Zn(NH₃)CO₃: A "Three-in-One" UV Nonlinear Optical

Crystal Built by Polar Molecule Bonding Strategy

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Supplementary DFT calculations

In the static case, the imaginary part of the static second-order optical susceptibility can be expressed as:

$$\begin{aligned} \chi^{abc} \\ &= \frac{e^{3}}{h^{2}\Omega} \sum_{nml,k} \frac{r_{nm}^{a} (r_{ml}^{b} r_{ln}^{c} + r_{ml}^{c} r_{ln}^{b})}{2\omega_{nm} \omega_{ml} \omega_{ln}} [\omega_{n} f_{ml} + \omega_{m} f_{ln} + \omega_{l} f_{nm}] \\ &+ \frac{ie^{3}}{4h^{2}\Omega} \sum_{nm,k} \frac{f_{nm}}{\omega_{mn}^{2}} [r_{nm}^{a} (r_{mn;c}^{b} + r_{mn;b}^{c}) + r_{nm}^{b} (r_{mn;c}^{a} + r_{mn;a}^{c}) + r_{nm}^{c} (r_{mn;b}^{a} + r_{mn;a}^{b})] \end{aligned}$$
(1)

where *r* is the position operator, $\hbar\omega_{nm} = \hbar\omega_n - \hbar\omega_m$ is the energy difference for the bands *m* and *n*, $f_{mn} = f_m - f_n$ is the difference of the Fermi distribution functions, subscripts *a*, *b*, and *c* are Cartesian indices, and $r^b_{mn;a}$ is the so-called generalized derivative of the coordinate operator in *k* space,

$$r_{nm;a}^{b} = \frac{r_{nm}^{a}\Delta_{mn}^{b} + r_{nm}^{b}\Delta_{mn}^{a}}{\omega_{nm}} + \frac{i}{\omega_{nm}} \times \sum_{l} (\omega_{lm}r_{nl}^{a}r_{lm}^{b} - \omega_{nl}r_{nl}^{b}r_{lm}^{a})$$
(2)

where $\Delta^a_{nm} = (p^a_{nn} - p^a_{mm}) / m$ is the difference between the electronic velocities at the bands *n* and *m*. The $\chi^{(2)}$ coefficients here were calculated from PBE wave functions with a 5×7×9 k-point grid and about 168 bands.

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Table S1. Crystallographic data for Zn(NH₃)CO₃.

Empirical formula	Zn(NH ₃)CO ₃
Formula weight	142.41
<i>T</i> (K)	293(2)
Crystal system	orthorhombic
Space group	Pna2 ₁
<i>a</i> (Å)	9.161(7)
<i>b</i> (Å)	7.592(6)
<i>c</i> (Å)	5.498(4)
$V(Å^3)$	382.4(5)
Ζ	4
$ ho_{ m caled} \left({ m g} \cdot { m cm}^{-3} ight)$	2.474
$\mu (\mathrm{mm}^{-1})$	6.266
F (000)	280.0
R _{int}	0.0445
GOF on F^2	1.153
Flack factor	0.04(5)
$R_1, wR_2 (\mathbf{I} > 2\sigma(\mathbf{I}))^{[\mathbf{a}]}$	0.0332, 0.0803
R_1, wR_2 (all data)	0.0343, 0.0812
[a] $R_1 = \sum F_o - F_c / \sum F_o ; wR_2 = \{\sum w[(F_o)^2 - (F_c)^2]^2 / \sum w[(F_o)^2]^2 \}^{1/2}.$	

Table S2. Atomic coordinates, equivalent isotropic displacement parameters (Å²) and bond valence sums (BVS) of Zn(NH₃)CO₃. U_{eq} is defined as one-third of the trace of the orthogonalized U_{ij} tensor.

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Atom	Wyckoff	Х	У	Z	U_{eq}	BVS
Zn1	4a	0.14437(6)	-0.16822(8)	0.4629(3)	0.0213(2)	2.03
01	4a	0.2213(5)	0.0466(6)	0.3001(10)	0.0278(10)	1.85
02	4a	0.1587(5)	0.2783(7)	0.0786(10)	0.0276(11)	1.84
03	4a	-0.0128(4)	0.1011(6)	0.2235(9)	0.0217(9)	1.84
N1	4a	0.0671(7)	-0.3304(7)	0.2051(12)	0.0301(13)	2.96
C1	4a	0.1234(7)	0.1420(8)	0.2035(13)	0.0186(11)	4.03
H1	4a	0.08704	-0.28608	0.05896	0.0360	0.99
H2	4a	-0.02908	-0.34146	0.22203	0.0360	0.99
Н3	4a	0.10907	-0.43557	0.21995	0.0360	0.99

Table S3. Selected bond lengths (Å) of Zn(NH₃)CO₃.

Bond	Bond lengths	Bond	Bond lengths
Zn(1)–O(1)	1.989(5)	C(1)–O(1)	1.270(8)
Zn(1)-O(2)#1	1.956(5)	C(1)–O(2)	1.283(8)
Zn(1)-O(3)#2	1.940(5)	C(1)–O(3)	1.291(8)
Zn(1)-N(1)	2.007(6)		
Symmetry codes: #1 1/2-x, -1/2+y, 1/2+z; #2 -x, -y, 1/2+z.			

Table S4. Selected bond angles (deg.) of Zn(NH₃)CO₃.

Bond	Bond angles	Bond	Bond angles
O(1)–Zn(1)–N(1)	108.1(2)	N(1)-Zn(1)-O(3)#2	117.6(2)
O(1)-Zn(1)-O(2)#1	89.4(2)	O(1)–C(1)–O(2)	120.4(6)
O(1)–Zn(1)–O(3)#2	109.7(2)	O(1)–C(1)–O(3)	120.7(6)
O(2)#1–Zn(1)–O(3)#2	112.8(2)	O(2)–C(1)–O(3)	118.9(6)
N(1)-Zn(1)-O(2)#1	115.3(3)		
Symmetry codes: #1 1/2-x, -1/2+y, 1/2+z; #2 -x, -y, 1/2+z.			

Table S5. The local dipole moment (μ) of Zn(NH₃)CO₃ in Debye.

	1 47	(5) 5	5	
	$\mu_{ m x}$	$\mu_{ m y}$	$\mu_{ m z}$	$ \mu $
ZnO ₃ (NH ₃)	-3.0699	-5.1258	-5.0941	7.85
ZnO ₃ (NH ₃)	-3.0699	5.1258	-5.0941	7.85
ZnO ₃ (NH ₃)	3.0699	5.1258	-5.0941	7.85
ZnO ₃ (NH ₃)	3.0699	-5.1258	-5.0941	7.85
Total	0	0	-20.3764	

Figures





Figure S2. PXRD pattern of Zn(NH₃)CO₃.



Figure S3. IR spectrum of Zn(NH₃)CO₃.



Figure S4. A Chinese knot.



Figure S5. The calculated frequency-dependent refractive indices of Zn(NH₃)CO₃.



Figure S6. The birefringence of Zn(NH₃)CO₃.



Figure S7. The UV-vis-NIR diffuse reflectance spectrum of Zn(NH₃)CO₃. The absorption peak at 1543, 1900–2300 nm may be caused by the overtone vibration of N–H bond.



Figure S8. TG curve of Zn(NH₃)CO₃.



Figure S9. Variable temperature PXRD pattern of Zn(NH₃)CO₃.





Figure S11. The frequency-dependent SHG coefficients of $Zn(NH_3)CO_3$.