10^{19}$
Se, PbSe, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub>	-0.602	-0.708	-1.61	-0.942	0.0	$1.92 \times 10^{20}$
Se, PbSe, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.708	-1.835	-0.942	0.0	$1.3 \times 10^{20}$
Se, PbSe, Cu <sub>3</sub> Se <sub>2</sub> , O <sub>5</sub> Pb <sub>3</sub> Se	-0.772	-0.62	-1.528	-0.942	0.0	$4 \times 10^{20}$
Se, O <sub>3</sub> PbSe, Cu <sub>3</sub> Se <sub>2</sub> , O <sub>5</sub> Pb <sub>3</sub> Se	-0.773	-0.62	-1.527	-0.943	0.0	$4 \times 10^{20}$
Se, O <sub>3</sub> PbSe, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-0.865	-0.62	-1.435	-1.22	0.0	$1.54 \times 10^{20}$
Se, O <sub>3</sub> PbSe, Bi <sub>2</sub> O <sub>3</sub> , O <sub>5</sub> Pb <sub>3</sub> Se	-0.727	-0.666	-1.527	-0.943	0.0	$3.17 \times 10^{20}$
Se, PbSe, Bi <sub>2</sub> O <sub>3</sub> , O <sub>5</sub> Pb <sub>3</sub> Se	-0.726	-0.667	-1.528	-0.942	0.0	$3.17 \times 10^{20}$
Bi, PbSe, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.582	-2.087	-0.69	-0.252	$5.62 \times 10^{19}$
Bi, Cu <sub>2</sub> Se, Cu <sub>2</sub> O <sub>2</sub> Pb, OPb	0.0	-0.228	-2.059	-0.335	-0.632	$6.01 \times 10^{19}$
Bi, PbSe, Cu <sub>2</sub> Se, OPb	0.0	-0.237	-2.068	-0.326	-0.616	$6.59 \times 10^{19}$
Bi, Cu <sub>2</sub> Se, Cu <sub>2</sub> O, Cu <sub>2</sub> O <sub>2</sub> Pb	0.0	-0.223	-2.054	-0.356	-0.643	$5.31 \times 10^{19}$
Bi, Cu <sub>2</sub> O <sub>2</sub> Pb, Bi <sub>2</sub> O <sub>3</sub> , OPb	0.0	-0.252	-2.012	-0.382	-0.656	$4.6 \times 10^{19}$
Bi, Cu <sub>2</sub> O, Cu <sub>2</sub> O <sub>2</sub> Pb, Bi <sub>2</sub> O <sub>3</sub>	0.0	-0.244	-2.012	-0.398	-0.664	$4.18 \times 10^{19}$
Bi, PbSe, Bi <sub>2</sub> O <sub>3</sub> , OPb	0.0	-0.349	-2.012	-0.382	-0.56	$6.32 \times 10^{19}$
Bi, PbSe, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub>	0.0	-0.507	-2.012	-0.54	-0.402	$5.11 \times 10^{19}$
Bi, PbSe, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.452	-2.216	-0.69	-0.252	$2.74 \times 10^{19}$
Bi, PbSe, Cu <sub>2</sub> Se, Cu <sub>3</sub> Se <sub>2</sub>	0.0	-0.318	-2.149	-0.489	-0.453	$4.58 \times 10^{19}$
Cu <sub>2</sub> O, Cu <sub>2</sub> O <sub>2</sub> Pb, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-0.603	-0.445	-1.61	-0.8	-0.262	$2.94 \times 10^{20}$
Cu <sub>2</sub> O <sub>2</sub> Pb, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , OPb	-0.627	-0.461	-1.594	-0.8	-0.238	$3.42 \times 10^{20}$
PbSe, Cu <sub>3</sub> Se <sub>2</sub> , O <sub>5</sub> Pb <sub>3</sub> Se, OPb	-0.679	-0.536	-1.579	-0.815	-0.127	$4.58 \times 10^{20}$
Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , O <sub>5</sub> Pb <sub>3</sub> Se, OPb	-0.688	-0.502	-1.553	-0.841	-0.178	$4.03 \times 10^{20}$
O <sub>3</sub> PbSe, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , O <sub>5</sub> Pb <sub>3</sub> Se	-0.786	-0.567	-1.488	-0.983	-0.079	$3.36 \times 10^{20}$
PbSe, Bi <sub>2</sub> O <sub>3</sub> , O <sub>5</sub> Pb <sub>3</sub> Se, OPb	-0.649	-0.565	-1.579	-0.815	-0.127	$3.91 \times 10^{20}$
PbSe, Cu <sub>2</sub> Se, Cu <sub>3</sub> Se <sub>2</sub> , OPb	-0.244	-0.318	-1.905	-0.489	-0.453	$1.56 \times 10^{20}$
Cu <sub>2</sub> Se, Cu <sub>2</sub> O <sub>2</sub> Pb, Cu <sub>3</sub> Se <sub>2</sub> , OPb	-0.269	-0.318	-1.88	-0.514	-0.453	$1.56 \times 10^{20}$
Cu <sub>2</sub> Se, Cu <sub>2</sub> O, Cu <sub>2</sub> O <sub>2</sub> Pb, Cu <sub>3</sub> Se <sub>2</sub>	-0.285	-0.318	-1.864	-0.546	-0.453	$1.46 \times 10^{20}$

Table S17: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-Pb phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## Phase Equilibria of Sc-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Sc}}$	$\Delta\mu_{\text{Se}}$	$p - n$ ( $\text{cm}^{-3}$ )
Se, $\text{O}_3\text{Sc}_2$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{Se}_3$	-0.378	-0.62	-1.923	-6.969	0.0	$7.36 \times 10^{19}$
Se, $\text{O}_3\text{Sc}_2$ , $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{O}_3$	-0.602	-0.708	-1.61	-7.437	0.0	$1.26 \times 10^{20}$
Se, $\text{O}_3\text{Sc}_2$ , $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{Se}_3$	-0.378	-0.708	-1.835	-7.1	0.0	$1.25 \times 10^{20}$
Se, $\text{O}_3\text{Sc}_2$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_3$	-0.865	-0.62	-1.435	-7.7	0.0	$7.5 \times 10^{19}$
Bi, $\text{O}_3\text{Sc}_2$ , $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{Se}_3$	0.0	-0.582	-2.087	-6.723	-0.252	$5.39 \times 10^{19}$
Bi, $\text{Cu}_2\text{Se}$ , $\text{Cu}_2\text{O}$ , $\text{CuO}_2\text{Sc}$	0.0	-0.223	-2.054	-6.817	-0.643	$5.11 \times 10^{18}$
Bi, $\text{O}_3\text{Sc}_2$ , $\text{Cu}_2\text{Se}$ , $\text{CuO}_2\text{Sc}$	0.0	-0.253	-2.084	-6.726	-0.582	$6.72 \times 10^{18}$
Bi, $\text{O}_3\text{Sc}_2$ , $\text{CuO}_2\text{Sc}$ , $\text{Bi}_2\text{O}_3$	0.0	-0.29	-2.012	-6.835	-0.619	$7.98 \times 10^{18}$
Bi, $\text{Cu}_2\text{O}$ , $\text{CuO}_2\text{Sc}$ , $\text{Bi}_2\text{O}_3$	0.0	-0.244	-2.012	-6.881	-0.664	$5.61 \times 10^{18}$
Bi, $\text{O}_3\text{Sc}_2$ , $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{O}_3$	0.0	-0.507	-2.012	-6.835	-0.402	$3.45 \times 10^{19}$
Bi, $\text{O}_3\text{Sc}_2$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{Se}_3$	0.0	-0.452	-2.216	-6.528	-0.252	$2.34 \times 10^{19}$
Bi, $\text{O}_3\text{Sc}_2$ , $\text{Cu}_2\text{Se}$ , $\text{Cu}_3\text{Se}_2$	0.0	-0.318	-2.149	-6.629	-0.453	$1.1 \times 10^{19}$
$\text{O}_3\text{Sc}_2$ , $\text{Cu}_2\text{Se}$ , $\text{CuO}_2\text{Sc}$ , $\text{Cu}_3\text{Se}_2$	-0.194	-0.318	-1.955	-6.92	-0.453	$1.13 \times 10^{19}$
$\text{Cu}_2\text{Se}$ , $\text{Cu}_2\text{O}$ , $\text{CuO}_2\text{Sc}$ , $\text{Cu}_3\text{Se}_2$	-0.285	-0.318	-1.864	-7.102	-0.453	$1.13 \times 10^{19}$
$\text{O}_3\text{Sc}_2$ , $\text{CuO}_2\text{Sc}$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_3$	-0.739	-0.536	-1.519	-7.574	-0.126	$4.54 \times 10^{19}$
$\text{Cu}_2\text{O}$ , $\text{CuO}_2\text{Sc}$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_3$	-0.603	-0.445	-1.61	-7.483	-0.262	$2.61 \times 10^{19}$

Table S18: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-Sc phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## Phase Equilibria of Y-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$\Delta\mu_{\text{Y}}$	$p - n$ ( $\text{cm}^{-3}$ )
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> Se <sub>3</sub> , O <sub>3</sub> Y <sub>2</sub>	0.0	-0.582	-2.087	-0.252	-6.748	5.31e+19
Bi, Cu <sub>2</sub> O, Bi <sub>2</sub> O <sub>3</sub> , O <sub>3</sub> Y <sub>2</sub>	0.0	-0.244	-2.012	-0.664	-6.86	5.59e+18
Bi, Cu <sub>2</sub> Se, Cu <sub>2</sub> O, O <sub>3</sub> Y <sub>2</sub>	0.0	-0.223	-2.054	-0.643	-6.796	5.08e+18
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub> , O <sub>3</sub> Y <sub>2</sub>	0.0	-0.507	-2.012	-0.402	-6.86	3.44e+19
Bi, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub> , O <sub>3</sub> Y <sub>2</sub>	0.0	-0.452	-2.216	-0.252	-6.553	2.04e+19
Bi, Cu <sub>2</sub> Se, Cu <sub>3</sub> Se <sub>2</sub> , O <sub>3</sub> Y <sub>2</sub>	0.0	-0.318	-2.149	-0.453	-6.654	1.05e+19
Cu <sub>2</sub> Se, Cu <sub>2</sub> O, Cu <sub>3</sub> Se <sub>2</sub> , O <sub>3</sub> Y <sub>2</sub>	-0.285	-0.318	-1.864	-0.453	-7.082	1.12e+19
Cu <sub>2</sub> O, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , O <sub>3</sub> Y <sub>2</sub>	-0.603	-0.445	-1.61	-0.262	-7.463	2.59e+19
Se, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , O <sub>3</sub> Y <sub>2</sub>	-0.865	-0.62	-1.435	0.0	-7.725	7.46e+19
Se, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> Se <sub>3</sub> , O <sub>3</sub> Y <sub>2</sub>	-0.378	-0.708	-1.835	0.0	-7.125	1.22e+20
Se, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub> , O <sub>3</sub> Y <sub>2</sub>	-0.602	-0.708	-1.61	0.0	-7.462	1.25e+20
Se, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub> , O <sub>3</sub> Y <sub>2</sub>	-0.378	-0.62	-1.923	0.0	-6.994	6.67e+19

Table S19: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-Y phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## Phase Equilibria of Ti-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$\Delta\mu_{\text{Ti}}$	$p - n$ (cm <sup>-3</sup> )
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>7</sub> Ti <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.582	-2.087	-0.252	-5.733	$5.39 \times 10^{19}$
Bi, Bi <sub>2</sub> O <sub>7</sub> Ti <sub>2</sub> , O <sub>2</sub> Ti, Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.567	-2.101	-0.252	-5.683	$4.91 \times 10^{19}$
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>7</sub> Ti <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	0.0	-0.507	-2.012	-0.402	-5.996	$3.45 \times 10^{19}$
Bi, Cu <sub>2</sub> Se, Cu <sub>2</sub> O, Bi <sub>2</sub> O <sub>7</sub> Ti <sub>2</sub>	0.0	-0.223	-2.054	-0.643	-5.847	$5.11 \times 10^{18}$
Bi, Cu <sub>2</sub> Se, Bi <sub>2</sub> O <sub>7</sub> Ti <sub>2</sub> , O <sub>2</sub> Ti	0.0	-0.27	-2.101	-0.549	-5.683	$7.74 \times 10^{18}$
Bi, Cu <sub>2</sub> O, Bi <sub>2</sub> O <sub>7</sub> Ti <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	0.0	-0.244	-2.012	-0.664	-5.996	$5.61 \times 10^{18}$
Bi, Cu <sub>3</sub> Se <sub>2</sub> , O <sub>2</sub> Ti, Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.452	-2.216	-0.252	-5.453	$2.34 \times 10^{19}$
Bi, Cu <sub>2</sub> Se, Cu <sub>3</sub> Se <sub>2</sub> , O <sub>2</sub> Ti	0.0	-0.318	-2.149	-0.453	-5.587	$1.1 \times 10^{19}$
Cu <sub>2</sub> Se, Cu <sub>2</sub> O, Bi <sub>2</sub> O <sub>7</sub> Ti <sub>2</sub> , Cu <sub>3</sub> Se <sub>2</sub>	-0.285	-0.318	-1.864	-0.453	-6.227	$1.13 \times 10^{19}$
Cu <sub>2</sub> Se, Bi <sub>2</sub> O <sub>7</sub> Ti <sub>2</sub> , Cu <sub>3</sub> Se <sub>2</sub> , O <sub>2</sub> Ti	-0.144	-0.318	-2.005	-0.453	-5.875	$1.13 \times 10^{19}$
Cu <sub>2</sub> O, Bi <sub>2</sub> O <sub>7</sub> Ti <sub>2</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-0.603	-0.445	-1.61	-0.262	-6.799	$2.61 \times 10^{19}$
Se, Bi <sub>2</sub> O <sub>7</sub> Ti <sub>2</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-0.865	-0.62	-1.435	0.0	-7.149	$7.5 \times 10^{19}$
Se, Bi <sub>2</sub> O <sub>7</sub> Ti <sub>2</sub> , Cu <sub>3</sub> Se <sub>2</sub> , O <sub>2</sub> Ti	-0.597	-0.62	-1.703	0.0	-6.479	$7.48 \times 10^{19}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>7</sub> Ti <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.708	-1.835	0.0	-6.237	$1.25 \times 10^{20}$
Se, Bi <sub>2</sub> O <sub>7</sub> Ti <sub>2</sub> , O <sub>2</sub> Ti, Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.693	-1.849	0.0	-6.186	$1.14 \times 10^{20}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>7</sub> Ti <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-0.602	-0.708	-1.61	0.0	-6.799	$1.26 \times 10^{20}$
Se, Cu <sub>3</sub> Se <sub>2</sub> , O <sub>2</sub> Ti, Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.62	-1.923	0.0	-6.04	$7.36 \times 10^{19}$

Table S20: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-Ti phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.



## Phase Equilibria of Zr-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$\Delta\mu_{\text{Zr}}$	$p - n$ ( $\text{cm}^{-3}$ )
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, O <sub>2</sub> Zr, Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.582	-2.087	-0.252	-7.229	$5.39 \times 10^{19}$
Bi, Cu <sub>2</sub> Se, Cu <sub>2</sub> O, O <sub>2</sub> Zr	0.0	-0.223	-2.054	-0.643	-7.294	$5.11 \times 10^{18}$
Bi, Cu <sub>2</sub> O, O <sub>2</sub> Zr, Bi <sub>2</sub> O <sub>3</sub>	0.0	-0.244	-2.012	-0.664	-7.379	$5.61 \times 10^{18}$
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, O <sub>2</sub> Zr, Bi <sub>2</sub> O <sub>3</sub>	0.0	-0.507	-2.012	-0.402	-7.379	$3.45 \times 10^{19}$
Bi, O <sub>2</sub> Zr, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.452	-2.216	-0.252	-6.97	$2.34 \times 10^{19}$
Bi, Cu <sub>2</sub> Se, O <sub>2</sub> Zr, Cu <sub>3</sub> Se <sub>2</sub>	0.0	-0.318	-2.149	-0.453	-7.104	$1.1 \times 10^{19}$
Cu <sub>2</sub> O, O <sub>2</sub> Zr, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-0.603	-0.445	-1.61	-0.262	-8.182	$2.61 \times 10^{19}$
Cu <sub>2</sub> Se, Cu <sub>2</sub> O, O <sub>2</sub> Zr, Cu <sub>3</sub> Se <sub>2</sub>	-0.285	-0.318	-1.864	-0.453	-7.674	$1.13 \times 10^{19}$
Se, O <sub>2</sub> Zr, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-0.865	-0.62	-1.435	0.0	-8.532	$7.5 \times 10^{19}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, O <sub>2</sub> Zr, Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.708	-1.835	0.0	-7.732	$1.25 \times 10^{20}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, O <sub>2</sub> Zr, Bi <sub>2</sub> O <sub>3</sub>	-0.602	-0.708	-1.61	0.0	-8.182	$1.26 \times 10^{20}$
Se, O <sub>2</sub> Zr, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.62	-1.923	0.0	-7.557	$7.36 \times 10^{19}$

Table S21: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-Zr phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## Phase Equilibria of Hf-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{Hf}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$p - n$ ( $\text{cm}^{-3}$ )
Se, HfO <sub>2</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.62	-8.0	-1.923	0.0	$7.36 \times 10^{19}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, HfO <sub>2</sub> , Bi <sub>8</sub> Hf <sub>8</sub> O <sub>28</sub>	-0.517	-0.708	-8.454	-1.695	0.0	$1.25 \times 10^{20}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub> , Bi <sub>8</sub> Hf <sub>8</sub> O <sub>28</sub>	-0.603	-0.708	-8.668	-1.61	0.0	$1.26 \times 10^{20}$
Se, Bi <sub>2</sub> O <sub>2</sub> Se, HfO <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.708	-8.175	-1.835	0.0	$1.25 \times 10^{20}$
Se, HfO <sub>2</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>8</sub> Hf <sub>8</sub> O <sub>28</sub>	-0.78	-0.62	-8.805	-1.52	0.0	$7.48 \times 10^{19}$
Se, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , Bi <sub>8</sub> Hf <sub>8</sub> O <sub>28</sub>	-0.865	-0.62	-9.018	-1.435	0.0	$7.48 \times 10^{19}$
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, HfO <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.582	-7.672	-2.087	-0.252	$5.4 \times 10^{19}$
Bi, Cu <sub>2</sub> Se, Cu <sub>2</sub> O, HfO <sub>2</sub>	0.0	-0.223	-7.737	-2.054	-0.643	$5.11 \times 10^{18}$
Bi, Cu <sub>2</sub> O, HfO <sub>2</sub> , Bi <sub>8</sub> Hf <sub>8</sub> O <sub>28</sub>	0.0	-0.23	-7.765	-2.04	-0.65	$5.29 \times 10^{18}$
Bi, Cu <sub>2</sub> O, Bi <sub>2</sub> O <sub>3</sub> , Bi <sub>8</sub> Hf <sub>8</sub> O <sub>28</sub>	0.0	-0.244	-7.864	-2.012	-0.664	$5.61 \times 10^{18}$
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub> , Bi <sub>8</sub> Hf <sub>8</sub> O <sub>28</sub>	0.0	-0.507	-7.864	-2.012	-0.402	$3.44 \times 10^{19}$
Bi, Bi <sub>2</sub> O <sub>2</sub> Se, HfO <sub>2</sub> , Bi <sub>8</sub> Hf <sub>8</sub> O <sub>28</sub>	0.0	-0.535	-7.765	-2.04	-0.345	$4.14 \times 10^{19}$
Bi, HfO <sub>2</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.452	-7.413	-2.216	-0.252	$2.33 \times 10^{19}$
Bi, Cu <sub>2</sub> Se, HfO <sub>2</sub> , Cu <sub>3</sub> Se <sub>2</sub>	0.0	-0.318	-7.547	-2.149	-0.453	$1.1 \times 10^{19}$
Cu <sub>2</sub> O, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , Bi <sub>8</sub> Hf <sub>8</sub> O <sub>28</sub>	-0.603	-0.445	-8.668	-1.61	-0.262	$2.6 \times 10^{19}$
Cu <sub>2</sub> O, HfO <sub>2</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>8</sub> Hf <sub>8</sub> O <sub>28</sub>	-0.39	-0.36	-8.284	-1.78	-0.39	$1.51 \times 10^{19}$
Cu <sub>2</sub> Se, Cu <sub>2</sub> O, HfO <sub>2</sub> , Cu <sub>3</sub> Se <sub>2</sub>	-0.285	-0.318	-8.117	-1.864	-0.453	$1.13 \times 10^{19}$

Table S22: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-Hf phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## Phase Equilibria of F-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{F}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$p - n$ ( $\text{cm}^{-3}$ )
Cu <sub>2</sub> O, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , BiFO	-0.632	-0.465	-3.449	-1.601	-0.25	$2.62 \times 10^{19}$
Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>7</sub> F <sub>11</sub> O <sub>5</sub> , Cu <sub>2</sub> Se, BiFO	-0.263	-0.349	-3.507	-1.913	-0.423	$8.12 \times 10^{18}$
Cu <sub>2</sub> O, Cu <sub>3</sub> Se <sub>2</sub> , Cu <sub>2</sub> Se, BiFO	-0.343	-0.349	-3.507	-1.832	-0.423	$9.53 \times 10^{18}$
Bi, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>7</sub> F <sub>11</sub> O <sub>5</sub> , Cu <sub>2</sub> Se	0.0	-0.349	-3.555	-2.176	-0.423	$2.99 \times 10^{18}$
Bi, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>7</sub> F <sub>11</sub> O <sub>5</sub> , Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.46	-3.53	-2.231	-0.256	$3.82 \times 10^{18}$
Bi, Bi <sub>7</sub> F <sub>11</sub> O <sub>5</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, BiFO	0.0	-0.583	-3.595	-2.088	-0.277	$2.61 \times 10^{19}$
Bi, Bi <sub>2</sub> O <sub>3</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, BiFO	0.0	-0.518	-3.66	-2.023	-0.408	$2.77 \times 10^{19}$
Bi, Bi <sub>7</sub> F <sub>11</sub> O <sub>5</sub> , Cu <sub>2</sub> Se, BiFO	0.0	-0.262	-3.595	-2.088	-0.598	$2.93 \times 10^{18}$
Bi, Cu <sub>2</sub> O, Cu <sub>2</sub> Se, BiFO	0.0	-0.235	-3.621	-2.061	-0.652	$2.61 \times 10^{18}$
Bi, Cu <sub>2</sub> O, Bi <sub>2</sub> O <sub>3</sub> , BiFO	0.0	-0.254	-3.66	-2.023	-0.671	$3.59 \times 10^{18}$
Bi, Bi <sub>7</sub> F <sub>11</sub> O <sub>5</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.593	-3.59	-2.098	-0.256	$2.59 \times 10^{19}$
Se, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>7</sub> F <sub>11</sub> O <sub>5</sub> , BiFO	-0.686	-0.631	-3.366	-1.631	0.0	$7 \times 10^{19}$
Se, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , BiFO	-0.882	-0.631	-3.366	-1.435	0.0	$7.77 \times 10^{19}$
Se, Bi <sub>7</sub> F <sub>11</sub> O <sub>5</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> Se <sub>3</sub>	-0.385	-0.722	-3.462	-1.842	0.0	$9.44 \times 10^{19}$
Se, Bi <sub>2</sub> O <sub>3</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, BiFO	-0.611	-0.722	-3.456	-1.615	0.0	$1.31 \times 10^{20}$
Se, Bi <sub>7</sub> F <sub>11</sub> O <sub>5</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, BiFO	-0.415	-0.722	-3.456	-1.811	0.0	$1.01 \times 10^{20}$
Se, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>7</sub> F <sub>11</sub> O <sub>5</sub> , Bi <sub>2</sub> Se <sub>3</sub>	-0.385	-0.631	-3.421	-1.932	0.0	$3.23 \times 10^{19}$

Table S23: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-F phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## Phase Equilibria of Cl-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cl}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$p - n$ ( $\text{cm}^{-3}$ )
Se, BiClO, $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{Se}_3$	-0.378	-1.43	-0.62	-1.923	0.0	$3.32 \times 10^{19}$
Se, $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{O}_3$ , $\text{Bi}_{48}\text{Cl}_{20}\text{O}_{62}$	-0.603	-1.627	-0.708	-1.61	0.0	$1.05 \times 10^{20}$
Se, BiClO, $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_{48}\text{Cl}_{20}\text{O}_{62}$	-0.446	-1.518	-0.708	-1.767	0.0	$7.95 \times 10^{19}$
Se, BiClO, $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{Se}_3$	-0.378	-1.518	-0.708	-1.835	0.0	$7.92 \times 10^{19}$
Se, BiClO, $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_{48}\text{Cl}_{20}\text{O}_{62}$	-0.708	-1.43	-0.62	-1.592	0.0	$3.34 \times 10^{19}$
Se, $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_3$ , $\text{Bi}_{48}\text{Cl}_{20}\text{O}_{62}$	-0.865	-1.54	-0.62	-1.435	0.0	$5.15 \times 10^{19}$
Bi, BiClO, $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{Se}_3$	0.0	-1.643	-0.582	-2.087	-0.252	$2.18 \times 10^{19}$
Bi, BiClO, $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_{48}\text{Cl}_{20}\text{O}_{62}$	0.0	-1.666	-0.559	-2.064	-0.297	$1.71 \times 10^{19}$
Bi, $\text{Bi}_2\text{O}_2\text{Se}$ , $\text{Bi}_2\text{O}_3$ , $\text{Bi}_{48}\text{Cl}_{20}\text{O}_{62}$	0.0	-1.828	-0.507	-2.012	-0.402	$1.66 \times 10^{19}$
Bi, $\text{Cu}_2\text{Se}$ , $\text{Cu}_2\text{O}$ , $\text{Bi}_{48}\text{Cl}_{20}\text{O}_{62}$	0.0	-1.697	-0.223	-2.054	-0.643	$-2.32 \times 10^{18}$
Bi, $\text{Cu}_2\text{Se}$ , BiClO, $\text{Bi}_{48}\text{Cl}_{20}\text{O}_{62}$	0.0	-1.666	-0.233	-2.064	-0.623	$-2.35 \times 10^{18}$
Bi, $\text{Cu}_2\text{O}$ , $\text{Bi}_2\text{O}_3$ , $\text{Bi}_{48}\text{Cl}_{20}\text{O}_{62}$	0.0	-1.828	-0.244	-2.012	-0.664	$-4.58 \times 10^{17}$
Bi, BiClO, $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{Se}_3$	0.0	-1.514	-0.452	-2.216	-0.252	$4.83 \times 10^{18}$
Bi, $\text{Cu}_2\text{Se}$ , BiClO, $\text{Cu}_3\text{Se}_2$	0.0	-1.581	-0.318	-2.149	-0.453	$9.94 \times 10^{14}$
$\text{Cu}_2\text{O}$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_2\text{O}_3$ , $\text{Bi}_{48}\text{Cl}_{20}\text{O}_{62}$	-0.603	-1.627	-0.445	-1.61	-0.262	$8.51 \times 10^{18}$
$\text{Cu}_2\text{Se}$ , BiClO, $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_{48}\text{Cl}_{20}\text{O}_{62}$	-0.255	-1.581	-0.318	-1.894	-0.453	$3.5 \times 10^{16}$
$\text{Cu}_2\text{Se}$ , $\text{Cu}_2\text{O}$ , $\text{Cu}_3\text{Se}_2$ , $\text{Bi}_{48}\text{Cl}_{20}\text{O}_{62}$	-0.285	-1.602	-0.318	-1.864	-0.453	$3.02 \times 10^{17}$

Table S24: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-Cl phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## Phase Equilibria of Br-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Br}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$p - n$ ( $\text{cm}^{-3}$ )
Bi <sub>4</sub> Br <sub>2</sub> O <sub>5</sub> , Cu <sub>2</sub> O, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-0.603	-1.082	-0.445	-1.61	-0.262	$1.02 \times 10^{19}$
Bi <sub>4</sub> Br <sub>2</sub> O <sub>5</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , Bi <sub>6</sub> Br <sub>2</sub> O <sub>14</sub> Se <sub>3</sub>	-0.833	-1.006	-0.599	-1.456	-0.032	$4.75 \times 10^{19}$
Bi <sub>4</sub> Br <sub>2</sub> O <sub>5</sub> , Cu <sub>2</sub> Se, Cu <sub>3</sub> Se <sub>2</sub> , BiBrO	-0.152	-1.016	-0.318	-1.997	-0.453	$2.06 \times 10^{17}$
Bi <sub>4</sub> Br <sub>2</sub> O <sub>5</sub> , Cu <sub>2</sub> O, Cu <sub>2</sub> Se, Cu <sub>3</sub> Se <sub>2</sub>	-0.285	-1.082	-0.318	-1.864	-0.453	$1.07 \times 10^{18}$
Bi, Cu <sub>2</sub> Se, Cu <sub>3</sub> Se <sub>2</sub> , BiBrO	0.0	-1.016	-0.318	-2.149	-0.453	$1.92 \times 10^{17}$
Bi, Cu <sub>3</sub> Se <sub>2</sub> , BiBrO, Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.949	-0.452	-2.216	-0.252	$5.31 \times 10^{18}$
Bi, Bi <sub>4</sub> Br <sub>2</sub> O <sub>5</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub>	0.0	-1.283	-0.507	-2.012	-0.402	$1.94 \times 10^{19}$
Bi, Bi <sub>4</sub> Br <sub>2</sub> O <sub>5</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> Se <sub>3</sub>	0.0	-1.096	-0.582	-2.087	-0.252	$2.57 \times 10^{19}$
Bi, Bi <sub>4</sub> Br <sub>2</sub> O <sub>5</sub> , BiBrO, Bi <sub>2</sub> Se <sub>3</sub>	0.0	-1.067	-0.57	-2.098	-0.252	$2.08 \times 10^{19}$
Bi, Bi <sub>4</sub> Br <sub>2</sub> O <sub>5</sub> , Cu <sub>2</sub> O, Bi <sub>2</sub> O <sub>3</sub>	0.0	-1.283	-0.244	-2.012	-0.664	$-2.62 \times 10^{16}$
Bi, Bi <sub>4</sub> Br <sub>2</sub> O <sub>5</sub> , Cu <sub>2</sub> O, Cu <sub>2</sub> Se	0.0	-1.177	-0.223	-2.054	-0.643	$-1.37 \times 10^{18}$
Bi, Bi <sub>4</sub> Br <sub>2</sub> O <sub>5</sub> , Cu <sub>2</sub> Se, BiBrO	0.0	-1.067	-0.267	-2.098	-0.554	$-1.07 \times 10^{18}$
Se, Bi <sub>4</sub> Br <sub>2</sub> O <sub>5</sub> , Bi <sub>2</sub> O <sub>3</sub> , Bi <sub>6</sub> Br <sub>2</sub> O <sub>14</sub> Se <sub>3</sub>	-0.809	-1.014	-0.639	-1.472	0.0	$6.63 \times 10^{19}$
Se, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub> , Bi <sub>6</sub> Br <sub>2</sub> O <sub>14</sub> Se <sub>3</sub>	-0.865	-1.108	-0.62	-1.435	0.0	$6.84 \times 10^{19}$
Se, Bi <sub>4</sub> Br <sub>2</sub> O <sub>5</sub> , Cu <sub>3</sub> Se <sub>2</sub> , BiBrO	-0.605	-0.865	-0.62	-1.695	0.0	$3.58 \times 10^{19}$
Se, Bi <sub>4</sub> Br <sub>2</sub> O <sub>5</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>6</sub> Br <sub>2</sub> O <sub>14</sub> Se <sub>3</sub>	-0.833	-0.979	-0.62	-1.467	0.0	$5.45 \times 10^{19}$
Se, Bi <sub>4</sub> Br <sub>2</sub> O <sub>5</sub> , BiBrO, Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.941	-0.696	-1.847	0.0	$7.51 \times 10^{19}$
Se, Bi <sub>4</sub> Br <sub>2</sub> O <sub>5</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.97	-0.708	-1.835	0.0	$8.8 \times 10^{19}$
Se, Bi <sub>4</sub> Br <sub>2</sub> O <sub>5</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub>	-0.603	-1.083	-0.708	-1.61	0.0	$1.11 \times 10^{20}$
Se, Cu <sub>3</sub> Se <sub>2</sub> , BiBrO, Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.865	-0.62	-1.923	0.0	$3.57 \times 10^{19}$

Table S25: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-Br phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## Phase Equilibria of I-Doped BiCuSeO

Equilibrium Phases	$\Delta\mu_{\text{Bi}}$	$\Delta\mu_{\text{Cu}}$	$\Delta\mu_{\text{I}}$	$\Delta\mu_{\text{O}}$	$\Delta\mu_{\text{Se}}$	$p - n$ ( $\text{cm}^{-3}$ )
Se, Bi <sub>4</sub> I <sub>2</sub> O <sub>5</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub>	-0.602	-0.708	-0.547	-1.61	0.0	$1.24 \times 10^{20}$
Se, Bi <sub>4</sub> I <sub>2</sub> O <sub>5</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.708	-0.435	-1.835	0.0	$1.18 \times 10^{20}$
Se, BiIO, Bi <sub>4</sub> I <sub>2</sub> O <sub>5</sub> , Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.685	-0.379	-1.857	0.0	$9.84 \times 10^{19}$
Se, BiIO, Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> Se <sub>3</sub>	-0.378	-0.62	-0.314	-1.923	0.0	$6.1 \times 10^{19}$
Se, BiIO, Bi <sub>4</sub> I <sub>2</sub> O <sub>5</sub> , Cu <sub>3</sub> Se <sub>2</sub>	-0.573	-0.62	-0.314	-1.727	0.0	$6.16 \times 10^{19}$
Se, Bi <sub>4</sub> I <sub>2</sub> O <sub>5</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-0.865	-0.62	-0.46	-1.435	0.0	$7.2 \times 10^{19}$
Bi, BiIO, CuI, Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.455	-0.401	-2.213	-0.252	$1.33 \times 10^{19}$
Bi, BiIO, Bi <sub>4</sub> I <sub>2</sub> O <sub>5</sub> , Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.559	-0.505	-2.109	-0.252	$3.57 \times 10^{19}$
Bi, Bi <sub>4</sub> I <sub>2</sub> O <sub>5</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.582	-0.561	-2.087	-0.252	$4.6 \times 10^{19}$
Bi, Cu <sub>2</sub> O, Bi <sub>4</sub> I <sub>2</sub> O <sub>5</sub> , Bi <sub>2</sub> O <sub>3</sub>	0.0	-0.244	-0.748	-2.012	-0.664	$2.41 \times 10^{18}$
Bi, Bi <sub>4</sub> I <sub>2</sub> O <sub>5</sub> , Bi <sub>2</sub> O <sub>2</sub> Se, Bi <sub>2</sub> O <sub>3</sub>	0.0	-0.507	-0.748	-2.012	-0.402	$3.1 \times 10^{19}$
Bi, BiIO, Bi <sub>4</sub> I <sub>2</sub> O <sub>5</sub> , CuI	0.0	-0.351	-0.505	-2.109	-0.46	$4.14 \times 10^{18}$
Bi, Cu <sub>2</sub> Se, Cu <sub>2</sub> O, Bi <sub>4</sub> I <sub>2</sub> O <sub>5</sub>	0.0	-0.223	-0.642	-2.054	-0.643	$9.13 \times 10^{17}$
Bi, Cu <sub>2</sub> Se, Bi <sub>4</sub> I <sub>2</sub> O <sub>5</sub> , CuI	0.0	-0.229	-0.627	-2.06	-0.63	$9.66 \times 10^{17}$
Bi, Cu <sub>3</sub> Se <sub>2</sub> , CuI, Bi <sub>2</sub> Se <sub>3</sub>	0.0	-0.452	-0.404	-2.216	-0.252	$1.32 \times 10^{19}$
Bi, Cu <sub>2</sub> Se, Cu <sub>3</sub> Se <sub>2</sub> , CuI	0.0	-0.318	-0.538	-2.149	-0.453	$4.2 \times 10^{18}$
BiIO, Cu <sub>3</sub> Se <sub>2</sub> , CuI, Bi <sub>2</sub> Se <sub>3</sub>	-0.027	-0.464	-0.392	-2.195	-0.234	$1.47 \times 10^{19}$
BiIO, Bi <sub>4</sub> I <sub>2</sub> O <sub>5</sub> , Cu <sub>3</sub> Se <sub>2</sub> , CuI	-0.339	-0.464	-0.392	-1.883	-0.234	$1.5 \times 10^{19}$
Cu <sub>2</sub> O, Bi <sub>4</sub> I <sub>2</sub> O <sub>5</sub> , Cu <sub>3</sub> Se <sub>2</sub> , Bi <sub>2</sub> O <sub>3</sub>	-0.603	-0.445	-0.547	-1.61	-0.262	$2.05 \times 10^{19}$
Cu <sub>2</sub> Se, Cu <sub>2</sub> O, Bi <sub>4</sub> I <sub>2</sub> O <sub>5</sub> , Cu <sub>3</sub> Se <sub>2</sub>	-0.285	-0.318	-0.547	-1.864	-0.453	$4.45 \times 10^{18}$
Cu <sub>2</sub> Se, Bi <sub>4</sub> I <sub>2</sub> O <sub>5</sub> , Cu <sub>3</sub> Se <sub>2</sub> , CuI	-0.266	-0.318	-0.538	-1.883	-0.453	$4.22 \times 10^{18}$

Table S26: Chemical potentials  $\Delta\mu_i$  (in eV) in all phase regions of the quinary Bi-Cu-Se-O-I phase space that are in equilibrium with BiCuSeO. The corresponding charge carrier concentration in each phase region, as determined by charge neutrality at the typical synthesis temperature of 973 K, is listed.

## References

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