

Supporting Information

Novel IV-V-VI Semiconductors with Ultralow Lattice Thermal Conductivity

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Estimation of elastic moduli

According to the Voigt approximation, the bulk modulus (B_V) and shear modulus (G_V) are defined as¹

$$B_V = \frac{2(c_{11} + c_{12}) + c_{33} + 4c_{13}}{9}, \quad (* \text{ MERGEFORMAT } 1)$$

$$G_V = \frac{c_{11} + c_{12} + 2c_{33} + 12(c_{44} + c_{66}) - 4c_{13}}{30}, \quad (* \text{ MERGEFORMAT } 2)$$

where c_{ij} is the elastic stiffness constant. Within the Reuss model, they can be expressed as¹

$$B_R = \frac{c_{33}(c_{11} + c_{12}) - 2c_{13}^2}{2c_{33} + c_{11} + c_{12} - 4c_{13}}, \quad (* \text{ MERGEFORMAT } 3)$$

$$G_R = \frac{5[c_{33}(c_{11} + c_{12}) - 2c_{13}^2](c_{44}c_{66} - c_{14}^2)}{6B_V(c_{44}c_{66} - c_{14}^2) + 2[c_{33}(c_{11} + c_{12}) - 2c_{13}^2](c_{44} + c_{66})}. \quad (\backslash* \text{MERGEFORMAT } 4)$$

The Reuss moduli based on uniform stress indicate the lower limit of actual moduli while Voigt moduli from uniform strain represent the upper limit. Hill proposed a method that is the arithmetic average of Reuss and Voigt values.² In this work, the bulk modulus (B_H) and shear modulus (G_H) are obtained in terms of the Voigt-Reuss-Hill approximation

$$B_H = \frac{B_V + B_R}{2}, \quad (\backslash* \text{MERGEFORMAT } 5)$$

$$G_H = \frac{G_V + G_R}{2}. \quad (\backslash* \text{MERGEFORMAT } 6)$$

Young's modulus (E) is determined by

$$E = \frac{9B_H G_H}{3B_H + G_H}. \quad (\backslash* \text{MERGEFORMAT } 7)$$

Table S1 The used k -point meshes for self-consistent field (SCF) as well as 2nd and 3rd order IFC calculations. The size of the supercells employed in the calculations of IFCs is shown in parentheses. We present the specific parameters of q-points and scalebroad (parentheses) for the solution of the BTE as implemented in ShengBTE package.

System	SCF k -point mesh	2nd order IFC	3rd order IFC	BTE solution
$A_1B_2C_4$	$9 \times 9 \times 3$	$5 \times 5 \times 3$ (2×2×1)	Γ (2×2×1)	$17 \times 17 \times 2$ (0.5)
$A_1B_4C_7$	$9 \times 9 \times 5$	$5 \times 5 \times 3$ (2×2×2)	Γ (2×2×2)	$15 \times 15 \times 4$ (1.0)
$A_2B_2C_5$	$9 \times 9 \times 5$	$5 \times 5 \times 3$ (2×2×2)	Γ (2×2×2)	$15 \times 15 \times 5$ (1.0)
$A_3B_2C_6$	$9 \times 9 \times 3$	$5 \times 5 \times 3$ (2×2×1)	Γ (2×2×1)	$15 \times 15 \times 2$ (0.2)

Table S2 The complete list of 144 compositions and their competing stable phases as well as the calculated total energy E_{total} (eV/atom) and formation energy. E_{f1} (eV/atom) is the formation energy of a compound with respect to its elements, whereas E_{f2} (meV/atom) corresponds to the formation energy of a compound relative to their competing stable phases.

$A_1B_2C_4$	E_{f1}	Competing Stable Phases				$ E_{\text{total}} $			E_{f2}
SiAsS	-0.244	SiS ₂	AsS		4.713	5.336	4.715		267.86
SiAsSe	-0.329	SiSe ₂	As ₂ Se ₃	As	4.433	4.752	4.346	4.672	117.94
SiAsTe	-0.278	SiAs ₂	Te		4.18	5.279	3.143		-121.79
SiSbS	-0.350	SiS ₂	Sb ₂ S ₃	Sb	4.668	5.336	4.630	4.380	240.67
SiSbSe	-0.444	SiSe ₂	Sb ₂ Se ₃	Sb	4.396	4.752	4.306	4.380	108.42
SiSbTe	-0.370	Sb ₂ Te ₃	Si	Te	4.12	4.024	5.425	3.143	-22.00
SiBiS	-0.467	SiS ₂	Bi ₂ S ₃	Bi	4.715	5.336	4.704	3.833	176.71
SiBiSe	-0.559	SiSe ₂	Bi ₂ Se ₃	Bi	4.442	4.752	4.398	3.833	53.99
SiBiTe	-0.467	Bi ₂ Te ₃	Si	Te	4.148	4.076	5.425	3.143	-12.93
GeAsS	-0.308	GeS ₂	AsS		4.662	4.715	4.715		52.63
GeAsSe	-0.402	GeSe ₂	As ₂ Se ₃	As	4.391	4.316	4.346	4.672	-27.17
GeAsTe	-0.348	GeTe	As ₂ Te ₃		4.135	4.245	4.100		6.46
GeSbS	-0.441	GeS ₂	Sb ₂ S ₃	Sb	4.644	4.715	4.630	4.380	-1.56
GeSbSe	-0.534	GeSe	Sb ₂ Se ₃		4.371	4.508	4.306		-7.16
GeSbTe	-0.451	GeTe	Sb ₂ Te ₃		4.086	4.245	4.024		0.74
GeBiS	-0.569	GeS	Bi ₂ S ₃		4.702	4.819	4.704		34.57
GeBiSe	-0.657	GeSe	Bi ₂ Se ₃		4.425	4.508	4.398		4.34
GeBiTe	-0.554	GeTe	Bi ₂ Te ₃		4.12	4.245	4.076		3.81
SnAsS	-0.354	SnS ₂	AsS		4.619	4.650	4.715		67.81

SnAsSe	-0.457	SnSe	As ₂ Se ₃	4.356	4.455	4.346	20.94
SnAsTe	-0.400	SnTe	As ₂ Te ₃	4.097	4.147	4.100	16.49
SnSbS	-0.515	SnS	Sb ₂ S ₃	4.628	4.766	4.630	40.74
SnSbSe	-0.604	SnSe	Sb ₂ Se ₃	4.352	4.455	4.306	-3.13
SnSbTe	-0.510	SnTe	Sb ₂ Te ₃	4.056	4.147	4.024	2.77
SnBiS	-0.654	SnS	Bi ₂ S ₃	4.698	4.766	4.704	23.46
SnBiSe	-0.736	SnSe	Bi ₂ Se ₃	4.414	4.455	4.398	0.37
SnBiTe	-0.618	SnTe	Bi ₂ Te ₃	4.095	4.147	4.076	0.84
PbAsS	-0.377	PbS	As ₂ S ₃	4.602	4.789	4.641	81.29
PbAsSe	-0.488	PbSe	As ₂ Se ₃	4.347	4.514	4.346	46.74
PbAsTe	-0.434	PbTe	As ₂ Te ₃	4.092	4.178	4.100	30.29
PbSbS	-0.560	PbS	Sb ₂ S ₃	4.634	4.789	4.630	41.29
PbSbSe	-0.651	PbSe	Sb ₂ Se ₃	4.359	4.514	4.306	6.67
PbSbTe	-0.551	PbTe	Sb ₂ Te ₃	4.057	4.178	4.024	10.57
PbBiS	-0.711	PbS	Bi ₂ S ₃	4.715	4.789	4.704	13.00
PbBiSe	-0.791	PbSe	Bi ₂ Se ₃	4.429	4.514	4.398	2.17
PbBiTe	-0.664	PbTe	Bi ₂ Te ₃	4.101	4.178	4.076	3.64

A ₁ B ₄ C ₇	E_{f1}	Competing Stable Phases				$ E_{total} $			E_{f2}
SiAsS	-0.253	SiS ₂	As ₂ S ₃	AsS	4.671	5.336	4.641	4.715	168.250
SiAsSe	-0.352	SiSe ₂	As ₂ Se ₃	As	4.396	4.752	4.346	4.672	69.383
SiAsTe	-0.308	SiAs ₂	As ₂ Te ₃	Te	4.146	5.279	4.100	3.143	-70.292
SiSbS	-0.392	SiS ₂	Sb ₂ S ₃	Sb	4.633	5.336	4.630	4.380	159.472
SiSbSe	-0.492	SiSe ₂	Sb ₂ Se ₃	Sb	4.360	4.752	4.306	4.380	61.869

SiSbTe	-0.417	Si	Sb ₂ Te ₃	Te	4.079	5.425	4.024	3.143	-12.000
SiBiS	-0.540	SiS ₂	Bi ₂ S ₃	Bi	4.700	5.336	4.704	3.833	113.333
SiBiSe	-0.635	SiSe ₂	Bi ₂ Se ₃	Bi	4.422	4.752	4.398	3.833	33.161
SiBiTe	-0.535	Si	Bi ₂ Te ₃	Te	4.116	5.425	4.076	3.143	-5.750
GeAsS	-0.291	GeS ₂	As ₂ S ₃	AsS	4.641	4.715	4.641	4.715	42.950
GeAsSe	-0.394	GeSe ₂	As ₂ Se ₃	As	4.371	4.316	4.346	4.672	-14.767
GeAsTe	-0.348	GeTe	As ₂ Te ₃		4.119	4.245	4.100		5.267
GeSbS	-0.446	GeS ₂	Sb ₂ S ₃	Sb	4.620	4.715	4.630	4.380	17.172
GeSbSe	-0.546	GeSe	Sb ₂ Se ₃		4.346	4.508	4.306		-6.133
GeSbTe	-0.465	GeTe	Sb ₂ Te ₃		4.060	4.245	4.024		0.433
GeBiS	-0.601	GeS	Bi ₂ S ₃		4.694	4.819	4.704		28.833
GeBiSe	-0.694	GeSe	Bi ₂ Se ₃		4.413	4.508	4.398		3.283
GeBiTe	-0.587	GeTe	Bi ₂ Te ₃		4.101	4.245	4.076		2.683
SnAsS	-0.315	SnS ₂	As ₂ S ₃	AsS	4.613	4.650	4.641	4.715	54.725
SnAsSe	-0.423	SnSe	As ₂ Se ₃		4.348	4.455	4.346		15.883
SnAsTe	-0.376	SnTe	As ₂ Te ₃		4.095	4.147	4.100		12.950
SnSbS	-0.489	SnS	Sb ₂ S ₃		4.611	4.766	4.630		41.517
SnSbSe	-0.587	SnSe	Sb ₂ Se ₃		4.335	4.455	4.306		-3.867
SnSbTe	-0.500	SnTe	Sb ₂ Te ₃		4.042	4.147	4.024		2.117
SnBiS	-0.652	SnS	Bi ₂ S ₃		4.693	4.766	4.704		21.017
SnBiSe	-0.740	SnSe	Bi ₂ Se ₃		4.407	4.455	4.398		0.550
SnBiTe	-0.626	SnTe	Bi ₂ Te ₃		4.087	4.147	4.076		0.367
PbAsS	-0.325	PbS	As ₂ S ₃		4.600	4.789	4.641		65.667

PbAsSe	-0.438	PbSe	As ₂ Se ₃	4.340	4.514	4.346	33.683
PbAsTe	-0.395	PbTe	As ₂ Te ₃	4.091	4.178	4.100	22.083
PbSbS	-0.515	PbS	Sb ₂ S ₃	4.613	4.789	4.630	43.333
PbSbSe	-0.613	PbSe	Sb ₂ Se ₃	4.338	4.514	4.306	2.933
PbSbTe	-0.523	PbTe	Sb ₂ Te ₃	4.042	4.178	4.024	7.250
PbBiS	-0.685	PbS	Bi ₂ S ₃	4.702	4.789	4.704	15.833
PbBiSe	-0.772	PbSe	Bi ₂ Se ₃	4.416	4.514	4.398	1.350
PbBiTe	-0.652	PbTe	Bi ₂ Te ₃	4.090	4.178	4.076	2.500

A ₂ B ₂ C ₅	E_{f1}	Competing Stable Phases				$ E_{total} $			E_{f2}
SiAsS	-0.224	AsS	SiS ₂	As	4.762	4.715	5.336	4.672	362.111
SiAsSe	-0.296	As ₂ Se ₃	SiSe ₂	As	4.479	4.346	4.752	4.672	186.022
SiAsTe	-0.238	Te	SiAs		4.225	3.143	5.396		-80.489
SiSbS	-0.297	Sb ₂ S ₃	SiS ₂	Sb	4.717	4.630	5.336	4.380	346.593
SiSbSe	-0.379	Sb ₂ Se ₃	SiSe ₂	Sb	4.444	4.306	4.752	4.380	170.485
SiSbTe	-0.305	Sb ₂ Te ₃	Si	Te	4.174	4.024	5.425	3.143	-34.667
SiBiS	-0.378	Bi ₂ S ₃	SiS ₂	Bi	4.744	4.704	5.336	3.833	252.222
SiBiSe	-0.463	Bi ₂ Se ₃	SiSe ₂	Bi	4.474	4.398	4.752	3.833	76.430
SiBiTe	-0.378	Bi ₂ Te ₃	Si	Te	4.193	4.076	5.425	3.143	-24.833
GeAsS	-0.329	AsS	GeS ₂	As	4.688	4.715	4.715	4.672	21.978
GeAsSe	-0.412	As ₂ Se ₃	GeSe ₂	As	4.416	4.346	4.316	4.672	-42.044
GeAsTe	-0.349	As ₂ Te ₃	GeTe		4.157	4.100	4.245		7.378
GeSbS	-0.432	Sb ₂ S ₃	GeS ₂	Sb	4.674	4.630	4.715	4.380	-24.541
GeSbSe	-0.515	Sb ₂ Se ₃	GeSe		4.401	4.306	4.508		-5.189

GeSbTe	-0.429	Sb ₂ Te ₃	GeTe		4.119	4.024	4.245		2.822
GeBiS	-0.526	Bi ₂ S ₃	GeS		4.714	4.704	4.819		40.889
GeBiSe	-0.608	Bi ₂ Se ₃	GeSe		4.440	4.398	4.508		6.756
GeBiTe	-0.508	Bi ₂ Te ₃	GeTe		4.144	4.076	4.245		6.656
SnAsS	-0.409	AsS	SnS ₂	SnS	4.629	4.715	4.650	4.766	75.433
SnAsSe	-0.502	As ₂ Se ₃	SnSe		4.367	4.346	4.455		27.356
SnAsTe	-0.432	As ₂ Te ₃	SnTe		4.101	4.100	4.147		19.867
SnSbS	-0.546	Sb ₂ S ₃	SnS		4.648	4.630	4.766		42.378
SnSbSe	-0.625	Sb ₂ Se ₃	SnSe		4.372	4.306	4.455		0.522
SnSbTe	-0.523	Sb ₂ Te ₃	SnTe		4.074	4.024	4.147		4.311
SnBiS	-0.655	Bi ₂ S ₃	SnS		4.703	4.704	4.766		28.378
SnBiSe	-0.729	Bi ₂ Se ₃	SnSe		4.422	4.398	4.455		1.467
SnBiTe	-0.609	Bi ₂ Te ₃	SnTe		4.106	4.076	4.147		1.144
PbAsS	-0.457	As ₂ S ₃	PbS		4.615	4.641	4.789		91.778
PbAsSe	-0.560	As ₂ Se ₃	PbSe		4.363	4.346	4.514		57.489
PbAsTe	-0.490	As ₂ Te ₃	PbTe		4.097	4.100	4.178		37.556
PbSbS	-0.622	Sb ₂ S ₃	PbS		4.662	4.630	4.789		38.556
PbSbSe	-0.703	Sb ₂ Se ₃	PbSe		4.388	4.306	4.514		10.656
PbSbTe	-0.590	Sb ₂ Te ₃	PbTe		4.079	4.024	4.178		13.000
PbBiS	-0.744	Bi ₂ S ₃	PbS		4.730	4.704	4.789		11.556
PbBiSe	-0.815	Bi ₂ Se ₃	PbSe		4.446	4.398	4.514		3.600
PbBiTe	-0.681	Bi ₂ Te ₃	PbTe		4.116	4.076	4.178		4.833

A ₃ B ₂ C ₆	E_{f1}	Competing Stable Phases				$ E_{total} $	E_{f2}
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SiAsS	-0.210	SiS ₂	As		4.792	5.336	4.672		423.273
SiAsSe	-0.274	SiSe ₂	As		4.507	4.752	4.672		230.618
SiAsTe	-0.212	Si	SiAs	Te	4.252	5.425	5.396	3.143	-82.127
SiSbS	-0.265	SiS ₂	Sb		4.751	5.336	4.380		411.182
SiSbSe	-0.339	SiSe ₂	Sb		4.476	4.752	4.380		208.527
SiSbTe	-0.264	Sb ₂ Te ₃	Si	Te	4.208	4.024	5.425	3.143	-42.364
SiBiS	-0.325	SiS ₂	Bi		4.767	5.336	3.833		295.727
SiBiSe	-0.405	SiSe ₂	Bi		4.497	4.752	3.833		88.073
SiBiTe	-0.323	Si	Bi ₂ Te ₃	Te	4.223	5.425	4.076	3.143	-33.773
GeAsS	-0.341	GeS ₂	As		4.704	4.715	4.672		3.018
GeAsSe	-0.420	GeSe ₂	As		4.433	4.316	4.672		-52.600
GeAsTe	-0.350	GeTe	As ₂ Te ₃		4.171	4.245	4.100		7.964
GeSbS	-0.427	GeS ₂	Sb		4.693	4.715	4.380		-39.073
GeSbSe	-0.503	GeSe	Sb ₂ Se ₃		4.420	4.508	4.306		-3.845
GeSbTe	-0.415	GeTe	Sb ₂ Te ₃		4.140	4.245	4.024		4.145
GeBiS	-0.501	GeS	Bi ₂ S ₃		4.723	4.819	4.704		43.545
GeBiSe	-0.578	GeSe	Bi ₂ Se ₃		4.451	4.508	4.398		6.836
GeBiTe	-0.480	GeTe	Bi ₂ Te ₃		4.160	4.245	4.076		7.736
SnAsS	-0.447	SnS ₂	AsS	SnS	4.639	4.650	4.715	4.766	76.645
SnAsSe	-0.534	SnSe	As ₂ Se ₃		4.377	4.455	4.346		28.436
SnAsTe	-0.454	SnTe	As ₂ Te ₃		4.104	4.147	4.100		21.564
SnSbS	-0.566	SnS	Sb ₂ S ₃		4.661	4.766	4.630		43.145
SnSbSe	-0.640	SnSe	Sb ₂ Se ₃		4.386	4.455	4.306		1.573

SnSbTe	-0.532	SnTe	Sb ₂ Te ₃	4.086	4.147	4.024	4.745
SnBiS	-0.656	SnS	Bi ₂ S ₃	4.707	4.766	4.704	30.691
SnBiSe	-0.725	SnSe	Bi ₂ Se ₃	4.427	4.455	4.398	2.255
SnBiTe	-0.603	SnTe	Bi ₂ Te ₃	4.113	4.147	4.076	1.336
PbAsS	-0.515	PbS	As ₂ S ₃	4.631	4.789	4.641	90.727
PbAsSe	-0.613	PbSe	As ₂ Se ₃	4.380	4.514	4.346	57.509
PbAsTe	-0.529	PbTe	As ₂ Te ₃	4.103	4.178	4.100	39.364
PbSbS	-0.663	PbS	Sb ₂ S ₃	4.682	4.789	4.630	34.636
PbSbSe	-0.737	PbSe	Sb ₂ Se ₃	4.407	4.514	4.306	12.645
PbSbTe	-0.616	PbTe	Sb ₂ Te ₃	4.094	4.178	4.024	13.545
PbBiS	-0.764	PbS	Bi ₂ S ₃	4.739	4.789	4.704	11.182
PbBiSe	-0.831	PbSe	Bi ₂ Se ₃	4.457	4.514	4.398	4.327
PbBiTe	-0.692	PbTe	Bi ₂ Te ₃	4.126	4.178	4.076	5.136

Table S3 Calculated lattice parameters of the 14 documented compounds. The available experimental data are listed in parentheses for comparison.³⁻⁸

Compound	a (Å)	c (Å)
Ge ₁ Sb ₂ Te ₄	4.22 (4.25)	41.25 (41.00)
Ge ₁ Bi ₂ Te ₄	4.28 (4.32)	41.83 (41.38)
Sn ₁ Bi ₂ Te ₄	4.36 (4.41)	42.32 (41.51)
Pb ₁ Bi ₂ Te ₄	4.38 (4.44)	42.67 (41.68)
Ge ₁ Sb ₄ Te ₇	4.23 (4.21)	24.06 (23.65)
Ge ₁ Bi ₄ Te ₇	4.30 (4.35)	24.41 (23.93)
Sn ₁ Bi ₄ Te ₇	4.35 (4.39)	24.58 (23.98)
Pb ₁ Bi ₄ Te ₇	4.36 (4.42)	24.70 (24.04)
Pb ₂ Bi ₂ Se ₅	4.20 (4.22)	16.68 (16.42)
Ge ₂ Sb ₂ Te ₅	4.21 (4.25)	17.16 (17.27)
Pb ₂ Sb ₂ Te ₅	4.36 (4.40)	17.79 (17.50)
Pb ₂ Bi ₂ Te ₅	4.42 (4.46)	17.91 (17.52)
Ge ₃ Sb ₂ Te ₆	4.21 (4.25)	61.83 (62.60)
Ge ₃ Bi ₂ Te ₆	4.24 (4.28)	62.48 (62.57)

Table S4 Electronic band gap E_g (eV) using HSE06 functional, mechanical properties including bulk modulus B_H (GPa), shear modulus G_H (GPa) and Young's modulus E (GPa), longitudinal group velocity v_L (ms⁻¹), transverse group velocity v_T (ms⁻¹) and mean group velocity v_m (ms⁻¹) as well as the room-temperature total mode Grüneisen parameter γ and lattice thermal conductivity κ_l (Wm⁻¹K⁻¹) for 70 stable compounds. The calculated bulk modulus and band gap of Ge₂Sb₂Te₅ agree well with experiments (parentheses).^{9,10}

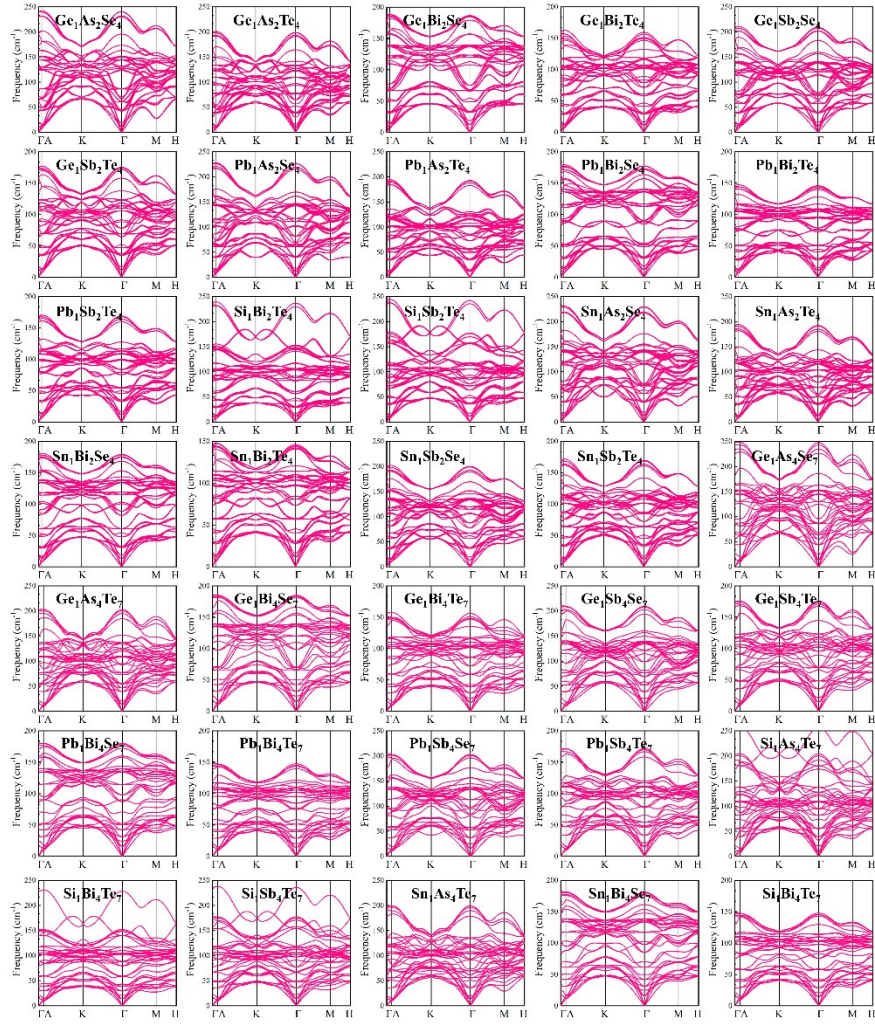
$A_1B_2C_4$	E_g	B_H	G_H	E	v_L	v_T	v_m	γ	κ_l
GeAsSe	0.89	51	39	93	4075	2635	2891	1.79	0.82
GeAsTe	0.75	49	30	75	3448	2188	2407	1.59	1.15
GeBiSe	0.87	36	26	63	2960	1906	2093	1.42	0.92
GeBiTe	1.03	37	24	59	2813	1793	1971	1.33	0.95
GeSbSe	0.55	47	28	69	3429	2164	2382	1.54	1.00
GeSbTe	0.61	44	30	72	3347	2140	2351	1.39	1.16
SiBiTe	0.95	41	28	68	3035	1940	2131	1.41	0.75
SiSbTe	0.45	43	33	78	3529	2281	2503	1.44	0.89
SnAsSe	0.69	48	30	75	3581	2272	2499	1.83	0.63
SnAsTe	0.68	34	29	68	3244	2124	2327	1.62	0.95
SnBiSe	0.76	32	20	49	2602	1652	1817	1.25	1.16
SnBiTe	0.89	37	22	55	2719	1719	1891	1.29	0.88
SnSbSe	0.48	40	23	59	3126	1973	2171	1.45	0.96
SnSbTe	0.57	33	21	52	2821	1791	1970	1.37	0.97
PbAsSe	0.90	51	31	78	3453	2185	2404	1.76	0.66
PbAsTe	0.95	43	23	58	2888	1809	1993	1.55	0.90
PbBiSe	0.90	44	27	67	2914	1847	2032	1.19	1.28
PbBiTe	1.03	38	18	46	2405	1491	1644	1.25	0.91
PbSbTe	0.70	37	22	55	2794	1766	1943	1.36	0.85
$A_1B_4C_7$	E_g	B_H	G_H	E	v_L	v_T	v_m	γ	κ_l
GeAsSe	0.72	46	34	81	3813	2455	2696	1.78	0.83
GeAsTe	0.76	49	31	77	3476	2209	2429	1.52	1.09
GeBiSe	0.75	31	23	55	2729	1758	1930	1.26	1.02
GeBiTe	0.89	33	13	35	2133	1311	1447	1.23	0.85
GeSbSe	0.29	37	27	65	3306	2128	2337	1.43	0.95
GeSbTe	0.46	37	24	59	3028	1926	2117	1.31	0.98
SiAsTe	0.50	43	29	71	3382	2159	2372	1.55	0.97
SiBiTe	0.86	39	23	58	2777	1755	1931	1.29	0.71
SiSbTe	0.37	42	28	69	3305	2109	2318	1.35	0.86
SnAsTe	0.65	40	21	53	2875	1796	1979	1.55	0.87

SnBiSe	0.63	39	24	60	2842	1803	1983	1.13	1.23
SnBiTe	0.76	39	21	54	2671	1678	1848	1.19	0.83
SnSbSe	0.20	44	26	66	3307	2091	2300	1.38	0.91
SnSbTe	0.33	40	10	28	2064	1241	1372	1.29	0.87
PbBiSe	0.72	36	22	55	2653	1682	1849	1.10	1.30
PbBiTe	0.85	32	19	47	2430	1531	1685	1.17	0.83
PbSbSe	0.29	33	23	55	2946	1886	2072	1.37	0.91
PbSbTe	0.42	33	15	39	2400	1486	1639	1.29	0.83
$A_2B_2C_5$	E_g	B_H	G_H	E	ν_L	ν_T	ν_m	$\mathcal{V}$	κ_l
GeAsSe	0.73	52	36	88	3928	2513	2761	1.93	0.75
GeBiSe	0.69	46	34	82	3445	2222	2439	1.87	0.62
GeBiTe	0.92	43	28	69	3075	1957	2152	1.62	0.99
GeSbSe	0.34	50	33	81	3702	2358	2592	1.85	0.89
GeSbTe	0.46(0.50 ⁹)	39(44 ¹⁰)	29	70	3284	2114	2321	1.64	1.20
SiBiTe	0.65	45	31	75	3278	2096	2303	1.69	0.66
SiSbTe	0.17	43	28	70	3374	2152	2365	1.73	0.75
SnAsSe	0.58	43	25	63	3257	2056	2263	2.15	0.37
SnAsTe	0.54	42	25	62	3093	1954	2150	1.80	0.71
SnBiSe	0.46	47	27	68	3104	1956	2153	1.49	1.11
SnBiTe	0.60	36	8	22	1744	1043	1154	1.52	0.92
SnSbSe	0.20	50	28	71	3409	2146	2362	1.66	1.00
SnSbTe	0.36	40	23	59	3009	1898	2089	1.57	0.90
PbAsSe	0.69	38	28	67	3098	1997	2192	2.35	0.28
PbAsTe	0.76	36	26	64	2941	1893	2078	1.55	1.65
PbBiSe	0.80	49	25	65	2848	1780	1961	1.49	1.68
PbBiTe	0.94	37	20	51	2510	1574	1734	1.71	1.00
PbSbS	0.91	44	29	71	3417	2175	2392	2.11	0.60
PbSbSe	0.47	51	28	71	3175	1994	2195	1.43	2.02
PbSbTe	0.60	39	22	56	2765	1743	1919	1.50	1.00
$A_3B_2C_6$	E_g	B_H	G_H	E	ν_L	ν_T	ν_m	$\mathcal{V}$	κ_l
GeAsSe	0.68	22	27	58	3181	2174	2368	1.97	0.78
GeBiTe	0.86	42	32	76	3255	2101	2306	1.77	0.93
GeSbTe	0.50	46	34	81	3539	2279	2503	1.76	1.09
SnAsSe	0.61	44	30	73	3475	2220	2439	2.32	0.29
SnAsTe	0.51	45	27	68	3222	2040	2244	1.78	0.75
SnBiSe	0.42	47	27	67	3114	1962	2159	1.55	1.23
SnBiTe	0.55	22	22	50	2639	1765	1929	1.56	1.08
SnSbSe	0.32	48	10	27	2100	1253	1387	1.68	1.08

SnSbTe	0.42	40	25	63	3100	1970	2166	1.61	1.04
PbAsTe	0.70	47	27	68	3002	1895	2085	1.78	0.67
PbBiSe	0.83	47	29	72	2981	1887	2076	1.43	1.25
PbSbSe	0.58	51	30	75	3206	2024	2227	1.63	0.83
PbSbTe	0.70	40	24	60	2826	1789	1968	1.59	0.81

Table S5 The calculated average $-IpCOHP$ (eV) and bond length ($\text{\AA}$) of different atomic interactions for four GST compounds.

Compound	$-IpCOHP$ (eV)			Bond length ($\text{\AA}$)		
	Ge-Te	Sb-Te	Te-Te	Ge-Te	Sb-Te	Te-Te
$\text{Ge}_1\text{Sb}_2\text{Te}_4$	1.774	1.658	0.146	2.958	3.071	3.830
$\text{Ge}_1\text{Sb}_4\text{Te}_7$	1.772	1.660	0.154	2.958	3.070	3.820
$\text{Ge}_2\text{Sb}_2\text{Te}_5$	1.780	1.659	0.148	2.957	3.071	3.830
$\text{Ge}_3\text{Sb}_2\text{Te}_6$	1.780	1.670	0.140	2.957	3.071	3.830



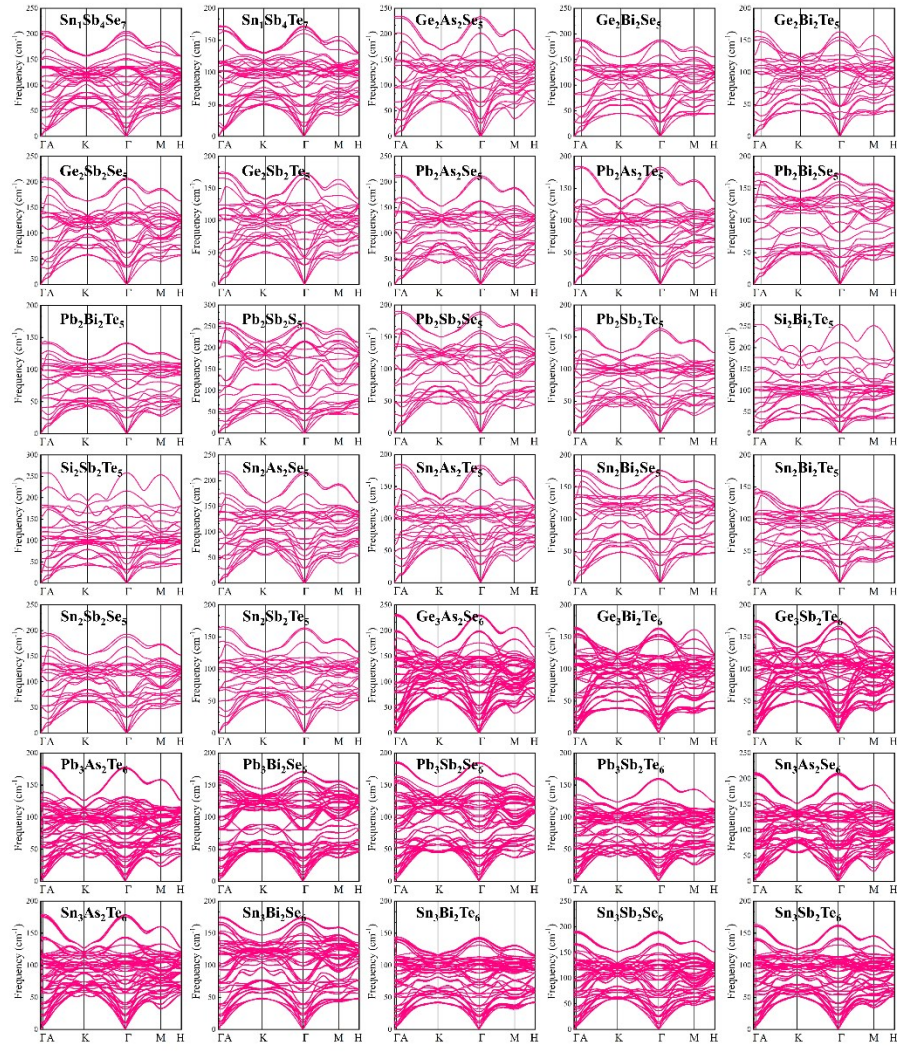


Fig. S1 Phonon dispersions of all 70 stable compounds.

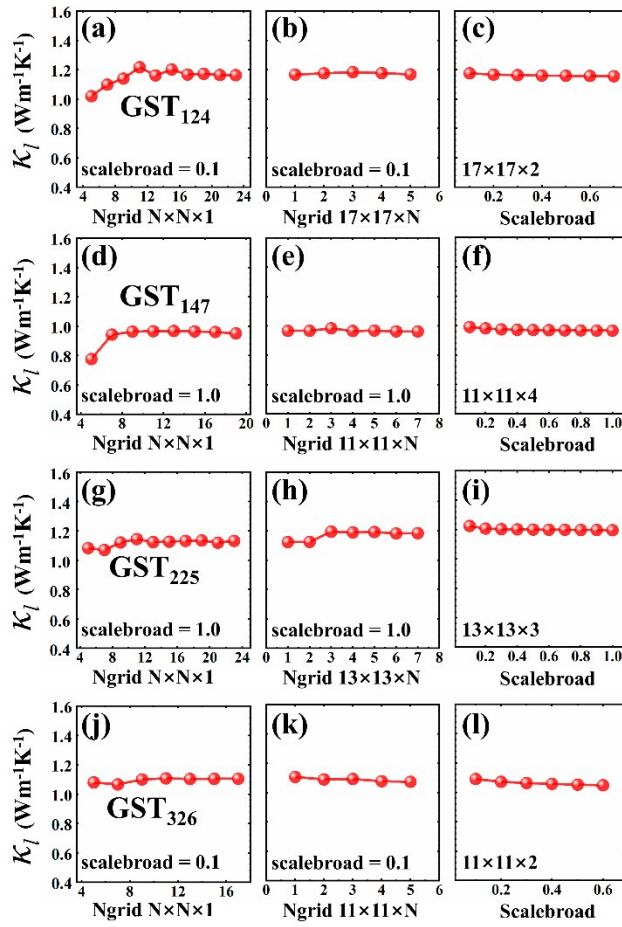


Fig. S2 The convergence tests of κ_l with respect to the q-point grid and scalebroad for (a-c) $\text{Ge}_1\text{Sb}_2\text{Te}_4$, (d-f) $\text{Ge}_1\text{Sb}_4\text{Te}_7$, (g-i) $\text{Ge}_2\text{Sb}_2\text{Te}_5$ and (j-l) $\text{Ge}_3\text{Sb}_2\text{Te}_6$, respectively.

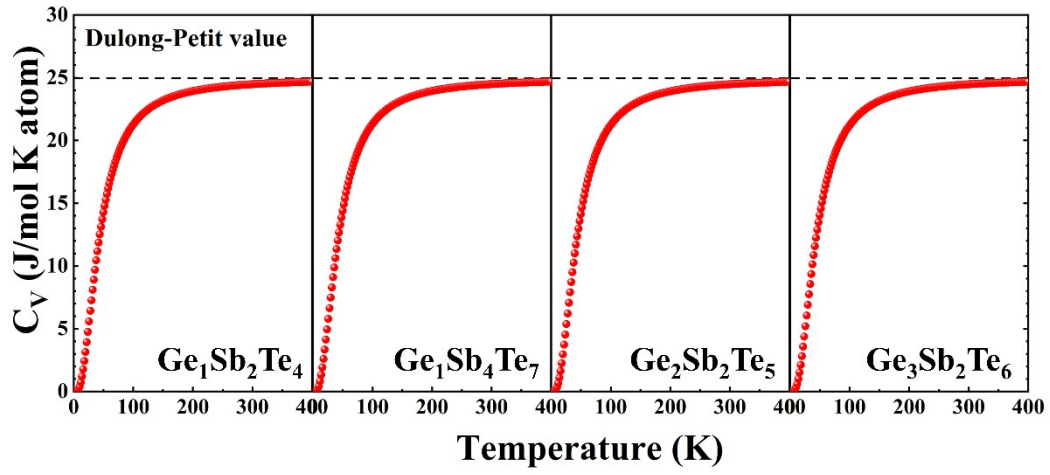


Fig. S3 Calculated heat capacity at constant volume of four GST compounds as a function of temperature.

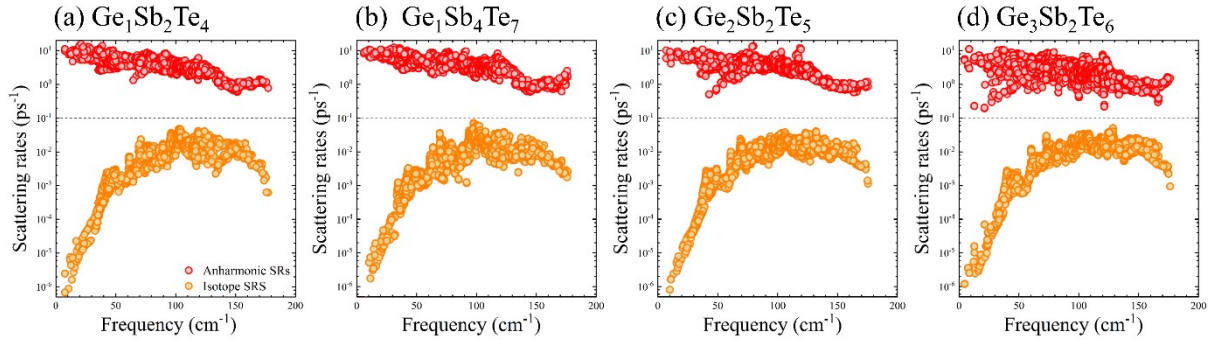


Fig. S4 Anharmonic scattering rates (SRs) and isotope SRs of four GST compounds as a function of phonon frequency.

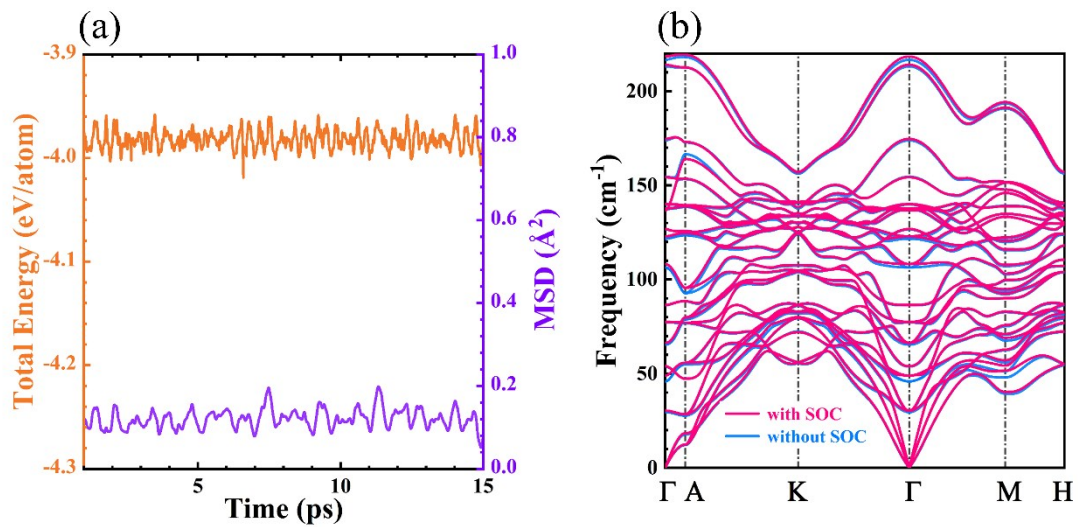


Fig. S5 (a) Evolution of total energy and average atomic mean-square displacement of $\text{Sn}_2\text{As}_2\text{Se}_5$ as a function of time in AIMD simulation. (b) Phonon dispersion curves of $\text{Sn}_2\text{As}_2\text{Se}_5$ with SOC and without SOC.

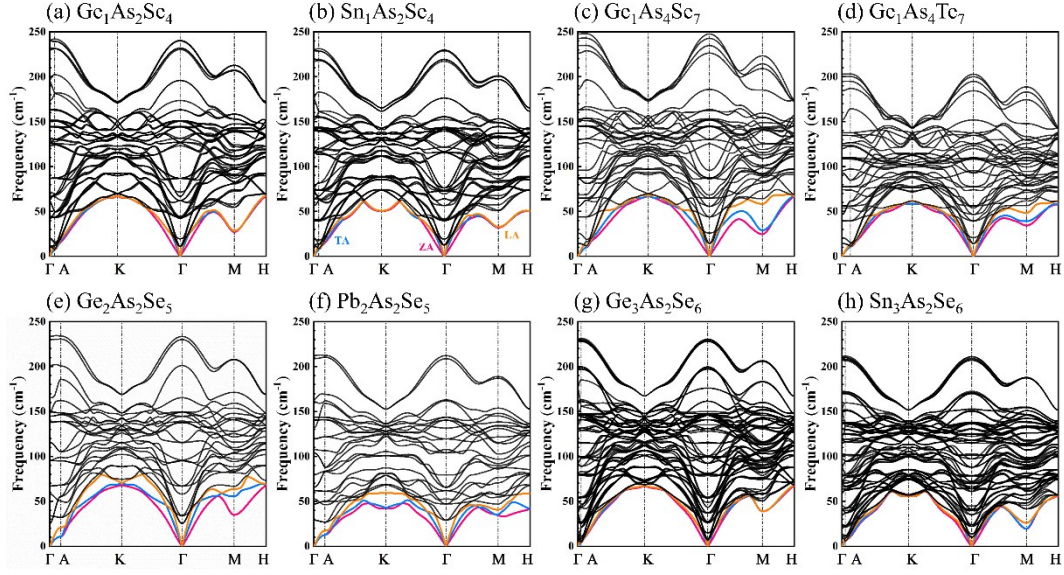


Fig. S6 Phonon dispersion curves of some low- κ_l compounds. The red, green and orange colors denote the acoustic branches of ZA, TA and LA, respectively.

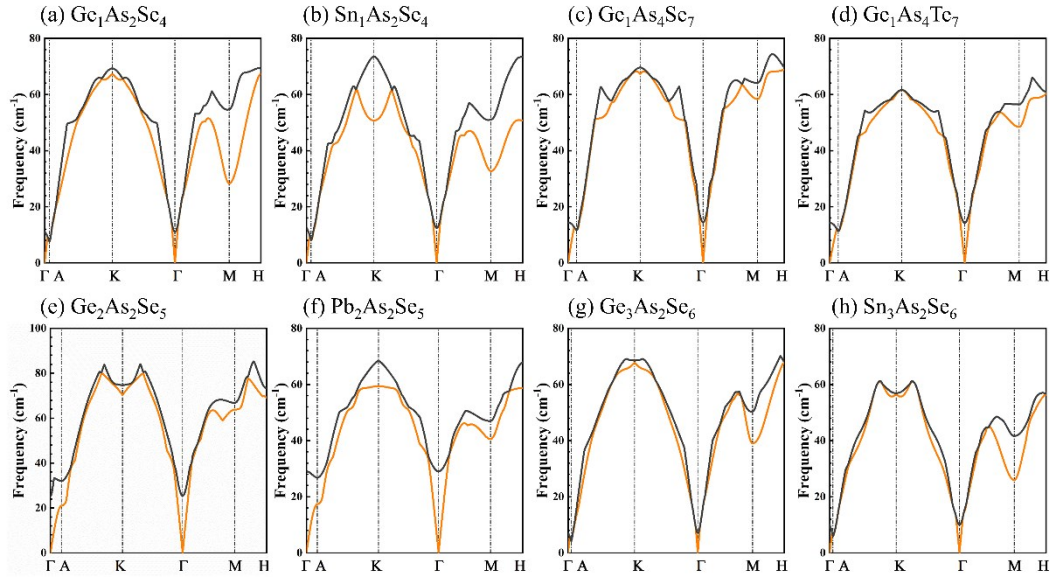


Fig. S7 Illustration of avoided-crossing between low-lying optic phonons and acoustic modes.

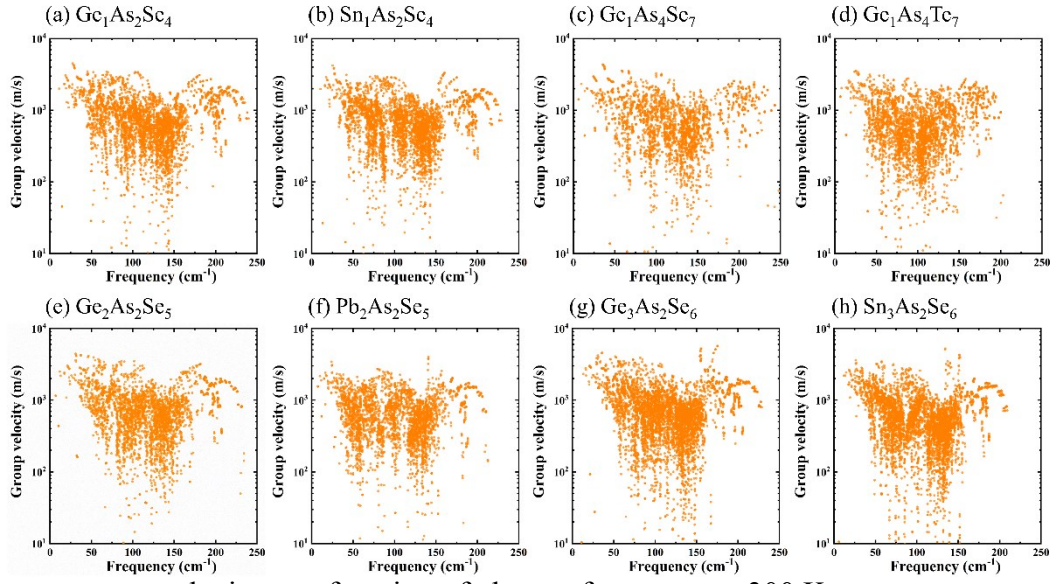


Fig. S8 Phonon group velocity as a function of phonon frequency at 300 K.

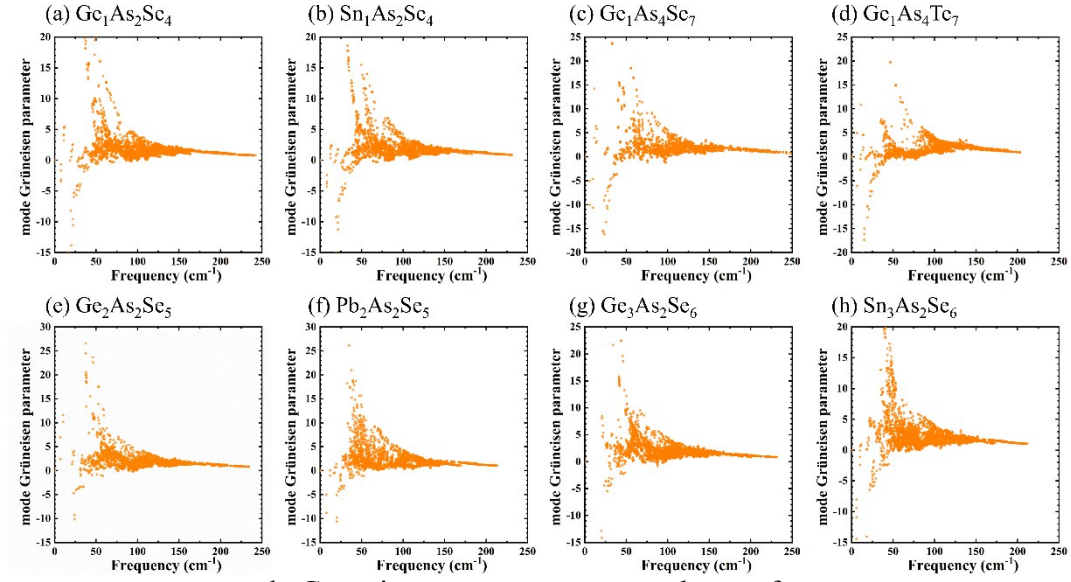


Fig. S9 Room-temperature mode Grüneisen parameter versus phonon frequency.

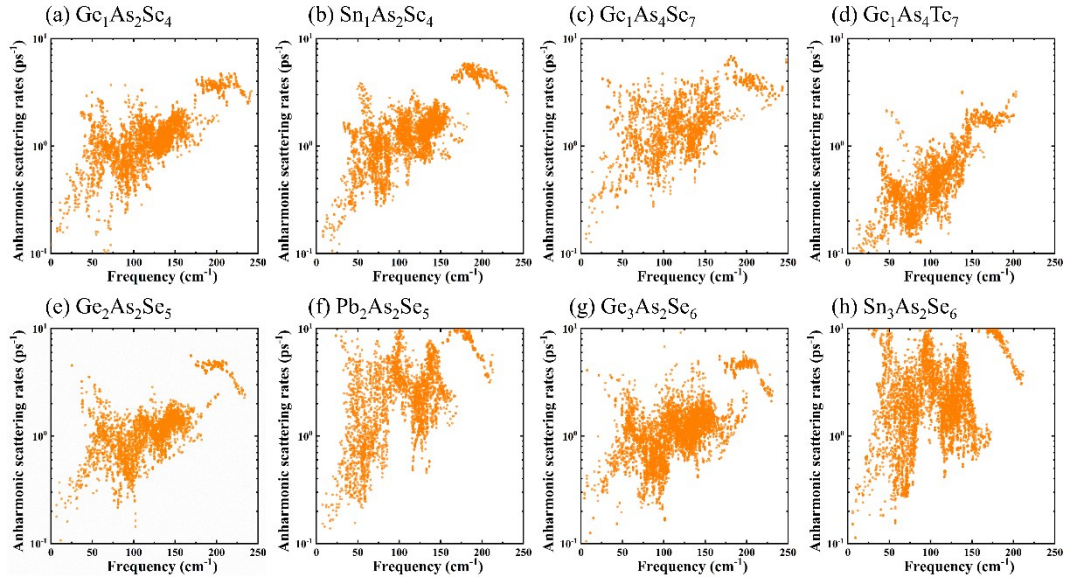


Fig. S10 Anharmonic phonon scattering rates at 300 K vs phonon frequency.

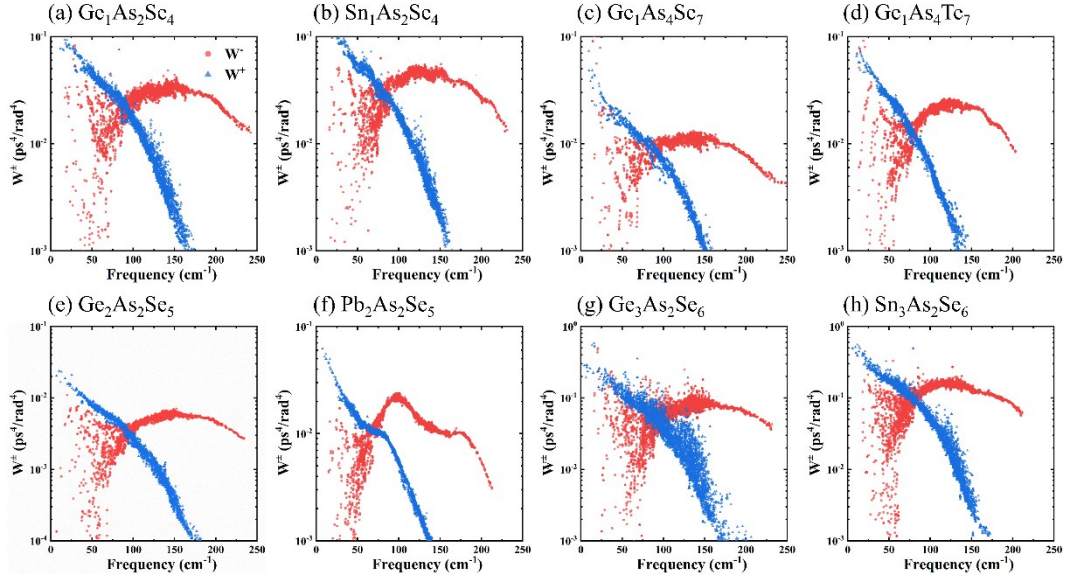


Fig. S11 Weighted phase space at 300K vs phonon frequency.

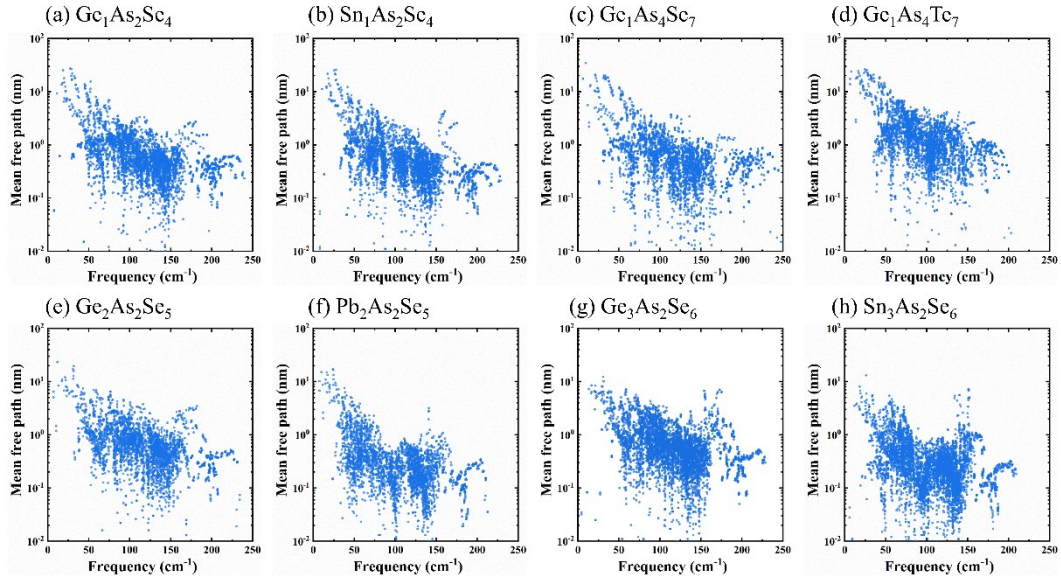


Fig. S12 Phonon mean free path at 300K vs phonon frequency.

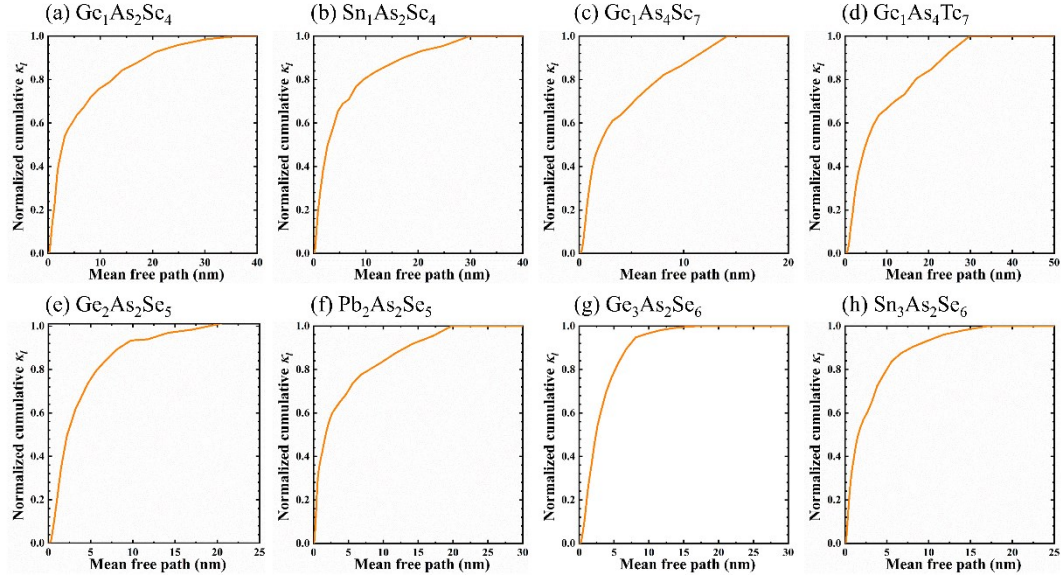


Fig. S13 Normalized cumulative room-temperature thermal conductivity with respect to phonon MFP.

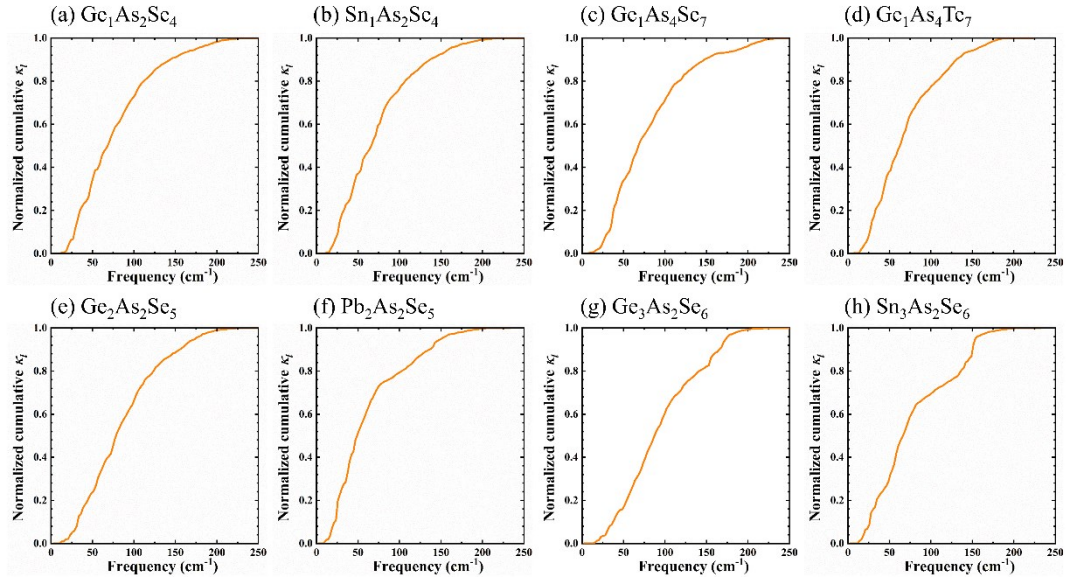


Fig. S14 Normalized cumulative room-temperature thermal conductivity with respect to phonon frequency.

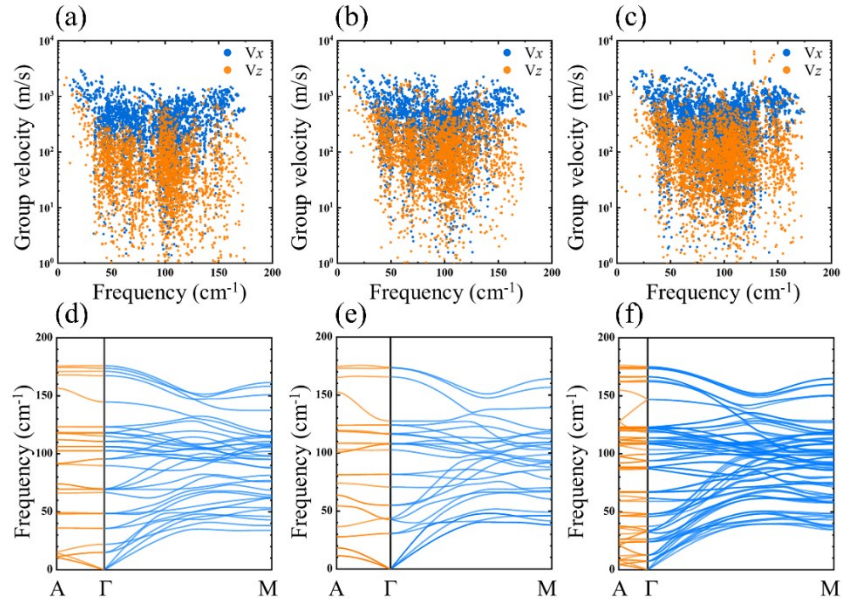


Fig. S15 Room-temperature phonon group velocities along the a -axis (v_x) and the c -axis (v_z) as well as phonon dispersion curves of (a, d) $\text{Ge}_1\text{Sb}_4\text{Te}_7$, (b, e) $\text{Ge}_2\text{Sb}_2\text{Te}_5$ and (c, f) $\text{Ge}_3\text{Sb}_2\text{Te}_6$.

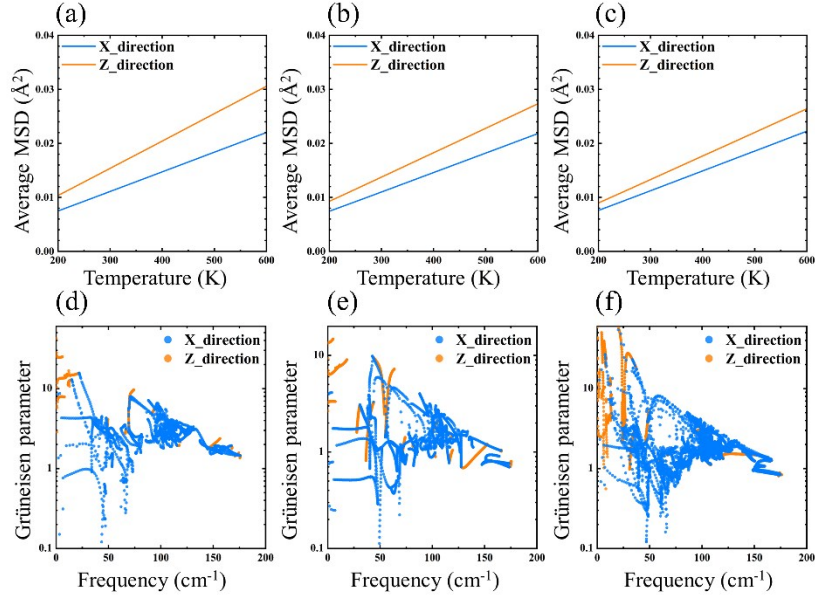


Fig. S16 Temperature-dependent averaged atomic mean-square displacements and phonon Grüneisen parameters of (a, d) $\text{Ge}_1\text{Sb}_4\text{Te}_7$, (b, e) $\text{Ge}_2\text{Sb}_2\text{Te}_5$ and (c, f) $\text{Ge}_3\text{Sb}_2\text{Te}_6$.

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