

Supplemental Material
for
Pressure-induced Boron Clathrate with Ambient-pressure
Superconductivity

Yiwei Liang, Meiling Xu*, Shuyi Lin, Xuanhao Yuan, Ziyang Qu, Jian Hao and Yinwei Li*

Laboratory of Quantum Functional Materials Design and Application, School of Physics and Electronic Engineering,
Jiangsu Normal University, Xuzhou 221116, China

To whom all correspondence should be addressed.

xml@calypso.cn and yinwei_li@jsnu.edu.cn

Computational Details

The crystal structure searching is performed with CALYPSO code¹⁻³. Unit cells containing 1-4 formula units were considered. In the first generation, a population of structures belonging to certain space group symmetries are randomly constructed. Starting from the second generation, 60% structures in the previous generation with the lower enthalpies are selected to produce the structures of next generation by the Particle Swarm Optimization (PSO) operators. The 40% structures in the new generation are randomly generated. A structure finger printing technique of bond characterization matrix is applied to the generated structures, so that identical structures are strictly forbidden. These procedures significantly enhance the diversity of the structures, which is crucial for structural global search efficiency. The structure search was considered converged when ~ 1000 successive structures were generated after a lowest energy structure was found.

The phonon spectrum and electron-phonon coupling were calculated within linear-response theory with the QUANTUM ESPRESSO code^{4,5}. Ultrasoft pseudopotentials for La and B were used. The kinetic cutoff energy of 70 Ry for $R-3m$ LaB and $P4/mmm$ LaB₅, 80 Ry for $P4/mbm$ LaB₄, $Cmmm$ LaB₄, $Pm-3m$ LaB₆ and $R-3m$ LaB₈, 90 Ry for $Cmmm$ LaB₆. The q mesh of $5 \times 5 \times 5$ (19 q points), $4 \times 4 \times 4$ (18 q points), $3 \times 3 \times 3$ (8 q points), $5 \times 5 \times 5$ (18 q points), $6 \times 6 \times 6$ (20 q points), $4 \times 4 \times 4$ (21 q points) and $5 \times 5 \times 5$ (19 q points) for the $R-3m$ LaB, $P4/mbm$ LaB₄, $Cmmm$ LaB₄, $P4/mmm$ LaB₅, $Pm-3m$ LaB₆, $Cmmm$ LaB₆ and $R-3m$ LaB₈, respectively, in the first Brillouin zone are used in the EPC calculations. Correspondingly, the k meshes was $20 \times 20 \times 20$, $16 \times 16 \times 16$, $12 \times 12 \times 12$, $20 \times 20 \times 20$, $24 \times 24 \times 24$, $16 \times 16 \times 16$ and $20 \times 20 \times 20$ for $R-3m$ LaB, $P4/mbm$ LaB₄, $Cmmm$ LaB₄, $P4/mmm$ LaB₅, $Pm-3m$ LaB₆, $Cmmm$ LaB₆ and $R-3m$ LaB₈, respectively.

Table SI. The optimized structural parameters of LaB, $Cmmm$ LaB₄, LaB₅, $Cmmm$ LaB₆ and LaB₈ compounds.

Phases	Pressure (GPa)	a, b, c (Å, deg)	Atomic position		
$R-3m$ LaB	0	$a=b=c=8.398$	La1 (2c) (0.91906	0.91906	0.91906)
		$\alpha=\gamma=\beta=23.193$	B1 (2c) (0.66667	0.66667	0.66667)
$Cmmm$ LaB ₄	90	$a=b=8.06570$	La1 (2) (-0.31475	-0.68525	-0.50000)
		$c=3.85730$	La3 (2) (-0.25340	-0.25340	-0.50000)

		$\alpha=\beta=90.0000$	B1 (4) (-0.36493	-0.94222	0.00000)
		$\gamma=140.8757$	B5 (4) (-0.35576	-0.13386	0.00000)
			B9 (4) (-0.85727	-0.14273	-0.28772)
			B13 (2) (-0.44090	-0.55910	-0.00000)
			B15 (2) (-0.05288	-0.94712	0.00000)
<i>P4/mmm</i> LaB ₅	80	$a=b=3.976$	La1 (1b) (0.00000	0.00000	0.50000)
		$c=2.829$	B1 (1d) (0.50000	0.50000	0.50000)
		$\alpha=\gamma=\beta=90.000$	B2 (4n) (0.20473	0.50000	-0.00000)
<i>Cmmm</i> LaB ₆	75	$a=b=5.288$	La1 (2) (0.79536	-0.20464	-0.00000)
		$c=3.827$	B1 (4) (0.69112	-0.69112	0.79316)
		$\alpha=\gamma=90.000$	B2 (2) (0.88158	-0.88158	0.50000)
		$\beta=77.173$	B5 (2) (0.59418	-0.40582	0.50000)
			B6 (4) (0.56902	-0.88300	0.50000)
<i>R-3m</i> LaB ₈	0	$a=b=c=4.330$	La1 (1a) (0.00000	0.00000	0.00000)
		$\alpha=\gamma=\beta=77.834$	B1 (2c) (-0.70167	-0.70167	-0.70167)
			B3 (6h) (-0.86527	-0.41570	-0.41570)

Table SII. The optimized structural parameters of LaB, *Cmmm* LaB₄, LaB₅, *Cmmm* LaB₆ and LaB₈ compounds.

Phases	C_{11}	C_{22}	C_{33}	C_{44}	C_{55}	C_{66}	C_{12}	C_{13}	C_{23}	B	G	H_{vc}	H_{vt}
<i>R-3m</i> LaB	169	169	69	2	2	77	15	12	12	54	41	10	9
<i>P4/mbm</i> LaB ₄	396	396	409	144	144	148	60	51	51	170	156	32	30
<i>Cmmm</i> LaB ₄	395	340	404	147	136	176	42	45	93	166	156	32	30
<i>P4/mmm</i> LaB ₅	565	565	329	56	56	233	58	49	49	197	156	26	25
<i>Pm-3m</i> LaB ₆	476	476	476	100	100	100	23	23	23	174	150	29	27
<i>Cmmm</i> LaB ₆	439	436	447	124	45	147	75	16	70	176	125	20	19
<i>R-3m</i> LaB ₈	327	327	544	239	239	104	119	124	124	214	172	28	27

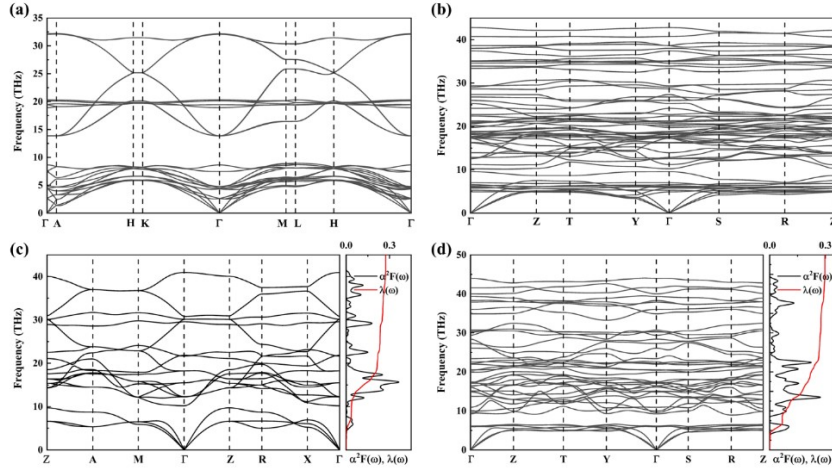


Fig. S1. The phonon dispersion relations of (a) $R\text{-}3m$ LaB at 100 GPa, (b) $Cmmm$ LaB₄ at 90 GPa. The phonon dispersion relations, Eliashberg function $\alpha^2F(\omega)$ and integrated electron-phonon coupling (EPC) strength $\lambda(\omega)$ of (c) $P4/mmm$ LaB₅ at 80 GPa, (d) $Cmmm$ LaB₆ at 75 GPa.

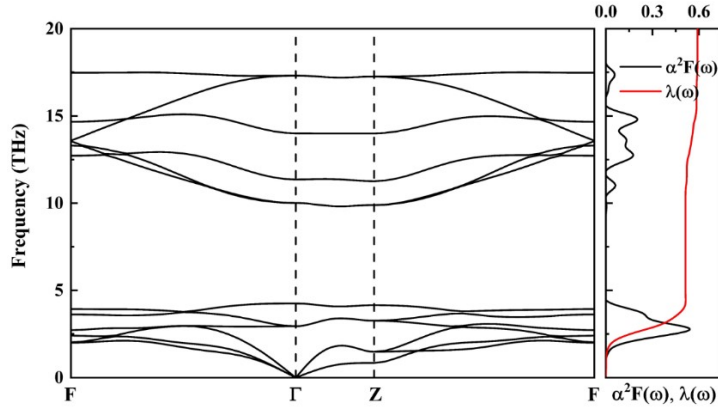


Fig. S2. The phonon dispersion relations, Eliashberg function $\alpha^2F(\omega)$ and integrated electron-phonon coupling (EPC) strength $\lambda(\omega)$ of LaB at 0 GPa.

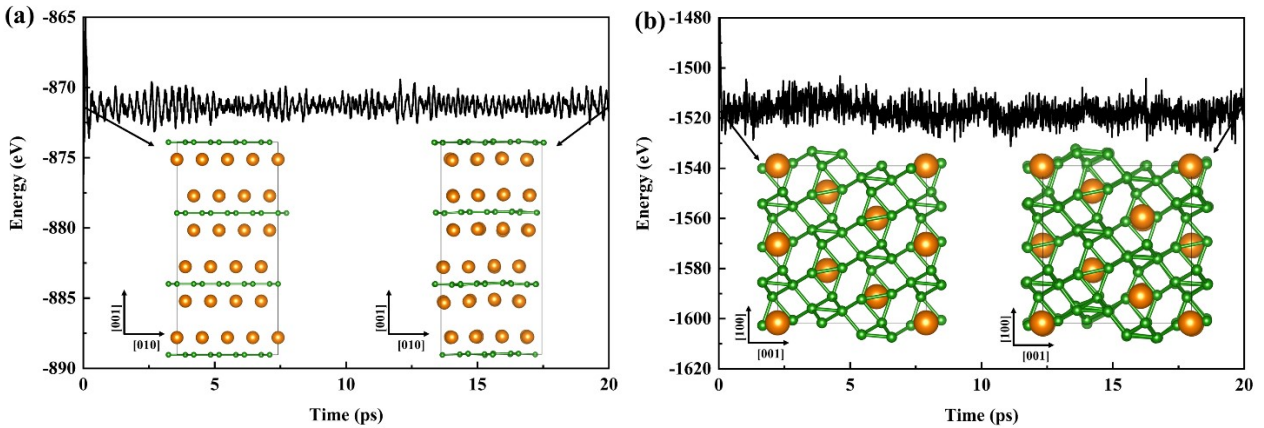


Fig. S3. Energy fluctuations during AIMD simulations up to 20 ps for (a) $R\text{-}3m$ LaB and (b) $R\text{-}3m$ LaB₈ at 0 GPa with 300 K.

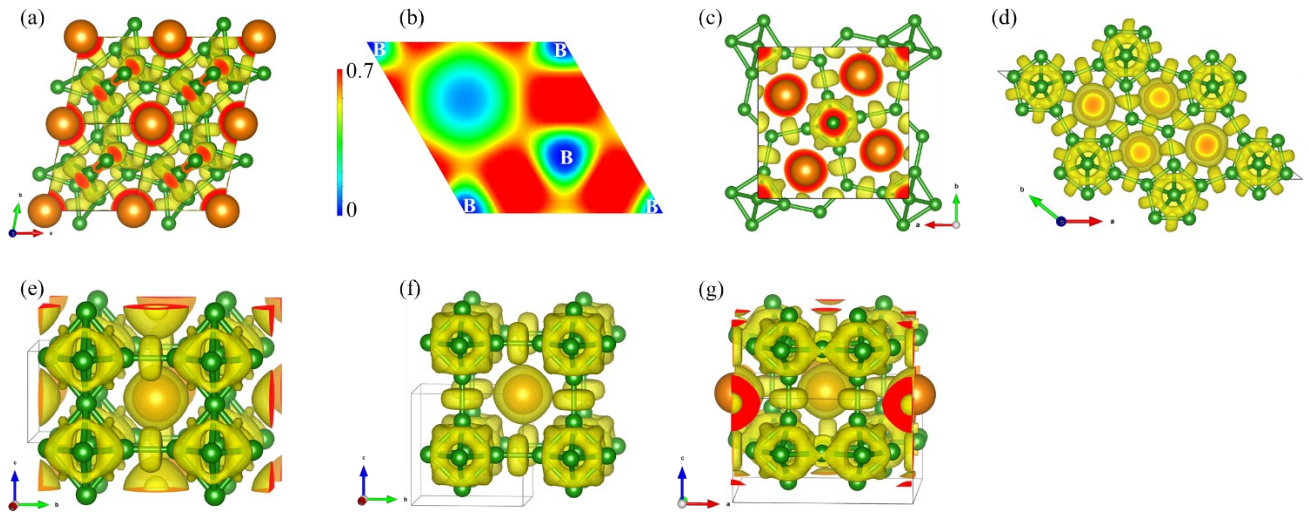


Fig. S4. Three-dimensional electron localization function (ELF) for (a) $R-3m$ LaB_8 (c) $P4/mbm$ LaB_4 , (d) $Cmmm$ LaB_4 , (e) $P4/mmm$ LaB_5 , (f) $Pm-3m$ LaB_6 , (g) $Cmmm$ LaB_6 and two-dimensional ELF of (b) $R-3m$ LaB .

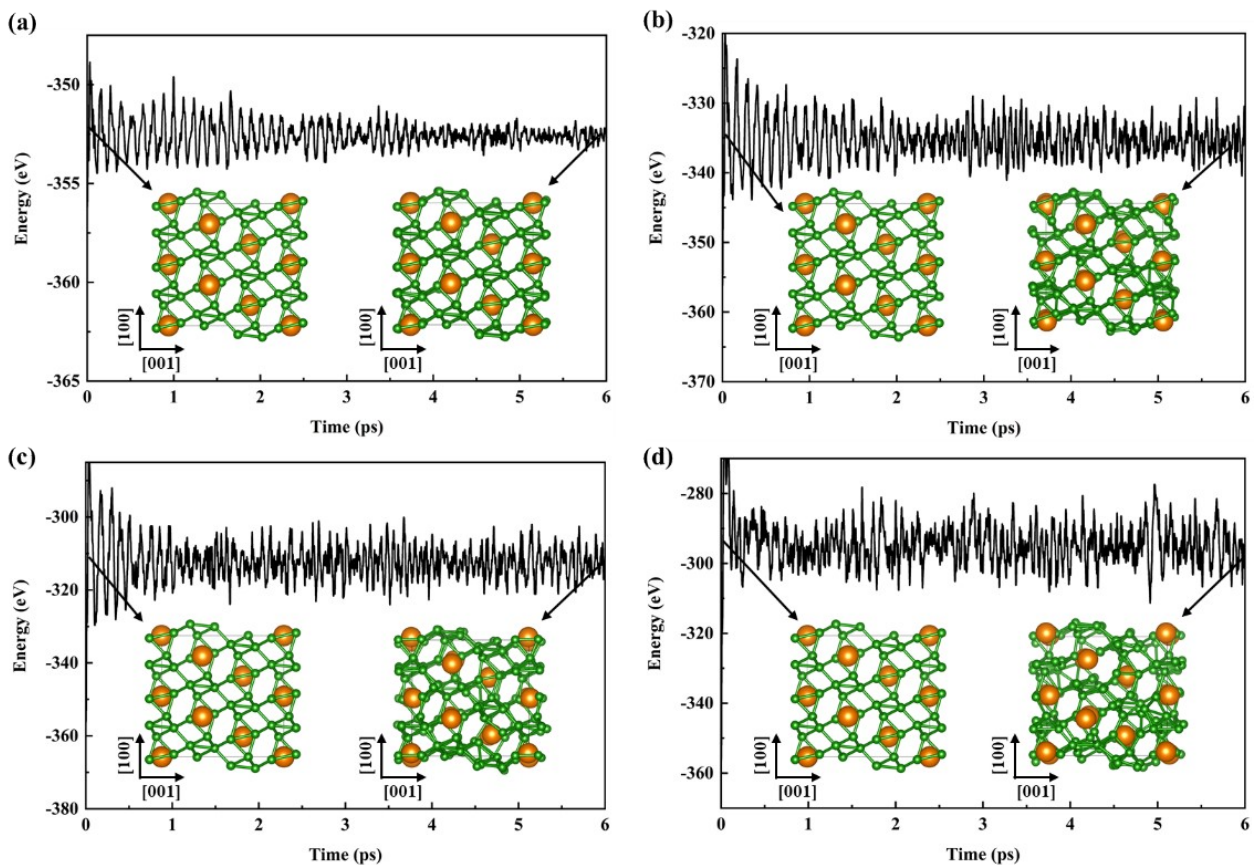


Fig. S5 Evolution of relative energies during MD simulations of LaB_8 at 70 GPa with (a) 300 K, (b) 1500 K, (c) 3000 K and (d) 4000 K. The insets are snapshots of structures at the first state and final state.

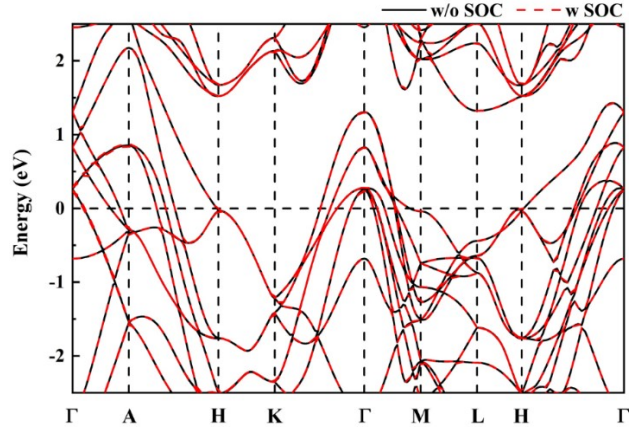


Fig. S6 Band structures of LaB_8 with and without spin-orbit effect.

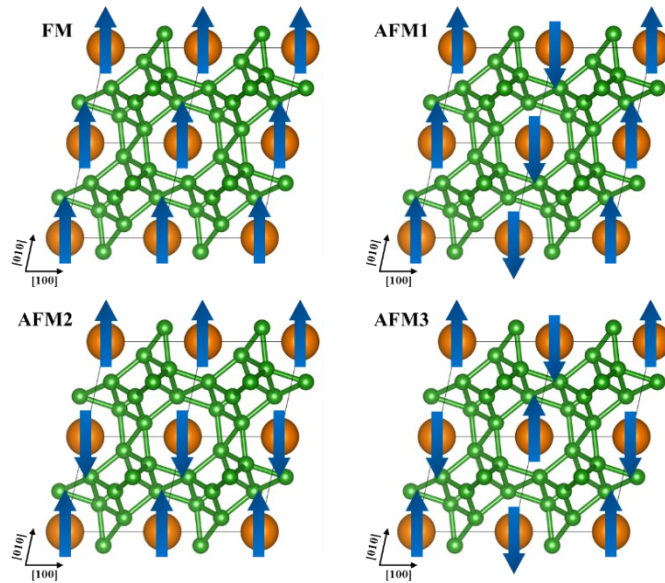


Fig. S7 Four possible magnetic configurations of LaB_8 . Large and small spheres represent La and B atoms, respectively. The blue arrows represent the spin directions of La atoms. Results suggest that LaB_8 is nonmagnetic because the magnetic moment of each La atom is zero in considered magnetic phases.

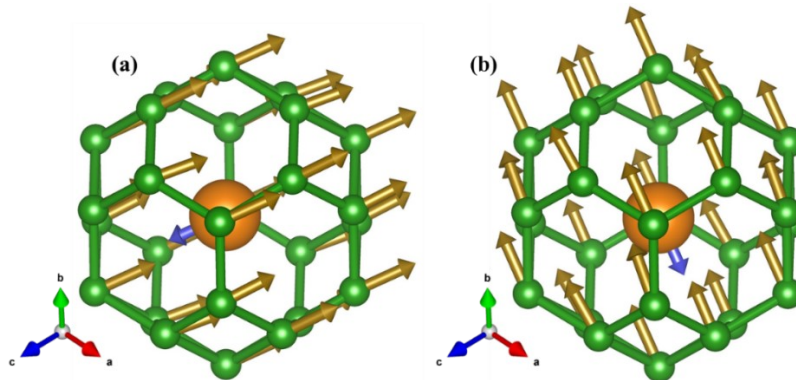


Fig. S8. Schematic illustrations of the atomic displacements of the Raman active E_u modes at the Γ point in $R\text{-}3m$ LaB_8 .

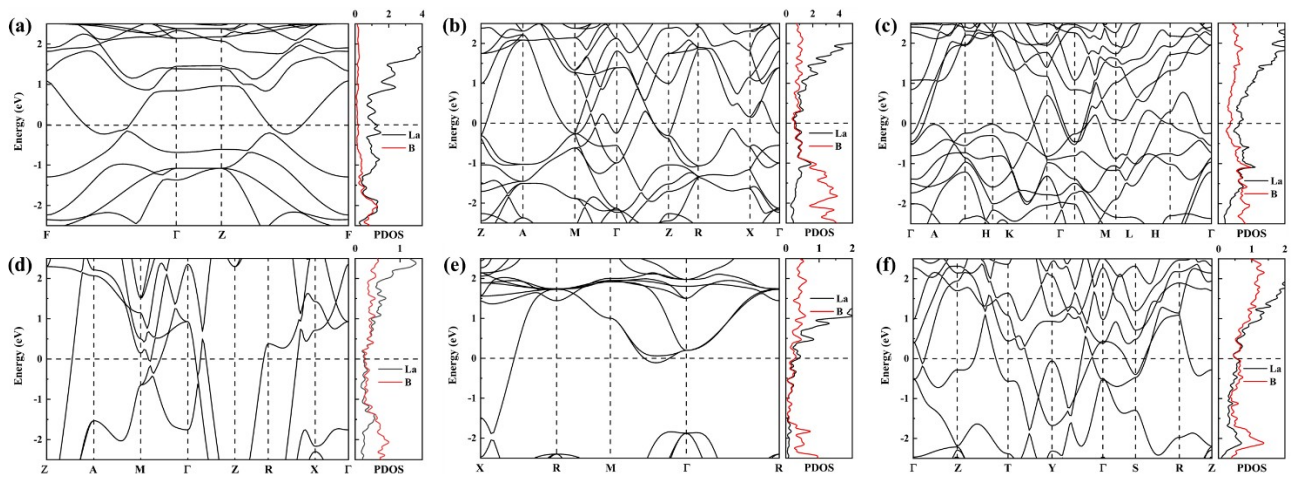


Fig. S9. Band structures and projected density of states (PDOS, in unit of states/eV/f.u.) of (a) $R\bar{3}m$ LaB at 0 GPa, (b) $P4/m\bar{b}m$ LaB₄ at 0 GPa, (c) $Cmmm$ LaB₄ at 90 GPa, (d) $P4/m\bar{m}m$ LaB₅ at 80 GPa, (e) $Pm\bar{3}m$ LaB₆ at 0 GPa and (f) $Cmmm$ LaB₆ at 75 GPa.

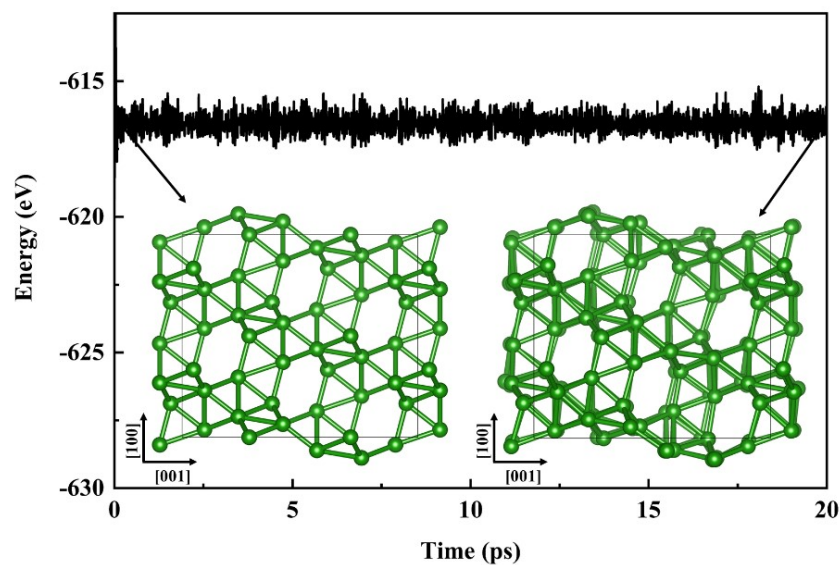


Fig. S10. Energy fluctuations during AIMD simulations up to 20 ps for the pure B₂₆ cage structure at 0 GPa with 300 K.

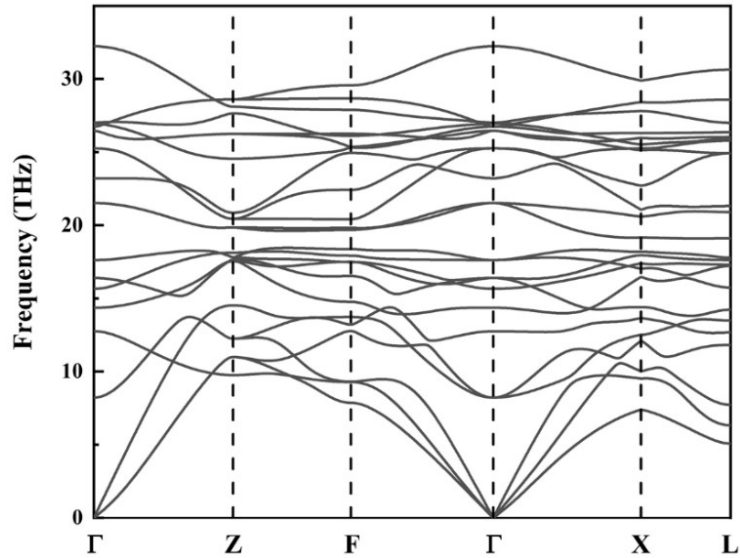


Fig. S11. Phonon dispersion relations for pure B₂₆ cage at 0 GPa, which is calculated by temperature dependent effective potential method^{6,7} at 300 K.

References

- 1 Y. Wang, J. Lv, L. Zhu and Y. Ma, *Comput. Phys. Commun.*, 2012, **183**, 2063–2070.
- 2 Y. Wang, J. Lv, L. Zhu and Y. Ma, *Phys. Rev. B*, 2010, **82**, 094116.
- 3 B. Gao, P. Gao, S. Lu, J. Lv, Y. Wang and Y. Ma, *Sci. Bull.*, 2019, **64**, 301–309.
- 4 S. Baroni, S. de Gironcoli, A. Dal Corso and P. Giannozzi, *Rev. Mod. Phys.*, 2001, **73**, 515–562.
- 5 P. Giannozzi, S. Baroni, N. Bonini, M. Calandra, R. Car, C. Cavazzoni, D. Ceresoli, G. L. Chiarotti, M. Cococcioni, I. Dabo, A. Dal Corso, S. de Gironcoli, S. Fabris, G. Fratesi, R. Gebauer, U. Gerstmann, C. Gougoussis, A. Kokalj, M. Lazzeri, L. Martin-Samos, N. Marzari, F. Mauri, R. Mazzarello, S. Paolini, A. Pasquarello, L. Paulatto, C. Sbraccia, S. Scandolo, G. Sclauzero, A. P. Seitsonen, A. Smogunov, P. Umari and R. M. Wentzcovitch, *J. Phys. Condens. Matter*, 2009, **21**, 395502.
- 6 O. Hellman, I. A. Abrikosov and S. I. Simak, *Phys. Rev. B*, 2011, **84**, 180301.
- 7 O. Hellman and I. A. Abrikosov, *Phys. Rev. B*, 2013, **88**, 144301.