

## Supplementary information

### Strain-induced spin-gapless semiconductors and pure thermal spin-current in magnetic black arsenic-phosphorus monolayer

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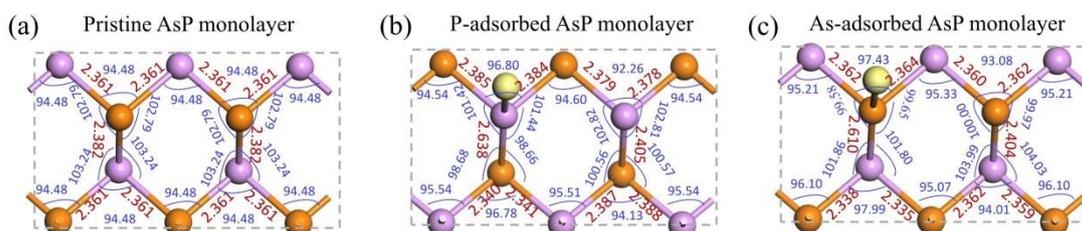
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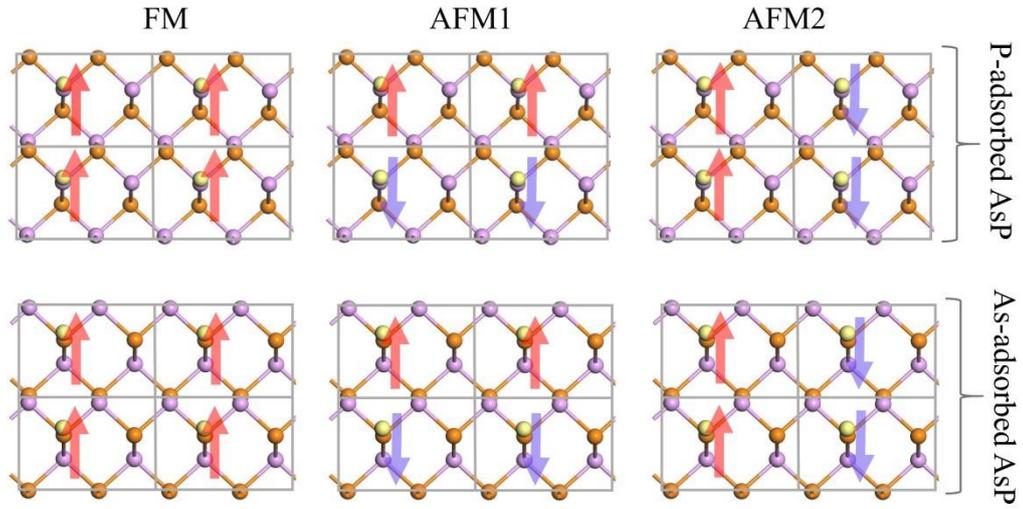
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**Fig. S1** (a)-(c) The optimized bond lengths and bond angles of the pristine AsP monolayer, P- and As-adsorbed AsP nanosheets, respectively.

**Table S1:** The optimized lattice constants ( $a$ ,  $b$ ,  $c$ ), three angles ( $\alpha$ ,  $\beta$ ,  $\gamma$ ) and the bond length ( $l$ ) of P-Cl (As-Cl) for pristine AsP monolayer, P- and As-adsorbed AsP nanosheets, respectively.

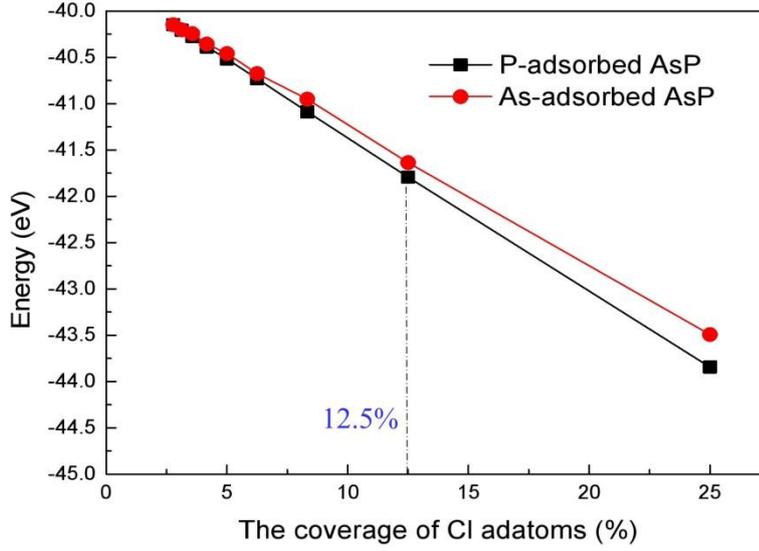
	$a$ (Å)	$b$ (Å)	$c$ (Å)	$\alpha$ (°C)	$\beta$ (°C)	$\gamma$ (°C)	$l$ (Å)
Pristine AsP	4.787	6.934	9.792	90	90	90	—
P-adsorbed AsP	4.593	6.996	9.997	89.957	90.885	89.980	2.194
As-adsorbed AsP	4.607	6.971	10.020	90.109	90.828	89.987	2.0285



**Fig. S2** Three different spin configurations of ferromagnetic (FM) and antiferromagnetic states (AFM1 or AFM2) for P- and As-adsorbed AsP monolayer, respectively.

**Table S2:** The energies (in meV) of antiferromagnetic states (AFM1 and AFM2) compared with the ferromagnetic (FM) state (set as 0).

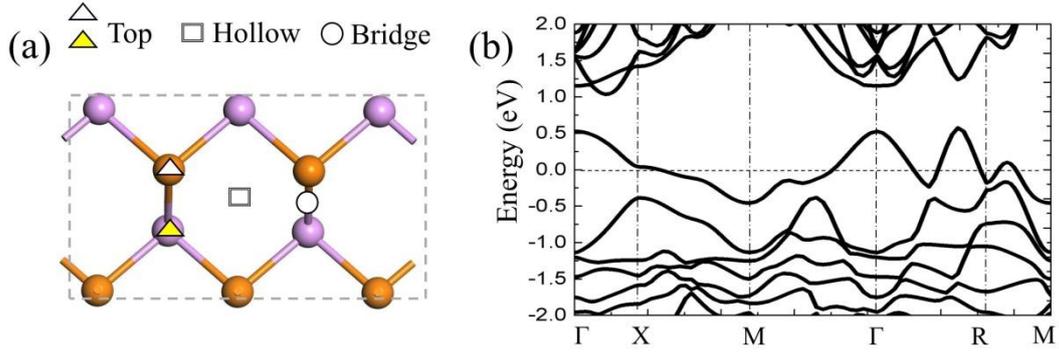
	FM	AFM1	AFM2
P-adsorbed AsP	0	27.5	6.2
As-adsorbed AsP	0	22.4	5.8



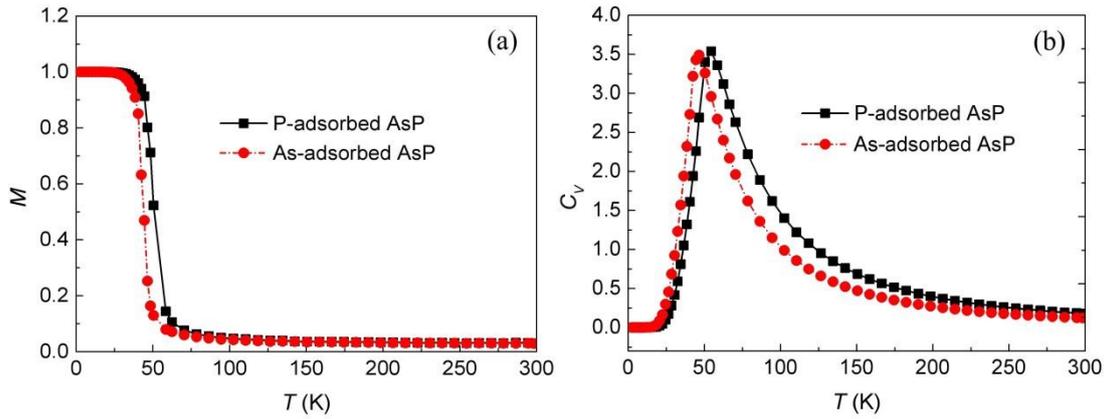
**Fig. S3** The equivalent energies of the different coverages for Cl adatoms compared to P- and As-adsorbed monolayer with the 12.5% coverage, respectively.

**Table S3:** Binding energies of P- and As-adsorbed AsP monolayer, defined as  $E_b = E_S - E_{AsP} - E_{Cl_2}/2$ , where  $E_S$ ,  $E_{AsP}$  and  $E_{Cl_2}$  stand for the energies of AsP monolayer with one Cl adatom, pristine AsP monolayer and  $Cl_2$  molecule, respectively.

	$E_b$ (eV)	$E_S$ (eV)	$E_{AsP}$ (eV)	$E_{Cl_2}$ (eV)
P-adsorbed AsP	-0.877	-41.793	-39.128	-3.575
As-adsorbed AsP	-0.720	-41.636	-39.128	-3.575



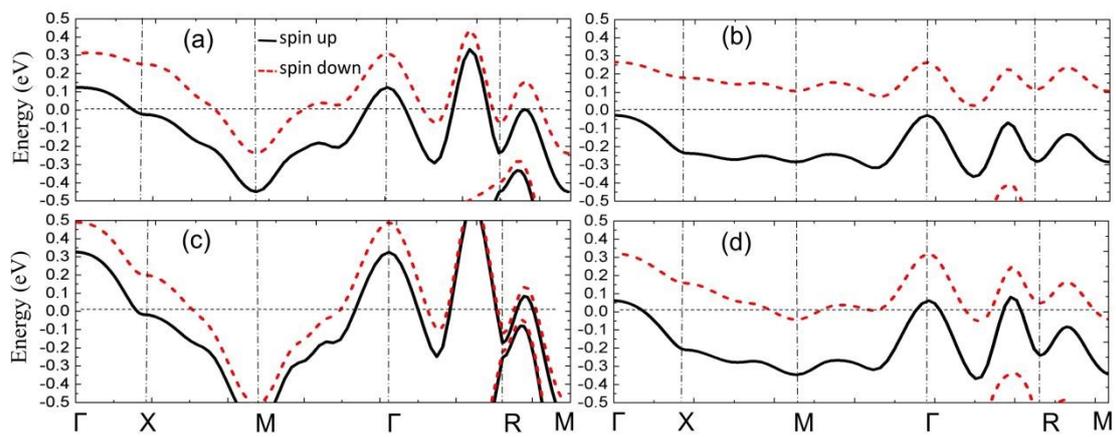
**Fig. S4** (a) Three adsorption positions for AsP monolayer with the Cl adatom: top, hollow and bridge sites. (b) Band structures of AsP monolayer with the Cl adatom on bridge site.



**Fig. S5** Monte Carlo simulations for the P- and As-adsorbed AsP monolayer: (a) magnetism ( $M$ ) and (b) heat capacity ( $C_V$ ) versus temperature. We use the Heisenberg model to describe the spin interaction and the related lattice Hamiltonian can be expressed as follows:

$$H = -J_1 \sum_{\langle i,j \rangle} S_i S_j - J_2 \sum_{\langle k,l \rangle} S_k S_l$$

where  $S_i, S_j$  and  $S_k, S_l$  refer to the spin operators on the nearest and next nearest-neighbour lattice points  $\langle i,j \rangle$  and  $\langle k,l \rangle$ , respectively.  $J_1$  and  $J_2$  stand for the nearest and next nearest-neighbour interaction energies, respectively, estimated by the energy difference between the ferromagnetic and anti-ferromagnetic state shown in Table S2 and Fig. S2.



**Fig. S6** (a) and (b) Band structures of the AsP monolayer with one P atom adsorbed by one fluorine (F) and one bromine (Br) atom, respectively. (c) and (d) Band structures of the AsP monolayer with one As atom adsorbed by one F and one Br atom, respectively.