

Supporting Information

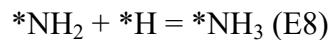
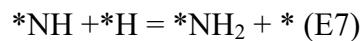
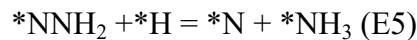
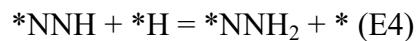
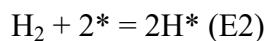
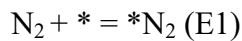
Computational Screening of Single-Atom Alloy TM@Ru(0001) for Enhanced Electrochemical Nitrogen Reduction Reaction

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Details of Micro-kinetic simulations

The following are the various elementary steps involved during the N₂ reduction via consecutive mechanism



* Represents a reaction site

The set of rate and equilibrium equations considered in the kinetic model are as follows:

$$\theta_{*N_2} = K_1 p_{N_2} \theta_v \quad (1)$$

$$\theta_{*H} = \sqrt{K_2 P_{H_2} \theta_v} \quad (2)$$

$$r_3 = \bar{k}_3 \theta_{*N_2} \theta_{*H} - \bar{k}_3 \theta_{*NNH} \theta_v \quad (3)$$

$$r_4 = \bar{k}_4 \theta_{*NNH} \theta_{*H} - \bar{k}_4 \theta_{*NNH_2} \theta_v \quad (4)$$

$$r_5 = \bar{k}_5 \theta_{*NNH_2} \theta_{*H} - \bar{k}_5 \theta_{*N} \theta_{*NH_3} \theta_v \quad (5)$$

$$r_6 = \bar{k}_6 \theta_{*N} \theta_{*H} - \bar{k}_6 \theta_{*NH} \theta_v \quad (6)$$

$$r_7 = \bar{k}_7 \theta_{*NH} \theta_{*H} - \bar{k}_7 \theta_{*NH_2} \theta_v \quad (7)$$

$$r_8 = \bar{k}_8 \theta_{*NH_2} \theta_{*H} - \bar{k}_8 \theta_{*NH_3} \theta_v \quad (8)$$

$$\theta_{*NH_3} = \frac{p_{NH_3} \theta_v}{K_9} \quad (9)$$

k_i are the rate constants assumed to be of the Arrhenius form, K_i are the adsorption or desorption equilibrium constants, θ_v is the free active sites, θ_{*M} is the coverage of the species, $*M$, p is the gas partial pressure. The ammonia conversion factor is assumed to be 0.1. The reaction rate for the N_2 adsorption and ammonia desorption can be given by the equation

$k_i = A_i^* \exp\left(-\frac{G_{a,i}}{k_B T}\right)$, where $G_{a,i}$ stands for the activation free energy of the reaction, A_i^* is an effective pre-exponential factor given by $A_i^* = x \frac{k_B T}{h}$, where x is the effective coefficient, T is the temperature, k_B is the Boltzmann constant, h is the Plank constant.

The equilibrium constant can be given by the equation as follows

$$K_i = \exp\left(-\frac{\Delta G_i}{k_B T}\right)$$

In which, ΔG_i is the free energy change for N_2 adsorption and NH_3 desorption step.

Furthermore, the reaction rate for the electrochemical steps such as E3-E8 while taking electrode potential into consideration can be given by

$$\bar{k}_i = A_i \exp\left(-\frac{E_{a,i}}{k_B T}\right) \exp\left(-\frac{e\beta_i(U - U_i)}{k_B T}\right)$$

Where $E_{a,i}$ represents the activation barrier which can be calculated by CI-NEB method,

$U_i = \frac{-\Delta G_i}{e}$ and β_i accounts for the symmetric factor which is taken equal to 0.50. Also, the equilibrium constant K_i for the electrochemical step can be written as $K_i = \exp\left(-\frac{eU + \Delta G_i}{k_B T}\right)$.

Thus, the \bar{k}_i , the reverse rate constant can be derived from the forward rate constant and equilibrium constant as follows

$$\bar{k}_i = \frac{K_i}{\bar{k}_i}$$

As E3 is only rate limiting step, all other hydrogenation steps are in equilibrium, therefore,

$$r_4=r_5=r_6=r_7=r_8=0.$$

Moreover, based on conversion law, the sum of coverage of all the reaction species equals to one. Thus,

$$\theta_{*N_2} + \theta_{*H} + \theta_{*NNH} + \theta_{*NNH_2} + \theta_{*N} + \theta_{*NH} + \theta_{*NH_2} + \theta_{*NH_3} + \theta_{*NH_3} + \theta_v = 1 \quad (10)$$

The free active site can be obtained as θ_v

$$\begin{aligned} \theta_v &= 1/(1 + K_1 p N_2 + \sqrt{K_2 p H_2}) + \frac{\tilde{k}_4 \tilde{k}_5 \tilde{k}_6 \tilde{k}_7 \tilde{k}_8 p_{NH_3}^2}{\tilde{k}_4 \tilde{k}_5 \tilde{k}_6 \tilde{k}_7 \tilde{k}_8 K_9^2 (K_2 p H_2)^{\frac{5}{2}}} + \frac{\tilde{k}_8 p_{NH_3}^2}{\tilde{k}_5 \tilde{k}_6 \tilde{k}_7} \\ &\quad \frac{\tilde{k}_6 \tilde{k}_7 \tilde{k}_8 \tilde{k}_9^3 \tilde{k}_7 \tilde{k}_8 K_9^2 (K_2 p H_2)^{\frac{3}{2}}}{\tilde{k}_6} + \frac{\tilde{k}_7 \tilde{k}_8 p_{NH_3}^2}{\tilde{k}_7 \tilde{k}_8 (K_2 p H_2)} + \frac{\tilde{k}_8 p_{NH_3}}{\tilde{k}_8 K_9 \sqrt{K_2 p H_2}} + \\ &\quad K_9 \\ &= 1/(1 + K_1 p N_2 + \sqrt{K_2 p H_2}) + \frac{p_{NH_3}^2}{K_4 K_5 K_6 K_7 K_8 K_9^2 (K_2 p H_2)^{\frac{5}{2}}} + \frac{p_{NH_3}^2}{K_5 K_6 K_7 K_8 K_9^2 (K_2 p H_2)^2} \\ &\quad + \frac{p_{NH_3}^2}{K_6 K_7 K_8 K_9^2 (K_2 p H_2)^{\frac{3}{2}}} + \frac{p_{NH_3}}{K_7 K_8 K_9^2 (K_2 p H_2)} + \frac{p_{NH_3}}{K_8 K_9 \sqrt{K_2 p H_2}} + \frac{p_{NH_3}}{K_9} \end{aligned} \quad (11)$$

Using the values of various parameters in the above equation to calculate the free active site

θ_v , all the terms except $K_1 p N_2 + \sqrt{K_2 p H_2}$ and $\frac{p_{NH_3}}{K_9}$ are very small and thus can be neglected. Thus, the reaction rate r_3 can be calculated by using the above obtained value of θ_v in equation (3) as follows.

$$\begin{aligned} r_3 &= \tilde{k}_3 \theta_{*N_2} \theta_{*H} - \tilde{k}_3 \theta_{*NNH} \theta_v \\ &= \tilde{k}_3 K_1 p N_2 \sqrt{K_2 p H_2} \theta_v^2 - \tilde{k}_3 p_{NH_3}^2 / K_4 K_5 K_6 K_7 K_8 K_9^2 (K_2 p H_2) \end{aligned}$$

The reverse reaction rate can be neglected as compared to the forward reaction rate, the value of θ_v can be used to obtain the value of turnover frequency.

Table S1: Free energy of hydrogen adsorption on the surface of the TM@Ru(0001) catalyst.

| Catalyst, TM@Ru(0001) | ΔG (eV) |
|-----------------------|-----------------|
| V@Ru(0001) | -1.15 |
| Ti@Ru(0001) | -0.99 |

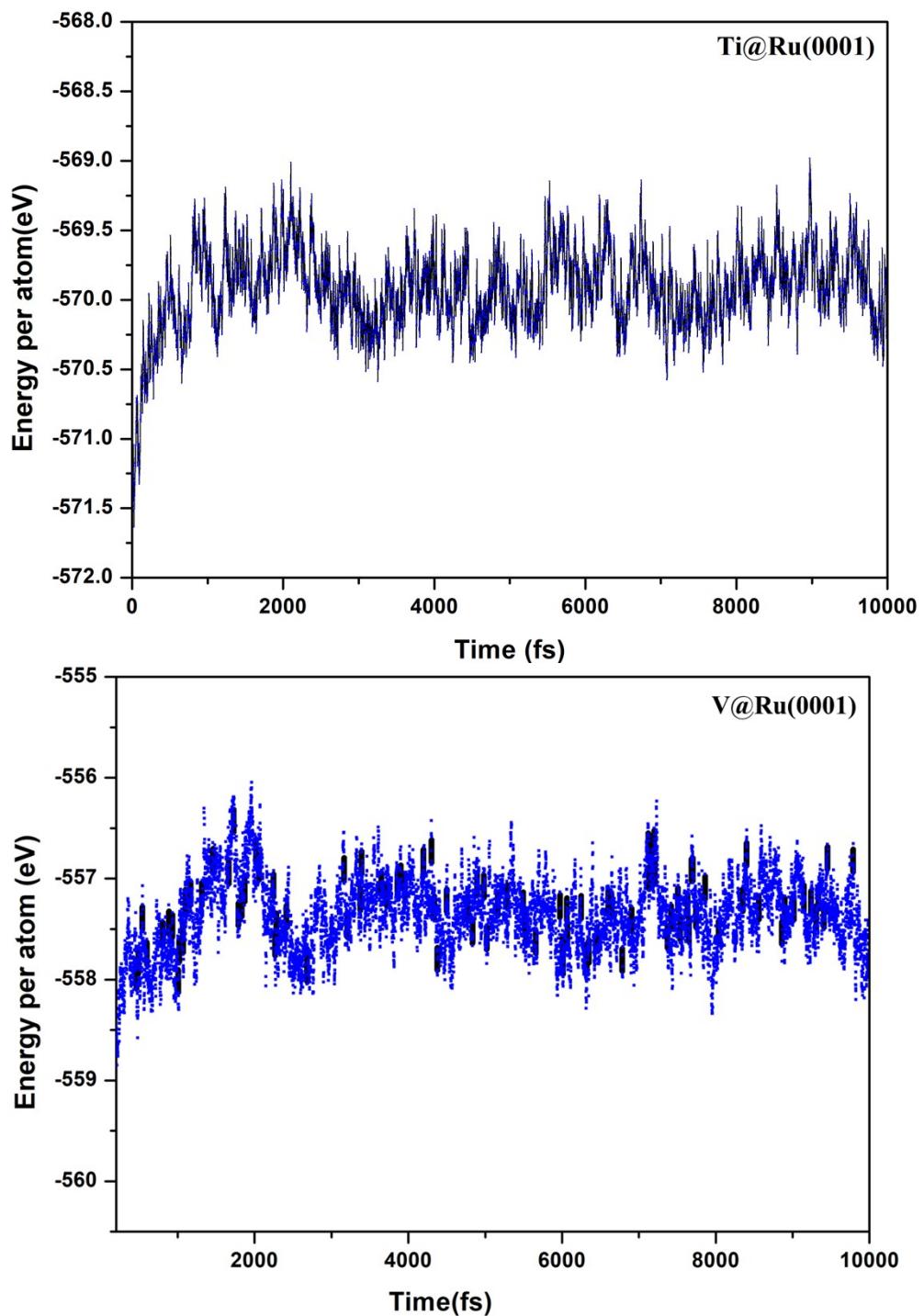


Figure S1: Variation of the energy per atom with the time for AIMD simulations for V@Ru(0001) and Ti@Ru(0001) complexes. The simulation run under 400K for 10ps with a time step of 1 fs.

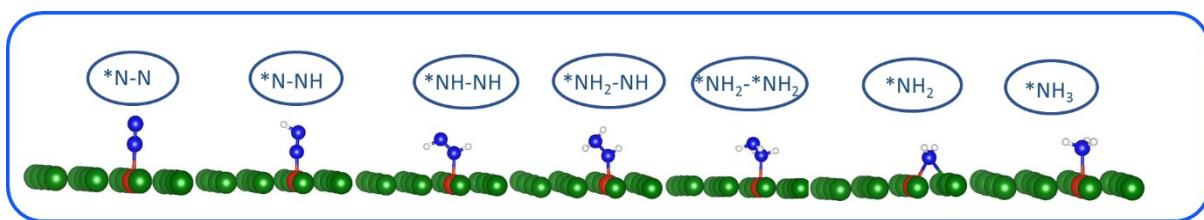
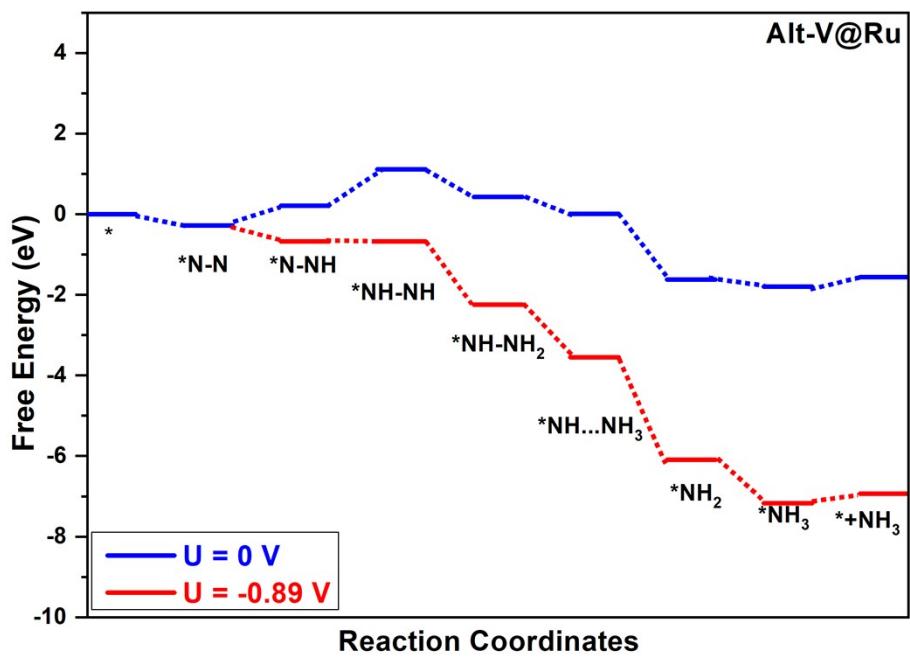


Figure S2: The free energy diagram for the conversion of N_2 to NH_3 using $\text{V}@\text{Ru}(0001)$ following alternating reaction pathway. The optimized structures of the involved intermediates are shown at the bottom of the figure.

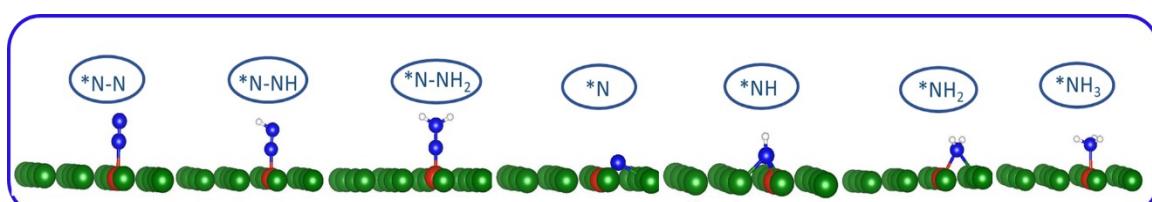
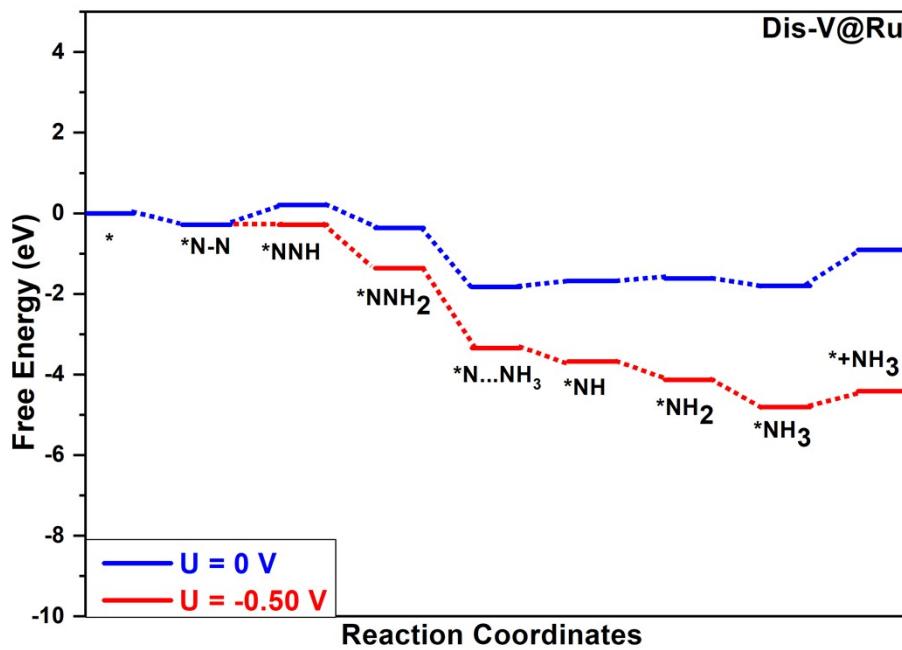


Figure S3: The free energy diagram for the conversion of N_2 to NH_3 using $\text{V}@\text{Ru}(0001)$ following Distal reaction pathway. The optimized structures of the involved intermediates are shown at the bottom of the figure.

Table S2: Cartesian Coordinates of all the intermediates formed during the nitrogen reduction using $\text{V}@\text{Ru}(0001)$.

$^*\text{N-N}$

| | | |
|--------------------|--------------------|--------------------|
| 0.5225221242768356 | 0.5243587768122839 | 0.4115527964915471 |
| 0.4039276761358382 | 0.5267962871172462 | 0.4133922057785407 |
| 0.4190735657728194 | 0.5895929224707540 | 0.3188994349979279 |
| 0.0909643938894545 | 0.1704794515828789 | 0.0026255237242704 |
| 0.0807005346776807 | 0.1666694829256093 | 0.2170992451710851 |
| 0.1643029536953447 | 0.0815547680803528 | 0.1077256081193058 |
| 0.1691490929063882 | 0.0867238963076849 | 0.3229679834503817 |
| 0.3275549191417381 | 0.1682721887494521 | 0.0022292326690223 |
| 0.3329851305145872 | 0.1660825513578490 | 0.2179971142399948 |
| 0.4180400623737795 | 0.0840565266021342 | 0.1080034213047905 |
| 0.4086682882434208 | 0.0791049903154300 | 0.3236295158921409 |
| 0.5821344747770871 | 0.1682530519538378 | 0.0019242337900087 |
| 0.5832784266205411 | 0.1676411006515030 | 0.2186422980810225 |

| | | |
|--------------------|--------------------|--------------------|
| 0.6661655501712918 | 0.0858740379516447 | 0.1083525063081905 |
| 0.6642137110823049 | 0.0779353086532975 | 0.3236256889961289 |
| 0.8303661752449225 | 0.1697240288898821 | 0.0022034545529121 |
| 0.8323141028727987 | 0.1657627634496472 | 0.2178045379179534 |
| 0.9149211875327481 | 0.0845190360417744 | 0.1068105181828824 |
| 0.9158471719716624 | 0.0797235100442000 | 0.3237684611254752 |
| 0.0755283143167035 | 0.4143119755716217 | 0.0032127099615179 |
| 0.0843029767212708 | 0.4171415361692163 | 0.2179365841001520 |
| 0.1684422206422599 | 0.3350384712549334 | 0.1074985161492738 |
| 0.1618544278622805 | 0.3266280025801162 | 0.3230665431441083 |
| 0.3332927867639644 | 0.4114988766979804 | 0.0028576575593742 |
| 0.3323788497010540 | 0.4185812815325745 | 0.2200846644805161 |
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| 0.5809761666507496 | 0.4123586673407207 | 0.0030791529122819 |
| 0.5837627754402609 | 0.4185905352015971 | 0.2185082203373561 |
| 0.6639622154019056 | 0.3318182499470628 | 0.1088142188712475 |
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| 0.1670641006048806 | 0.5834686285030299 | 0.1076369260113555 |
| 0.1595063053786065 | 0.5821404124525283 | 0.3230968856843568 |
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| 0.3330761154086134 | 0.6672457762939428 | 0.2185567358343633 |
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| 0.6683805620899766 | 0.8409541431142681 | 0.3224371239672625 |

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*N-*NH

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*N-NH2

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|--------------------|--------------------|--------------------|
| 0.5558760041413043 | 0.5290744531833582 | 0.4584141223275178 |
| 0.7116246657313801 | 0.6961768029454681 | 0.4584659401974792 |
| 0.6306764570545736 | 0.6153480489975047 | 0.4303275370267737 |
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| 0.0832268560161627 | 0.1660816596304290 | 0.2168453343519191 |
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| 0.1655047244408926 | 0.0899943608636399 | 0.3223006163342138 |
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| 0.5833340000000007 | 0.1666700000000034 | 0.0031000000000034 |
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| 0.9168315239050809 | 0.0835248024249149 | 0.3232964081238380 |
| 0.0833340000000007 | 0.4166659999999993 | 0.003100000000034 |
| 0.0839498799176451 | 0.4166164456841955 | 0.2171520696664432 |
| 0.1666650000000018 | 0.3333349999999982 | 0.1072190000000006 |
| 0.1617302141326437 | 0.3278251840461397 | 0.3225405525536662 |
| 0.3333299999999966 | 0.4166659999999993 | 0.003100000000034 |
| 0.3346803103420845 | 0.4185329812394527 | 0.2183525986577048 |
| 0.4166680000000014 | 0.3333409999999972 | 0.1072180000000031 |
| 0.4177966162896905 | 0.3278054448467553 | 0.3224953086738794 |
| 0.5833340000000007 | 0.4166669999999968 | 0.003100000000034 |
| 0.5835955753570213 | 0.4166440950295310 | 0.2171442865085572 |
| 0.6666650000000018 | 0.3333349999999982 | 0.1072190000000006 |

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| 0.6627870167511132 | 0.3375924145337228 | 0.3233674818524559 |
| 0.8333310000000012 | 0.4166659999999993 | 0.0031000000000034 |
| 0.8333088030489963 | 0.4157446565770735 | 0.2173891062034088 |
| 0.9166680000000014 | 0.3333409999999972 | 0.1072180000000031 |
| 0.9264451930775982 | 0.3375354184889022 | 0.3233554030345359 |
| 0.0833330000000032 | 0.6666689999999988 | 0.0031000000000034 |
| 0.0835402087270870 | 0.6665372250534203 | 0.2173274467722746 |
| 0.1666590000000028 | 0.5833319999999986 | 0.1072180000000031 |
| 0.1616647277736881 | 0.5826434254457390 | 0.3224985250144448 |
| 0.3333330000000032 | 0.6666669999999968 | 0.0031090000000020 |
| 0.3347156950602784 | 0.6654976723490523 | 0.2183593246450983 |
| 0.4166680000000014 | 0.5833319999999986 | 0.1072180000000031 |
| 0.5833340000000007 | 0.6666689999999988 | 0.0031000000000034 |
| 0.5816599061365684 | 0.6654886238105642 | 0.2183503677408084 |
| 0.6666590000000028 | 0.5833319999999986 | 0.1072180000000031 |
| 0.6724686915045049 | 0.5825611915504091 | 0.3225473394876291 |
| 0.8333319999999986 | 0.6666669999999968 | 0.0031090000000020 |
| 0.8338482760123872 | 0.6665410050226820 | 0.2173228239283314 |
| 0.9166680000000014 | 0.5833319999999986 | 0.1072180000000031 |
| 0.9168497506682114 | 0.5820434091197325 | 0.3232954057766052 |
| 0.0833340000000007 | 0.9166669999999968 | 0.0031000000000034 |
| 0.0836733400230164 | 0.9165145223382400 | 0.2179891404698560 |
| 0.1666650000000018 | 0.8333349999999982 | 0.1072190000000006 |
| 0.1717103553421170 | 0.8286622606677695 | 0.3226971483492228 |
| 0.3333310000000012 | 0.9166659999999993 | 0.0031000000000034 |
| 0.3336585153783551 | 0.9166290176673834 | 0.2173245773356356 |
| 0.4166680000000014 | 0.8333409999999972 | 0.1072180000000031 |
| 0.4177420276623262 | 0.8386152176679009 | 0.3225457011961812 |
| 0.5833340000000007 | 0.9166659999999993 | 0.0031000000000034 |
| 0.5835474617023795 | 0.9162517359236476 | 0.2171497270612353 |
| 0.6666650000000018 | 0.8333349999999982 | 0.1072190000000006 |
| 0.6726176294822296 | 0.8387339449025260 | 0.3225000059680051 |
| 0.8333299999999966 | 0.9166659999999993 | 0.0031000000000034 |
| 0.8338527549059658 | 0.9166172859418452 | 0.2173208267470630 |
| 0.9166680000000014 | 0.8333409999999972 | 0.1072180000000031 |
| 0.9086513426827052 | 0.8286896317378040 | 0.3226931339145882 |

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| 0.3961354111276879 | 0.5578492807057309 | 0.4640405265714913 |
| 0.1538124349416463 | 0.4502730237617213 | 0.4532682406103120 |
| 0.2101415608299221 | 0.4787153721398156 | 0.4081728337777634 |
| 0.3595793781489005 | 0.5503642571363144 | 0.4151898633592405 |
| 0.4191606929367854 | 0.5845176311758463 | 0.3200101167753887 |
| 0.0833340000000007 | 0.1666700000000034 | 0.0031000000000034 |
| 0.0826037097280405 | 0.1646708923176468 | 0.2169086099814501 |

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| 0.1666590000000028 | 0.0833319999999986 | 0.1072180000000031 |
| 0.1736198879072910 | 0.0870698426575767 | 0.3230778939888207 |
| 0.3333330000000032 | 0.1666680000000014 | 0.0031090000000020 |
| 0.3324863983836296 | 0.1661435736898425 | 0.2176178993612763 |
| 0.4166680000000014 | 0.0833319999999986 | 0.1072180000000031 |
| 0.4091740007445447 | 0.0790948462429149 | 0.3231959746626814 |
| 0.5833340000000007 | 0.1666700000000034 | 0.0031000000000034 |
| 0.5841886734939319 | 0.1670530452631800 | 0.2173509322797451 |
| 0.6666590000000028 | 0.0833319999999986 | 0.1072180000000031 |
| 0.6653760878135904 | 0.0760465582285345 | 0.3232595010489880 |
| 0.8333330000000032 | 0.1666669999999968 | 0.0031090000000020 |
| 0.8330844228879387 | 0.1664727427265747 | 0.2175772376437949 |
| 0.9166680000000014 | 0.0833319999999986 | 0.1072180000000031 |
| 0.9104393523596138 | 0.0834036528455164 | 0.3232979632224040 |
| 0.0833340000000007 | 0.4166659999999993 | 0.0031000000000034 |
| 0.0840250474691918 | 0.4169646904897010 | 0.2172096199572239 |
| 0.1666650000000018 | 0.3333349999999982 | 0.1072190000000006 |
| 0.1638305170113387 | 0.3350235140500871 | 0.3238875868917354 |
| 0.3333299999999966 | 0.4166659999999993 | 0.0031000000000034 |
| 0.3338467499182167 | 0.4164669561887824 | 0.2179311908542324 |
| 0.4166680000000014 | 0.3333409999999972 | 0.1072180000000031 |
| 0.4183169127797534 | 0.3287878942619392 | 0.3229909746607193 |
| 0.5833340000000007 | 0.4166669999999968 | 0.0031000000000034 |
| 0.5829152736792701 | 0.4167323139106555 | 0.2170772484221667 |
| 0.6666650000000018 | 0.3333349999999982 | 0.1072190000000006 |
| 0.6655594681410795 | 0.3387644697406125 | 0.3232818165267347 |
| 0.8333310000000012 | 0.4166659999999993 | 0.0031000000000034 |
| 0.8329711837267455 | 0.4161956768594759 | 0.2175621254577592 |
| 0.9166680000000014 | 0.3333409999999972 | 0.1072180000000031 |
| 0.9170859458133264 | 0.3327027759249070 | 0.3221671976547724 |
| 0.0833330000000032 | 0.6666689999999988 | 0.0031000000000034 |
| 0.0827506123246999 | 0.6675174125069234 | 0.2171453026466170 |
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| 0.1650731966725872 | 0.5777420541965956 | 0.3240075650759140 |
| 0.3333330000000032 | 0.6666669999999968 | 0.0031090000000020 |
| 0.3335358359974784 | 0.6669448287052194 | 0.2179657305188678 |
| 0.4166680000000014 | 0.5833319999999986 | 0.1072180000000031 |
| 0.5833340000000007 | 0.6666689999999988 | 0.0031000000000034 |
| 0.5823252402246880 | 0.6660668630694738 | 0.2178859325072388 |
| 0.6666590000000028 | 0.5833319999999986 | 0.1072180000000031 |
| 0.6738283223028917 | 0.5835742053281912 | 0.3233309198577632 |
| 0.8333319999999986 | 0.6666669999999968 | 0.0031090000000020 |
| 0.8319517639222581 | 0.6649298260501189 | 0.2175997012660546 |
| 0.9166680000000014 | 0.5833319999999986 | 0.1072180000000031 |
| 0.9102926526995937 | 0.5770934037454931 | 0.3233391369176443 |
| 0.0833340000000007 | 0.9166669999999968 | 0.0031000000000034 |
| 0.0838253279314290 | 0.9167361654363730 | 0.2181972775734452 |
| 0.1666650000000018 | 0.8333349999999982 | 0.1072190000000006 |
| 0.1736122133125878 | 0.8361575171062305 | 0.3232403800936611 |

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| 0.3333310000000012 | 0.9166659999999993 | 0.0031000000000034 |
| 0.3323226080871696 | 0.9160733425505030 | 0.2176050070851389 |
| 0.4166680000000014 | 0.8333409999999972 | 0.1072180000000031 |
| 0.4186244920873229 | 0.8395029536405184 | 0.3228754423067507 |
| 0.5833340000000007 | 0.9166659999999993 | 0.0031000000000034 |
| 0.5830203862401971 | 0.9158403348706798 | 0.2170595659139288 |
| 0.6666650000000018 | 0.8333349999999982 | 0.1072190000000006 |
| 0.6735131102251039 | 0.8392229696055766 | 0.3233115832627846 |
| 0.8333299999999966 | 0.9166659999999993 | 0.0031000000000034 |
| 0.8318006294723344 | 0.9165851773992082 | 0.2175918885120945 |
| 0.9166680000000014 | 0.8333409999999972 | 0.1072180000000031 |
| 0.9095613210921806 | 0.8288651051906185 | 0.3223051616528345 |

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| 0.5526478050890482 | 0.7837604323436709 | 0.4528016542586196 |
| 0.7113602239599203 | 0.7840666030223600 | 0.4557596068675964 |
| 0.5187993310033000 | 0.5382224281692144 | 0.4519191076020813 |
| 0.5440530969743117 | 0.6032871291107503 | 0.4096400347787977 |
| 0.6194926615091502 | 0.7553824897307979 | 0.4276046948886912 |
| 0.4244931437546682 | 0.5806944913835304 | 0.3217391841389079 |
| 0.0833340000000007 | 0.1666700000000034 | 0.0031000000000034 |
| 0.0822959380908928 | 0.1665269212939048 | 0.2174943641314922 |
| 0.1666590000000028 | 0.0833319999999986 | 0.1072180000000031 |
| 0.1718169187418196 | 0.0852040642217188 | 0.3225169207431638 |
| 0.3333330000000032 | 0.1666680000000014 | 0.0031090000000020 |
| 0.3323107462250897 | 0.1656313880598700 | 0.2169127087561927 |
| 0.4166680000000014 | 0.0833319999999986 | 0.1072180000000031 |
| 0.4077528482862445 | 0.0779339174640848 | 0.3232444965689566 |
| 0.5833340000000007 | 0.1666700000000034 | 0.0031000000000034 |
| 0.5840261195332159 | 0.1673395641901840 | 0.2176269605419600 |
| 0.6666590000000028 | 0.0833319999999986 | 0.1072180000000031 |
| 0.6683193591625517 | 0.0825638383908990 | 0.3226299645129113 |
| 0.8333330000000032 | 0.1666669999999968 | 0.0031090000000020 |
| 0.8330423351158289 | 0.1668104730292254 | 0.2171259096016059 |
| 0.9166680000000014 | 0.0833319999999986 | 0.1072180000000031 |
| 0.9138000874418364 | 0.0884918839012439 | 0.3234299155686623 |
| 0.0833340000000007 | 0.4166659999999993 | 0.0031000000000034 |
| 0.0843427993205888 | 0.4165995895027513 | 0.2178291442531342 |
| 0.1666650000000018 | 0.3333349999999982 | 0.1072190000000006 |
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| 0.3333299999999966 | 0.4166659999999993 | 0.0031000000000034 |
| 0.3337900694580880 | 0.4176118787755286 | 0.2185017944963112 |
| 0.4166680000000014 | 0.3333409999999972 | 0.1072180000000031 |
| 0.4163844322300295 | 0.3250328383780179 | 0.3216981054666236 |
| 0.5833340000000007 | 0.4166669999999968 | 0.0031000000000034 |
| 0.5838220642212402 | 0.4161126455686854 | 0.2170004683556481 |

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| 0.6666650000000018 | 0.333349999999982 | 0.1072190000000006 |
| 0.6641283624116057 | 0.3334249959074333 | 0.3231835329978753 |
| 0.833331000000012 | 0.4166659999999993 | 0.003100000000034 |
| 0.8326129174402567 | 0.415986672196253 | 0.2172929079936368 |
| 0.916668000000014 | 0.3333409999999972 | 0.1072180000000031 |
| 0.9259851685635686 | 0.3360239824738708 | 0.3250448794679927 |
| 0.0833330000000032 | 0.6666689999999988 | 0.003100000000034 |
| 0.0817997161481378 | 0.6651680932626373 | 0.2176511071066693 |
| 0.1666590000000028 | 0.5833319999999986 | 0.1072180000000031 |
| 0.1596748047926853 | 0.5815526028423791 | 0.3234613968476274 |
| 0.3333330000000032 | 0.6666669999999968 | 0.0031090000000020 |
| 0.3336706176804131 | 0.6664089899162497 | 0.2183700766523418 |
| 0.4166680000000014 | 0.5833319999999986 | 0.1072180000000031 |
| 0.5833340000000007 | 0.6666689999999988 | 0.003100000000034 |
| 0.5822206496074670 | 0.6658733261213881 | 0.2180223903666716 |
| 0.6666590000000028 | 0.5833319999999986 | 0.1072180000000031 |
| 0.6565383802414536 | 0.5818945008546982 | 0.3247264953309235 |
| 0.8333319999999986 | 0.6666669999999968 | 0.0031090000000020 |
| 0.8335677496234801 | 0.6661710273504711 | 0.2179540715045040 |
| 0.9166680000000014 | 0.5833319999999986 | 0.1072180000000031 |
| 0.9174256073065002 | 0.5795814879084209 | 0.3236117212879867 |
| 0.0833340000000007 | 0.9166669999999968 | 0.003100000000034 |
| 0.0821780953795986 | 0.9153485859520248 | 0.2177687069978044 |
| 0.166665000000018 | 0.8333349999999982 | 0.1072190000000006 |
| 0.1713351919216979 | 0.8320035430018284 | 0.3228180621181222 |
| 0.333331000000012 | 0.9166659999999993 | 0.003100000000034 |
| 0.3332213429013230 | 0.9160154887866494 | 0.2167991551357601 |
| 0.4166680000000014 | 0.8333409999999972 | 0.1072180000000031 |
| 0.4165114915458006 | 0.8393833400245757 | 0.3217859661376176 |
| 0.5833340000000007 | 0.9166659999999993 | 0.003100000000034 |
| 0.5828169103200563 | 0.917223398474757 | 0.2168832499712888 |
| 0.6666650000000018 | 0.8333349999999982 | 0.1072190000000006 |
| 0.6680900025640580 | 0.8366508142699484 | 0.3237071731685852 |
| 0.8333299999999966 | 0.9166659999999993 | 0.003100000000034 |
| 0.8349341427216587 | 0.9173860841729723 | 0.2172233879713762 |
| 0.9166680000000014 | 0.8333409999999972 | 0.1072180000000031 |
| 0.9146109526971202 | 0.8313777988522186 | 0.3222504016062859 |

*NH2-*NH2

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| 0.1566784658428721 | 0.4379250241547222 | 0.4480228494418811 |
| 0.3822578337869824 | 0.6109046054422158 | 0.4637092460420530 |
| 0.2237216730723039 | 0.3275646831707172 | 0.4637655086299773 |
| 0.4468111835344118 | 0.5002166921850836 | 0.4435584006615002 |
| 0.3739273422482160 | 0.5329986347358890 | 0.4300997287810610 |
| 0.2278877448594823 | 0.4055786018506000 | 0.4315285832014943 |
| 0.4136523318436577 | 0.5823319435016795 | 0.3205826767691173 |
| 0.0833340000000007 | 0.1666700000000034 | 0.003100000000034 |

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| 0.0825482421865321 | 0.1661117514900247 | 0.2178274222455163 |
| 0.1666590000000028 | 0.0833319999999986 | 0.1072180000000031 |
| 0.1734464957978591 | 0.0886307353052677 | 0.3232861646705321 |
| 0.3333330000000032 | 0.1666680000000014 | 0.0031090000000020 |
| 0.3315500481134342 | 0.1647398535642458 | 0.2168756059139529 |
| 0.4166680000000014 | 0.0833319999999986 | 0.1072180000000031 |
| 0.4108005745141555 | 0.0803704896185513 | 0.3238162627175412 |
| 0.5833340000000007 | 0.1666700000000034 | 0.0031000000000034 |
| 0.5837010940653142 | 0.1658470069433280 | 0.2171851486337947 |
| 0.6666590000000028 | 0.0833319999999986 | 0.1072180000000031 |
| 0.6638670436662689 | 0.0738903855413636 | 0.3245444462339298 |
| 0.8333330000000032 | 0.1666699999999968 | 0.0031090000000020 |
| 0.8320906997140409 | 0.1665375411320335 | 0.2175167692085499 |
| 0.9166680000000014 | 0.0833319999999986 | 0.1072180000000031 |
| 0.9111044888126573 | 0.0786160029976780 | 0.3232876586016880 |
| 0.0833340000000007 | 0.4166659999999993 | 0.0031000000000034 |
| 0.0827190187758430 | 0.4156999152725439 | 0.2175190981913752 |
| 0.1666650000000018 | 0.3333349999999982 | 0.1072190000000006 |
| 0.1711973371647655 | 0.3374975744612926 | 0.3250091009667793 |
| 0.3333299999999966 | 0.4166659999999993 | 0.0031000000000034 |
| 0.3334246711686146 | 0.4174038002057728 | 0.217883473239081 |
| 0.4166680000000014 | 0.3333409999999972 | 0.1072180000000031 |
| 0.4185820238291867 | 0.3249546011828899 | 0.3210841663968366 |
| 0.5833340000000007 | 0.4166669999999968 | 0.0031000000000034 |
| 0.5840501099071422 | 0.4180406831767989 | 0.216888804995269 |
| 0.6666650000000018 | 0.3333349999999982 | 0.1072190000000006 |
| 0.6655228733574191 | 0.3390431899982604 | 0.3230612429997830 |
| 0.8333310000000012 | 0.4166659999999993 | 0.0031000000000034 |
| 0.8328536187112344 | 0.4153164163732547 | 0.2177019140723417 |
| 0.9166680000000014 | 0.3333409999999972 | 0.1072180000000031 |
| 0.9201467109517042 | 0.3397571879898465 | 0.3234946541673748 |
| 0.0833330000000032 | 0.6666689999999988 | 0.0031000000000034 |
| 0.0820913364477758 | 0.6666912542018303 | 0.2171039764035651 |
| 0.1666590000000028 | 0.5833319999999986 | 0.1072180000000031 |
| 0.1576706422495407 | 0.5858511160081885 | 0.3214396791596466 |
| 0.3333330000000032 | 0.6666669999999968 | 0.0031090000000020 |
| 0.3339664079018417 | 0.6660904669310118 | 0.2180772307995545 |
| 0.4166680000000014 | 0.5833319999999986 | 0.1072180000000031 |
| 0.5833340000000007 | 0.6666689999999988 | 0.0031000000000034 |
| 0.5818546242258462 | 0.6656079457860409 | 0.2184279940228543 |
| 0.6666590000000028 | 0.5833319999999986 | 0.1072180000000031 |
| 0.6703684942921913 | 0.5825822119118519 | 0.3235688937629166 |
| 0.8333319999999986 | 0.6666669999999968 | 0.0031090000000020 |
| 0.8313439476132191 | 0.6657720804752355 | 0.2169322685608493 |
| 0.9166680000000014 | 0.5833319999999986 | 0.1072180000000031 |
| 0.9124158551162506 | 0.5764743543346719 | 0.3237257773779643 |
| 0.0833340000000007 | 0.9166669999999968 | 0.0031000000000034 |
| 0.0829350640429274 | 0.9170389353938099 | 0.2177419629612226 |
| 0.1666650000000018 | 0.8333349999999982 | 0.1072190000000006 |

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| 0.1712803511361860 | 0.8325775881516008 | 0.3226154872992471 |
| 0.3333310000000012 | 0.9166659999999993 | 0.0031000000000034 |
| 0.3333726851394632 | 0.9162634985519573 | 0.2171642765899078 |
| 0.4166680000000014 | 0.8333409999999972 | 0.1072180000000031 |
| 0.4171131702582533 | 0.8370961035710170 | 0.3232523878775235 |
| 0.5833340000000007 | 0.9166659999999993 | 0.0031000000000034 |
| 0.5823141724771226 | 0.9164203159505143 | 0.2174694910525463 |
| 0.6666650000000018 | 0.8333349999999982 | 0.1072190000000006 |
| 0.6715712400456135 | 0.8395851702969169 | 0.3237125250837773 |
| 0.8333299999999966 | 0.9166659999999993 | 0.0031000000000034 |
| 0.8331513504512000 | 0.9165600391239327 | 0.2179193278480839 |
| 0.9166680000000014 | 0.8333409999999972 | 0.1072180000000031 |
| 0.9077699194656665 | 0.8302738482672235 | 0.3230888524362796 |

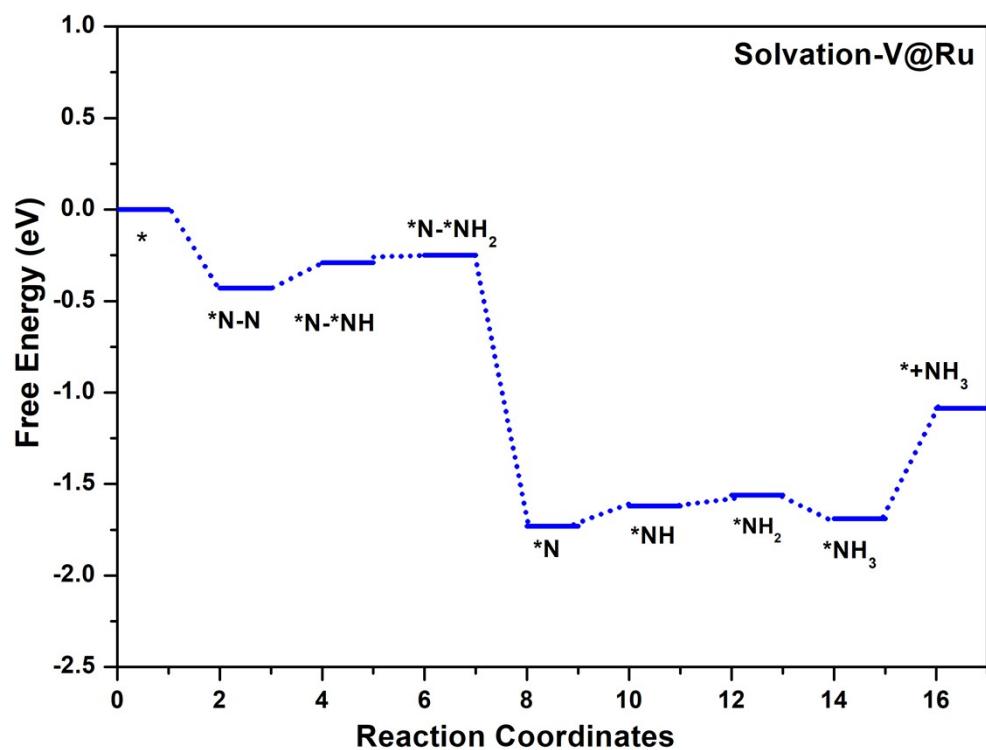


Figure S4: The free energy diagram for V@Ru(0001) together with the solvent effects.

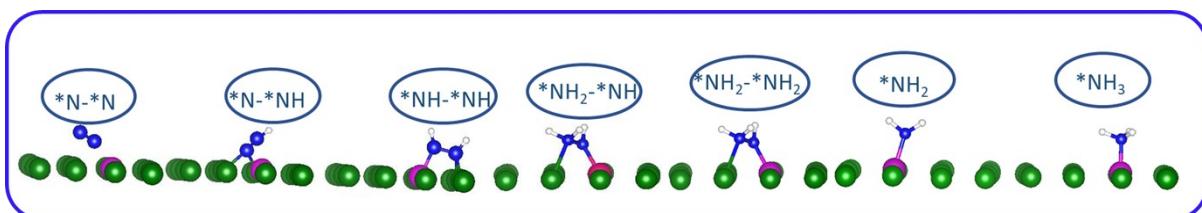
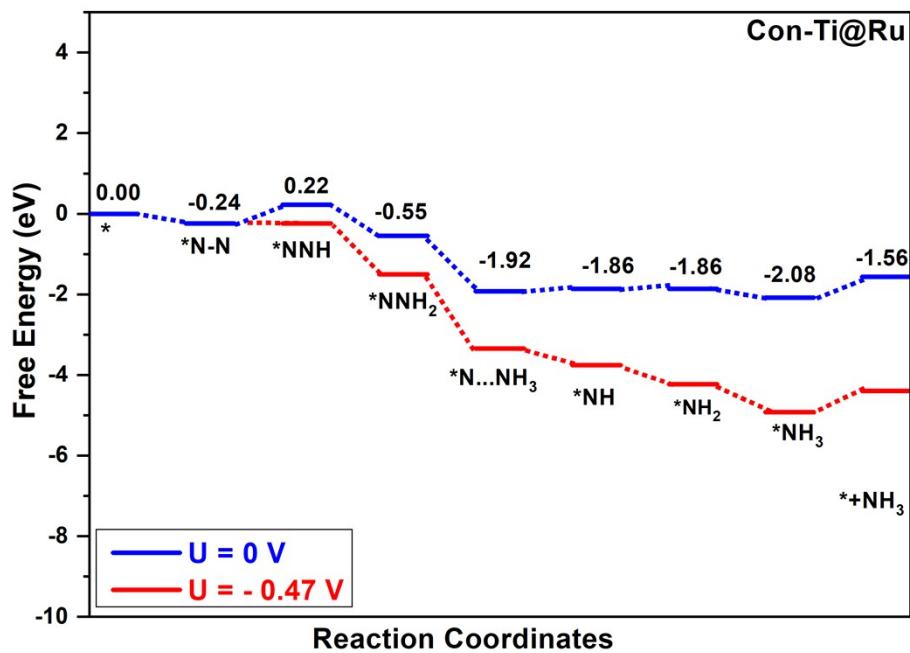
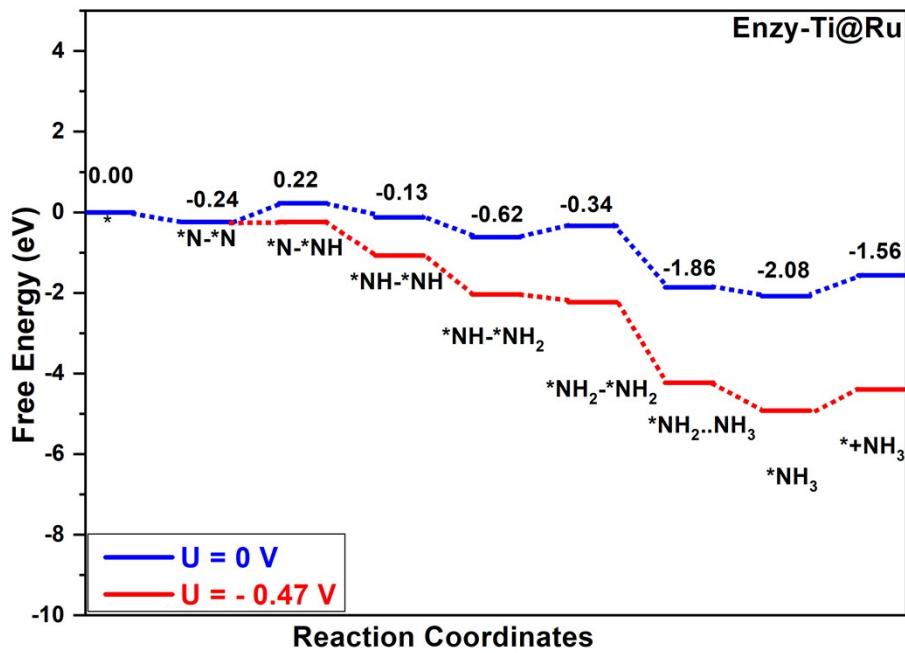


Figure S5: Free energy diagram for enzymatic and consecutive pathway for N_2 reduction to NH_3 using Ti@Ru(0001), at the bottom are various structures of reactive intermediates formed during the reduction process.

Table S3: Gives the kinetic barrier for each of the elementary step during the consecutive reduction pathway for V@Ru(0001)

| Elementary steps (Consecutive) | Energy barrier(eV) |
|-----------------------------------|--------------------|
| $*N-N \longrightarrow *N-*NH$ | 1.14 |
| $*N-*NH \longrightarrow *N-*NH_2$ | 0.85 |
| $*N-*NH_2 \longrightarrow *N$ | 0.86 |
| $*N \longrightarrow *NH$ | 1.31 |
| $*NH \longrightarrow *NH_2$ | 0.90 |
| $*NH_2 \longrightarrow *NH_3$ | 1.18 |

Table S4: Gives the kinetic barrier for each of the elementary step during the enzymatic reduction pathway for V@Ru(0001).

| Elementary steps (Enzymatic) | Energy barrier (eV) |
|---|---------------------|
| $*N-N \longrightarrow *N-*NH$ | 1.14 |
| $*N-*NH \longrightarrow *NH-*NH$ | 0.87 |
| $*NH-*NH \longrightarrow *NH-*NH_2$ | 0.72 |
| $*NH-*NH_2 \longrightarrow *NH_2-*NH_2$ | 1.51 |
| $*NH_2-*NH_2 \longrightarrow *NH_2$ | 0.43 |
| $*NH_2 \longrightarrow *NH_3$ | 1.19 |

Table S5: Gives the kinetic barrier for each of the elementary step during the consecutive reduction pathway for Ti@Ru(0001)

| Elementary steps (Consecutive) | Energy barrier(eV) |
|---|--------------------|
| $*\text{N-N} \longrightarrow *\text{N-}\text{*NH}$ | 1.48 |
| $*\text{N-}\text{*NH} \longrightarrow *\text{N-}\text{*NH}_2$ | 0.75 |
| $*\text{N-}\text{*NH}_2 \longrightarrow *\text{N}$ | 0.25 |
| $*\text{N} \longrightarrow *\text{NH}$ | 1.19 |
| $*\text{NH} \longrightarrow *\text{NH}_2$ | 0.87 |
| $*\text{NH}_2 \longrightarrow *\text{NH}_3$ | 1.27 |

Table S6: Gives the kinetic barrier for each of the elementary step during the enzymatic reduction pathway for Ti@Ru(0001).

| Elementary steps (Enzymatic) | Energy barrier (eV) |
|--|------------------------|
| $*\text{N-N} \longrightarrow *\text{N-}\text{*NH}$ | 1.48 |
| $*\text{N-}\text{*NH} \longrightarrow *\text{NH-}\text{*NH}$ | 1.28 |
| $*\text{NH-}\text{*NH} \longrightarrow *\text{NH-}\text{*NH}_2$ | 1.09 |
| $*\text{NH-}\text{*NH}_2 \longrightarrow *\text{NH}_2\text{-}\text{*NH}_2$ | 0.84 |
| $*\text{NH}_2\text{-}\text{*NH}_2 \longrightarrow *\text{NH}_2$ | 0.22 |
| $*\text{NH}_2 \longrightarrow *\text{NH}_3$ | 1.27 |