Supporting information

Revealing crystal structures and relative dielectric constants of fluorinated silicon oxides[†]

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I Prediction of Structural Connectivity of SiOF compounds

In general, connectivity of a structure is determined by the central atoms¹: in a typical 1D-connectivity structure, a central atom is coordinated with two ligands that are shared with other central atoms, leading to the formation of a chain with infinite length; 2D-connectivity structures are often obtained with three or more shared ligands coordinating around a central atom and the elementary motif expands in two directions to form a layer; with central atoms of four or more shared ligands, 3D-connectivity structures can be easily constructed. There are also a few 3D-connectivity structures (e.g., $P3_121$ -B₂O₃) in which central atoms only have three shared ligands.



Figure S1. A prediction of structural connectivity of SiOF compounds *vs.* F concentration; (a) 3D-Si₂O₂ (b) 3D-Si₂O₃F₂ (c) 2D-Si₂O₃F₂ (d) 1D-SiOF₂ (e) 0D-Si₂OF₆ and (f) 0D-SiF₄

According to these guidelines, structural connectivity of SiOF as a function of F concentration can be roughly predicted. As shown in Figure S1(a), if we have a central atom (Si) and four shared ligands (O), we can have 3D-connectivity structures - this is the case of SiO₂. If we have three shared ligands (O) and one unshared ligand (F), we also can have 3D-connectivity structures (but also an increased chance of 2D-connectivity structures). Both 2- and 3-D connectivity are found for Si₂O₃F₂, as shown in Figure S1(b) & 1(c). If we have two shared ligands (O) and two unshared

(F), we cannot have 3D-connected structures, but will have 1D-connected structures. This is the case of SiOF₂, as shown in Figure S1 (d). If we have no more than one shared ligand (O), then we can only have 0D structures. This is the cases of Si_2OF_6 and SiF_4 , as shown in Figure S1(e)&(f). Based on these simple geometric considerations we consider it more likely to find 3D-connectivity SiOF structures in the F concentration range (in at. %) from 0 (SiO₂) to 28.57 (Si₂O₃F₂).

II Dynamical stability of thermodynamically stable SiOF compounds



Figure S2 Phonon dispersion curves computed for three thermodynamically stable SiOF compounds; (a) *Aba*2-Si₂O₃F₂ (b) *P*2₁/*m*-SiOF2 and (c) *Cmca*-Si₂OF₆

III Thermodynamical stability of SiOF compounds



Figure S3 Thermodynamical convex hull constructed for SiO2-SiF4 system at zero temperature and ambient pressure; the stable structures of SiO₂ ($P3_121$) and SiF₄ (*I*-43*m*) were used.

Common d	C	ΔH	$H = E_{\text{hull}}$		CD true	Structure
Compound Spg		(meV/f.u.)	(meV/f.u.)	(%)	СР-туре	Connectivity
SiO ₂	I-42d	0	0	0	SiO ₄	3D
$\mathrm{Si}_8\mathrm{O}_{15}\mathrm{F}_2$	<i>P</i> 1	58.2	68.2	8	SiO ₄ +SiO ₃ F	3D
$\mathrm{Si}_6\mathrm{O}_{11}\mathrm{F}_2$	<i>P</i> -1	2.6	15.9	10.53	SiO ₄ +SiO ₃ F	3D
$Si_5O_9F_2$	<i>P</i> 1	-7.2	8.8	12.50	SiO ₄ +SiO ₃ F	3D
$Si_4O_7F_2$	<i>P</i> 1	-5.1	14.8	15.38	SiO ₄ +SiO ₃ F	3D
$Si_3O_5F_2$	<i>P</i> 1	-3.1	23.4	20	SiO ₄ +SiO ₃ F	3D
$\mathrm{Si}_5\mathrm{O}_8\mathrm{F}_4$	<i>P</i> 1	-13.9	17.9	23.53	SiO ₄ +SiO ₃ F	3D
$Si_2O_3F_2$	Aba2	-39.8	0	28.57	SiO ₃ F	2D
Si ₃ O ₄ F ₄	<i>P</i> 1	-30.8	10.1	36.36	SiO ₃ F+SiO ₂ F ₂	2D
$Si_5O_6F_8$	<i>P</i> 1	-20.8	21.1	42.11	SiO ₃ F+SiO ₂ F ₂	2D
$Si_2O_2F_4$	$P2_{1}/m$	-43.3	0	50	SiO_2F_2	1D
$\mathrm{Si}_5\mathrm{O}_4\mathrm{F}_{12}$	<i>P</i> -43 <i>m</i>	-9.1	26.8	57.14	SiO ₂ F ₂ +SiOF ₃	0D
$Si_3O_2F_8$	<i>C</i> 2	-22.7	8.3	61.54	SiO ₂ F ₂ +SiOF ₃	0D
Si ₂ OF ₆	Cmca	-24.9	0	66.67	SiOF ₃	0D
SiF ₄	I-43m	0	0	80	SiF_4	0D

Table S1. Detailed information of predicted thermodynamically stable and metastable SiOF structures; the lowest energy structures at a given composition are listed.

IV Crystal structure and dynamical stability of Cc-Si₂O₃F₂



Figure S4 Crystal structure (a) and phonon dispersion curve of Cc-Si₂O₃F₂

V Test of the semi-empirical model

Table S2 The computed and predicted dielectric constants for seven more predicted metastable SiOF structures; Noting that these seven metastable SiOF compounds are the second lowest energy structures in their compositions.

Compound	Spg	ΔH	E_{hull}	V	CP-type	k	k
		(meV/atom)	(meV/atom)	(A ³)		(Predicted)	(DFPT)
$Si_6O_{11}F_2$	<i>P</i> -1	2.8	6.9	47.30	SiO ₄ +SiO ₃ F	3.91	3.84
$Si_5O_9F_2$	<i>C</i> 2	1.7	6.6	48.49	SiO ₄ +SiO ₃ F	3.81	3.84
$\mathrm{Si}_4\mathrm{O}_7\mathrm{F}_2$	<i>C</i> 2	-0.9	5.1	50.35	SiO ₄ +SiO ₃ F	3.68	3.79
$Si_3O_5F_2$	Ibam	3.2	11.0	56.45	SiO ₄ +SiO ₃ F	3.32	3.27
$\mathrm{Si}_5\mathrm{O}_8\mathrm{F}_4$	<i>P</i> 1	-3.0	6.2	54.70	SiO ₄ +SiO ₃ F	3.38	3.43
$Si_2O_3F_2$	Cm	-9.8	1.5	54.82	SiO ₃ F	3.34	3.58
SiOF ₂	Ama2	-6.8	3.9	68.17	SiO_2F_2	2.81	2.81

VI The effect of $E_{\rm g}$ on $\varepsilon_{\rm e}$ of SiOF compounds



Figure S5 Effect of $E_{\rm g}$ on $\varepsilon_{\rm e}$ of SiOF compounds

VII Phonon behaviors of three stable SiOF compounds

Table S3 Lattice contributions to $\varepsilon_{\rm L}$	of three SiOF compound	ds along with SiO	and SiF ₄ : only
	of three biof compound	as along with bio	$\frac{1}{2}$ und $\frac{1}{2}$ $\frac{1}{4}$, $\frac{1}{2}$

I-42d-SiO ₂		Aba2-Si ₂ O ₃ F ₂		$P2_1/m$ -SiOF ₂		<i>Cmca</i> -Si ₂ OF ₆		I-43m-SiF ₄	
$(\omega < 500 \text{ cm}^{-1})$									
$\omega(\text{cm}^{-1})$	$arepsilon_{ m L}$	$\omega(\text{cm}^{-1})$	$\varepsilon_{\rm L}$	$\omega(\text{cm}^{-1})$	$arepsilon_{ m L}$	$\omega(\text{cm}^{-1})$	$arepsilon_{ m L}$	$\omega(\text{cm}^{-1})$	\mathcal{E}_{L}
422	0.40	211	0.04	284	0.03	363	0.12	351	0.30
442	0.57	272	0.06	366	0.35	373	0.12		
		409	0.43	397	0.13	380	0.08		
		427	0.16	403	0.09	384	0.03		
SUM	0.85	SUM	0.69	SUM	0.60	SUM	0.41	SUM	0.30
				$(\omega > 500)$	cm ⁻¹)				
752	0.07	874	0.09	818	0.05	935	0.06	947	0.17
1047	0.21	1092	0.17	915	0.08	952	0.04		
1055	0.39	1104	0.16	1134	0.14	1193	0.11		
				1204	0.04				
SUM	0.67	SUM	0.42	SUM	0.31	SUM	0.21	SUM	0.17

those higher than	0.03	are	listed.
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References

1 B. Kesanli and W. Lin, Coord. Chem. Rev., 2003, 246(1-2), 305-326.