

**Supplementary Information:**

**Auxetic, Flexible, and Strain-Tunable**

**Two-Dimensional th-AlN with Anisotropic High**

**Carrier Mobility for Photocatalytic Visible Light**

**Water Splitting**

Mehmet Emin Kilic\* and Kwang-Ryeol Lee\*

*Computational Science Center, Korea Institute of Science and Technology, Seoul 136-791,*  
*Republic of Korea*

E-mail: mekilic@kist.re.kr; krlee@kist.re.kr

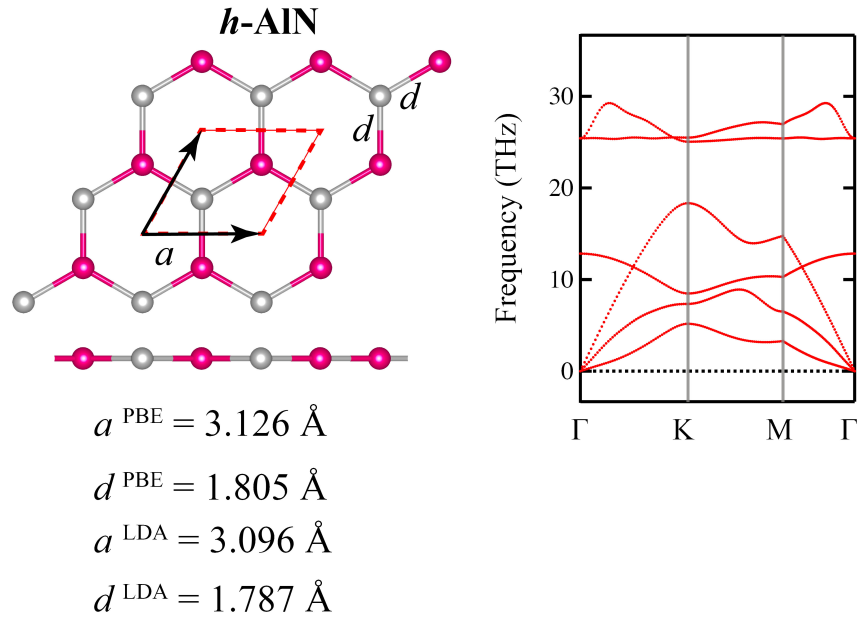


Fig. S1: Optimized atomic configurations (left panel) and phonon band structure (right panel) of hexagonal AlN (*h*-AlN). The value of lattice constant  $a$  and bond length  $d$  obtained from the LDA and PBE functional level is depicted in the figure.

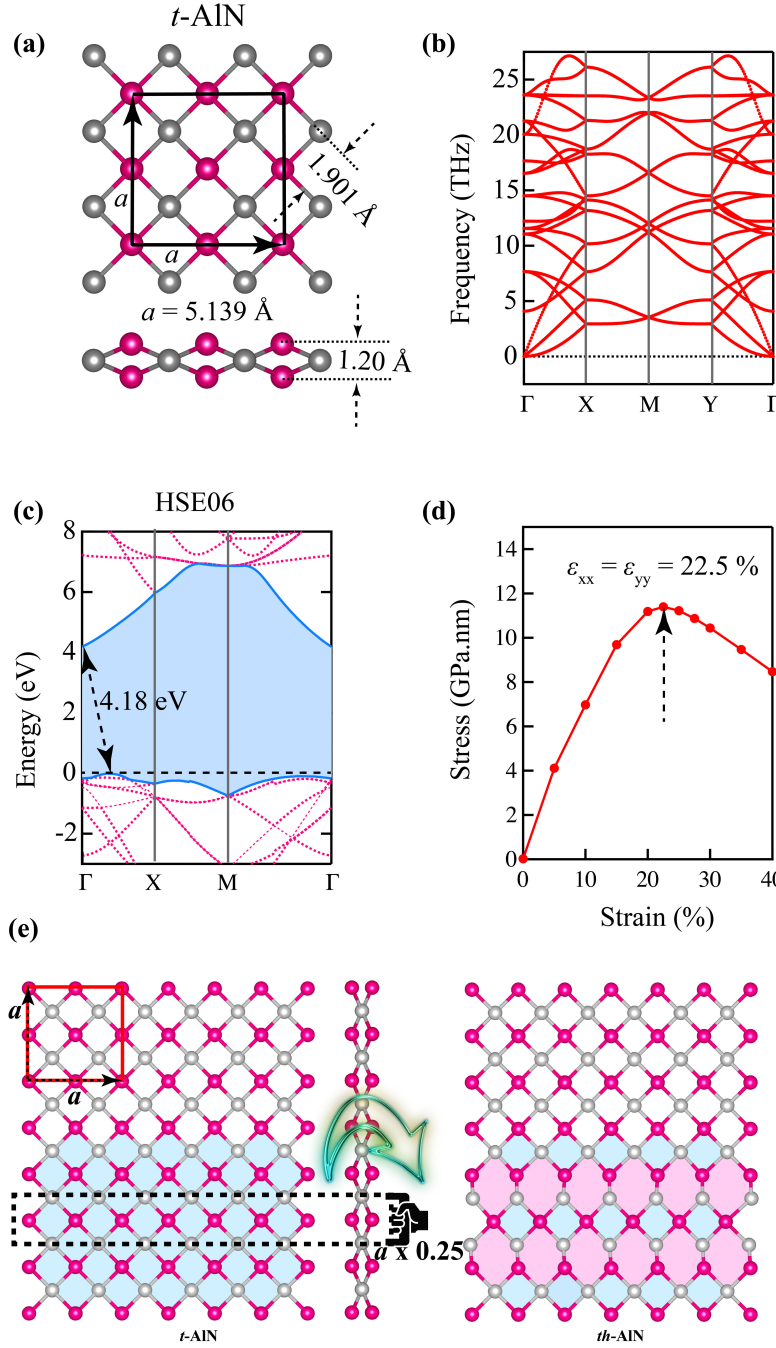


Fig. S2: (a) Optimized atomic structure, (b) phonon band structure, (c) electronic band structure obtained from the HSE06 hybrid functional level, and (d) stress-strain relation for tetragonal aluminum nitride (named as *t*-AlN). From the electronic band structure, the Fermi level energy is set to zero (depicted by the black dashed line). The electronic band gap energy of *th*-AlN is found to be 4.18 eV. Silver and pink spheres represent Al and N atoms, respectively. According to the phonon band dispersions, all the phonon modes are positive frequencies, thus, confirming its dynamic stability. (e) Deriving *th*-AlN from 2D *t*-AlN.

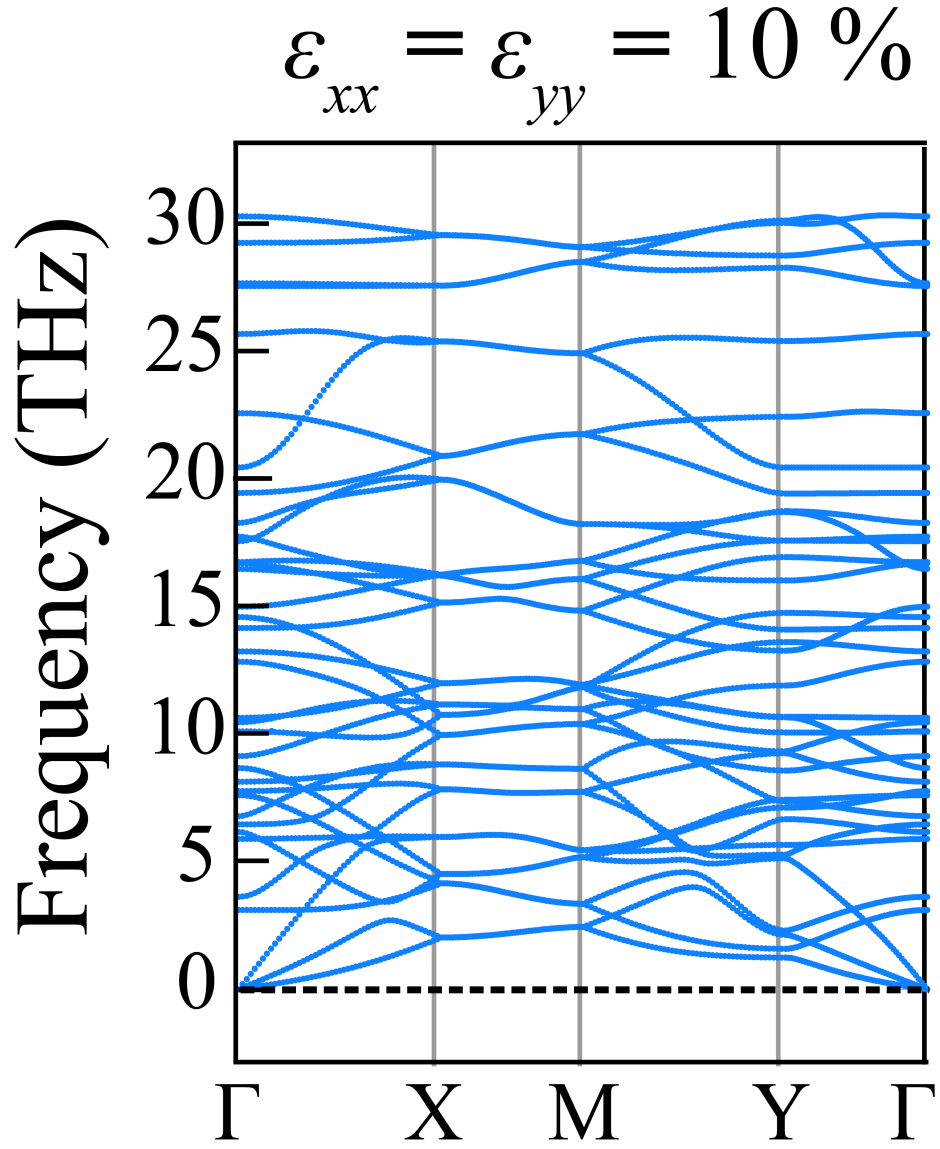


Fig. S3: Phonon dispersion curves of *th*-AlN when subjected to 10% equi-biaxial tensile strain.

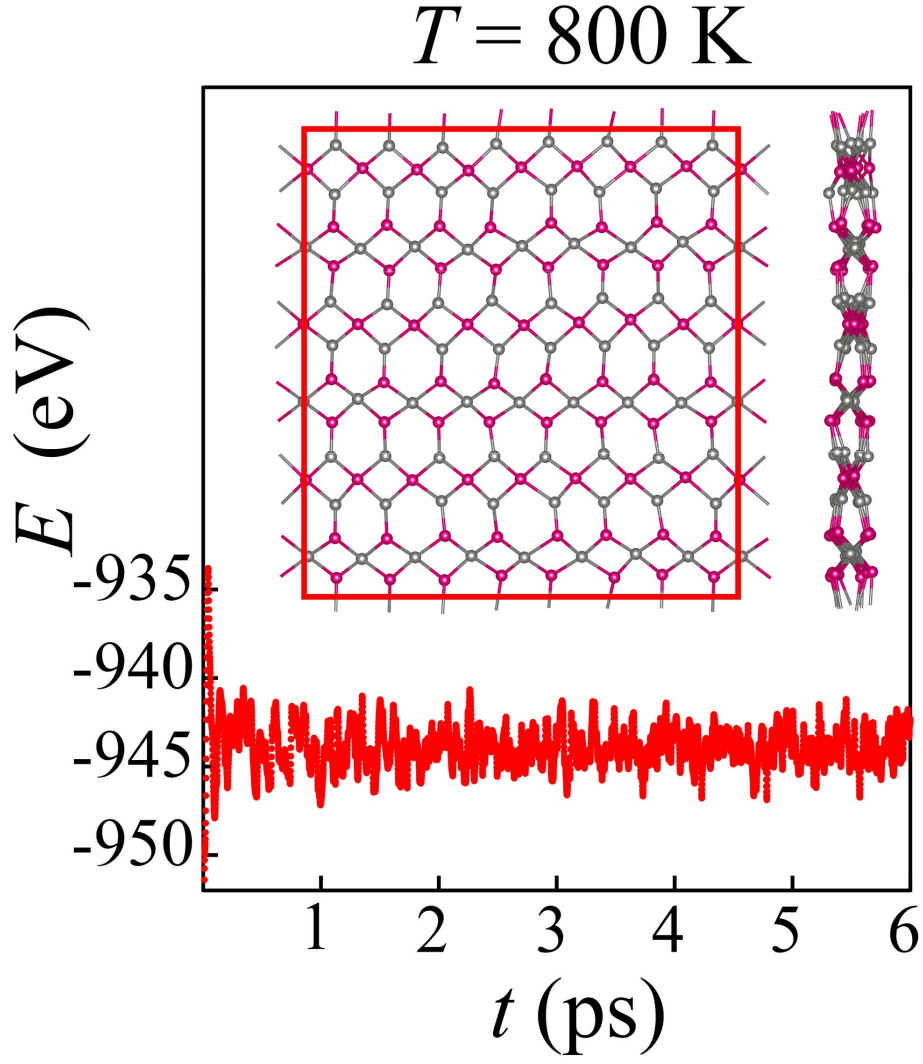


Fig. S4: Variation of total potential energy of *th*-AlN during the AIMD simulations at  $T = 800 \text{ K}$ . The inset is snapshot of the atomic structures at the end of simulation. The silver and pink balls represent Al and N atoms, respectively.

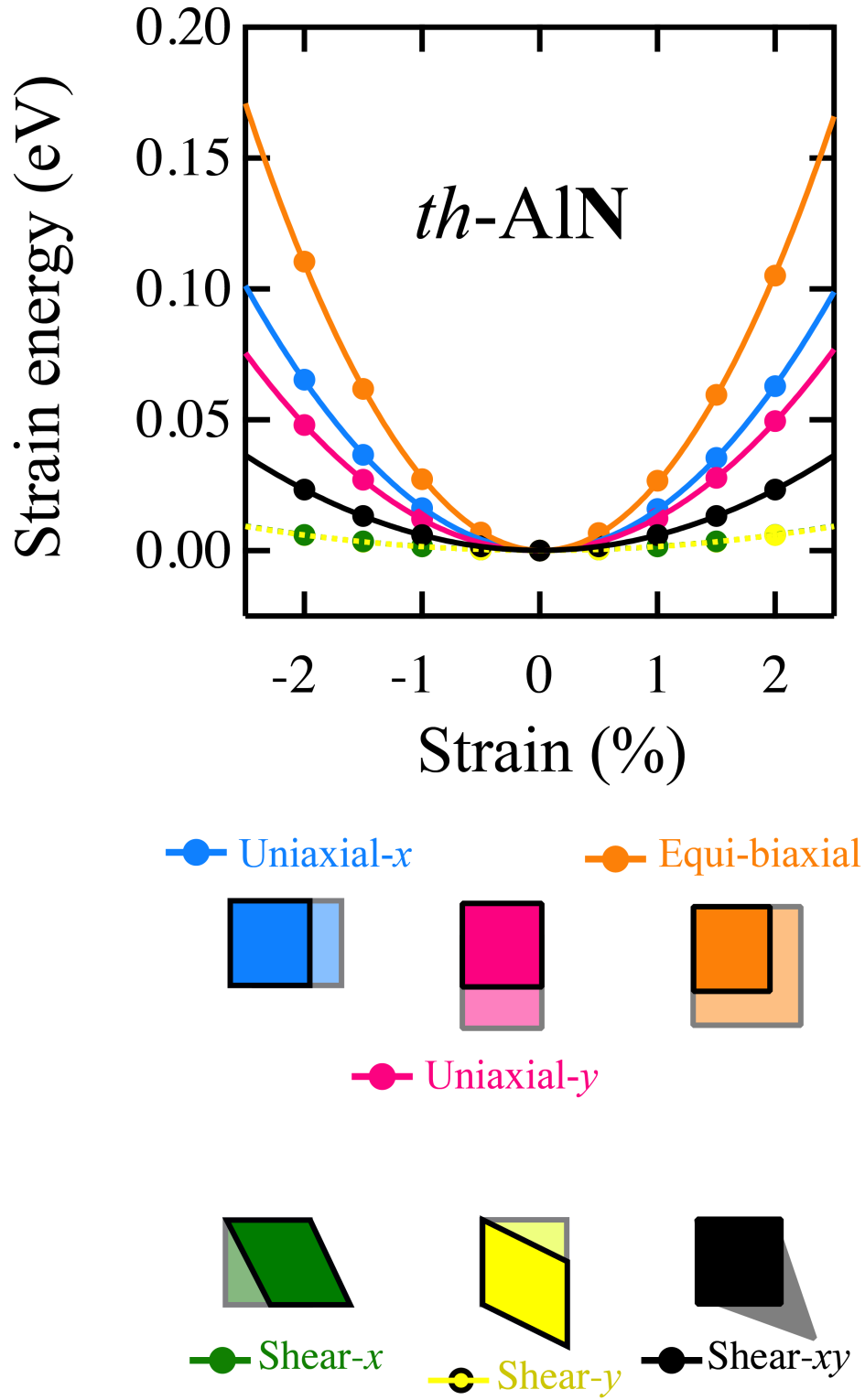


Fig. S5: Calculated strain energy of *th*-AlN with respect to various applied strains: uniaxial strain along the *x*- and *y*-directions, equi-biaxial strain, and shear strains.

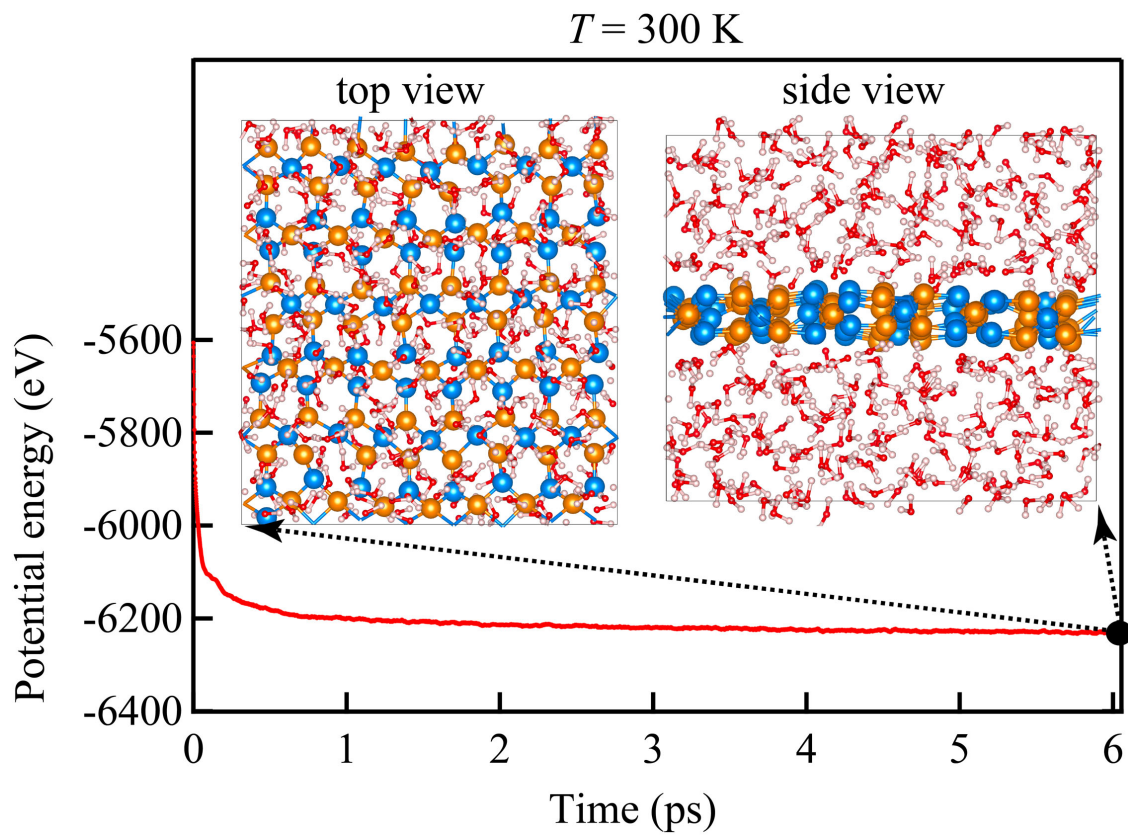


Fig. S6: Variation of total potential energy of *th*-AlN in the liquid water during the AIMD simulations at  $T = 300 \text{ K}$ . The inset is snapshot of the atomic structures at the end of simulation. The blue, orange, red, and white balls represent Al, N, O, and H atoms, respectively.

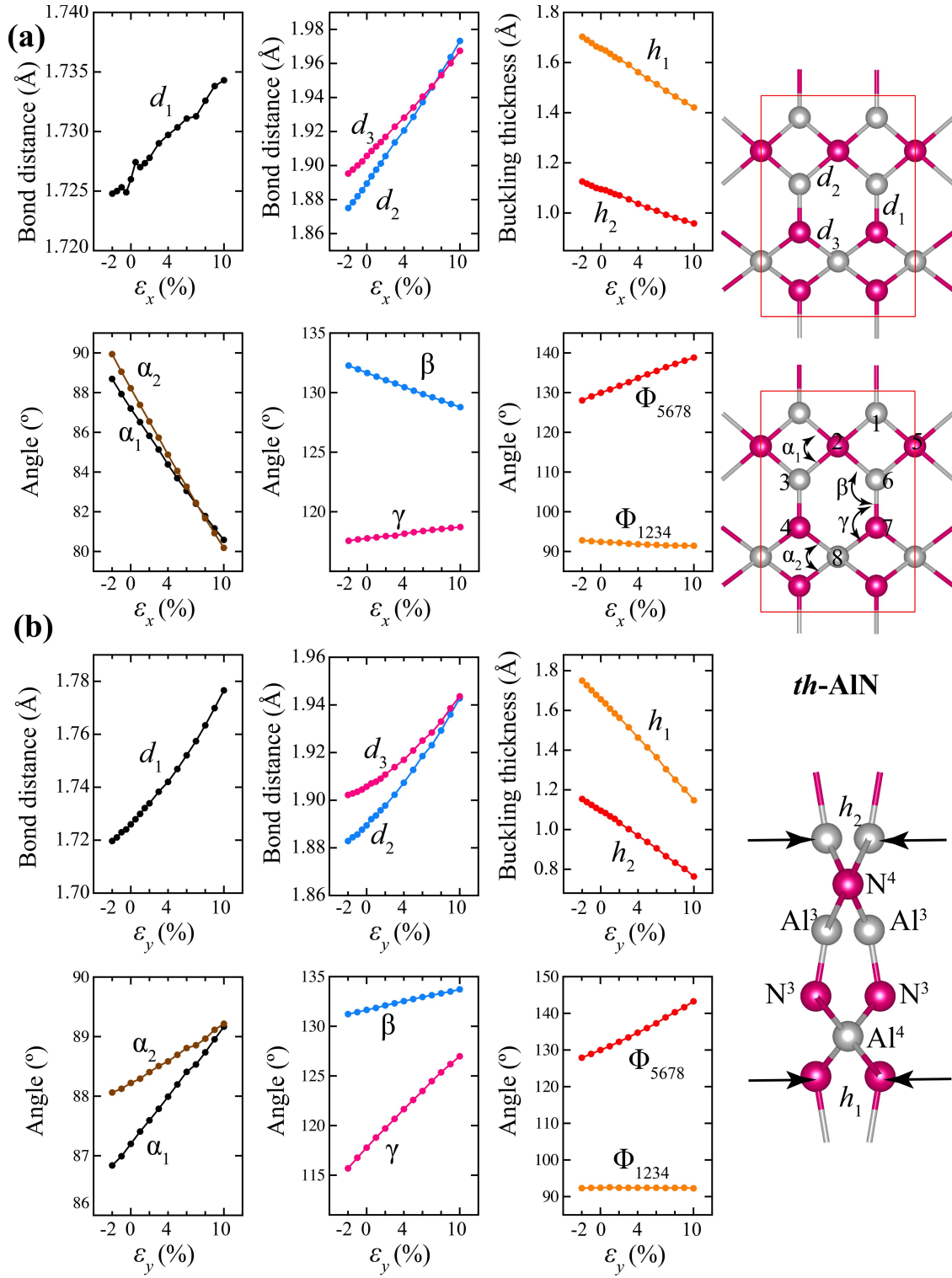


Fig. S7: The variation of bond length  $d_1$ ,  $d_2$ , and  $d_3$ , buckling height  $h_1$  and  $h_2$ , bond angles, and dihedral angles for *th*-AlN with respect to uniaxial- $x$  strain ( $\epsilon_x$ ) and uniaxial- $y$  strain ( $\epsilon_y$ ).

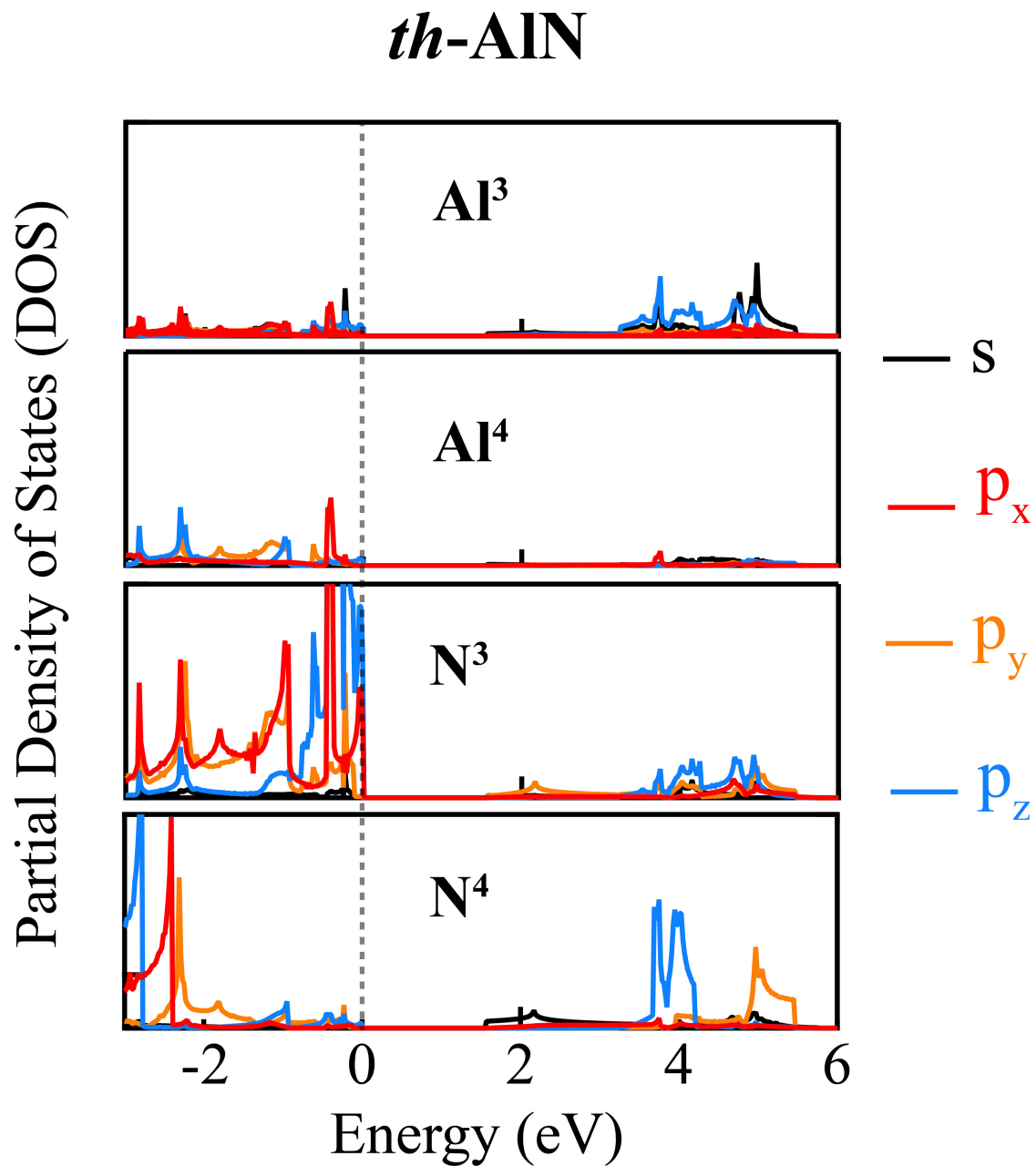


Fig. S8: Electronic density of states (DOS) of *th*-AlN. Here, black, pink, orange, and sky blue represent  $s$ ,  $p_x$ ,  $p_y$ , and  $p_z$  orbitals, respectively.

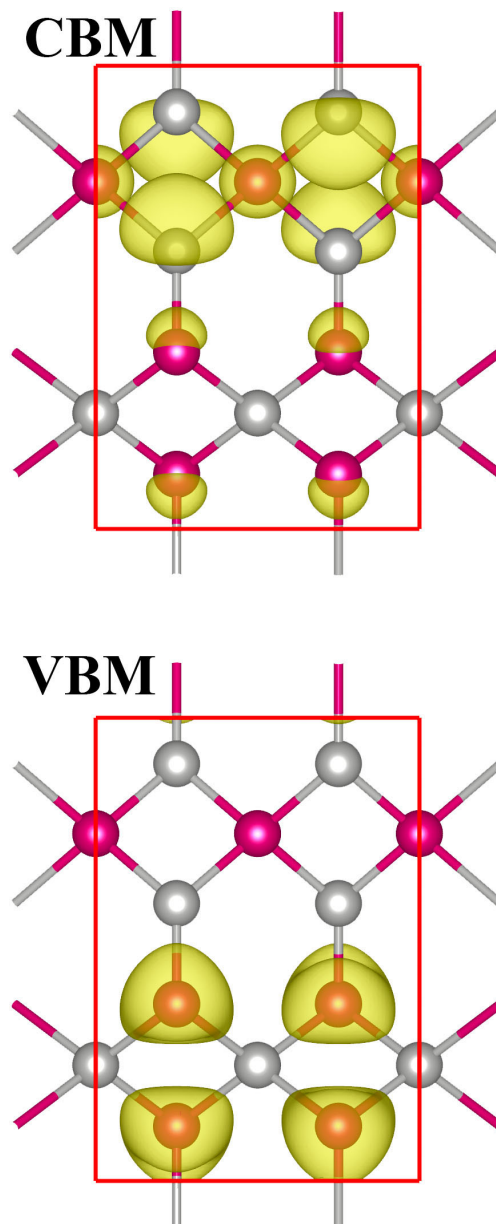


Fig. S9: Charge density of band edges (CBM and VBM) of *th*-AlN. Here, iso-surface of the charge density (yellow color lobes) is  $0.005 \text{ e}/\text{\AA}^3$ . The silver and pink balls represent Al and N atoms, respectively.

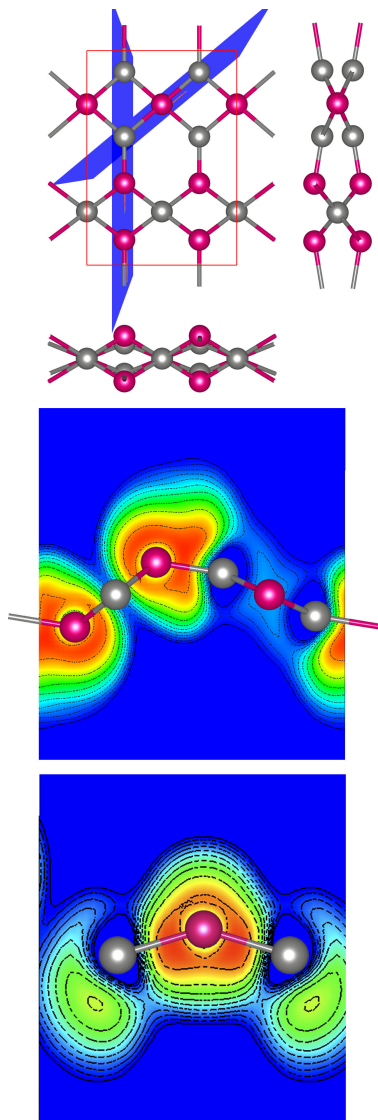


Fig. S10: Electron local function (ELF) of *th*-AlN. The specific 2D-slice projections are chosen to show the bonds between 3-fold coordinated Al and 4-fold coordinated N atoms ( $\text{Al}^3\text{--N}^4$ ) as depicted in the middle panel and between 3-fold coordinated Al and N atoms ( $\text{Al}^3\text{--N}^3$ ) as depicted in the lower panel. The ELF is dimensionless, and has a range from 0 (in blue color) to 1 (in red color). ELF=1 means highly localized and bounded electrons, while ELF=0 means lack of electron.

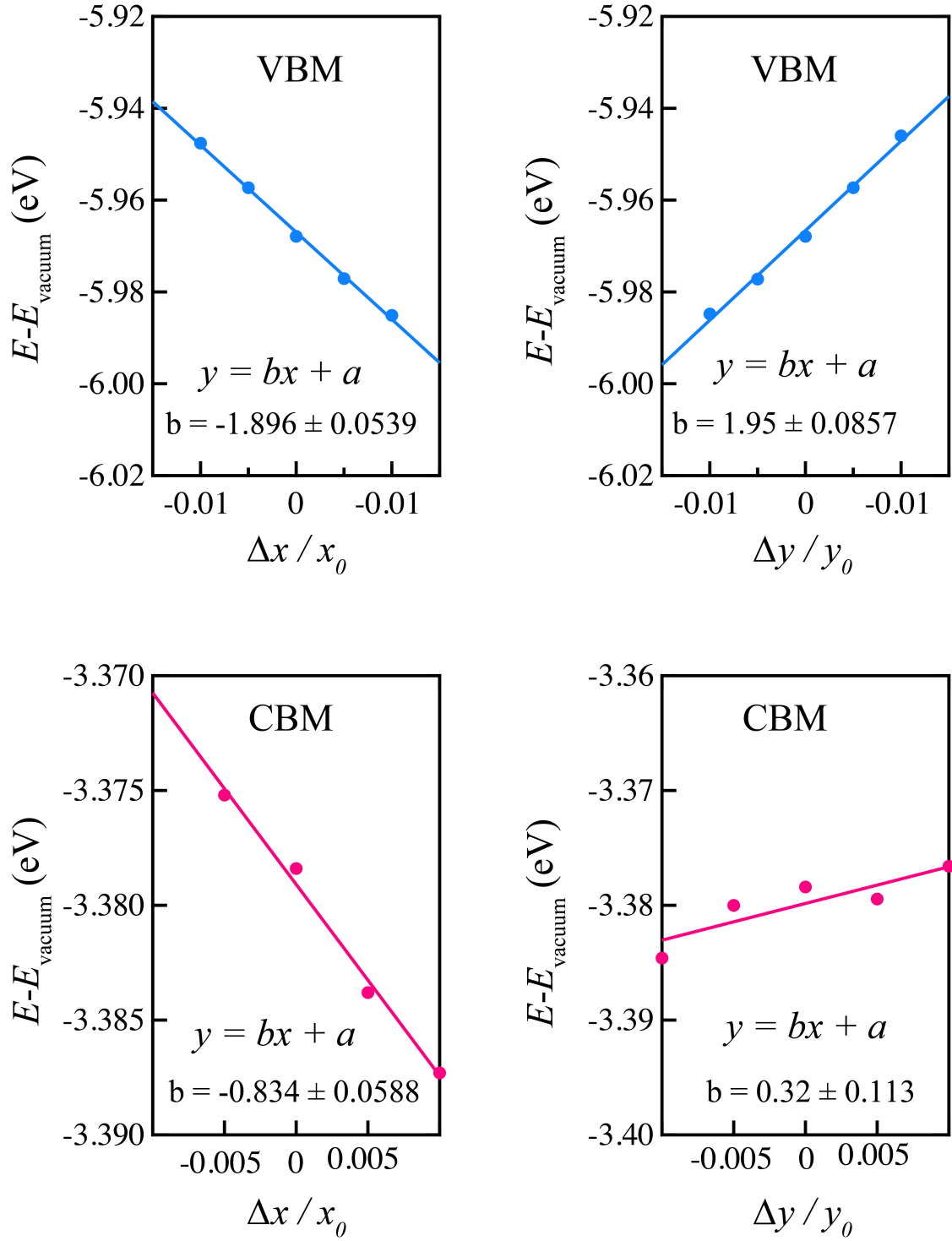


Fig. S11: Dependence of total energy (calculated by the HSE06 functional) of band edges (CBM and VBM positions) *versus* the vacuum level as a function of applied uniaxial strains along the transport direction for *th*-AlN.