# Intrinsic Valley Polarization in 2D Magnetic MXenes: Surface Engineering Induced Spin-valley Coupling 

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Fig. S1 Ferromagnetic (FM) and antiferromagnetic (AFM) states for $\mathrm{Cr}_{2} \mathrm{C}$ MXenes.


Fig. S2 (a) The high symmetry points of the first Brillouin zone for the band structure of $\mathrm{Cr}_{2} \mathrm{C}$ MXenes. (b) Schematic drawing of the band edge structures at two valleys. Down (up) opening parabolas are used to denote valence band maximum (VBM) and conduction band minimum (CBM).


Type III


- C $\odot \mathrm{Cr}$


Type VI

- $\mathrm{X}, \mathrm{X}^{\prime}=\mathrm{F}, \mathrm{Cl}, \mathrm{OH}$ and O

Fig. S3 Four possible types for functionalized $\mathrm{Cr}_{2} \mathrm{C}$ MXenes.


Fig. S4 Total potential energy of MXenes as a function of simulation time for $\mathrm{Cr}_{2} \mathrm{CX}_{2}$ and $\mathrm{Cr}_{2} \mathrm{COX}$ MXenes by using ab-initio molecular dynamics (300K) in 9 ps.


Fig. S5 Phonon spectra for $\mathrm{Cr}_{2} \mathrm{CX}_{2}$ and $\mathrm{Cr}_{2} \mathrm{COX}$ MXenes


Fig. S6 Spin polarized charge densities on (a) $\mathrm{Cr}_{2} \mathrm{CCl}_{2}$ and $\mathrm{Cr}_{2} \mathrm{COCl}$ and (b) $\mathrm{Cr}_{2} \mathrm{C}(\mathrm{OH})_{2}$ and $\mathrm{Cr}_{2} \mathrm{CO}(\mathrm{OH})$ MXenes, where spin-up and spin-down densities are shown in yellow and blue, respectively. The isosurface is $0.045 \mathrm{e} \cdot \mathrm{Bohr}^{-3}$. Electron localization functions (ELF) on (c) $\mathrm{Cr}_{2} \mathrm{CCl}_{2}$ and $\mathrm{Cr}_{2} \mathrm{COCl}$ and (d) $\mathrm{Cr}_{2} \mathrm{C}(\mathrm{OH})_{2}$ and $\mathrm{Cr}_{2} \mathrm{CO}(\mathrm{OH})$ MXenes. The color scale (from 0 to 1 ) shows the probability. The partial electronic density of states (PDOS) of (e) $\mathrm{Cr}_{2} \mathrm{COCl}$ and (f) $\mathrm{Cr}_{2} \mathrm{CO}(\mathrm{OH})$ MXenes.


Fig. S7 Band structures of $\mathrm{Cr}_{2} \mathrm{CX}_{2}$ at HSE06 level. Spin-up and spin-down bands are respectively denoted by black and pink lines.


Fig. S8 (a) Band structures at HSE06 level. Spin-up and spin-down bands are respectively denoted by black and pink lines. (b) Band structures with spin-orbit coupling (SOC). (c) Orbital projected band structures with SOC. Red, black and blue circles represent $d_{y z}+d_{x z}, d_{x^{2}-y^{2}}+d_{x y}$ and $d_{z^{2}}$ orbital composition. The sizes of the dots denote the weight of contribution. Note that each $d$ orbital of Cr atoms in mixed MXenes was not further analyzed.


Fig. S9 Spin polarized charge densities on (a) ferrimagnetic ( FIM ) $\mathrm{Cr}_{2} \mathrm{CO}_{0.75} \mathrm{~F}_{1.25}$ (b) ferromagnetic (FM) $\mathrm{Cr}_{2} \mathrm{CO}_{1.25} \mathrm{~F}_{0.75}$ MXenes, where spin-up and spin-down densities are shown in yellow and blue, respectively. The isosurface is $0.045 \mathrm{e} \cdot \mathrm{Bohr}^{-3}$.


Fig. S10 Berry curvatures of $\mathrm{Cr}_{2} \mathrm{COCl}, \mathrm{Cr}_{2} \mathrm{CO}(\mathrm{OH})$ and $\mathrm{Cr}_{2} \mathrm{CO}_{1.25} \mathrm{~F}_{0.75}$ along high-symmetry points (a) and in the full Brillouin zone (b). Unit of Berry curvatures is $\AA^{2}$.


Fig. S11 Band structures of $\mathrm{Cr}_{2} \mathrm{COX}$ with spin-orbit coupling (SOC) at HSE06 level. The black arrows in circles show the magnetization direction ( $\theta$ ) in the xz plane from -90 to 90.


Fig. S12 Orbital projected band structures of $\mathrm{Cr}_{2}$ COF MXene with SOC when (a) $\theta=45$ and (b) $\theta=0$. Red, black and blue circles represent $d_{y z}+d_{x z},{ }^{d} x^{2}-y^{2}+d_{x y}$ and ${ }^{d^{2}}$ orbital composition. The sizes of dots denote the weight of contribution.


Fig. S13 Specific heat $\left(C_{V}\right)$ calculated for $\mathrm{Cr}_{2} \mathrm{CX}_{2}, \mathrm{Cr}_{2} \mathrm{COX}$ and mixed $\mathrm{Cr}_{2} \mathrm{C}$ MXenes with respect to the temperature.


Fig. S14 (a) Spin polarized charge densities and electron localization functions. Spin-up and spin-down densities are shown in yellow and blue, respectively. The isosurface is $0.045 \mathrm{e} \cdot \mathrm{Bohr}^{-3}$. The color scale (from 0 to 1) shows the probability. (b) Band structures at HSE06 level. Spin-up and spin-down bands are respectively denoted by black and pink lines. (c) Band structures with spin-orbit coupling (SOC). (d) Orbital projected band structures with SOC. Red, black and blue circles represent $d_{y z}+d_{x z}$, $d_{x^{2}-y^{2}}+d_{x y}$ and $d_{z^{2}}$ orbital composition. The sizes of dots denote the weight of contribution. (e) Berry curvatures in the full Brillouin zone. Unit of Berry curvatures is $\AA^{2}$.

Table S1 Four types of functionalization adsorption sites on $\mathrm{Cr}_{2} \mathrm{CX}_{2}$ and Janus $\mathrm{Cr}_{2} \mathrm{COX}$ MXenes. The most stable type is set up to zero for each MXenes.

| MXenes | Type I | Type II | Type III | Type VI |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Cr}_{2} \mathrm{CF}_{2}$ | 0.52 | 0.00 | 0.17 | $/$ |
| $\mathrm{Cr}_{2} \mathrm{CCl}_{2}$ | 0.56 | 0.00 | 0.23 | $/$ |
| $\mathrm{Cr}_{2} \mathrm{C}(\mathrm{OH})_{2}$ | 2.64 | 0.00 | 0.13 | $/$ |
| $\mathrm{Cr}_{2} \mathrm{COF}$ | 0.40 | 0.00 | 0.22 | 0.33 |
| $\mathrm{Cr}_{2} \mathrm{COCl}$ | 0.82 | 0.00 | 0.59 | 0.38 |
| $\mathrm{Cr}_{2} \mathrm{COOH}$ | 0.21 | 0.00 | 0.12 | 0.21 |

Table S2 Calculated structural and magnetic characteristics of $\mathrm{Cr}_{2} \mathrm{CX}_{2}$ and Janus $\mathrm{Cr}_{2} \mathrm{COX}$ MXenes. L is the lattice constant ( $\AA$ ). Cr-C and $\mathrm{Cr}-\mathrm{X}\left(\mathrm{X}^{\prime}\right)$ are bond lengths ( $\AA$ ). Magnetic states include ferromagnetic (FM) and antiferromagnetic (AFM) states. M is magnetic moment $\left(\mu_{\mathrm{B}}\right) . J_{1}, J_{2}$ and $J_{3}$ are coupling constants (meV). $T_{C} / T_{N}$ stands for the Curie and Neel temperatures (K). Band gaps are in spin-up and spin-down channels (eV). $\Delta K_{V B M}$ and $\Delta K_{C B M}$ stands for the valley splitting (meV).

| MXenes | L ( $\AA$ ) | $\mathrm{Cr}-\mathrm{C}$ | $\mathrm{Cr}-\mathrm{X}\left(\mathrm{X}^{\prime}\right)$ | Magnetic states | $\mathrm{M}(\mathrm{Cr})$ | $J_{I}$ | $J_{2}$ | $J_{3}$ | $T_{C} / T_{N}$ | Gaps | $\Delta K_{V B M}$ | $\Delta K_{\text {CBM }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  | Up/down |  |  |
| $\mathrm{Cr}_{2} \mathrm{CF}_{2}$ | 3.01 | 2.05 | 2.12 | AFM | $\pm 2.65$ | 62.14 | 22.11 | 56.07 | 3830 | $3.40 / 3.40$ | 1 | 1 |
| $\mathrm{Cr}_{2} \mathrm{CCl}_{2}$ | 3.13 | 2.02 | 2.46 | AFM | $\pm 2.74$ | 181.39 | 61.79 | 78.4 | 6095 | 2.28/2.28 | 1 | 1 |
| $\mathrm{Cr}_{2} \mathrm{C}(\mathrm{OH})_{2}$ | 3.02 | 1.99 | 2.14 (Cr-OH) | AFM | $\pm 2.79$ | 154.83 | 32.01 | 53.74 | 6095 | 1.55/1.55 | 1 | 1 |
|  |  | $1.99\left(\mathrm{Cr}_{\mathrm{F}}-\mathrm{C}\right)$ | 2.11 (Cr-F) |  | $2.90\left(\mathrm{Cr}_{\mathrm{F}}\right)$ |  |  |  |  |  |  |  |
| $\mathrm{Cr}_{2} \mathrm{COF}$ | 2.94 |  |  | FM |  | 24.61 | 31.46 | 14.64 | 1146 | 0.40/3.46 | 334 | 421 |
|  |  | 2.17 ( $\left.\mathrm{Cr}_{\mathrm{O}}-\mathrm{C}\right)$ | $1.92(\mathrm{Cr}-\mathrm{O})$ |  | $2.56\left(\mathrm{Cr}_{\mathrm{O}}\right)$ |  |  |  |  |  |  |  |
|  |  | $1.96\left(\mathrm{Cr}_{\mathrm{Cl}}-\mathrm{C}\right)$ | $2.44(\mathrm{Cr}-\mathrm{Cl})$ |  | $2.75\left(\mathrm{Cr}_{\mathrm{Cl}}\right)$ |  |  |  |  |  |  |  |
| $\mathrm{Cr}_{2} \mathrm{COCl}$ | 2.98 |  |  | FM |  | 14.37 | 50.55 | 8.74 | 622 | /2.54 | -149 | -139 |
|  |  | 2.10 ( $\left.\mathrm{Cr}_{\mathrm{O}}-\mathrm{C}\right)$ | 1.95 (Cr-O) |  | 2.57 ( $\mathrm{Cr}_{\mathrm{O}}$ ) |  |  |  |  |  |  |  |
|  |  | $1.99\left(\mathrm{Cr}_{\mathrm{OH}}-\mathrm{C}\right)$ | $2.12(\mathrm{Cr}-\mathrm{OH})$ |  | $2.84\left(\mathrm{Cr}_{\mathrm{OH}}\right)$ |  |  |  |  |  |  |  |
| $\mathrm{Cr}_{2} \mathrm{COOH}$ | 2.95 |  |  | FM |  | 24.02 | 32.01 | 6.44 | 983 | /3.26 | 45 | 140 |
|  |  | 2.16 ( $\left.\mathrm{Cr}_{\mathrm{O}}-\mathrm{C}\right)$ | 1.93 (Cr-O) |  | $2.59\left(\mathrm{Cr}_{\mathrm{O}}\right)$ |  |  |  |  |  |  |  |

Table S3 Calculated structural and magnetic characteristics of two mixed MXenes. L is the lattice constant ( $\AA$ ). Magnetic states include ferromagnetic (FM) and ferrimagnetic (FIM) states. $T_{C} / T_{N}$ stands for the Curie and Neel temperatures ( K ). Band gaps are in spin-up and spin-down channels (eV). $\Delta K_{V B M}$ and $\Delta K_{C B M}$ stands for the valley splitting (meV).

| MXenes | $\mathrm{L}(\AA)$ | Magnetic <br> states | $T_{C} / T_{N}$ | Gaps |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Up/down | $\Delta K_{V B M}$ | $\Delta K_{C B M}$ |  |
| $\mathrm{Cr}_{2} \mathrm{CO}_{0.75} \mathrm{~F}_{1.25}$ | 5.96 | FIM | 1648 | $0.97 / 0.46$ | 11 | 11 |
| $\mathrm{Cr}_{8} \mathrm{C}_{4} \mathrm{O}_{1.25} \mathrm{~F}_{0.75}$ | 5.75 | FM | 314 | $0.31 / 2.66$ | 15 | -12 |

