

Supporting Information

Insight into the inclusion of heteroatom impurities in Silicon structures

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1 Reference systems

1.1 Bulk systems

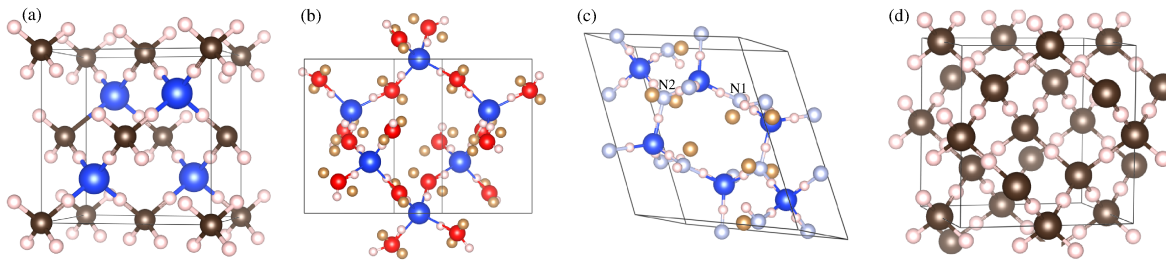


Figure 1: Bonds and lone pairs on (a) SiC (b) SiO₂ (c) Si₃N₄ (d)Diamond

	Si	SiC	SiO ₂	Si ₃ N ₄	Diamond
Bond Charges(BC)	1.999	2.000	1.908, 1.957	2.313	1.999
Bond length(BL)Å	2.351	1.896	1.625, 1.628	1.747	1.547
Lone Pair(LP)			4.1340	N2:(0.5289 each) 1.0578	

Table 1: Bond charge(BC), bond length (BL) and lone pair(LP) data for Si-Si, Si-C, Si-O, Si-N and C-C bond from respective bulk systems:Si, SiC, SiO₂, Si₃N₄ and diamond.

1.2 Molecular systems

	Ethane	Ethylene	Cyclopropane	Cyclopropene	Bicyclobutane
Bond Charges(BC)	1.81	3.42	1.70	1.80, 3.20	1.87, 1.72
Bond length(BL)Å	1.53	1.33	1.52	1.53, 1.30	1.46, 1.55

Table 2: Bond charge(BC), bond length (BL) of molecular systems

1.3 Silicon grain boundary without/with defects

	Bond Charges(BC)	Bond length(BL)Å	LP
Si-GB	2.00329 2.00096 1.98795	2.35084 2.35122 2.36642	
Si-GB: V1	2.0697 2.0138 2.0138 2.0192 2.0192 2.0712 2.0712 1.9712 2.0282 2.0062 2.0280 2.0280 1.5429	2.32564 2.37601 2.37601 2.36607 2.36607 2.31773 2.31773 2.42741 2.47125 2.50193 2.31424 2.31424 2.45097	Si1: 0.99 Si2: 1.00
Si-GB: V2	2.0172 2.0172 2.0609 2.0609 2.0676 2.0676 1.9926 1.9782 2.0207 2.0207 2.0273 2.0251 1.5522	2.37177 2.37177 2.32423 2.32423 2.32906 2.32906 2.35628 2.43172 2.43038 2.43038 2.48162 2.31610 2.44485	Si1: 0.97 Si2: 1.03

Table 3: Bond charge(BC), bond length (BL) and lone pair(LP) data for Si-Si bond without/with vacancy defect on Si-GB.

2 Systems with interstitial carbon impurities

2.1 Electronic properties

X	E_f^{XB}	E_f^{XGB}	E_f^{XV1GB}	E_f^{XV2GB}
1C	3.5467	3.5072	-1.6935	-1.8003
2C	4.6315	4.3359	0.4985	0.2165
3C	6.2242	5.2122	0.9758	0.8144
4C	8.1596	7.6275	2.2861	2.1306

Table 4: Formation energy (eV) of Si bulk and $\Sigma 3\{111\}$ Si GB without/with vacancies V1 and V2 with interstitial C atoms from 1 to 4. The values are reported for the lowest energy structures.

X	$E_g^{\text{Si-bulk}}$	E_g^{GB}	E_g^{V1GB}	E_g^{V2GB}
1C	0	0.0477	0.3587	0.4014
2C	0.4291	0.5235	0	0
3C	0.6944	0.4729	0.6066	0.5578
4C	0.4549	0.1319	0.6502	0.5978

Table 5: Energy gaps (eV) of Si bulk and $\Sigma 3\{111\}$ Si GB without/with vacancies V1 and V2 with interstitial C atoms from 1 to 4. The values are reported for the lowest energy structures.

X	$P(\text{X+B})$	$P(\text{X+GB})$	$P(\text{X+V1GB})$	$P(\text{X+V2GB})$
1C	2.564	2.281	0.674	0.673
2C	3.850	2.756	1.507	1.502
3C	3.742	2.845	2.343	2.359
4C	4.734	3.356	2.563	2.543

Table 6: Hydrostatic pressure (GPa) of Si bulk and $\Sigma 3\{111\}$ Si GB without/with vacancies V1 and V2 with interstitial C atoms from 1 to 4. The values are reported for the lowest energy structures.

2.2 Bonding analysis

Si-Bulk	BC(Si-Si)	BL(Si-Si)Å	BC(Si-C)	BL(Si-C)Å	BC(C-C)	BL(C-C)Å	LP
1C	1.9917 1.9916 1.9950 1.9948 2.2328 2.2350 1.9995	2.31736 2.31759 2.31807 2.31842 2.28068 2.28173 2.44675	2.4598 2.5371 2.3758	1.81289 1.81233 1.74694			0.14269
2C	1.9779 1.9781 1.9779 1.9782 2.1463 2.1460 1.9930	2.31447 2.31436 2.31428 2.31450 2.25425 2.25412 2.30624	2.4845 2.4843 1.7554 1.7557	1.78563 1.78585 1.84197 1.84192	3.0651	1.31413	
3C	2.0201 2.0046 2.0047 2.0202 2.0693 2.0693 2.1675 1.9581 1.9577	2.31590 2.30954 2.30951 2.31584 2.34550 2.28606 2.20866 2.34297 2.34290	2.3825 2.3820 1.9941 1.9021 1.9028	1.81499 1.81535 1.87728 1.87268 1.87244	1.5792 1.5777 1.41599	1.53572 1.53568 1.50008	
4C	1.9954 2.0178 2.0250 2.0650 2.0407 1.9946 1.9880 1.9545 1.9410	2.36665 2.32830 2.38233 2.26366 2.28754 2.30892 2.31720 2.34714 2.35165	2.2361 2.3127 2.2938 2.3754 1.9845 2.1936	1.84433 1.80898 1.85218 1.81756 1.86359 1.87557	2.1508 3.0399 1.7943 1.0551	1.41648 1.34593 1.46732 1.66790	C3: 0.01604

Table 7: Bond charge(BC), bond length (BL) and lone pair(LP) data for Si-Si, Si-C and C-C bonds with the inclusion of n numbers of C atoms (n=1,2,3 & 4) in Si-bulk.

Si-GB	BC(Si-Si)	BL(Si-Si)Å	BC(Si-C)	BL(Si-C)Å	BC(C-C)	BL(C-C)Å	LP
1C	1.9903	2.31786	2.2747	1.81425			0.5948
	2.0164	2.31981	2.2497	1.81470			
	1.9814	2.31807	2.4034	1.74762			
	2.2083	2.29283					
	2.0041	2.33252					
	2.2183	2.29363					
	2.0015	2.45067					
2C	2.0507	2.37415	2.3492	1.83840	2.8306	1.37792	
	2.0595	2.36930	2.3430	1.84499			
	2.0793	2.27725	2.1074	1.86866			
	2.0129	2.29788	2.1091	1.86785			
	2.0158	2.29966					
	1.9780	2.34655					
	1.9662	2.35109					
	2.0841	2.26822					
	2.0117	2.34787					
	1.9379	2.31357					
3C	2.0549	2.42702	2.2420	1.85243	1.5274	1.57712	C3: 0.001514
	2.0493	2.30263	2.2603	1.85057			
	2.0167	2.33603	2.2152	1.84016			
	2.0128	2.33161	2.1312	1.85078			
	2.0341	2.35625	2.1595	1.84555			
	2.0395	2.32409	1.8675	1.93941			
	2.0554	2.44381	1.8601	1.93139			
	1.9637	2.32060	1.8795	1.88733			
	2.2222	2.21525	1.6191	1.88109			
			1.5615	1.89062			
4C	2.0053	2.31422	2.3129	1.83722	2.5353	1.39499	
	2.0744	2.32324	2.2215	1.87488			
	2.0044	2.33814	2.1408	1.89536			
	2.0281	2.36433	2.4743	1.78531			
	1.9727	2.34566	2.4729	1.78473			
	1.9471	2.32925	2.4820	1.80381			
	1.8315	2.48968	2.5122	1.77339			
	1.8336	2.44290	2.1517	1.79929			
	1.1289	2.57283	2.7127	1.75854			
			1.7269	1.95371			
			1.1668	2.03012			

Table 8: Bond charge(BC), bond length (BL) and lone pair(LP) data for Si-Si, Si-C and C-C bonds with the inclusion of n numbers of C atoms (n=1,2,3 & 4) in Si-GB

	Si-VGB	BC(Si-Si)	BL(Si-Si)Å	BC(Si-C)	BL(Si-C)Å	BC(C-C)	BL(C-C)Å	LP
V1	1C	2.0243	2.39351	1.9629	1.99583			
		2.0242	2.39361	1.9526	2.00851			
		2.0205	2.39538	1.9201	2.03954			
		2.0289	2.39751	1.9199	2.03983			
		2.0210	2.40463					
		2.0211	2.40463					
		2.0291	2.39740					
		2.0115	2.34935					
		2.0237	2.40396					
		2.0115	2.34945					
		2.0238	2.40392					
		1.9847	2.34152					
		2.0026	2.46212					
	1.9689	2.42414						
	2C	2.0236	2.40835	2.4013	1.88745	2.3241	1.41529	
		2.0234	2.42022	2.4174	1.88984			
		2.0299	2.42408	2.4146	1.88913			
		2.0176	2.42635	2.4217	1.88409			
		2.0019	2.33929					
		2.0023	2.34743					
		2.0037	2.34256					
		1.9859	2.37766					
		1.9560	2.37192					
		1.9545	2.37375					
	3C	2.0355	2.32286	2.6560	1.80175	3.0039	1.31195	
		2.0148	2.39841	2.7033	1.80450	1.5660	1.51629	
		2.0329	2.29982	2.1869	1.89111	1.5181	1.52702	
		2.0273	2.33162	2.1780	1.90020			
		2.0332	2.32608					
		1.9774	2.32650					
		1.9799	2.34479					
		1.9779	2.34151					
		2.0099	2.42987					
		1.9848	2.31307					
		1.9863	2.37639					
		1.9979	2.37766					
1.9875		2.37762						
4C	2.0668	2.30703	2.3035	1.85418	1.6203	1.53713	C1: 0.010741	
	2.0139	2.31936	2.5360	1.83508	1.6193	1.53703	C3: 0.035845	
	2.0058	2.34112	2.5114	1.83507	1.5869	1.55733	C3: 0.021072	
	2.0131	2.34511	2.3171	1.85991	1.5648	1.55739		
	2.0274	2.37703	2.0619	1.84544	1.3678	1.46903		
	2.0276	2.37684	2.0494	1.90386				
	2.0429	2.35443						
	2.0429	2.35446						
	2.0115	2.29645						
	2.0414	2.36713						

Table 9: Bond charge(BC), bond length (BL) and lone pair(LP) data for Si-Si, Si-C and C-C bonds with the inclusion of n numbers of C atoms (n=1,2,3 & 4) in Si-GB with vacancy V1.

	Si-VGB	BC(Si-Si)	BL(Si-Si)Å	BC(Si-C)	BL(Si-C)Å	BC(C-C)	BL(C-C)Å	LP		
V2	1C	2.0281	2.38089	1.9623	2.00709					
		2.0281	2.38089	1.9271	2.01777					
		2.0184	2.38908	1.9333	2.03516					
		2.0207	2.40451	1.9333	2.03516					
		2.0207	2.40451							
		2.0272	2.39927							
		2.0272	2.39927							
		2.0224	2.39941							
		2.0224	2.39941							
		2.0196	2.39996							
		2.0022	2.46209							
		2.0022	2.46209							
V2	2C	2.0119	2.32572	2.3918	1.89263	2.3152	1.41603			
		2.0235	2.40835	2.4065	1.89224					
		2.0171	2.42459	2.4949	1.87145					
		2.0034	2.32550	2.4071	1.88101					
		1.9984	2.38682							
		1.9612	2.35986							
		1.9912	2.33270							
		1.9641	2.41901							
		1.9530	2.37274							
		1.9518	2.37180							
		V2	3C	2.0037	2.33228	2.6418	1.80187	2.9989	1.31248	
				1.9961	2.33392	2.7338	1.79859	1.5669	1.51368	
1.9890	2.33664			2.1864	1.89848	1.5185	1.52813			
2.0321	2.30156			2.1773	1.90683					
2.0308	2.33111									
2.0230	2.32828									
2.0121	2.41445									
2.0278	2.32947									
V2	4C	2.0689	2.31040	2.2894	1.86170	1.6442	1.53314			
		2.0040	2.33369	2.5498	1.83354	1.6105	1.53866			
		1.9870	2.32764	2.5521	1.84761	1.5948	1.55655			
		2.0023	2.33598	2.3272	1.86247	1.5870	1.55328			
		2.0042	2.33820	2.0410	1.84755	1.3498	1.47835			
		2.0345	2.35649	2.0608	1.90940					
		2.0533	2.31292							
		2.0063	2.33383							
		2.0353	2.34643							

Table 10: Bond charge(BC), bond length (BL) and lone pair(LP) data for Si-Si, Si-C and C-C bonds with the inclusion of n numbers of C atoms (n=1,2,3 & 4) in Si-GB with vacancy V2.

3 Systems with interstitial nitrogen impurities

3.1 Electronic properties

X	E_f^{XB}	E_f^{XGB}	E_f^{XV1GB}	E_f^{XV2GB}
1N	1.8155	1.3127	-0.8477	-1.8618
2N	-0.7577	-0.9272	-1.5182	-2.4698
3N	0.5968	-0.4488	-1.8968	-2.0912
4N	1.2163	-1.5700	-3.0445	-4.1177

Table 11: Formation energy (eV) of Si bulk and $\Sigma 3\{111\}$ Si GB without/with vacancies V1 and V2 with interstitial N atoms from 1 to 4. The values are reported for the lowest energy structures.

X	$E_g^{Si-bulk}$	E_g^{GB}	E_g^{V1GB}	E_g^{V2GB}
1N	0	0	0	0
2N	0.5427	0.5444	0.2439	0.6191
3N	0	0	0	0
4N	0.3464	0.6274	0.3966	0.6397

Table 12: Energy gaps (eV) of Si bulk and $\Sigma 3\{111\}$ Si GB without/with vacancies V1 and V2 with interstitial N atoms from 1 to 4. The values are reported for the lowest energy structures.

X	$P(X+B)$	$P(X+GB)$	$P(X+V1GB)$	$P(X+V2GB)$
1N	2.682	2.027	1.601	0.867
2N	2.959	2.577	1.275	0.820
3N	3.161	2.850	1.054	1.327
4N	3.464	3.017	1.331	1.376

Table 13: Hydrostatic pressure (GPa) of Si bulk and $\Sigma 3\{111\}$ Si GB without/with vacancies V1 and V2 with interstitial N atoms from 1 to 4. The values are reported for the lowest energy structures.

3.2 Bonding analysis

Si-Bulk	BC(Si-Si)	BL(Si-Si)Å	BC(Si-N)	BL(Si-N)Å	BC(N-N)	BL(N-N)Å	LP
1N	2.0478 1.9314 1.9270 2.0029 2.0013 2.0181 1.9412 1.9427	2.33613 2.32035 2.32165 2.35253 2.35318 2.35985 2.33676 2.33660	2.4274 2.4141	1.66719 1.66703			2.4509
2N	2.0849 2.0843 2.0843 2.0849 2.0244 2.0239	2.30713 2.30644 2.30645 2.30701 2.31767 2.31746	2.2752 2.2956 2.0008 2.0007 2.0293 2.0508	1.73464 1.73455 1.73999 1.73986 1.76801 1.76801			N1: 1.4121 N2: 1.3700
3N	2.0352 2.0792 2.0869 2.0827 2.0912 2.0617 2.0273 2.0109	2.28999 2.30490 2.31795 2.33198 2.30624 2.28782 2.31692 2.31369	2.2909 2.3008 1.9742 2.0136 1.9209 2.1595 1.8634 2.0166 1.8249	1.73687 1.73777 1.74611 1.74460 1.76536 1.76647 1.73632 1.76668 1.78669			N1: 0.7259 N2: 0.8651 N3: 1.9743
4N	2.0829 2.0801 2.0871 2.1036 2.1494 2.1334 1.9851	2.33553 2.32301 2.29693 2.30566 2.25315 2.35389 2.30198	2.3121 2.3443 2.0021 2.0234 1.9686 1.9389 2.2747 1.9527 2.0948 2.0943 1.9726 1.7351	1.73744 1.71281 1.75323 1.74916 1.75665 1.77627 1.72530 1.74615 1.76061 1.77118 1.73255 1.76306			N1: 1.2854 N2: 1.3015 N3: 1.5256 N4: 1.9553

Table 14: Bond charge(BC), bond length (BL) and lone pair(LP) data for Si-Si, Si-N and N-N bonds with the inclusion of n numbers of N atoms (n=1,2,3 & 4) in Si-bulk.

Si-GB	BC(Si-Si)	BL(Si-Si)Å	BC(Si-N)	BL(Si-N)Å	BC(N-N)	BL(N-N)Å	LP
1N	2.0376 2.0375 2.0492 2.0493 2.0331 2.1035 2.1035 2.0271	2.32647 2.32636 2.32064 2.32045 2.45711 2.31514 2.31462 2.43737	2.0010 1.9200 1.7552	1.76298 1.74187 1.76611			1.9985
2N	2.0834 2.0832 2.0883 2.0881 2.0104 2.0247	2.31385 2.31385 2.31135 2.31135 2.31162 2.32479	2.3180 2.5108 2.1484 2.0497 1.9979 1.9923	1.73044 1.72975 1.74457 1.74220 1.77111 1.76485			N1: 1.3607 N2: 1.0621
3N	2.1013 2.0927 2.0902 2.0275 2.0207 2.0532	2.29004 2.31424 2.30417 2.32465 2.33297 2.35819	2.1939 2.2970 2.6832 2.4427 2.2157 2.1275 2.0487 1.8478 1.9054	1.74968 1.72659 1.71560 1.74610 1.74352 1.73394 1.71729 1.75508 1.79481			N1: 1.1192 N2: 1.2278 N3: 1.1573
4N	2.1249 2.0931 2.0432 2.0634 2.0821 2.0068	2.27680 2.30091 2.30684 2.30310 2.34419 2.31122	2.4731 2.1082 2.3015 2.4608 2.3014 2.0111 2.1785 2.2933 1.9397 2.0967 1.9236 1.9361	1.73868 1.76076 1.72478 1.72397 1.74044 1.75477 1.74475 1.78921 1.77425 1.73882 1.77890 1.77797			N1: 1.4252 N2: 1.0691 N3: 1.1897 N4: 1.2506

Table 15: Bond charge(BC), bond length (BL) and lone pair(LP) data for Si-Si, Si-N and N-N bonds with the inclusion of n numbers of N atoms (n=1,2,3 & 4) in Si-GB.

	Si-VGB	BC(Si-Si)	BL(Si-Si)Å	BC(Si-N)	BL(Si-N)Å	BC(N-N)	BL(N-N)Å	LP		
V1	1N	2.0247	2.41953	2.3100	1.69449			2.9121		
		2.0197	2.43623	2.2639	1.69582					
		2.0010	2.35263							
		2.0038	2.34135							
		2.0009	2.35266							
		1.9653	2.38943							
		1.9649	2.38938							
		2.0462	2.30787							
		1.9577	2.38419							
		1.9570	2.38426							
		2.0887	2.32091							
		2.0894	2.31500							
		1.9718	2.30958							
	2N	2.0434	2.34686	1.7099	1.80391	1.0824	1.45049	N1: 2.8568 N2: 3.1440		
		2.0256	2.41936	1.6528	1.80577					
		2.0453	2.34935	1.5105	1.83934					
		2.0452	2.34960	1.5587	1.83902					
		2.0501	2.33689							
		2.0484	2.35730							
		2.0241	2.44403							
		2.0094	2.34903							
		1.9838	2.33999							
		1.9960	2.55257							
		3N	2.0773	2.41155	2.3000	1.73292				N1: 2.0548 N2: 2.7514 N3: 1.4688
			2.0422	2.37194	1.9799	1.82098				
			2.0225	2.33420	1.9268	1.78660				
	2.0439		2.40624	2.3839	1.68197					
	1.9813		2.31695	1.9969	1.79269					
	2.0262		2.37227	2.3275	1.70177					
	2.0281		2.42340	1.9324	1.81505					
	2.0372		2.40966	1.7521	1.84096					
	2.0574		2.48591							
	4N		2.1485	2.46424	2.0854	1.74349			N1: 1.8152 N2: 1.2873 N3: 1.2731 N4: 2.2097	
		2.0467	2.35171	2.0270	1.73643					
		2.0365	2.42135	2.0928	1.77086					
		2.0349	2.38921	2.1196	1.75251					
2.0348		2.41911	1.9919	1.77712						
2.0138		2.36413	2.0611	1.79525						
1.9812		2.32272	2.0450	1.79535						
2.0344		2.49119	1.8110	1.76966						
			2.2998	1.80866						
			1.8331	1.84124						
			2.3149	1.77682						
			1.6849	1.80845						

Table 16: Bond charge(BC), bond length (BL) and lone pair(LP) data for Si-Si, Si-N and N-N bonds with the inclusion of n numbers of N atoms (n=1,2,3 & 4) in Si-GB with vacancy V1.

	Si-VGB	BC(Si-Si)	BL(Si-Si)Å	BC(Si-N)	BL(Si-N)Å	BC(N-N)	BL(N-N)Å	LP
V2	1N	2.0564	2.36784	1.9553	1.87247			N: 1.6904 Si: 0.4432
		2.0509	2.40413	1.9558	1.87367			
		2.0493	2.40528	1.9353	1.86030			
		2.0511	2.38624					
		2.0483	2.38886					
		1.9908	2.40434					
		1.9654	2.40723					
		2.1537	2.33401					
		2.1767	2.33784					
		2.2444	2.32922					
	2N	2.0061	2.31947	2.0590	1.76352			N1: 1.8892 N2: 1.9015
		2.0063	2.31967	2.0490	1.76331			
		2.0476	2.36605	1.9409	1.80508			
		2.0227	2.33318	1.9121	1.80526			
		2.0426	2.45558	1.7975	1.82537			
		2.0550	2.53332	1.7913	1.82514			
		2.0549	2.53382					
		2.0252	2.36235	2.4391	1.75975			
		2.0156	2.33604	1.9526	1.77458			
		2.0422	2.35106	2.7003	1.65230			
	3N	2.0451	2.35443	1.9947	1.77620			N1: 1.2519 N2: 2.1413 N3: 2.1548
		2.0241	2.38609	2.0178	1.78340			
		2.0507	2.43521	2.5160	1.66644			
		2.0473	2.41717	1.8130	1.79287			
		2.0488	2.51035	1.7839	1.81480			
		2.0415	2.51595					
		1.7991	2.35569					
		2.0319	2.28568	2.2734	1.73678			
		2.1039	2.42680	2.1041	1.75573			
		2.0438	2.26015	2.1349	1.76866			
	4N	2.0431	2.35302	2.0410	1.74235			N1: 1.8719 N2: 1.3477 N3: 1.2853 N4: 2.0208
		2.0439	2.35439	2.4054	1.75972			
		2.0269	2.37705	1.9884	1.77301			
		1.9962	2.33643	2.0737	1.76081			
		2.0385	2.42899	1.9729	1.78870			
		2.0439	2.42410	1.8965	1.77478			
2.0702		2.47255	1.9491	1.77956				
2.0709		2.51903	1.8610	1.79077				
2.0000		2.46747	1.7530	1.80498				

Table 17: Bond charge(BC), bond length (BL) and lone pair(LP) data for Si-Si, Si-N and N-N bonds with the inclusion of n numbers of N atoms (n=1,2,3 & 4) in Si-GB with vacancy V2.

4 Systems with interstitial oxygen impurities

4.1 Electronic properties

X	E_f^{XB}	E_f^{XGB}	E_f^{XV1GB}	E_f^{XV2GB}
1O	-2.3649	-2.3950	-4.3281	-4.3036
2O	-5.2126	-5.2515	-7.9224	-7.8855
3O	-8.3195	-8.3974	-11.2368	-11.2213
4O	-11.0994	-11.1843	-14.2579	-14.5924

Table 18: Formation energy (eV) of Si bulk and $\Sigma 3\{111\}$ Si GB without/with vacancies V1 and V2 with interstitial O atoms from 1 to 4. The values are reported for the lowest energy structures.

X	$E_g^{Si-bulk}$	E_g^{GB}	E_g^{V1GB}	E_g^{V2GB}
1O	0.6086	0.5506	0.6274	0.6283
2O	0.5913	0.6073	0.6353	0.6292
3O	0.7285	0.6185	0.6306	0.6319
4O	0.7430	0.5569	0.6850	0.6989

Table 19: Energy gaps (eV) of Si bulk and $\Sigma 3\{111\}$ Si GB without/with vacancies V1 and V2 with interstitial O atoms from 1 to 4. The values are reported for the lowest energy structures.

X	$P(X+B)$	$P(X+GB)$	$P(X+V1GB)$	$P(X+V2GB)$
1O	2.776	2.413	1.697	1.692
2O	3.157	2.660	2.325	2.282
3O	3.479	2.864	2.981	2.616
4O	4.121	3.064	3.171	2.849

Table 20: Hydrostatic pressure (GPa) of Si bulk and $\Sigma 3\{111\}$ Si GB without/with vacancies V1 and V2 with interstitial O atoms from 1 to 4. The values are reported for the lowest energy structures.

4.2 Bonding analysis

Si-Bulk	BC(Si-Si)	BL(Si-Si)Å	BC(Si-O)	BL(Si-O)Å	LP
1O	1.9918	2.32115	1.7489	1.63550	O1: 4.283
	2.0069	2.32194	1.7479	1.63423	
	2.0467	2.32461			
	2.0555	2.32523			
2O	2.0789	2.30065	1.8939	1.64273	O1: 4.2801
	2.0795	2.30074	1.7391	1.66098	O2: 4.3145
	2.0221	2.32101	1.7493	1.63986	
	1.9685	2.31220	1.5902	1.67594	
	2.0680	2.33876			
	2.0681	2.33886			
	2.0950	2.33589			
3O	2.1373	2.24814	1.9606	1.62698	O1: 4.3299
	1.9904	2.30827	1.9473	1.62684	O2: 4.3404
	2.0606	2.33173	1.9752	1.62684	O3: 4.3299
	2.0602	2.33169	1.5148	1.68729	
	2.0598	2.33175	1.5429	1.68740	
	2.0714	2.35013	1.5191	1.68737	
	2.0710	2.34967			
4O	2.0971	2.22921	1.9675	1.63190	O1: 4.2585
	2.0108	2.32069	1.9450	1.62957	O2: 4.1269
	2.0322	2.32228	1.9281	1.62211	O3: 4.2659
	1.9837	2.30422	1.7651	1.66014	O4: 4.3555
	2.0497	2.33004	1.7301	1.63470	
	2.0734	2.34109	1.7331	1.65317	
			1.6537	1.66647	
			1.5824	1.68762	

Table 21: Bond charge(BC), bond length (BL) and lone pair(LP) data for Si-Si and Si-O bonds with the inclusion of n numbers of O atoms (n=1,2,3 & 4) in Si-bulk.

Si-GB	BC(Si-Si)	BL(Si-Si)Å	BC(Si-O)	BL(Si-O)Å	LP
1O	2.0093	2.32532	1.7792	1.63913	4.2934
	1.9902	2.32383	1.7035	1.63789	
	2.0134	2.33911			
	2.0425	2.32990			
	2.0564	2.32704			
	2.0781	2.32612			
	1.9997	2.32640			
	1.9931	2.34696			
	1.9959	2.36746			
2O	2.0872	2.31206	1.9142	1.64514	O1: 4.3003 O2: 4.3380
	2.0250	2.32108	1.7951	1.64091	
	2.0197	2.32159	1.7078	1.66111	
	2.0920	2.31034	1.5149	1.67498	
	2.0950	2.33289			
	2.0132	2.35452			
	2.0226	2.32704			
	1.9877	2.36383			
	1.9847	2.32704			
1.9957	2.35741				
3O	2.1448	2.25427	1.9600	1.62934	O1: 4.2309 O2: 4.3284 O3: 4.3491
	2.1231	2.28737	2.0395	1.62583	
	2.0699	2.34079	1.9255	1.63628	
	2.0687	2.36253	1.5670	1.68212	
	2.0445	2.33292	1.5497	1.68240	
	2.0624	2.34653	1.5057	1.69960	
	1.9502	2.32814			
	1.9914	2.33156			
	1.9873	2.33906			
4O	1.9968	2.30698	2.1162	1.60775	O1: 4.1798 O2: 4.3162 O3: 4.4751 O4: 4.3444
	2.0109	2.31411	1.9557	1.60825	
	2.0089	2.29839	2.0040	1.60321	
	2.0324	2.32370	1.9907	1.61242	
	2.0459	2.36708	1.5109	1.69476	
	2.0352	2.32384	1.5546	1.69474	
	2.0739	2.37431	1.5502	1.69645	
	2.1489	2.29031	1.4290	1.71093	
	1.9766	2.33417			

Table 22: Bond charge(BC), bond length (BL) and lone pair(LP) data for Si-Si and Si-O bonds with the inclusion of n numbers of O atoms (n=1,2,3 & 4) in Si-GB

	Si-VGB	BC(Si-Si)	BL(Si-Si)Å	BC(Si-O)	BL(Si-O)Å	LP
V1	1O	2.0433	2.35933	1.5763	1.70276	4.8177
		2.0432	2.35930	1.4038	1.70352	
		2.0504	2.34937			
		2.0503	2.34933			
		2.0493	2.41995			
		2.0374	2.44706			
		2.0781	2.32314			
		2.0788	2.31593			
		2.0029	2.31171			
		2O	2.0854	2.34609	1.8687	
	2.0853		2.34610	1.6492	1.68177	
	1.9984		2.31011	1.7409	1.66199	
	2.0531		2.38759	1.6583	1.66506	
	2.0612		2.35561			
	2.0613		2.35561			
	2.0745		2.32627			
	2.0759		2.32289			
	2.0046		2.31500			
	1.5825		2.45085			
	3O	2.0851	2.31788	1.8948	1.62656	O1: 4.2695 O2: 4.1855 O3: 4.3248
		2.0886	2.32236	1.8150	1.63978	
		2.0016	2.31408	1.7386	1.62749	
		2.0592	2.34710	1.7672	1.63987	
		2.0592	2.34711	1.7558	1.65652	
		2.0446	2.31293	1.7408	1.65403	
		2.0107	2.32353			
		1.9913	2.34144			
		1.9769	2.33572			
		2.0050	2.31155			
	4O	2.1503	2.27352	2.0133	1.62843	O1: 4.1015 O2: 4.1822 O3: 4.2785 O4: 4.2594
		2.0809	2.31442	1.8618	1.62652	
		2.0001	2.31435	1.8409	1.64666	
		1.9944	2.30186	1.7146	1.66121	
		2.0569	2.32987	1.9526	1.62095	
		2.0262	2.30338	1.8908	1.62452	
		2.0582	2.34486	1.7483	1.65339	
2.0608		2.34711	1.5363	1.69373		
2.0576		2.38358				
2.0007		2.33742				
1.9774	2.34089					

Table 23: Bond charge(BC), bond length (BL) and lone pair(LP) data for Si-Si and Si-O bonds with the inclusion of n numbers of O atoms (n=1,2,3 & 4) in Si-GB with vacancy V1.

	Si-VGB	BC(Si-Si)	BL(Si-Si)Å	BC(Si-O)	BL(Si-O)Å	LP
V2	1O	2.0490	2.35202	1.5907	1.70536	4.7927
		2.0490	2.35202	1.4133	1.70324	
		2.0389	2.34423			
		2.0479	2.39899			
		2.0479	2.39899			
		2.0459	2.42851			
		2.0673	2.32292			
		2.0017	2.31335			
		1.5752	2.43705			
	2O	2.0916	2.34935	1.7851	1.63329	O1: 4.3862 O2: 4.3375
		2.0916	2.34935	1.6953	1.66673	
		2.0257	2.32115	1.7470	1.68194	
		2.0257	2.32115	1.6959	1.66639	
		2.0504	2.36999			
		2.0504	2.36999			
		2.0360	2.33241			
2.0735		2.37747				
2.0611		2.32703				
3O	2.0823	2.30486	1.8844	1.65237	O1: 4.4063 O2: 4.2758 O3: 4.3626	
	2.0826	2.30432	1.7179	1.64360		
	2.0494	2.35862	1.6933	1.64503		
	2.0494	2.35862	1.7372	1.66772		
	2.0304	2.32693	1.7276	1.66736		
	2.0309	2.32429	1.6871	1.65621		
	2.0363	2.30348				
	1.9855	2.32768				
	2.0048	2.31078				
4O	2.1604	2.33661	1.8891	1.63356	O1: 4.2751 O2: 4.1492 O3: 4.3613 O4: 4.1261	
	2.0939	2.32015	1.9768	1.61832		
	2.0371	2.34213	1.8987	1.64051		
	2.0210	2.31449	1.8329	1.66554		
	2.0529	2.36183	1.7697	1.64925		
	2.0454	2.35171	1.7404	1.65316		
	2.0487	2.34450	1.6899	1.67462		
	2.0529	2.32527	1.6799	1.67034		
	2.0686	2.32756				
	2.0095	2.32386				
	1.6214	2.41121				

Table 24: Bond charge(BC), bond length (BL) and lone pair(LP) data for Si-Si and Si-O bonds for the inclusion of n numbers of O atoms (n=1,2,3 & 4) in Si-GB with vacancy V2.

5 Bond charge variations

5.1 Nitrogen

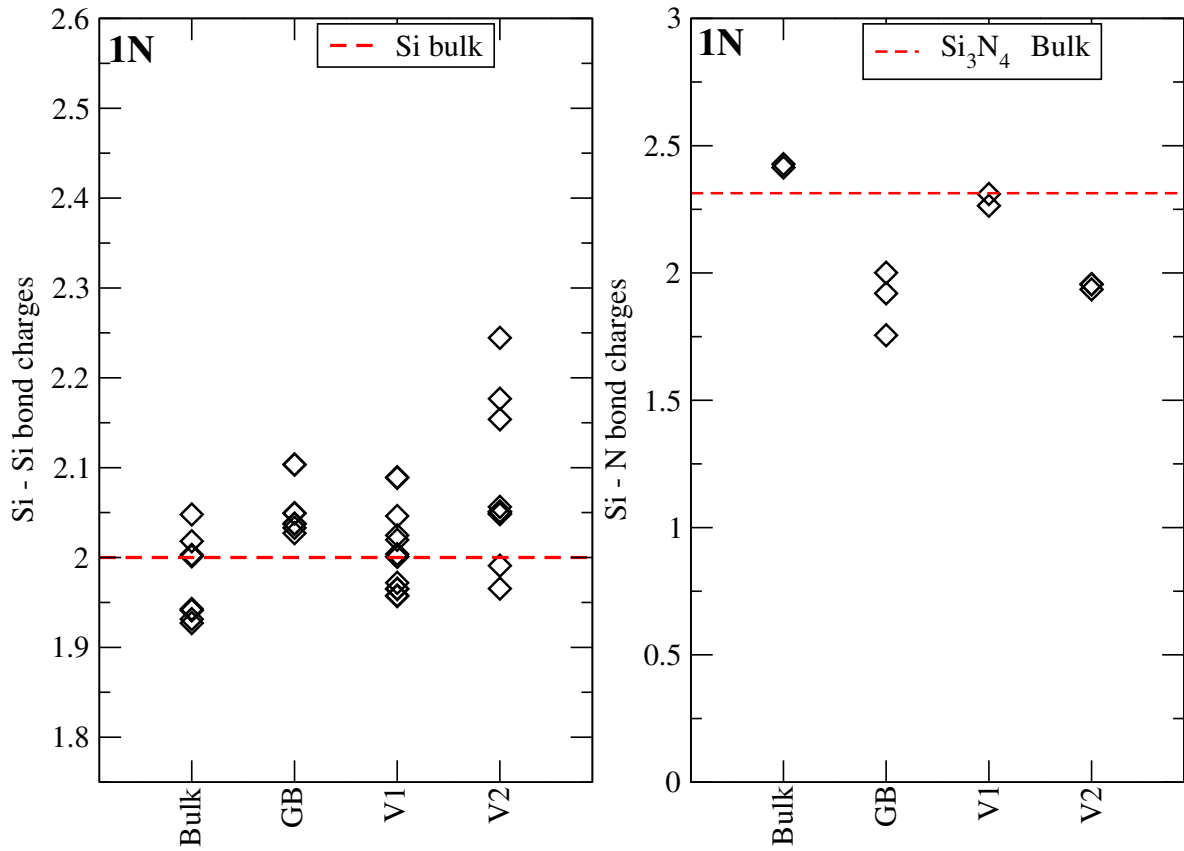


Figure 2: Bond charge variation of Si-Si and Si-N with the inclusion of one nitrogen atom in Si-bulk, Si-GB and in presence of vacancy V1 and V2. As a reference, Si-Si/Si-N bond charges from bulk phases of Si and Si_3N_4 are marked in the inset of respective plots.

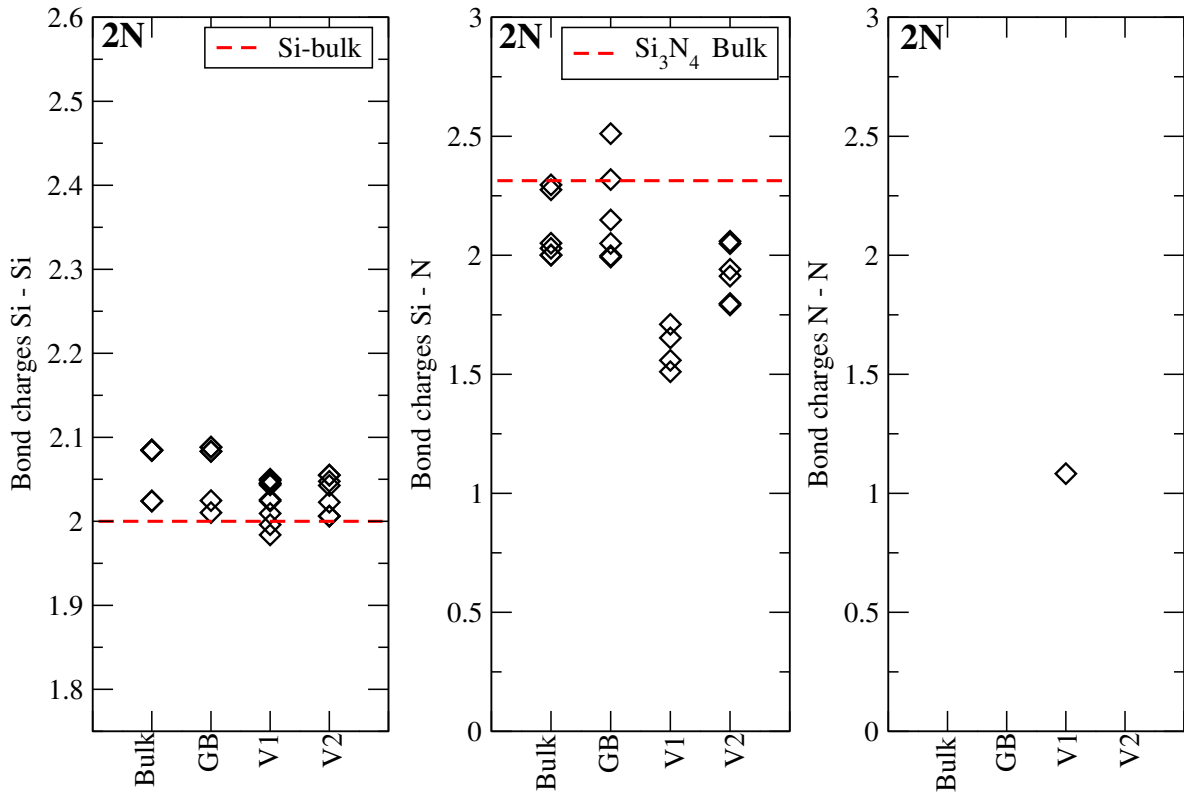


Figure 3: Bond charge variation of Si-Si, Si-N and N-N for the inclusion of two nitrogen atoms in Si-bulk, Si-GB and in presence of vacancy V1 and V2. As a reference, Si-Si/Si-N bond charges from bulk phases of Si and Si_3N_4 are marked in the inset of respective plots.

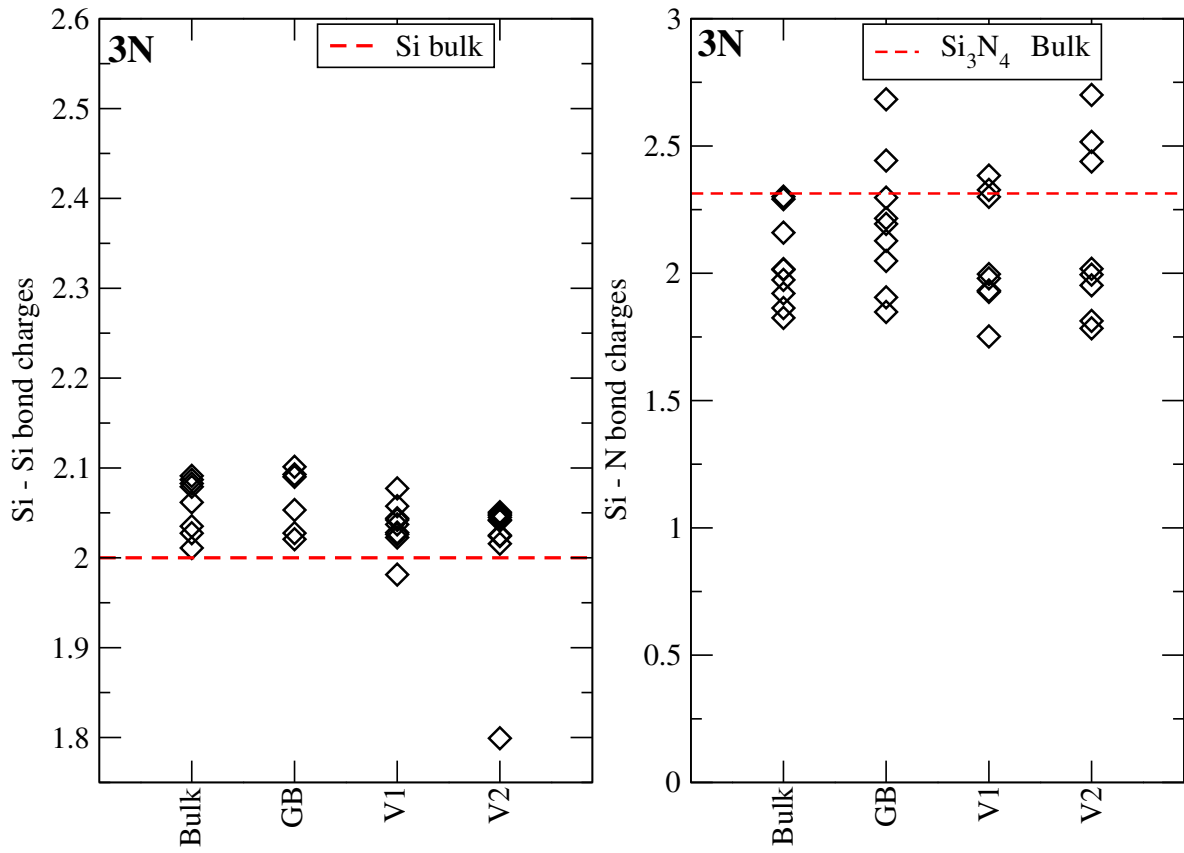


Figure 4: Bond charge variation of Si-Si and Si-N for the inclusion of three nitrogen atoms in Si-bulk, Si-GB and in presence of vacancy V1 and V2. As a reference, Si-Si/Si-N bond charges from bulk phases of Si and Si₃N₄ are marked in the inset of respective plots.

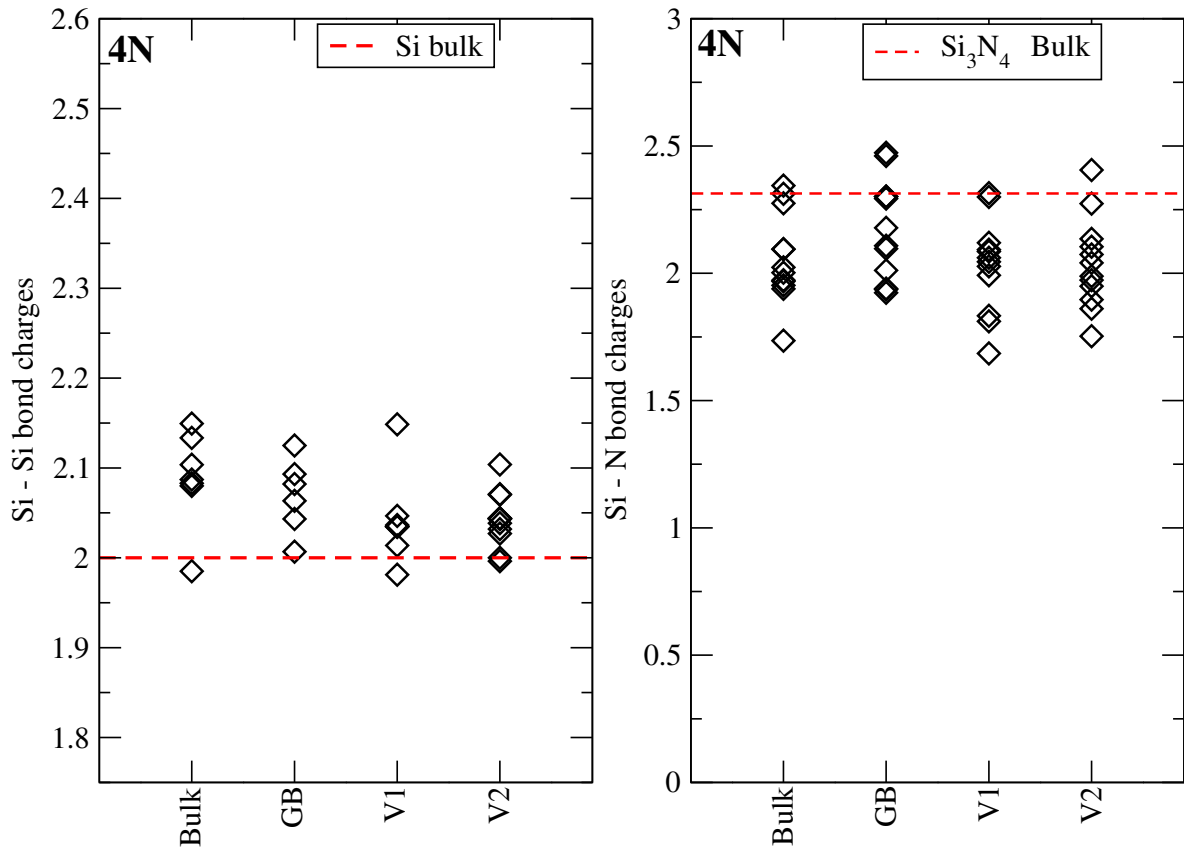


Figure 5: Bond charge variation of Si-Si and Si-N for the inclusion of four nitrogen atoms in Si-bulk, Si-GB and in presence of vacancy V1 and V2. As a reference, Si-Si/Si-N bond charges from bulk phases of Si and Si₃N₄ are marked in the inset of respective plots.

5.2 Oxygen

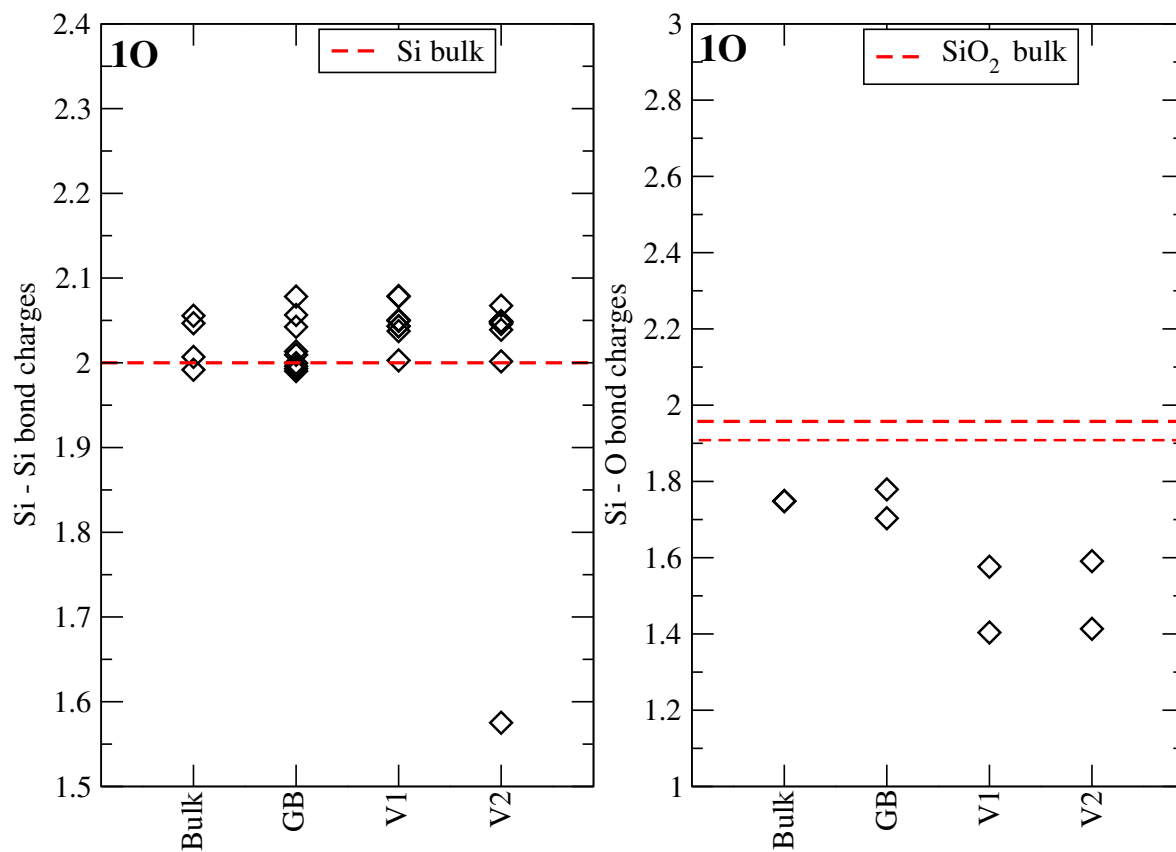


Figure 6: Bond charge variation of Si-Si and Si-O for the inclusion of one oxygen atom in Si-bulk, Si-GB and in presence of vacancy V1 and V2. As a reference, Si-Si/Si-O bond charges from bulk phases of Si and SiO₂ are marked in the inset of respective plots.

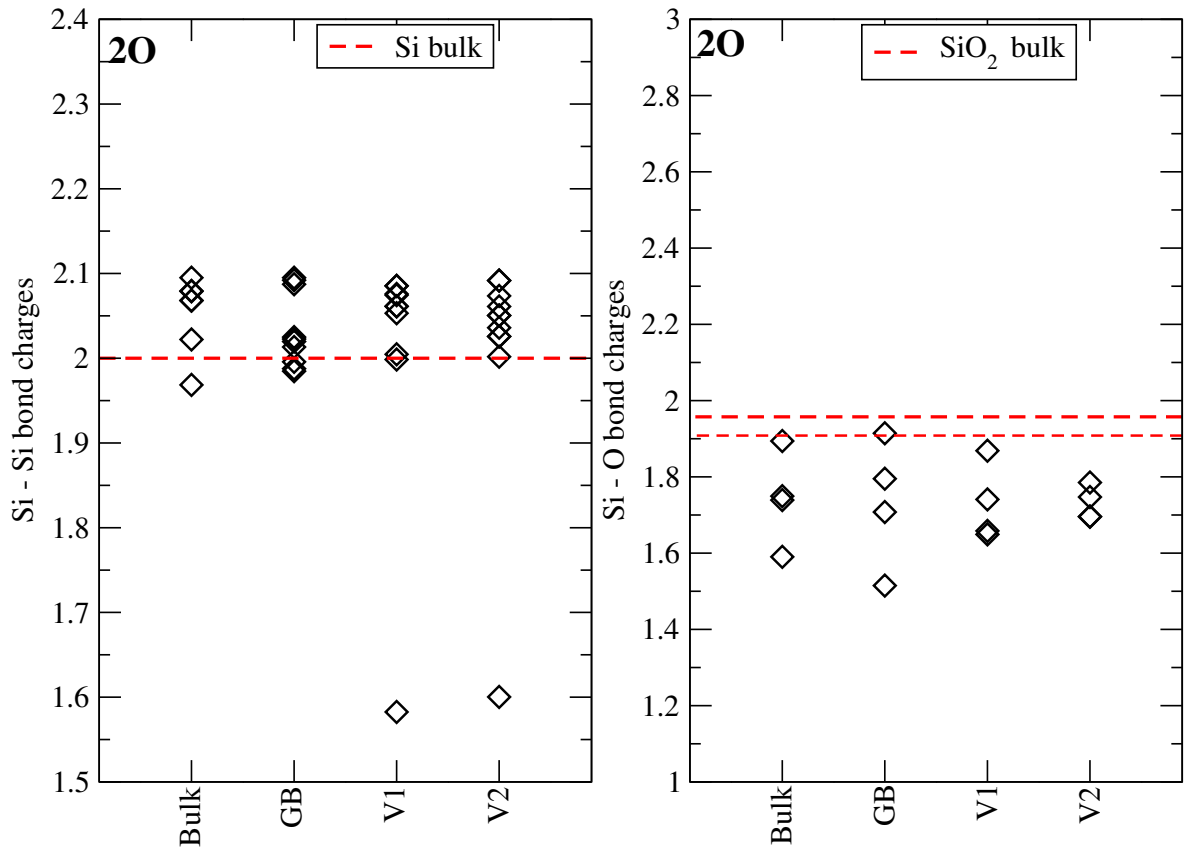


Figure 7: Bond charge variation of Si-Si and Si-O for the inclusion of two oxygen atoms in Si-bulk, Si-GB and in presence of vacancy V1 and V2. As a reference, Si-Si/Si-O bond charges from bulk phases of Si and SiO₂ are marked in the inset of respective plots.

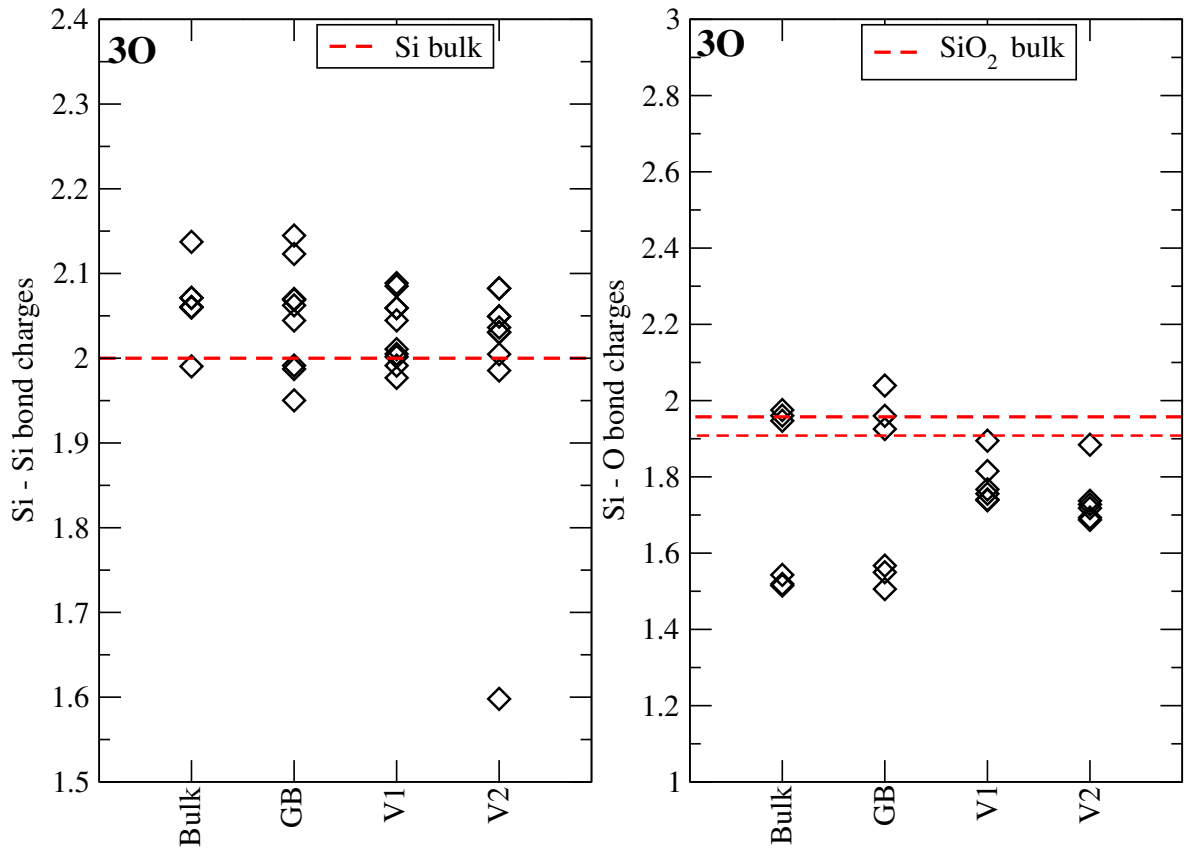


Figure 8: Bond charge variation of Si-Si and Si-O for the inclusion of three oxygen atoms in Si-bulk, Si-GB and in presence of vacancy V1 and V2. As a reference, Si-Si/Si-O bond charges from bulk phases of Si and SiO₂ are marked in the inset of respective plots.

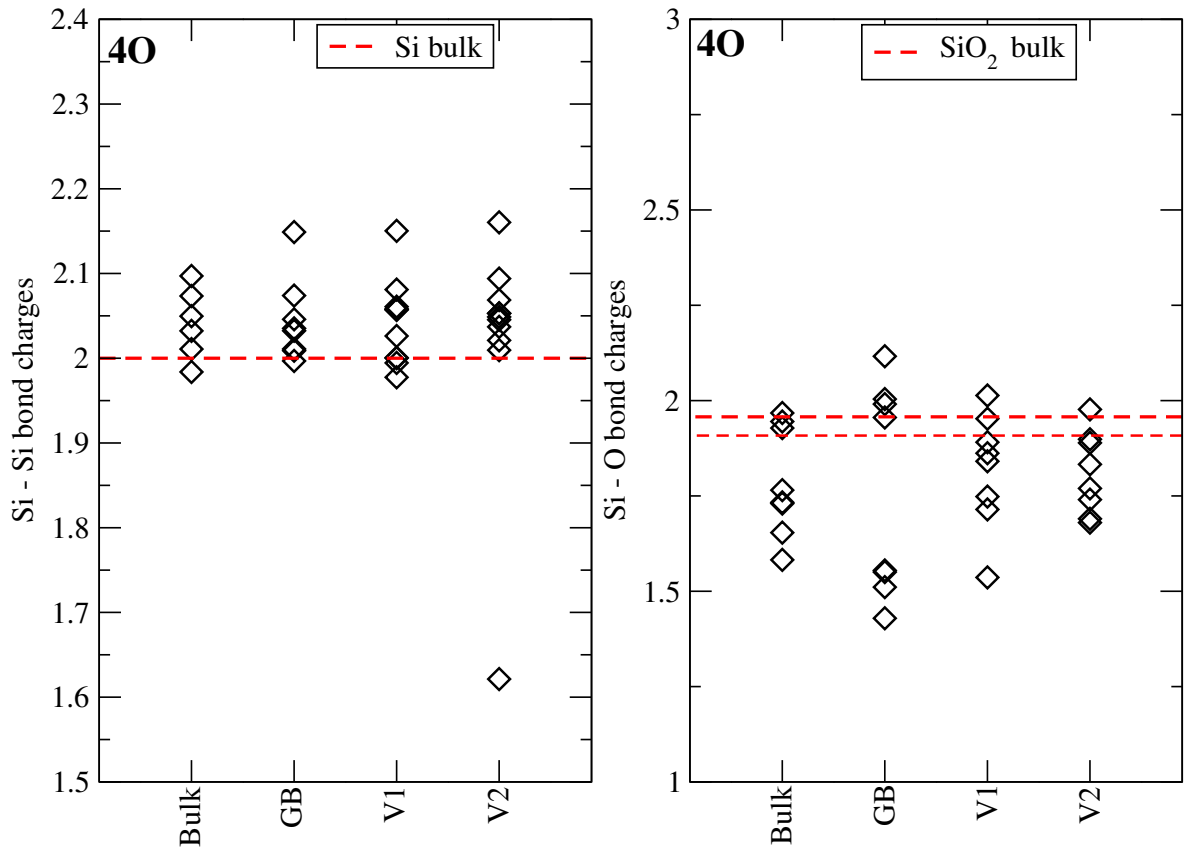


Figure 9: Bond charge variation of Si-Si and Si-O for the inclusion of four oxygen atoms in Si-bulk, Si-GB and in presence of vacancy V1 and V2. As a reference, Si-Si/Si-O bond charges from bulk phases of Si and SiO₂ are marked in the inset of respective plots.

6 Bond length variations

6.1 Carbon

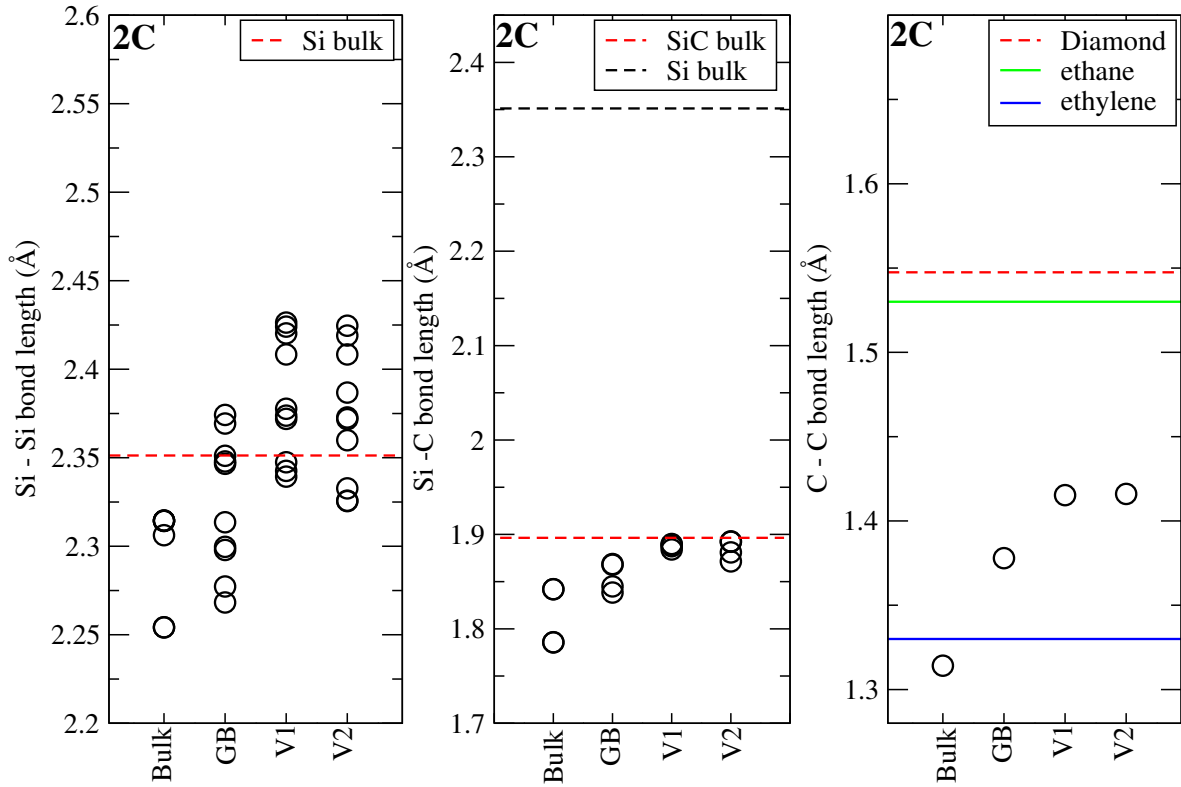


Figure 10: Bond length variation of Si-Si, Si-C and C-C for the inclusion of two carbon atoms in Si-bulk, Si-GB and in presence of vacancy V1 and V2. As a reference, Si-Si/Si-C/C-C bond length from bulk phases of Si, SiC, diamond and molecular systems ethylene and ethane are marked in the inset of respective plots.

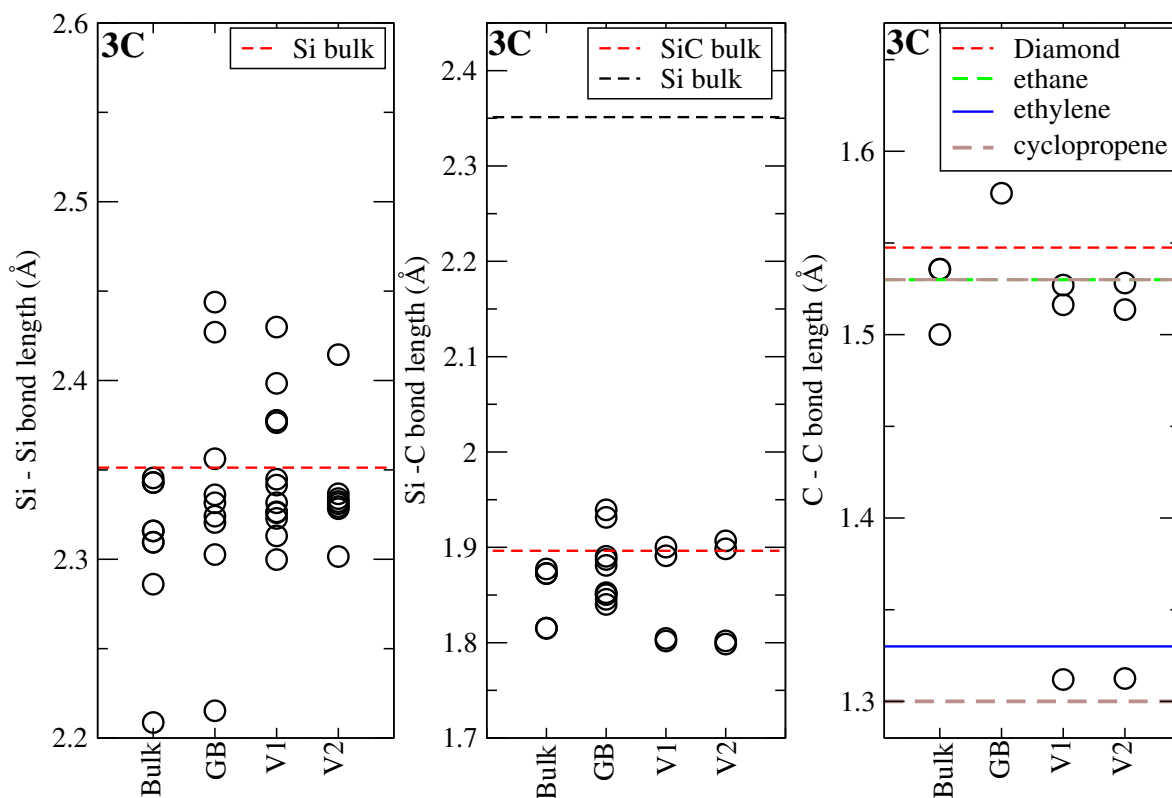


Figure 11: Bond length variation of Si-Si, Si-C and C-C for the inclusion of three carbon atoms in Si-bulk, Si-GB and in presence of vacancy V1 and V2. As a reference, Si-Si/Si-C/C-C bond length from bulk phases of Si, SiC, diamond and molecular systems ethylene, ethane, and cyclopropene are marked in the inset of respective plots

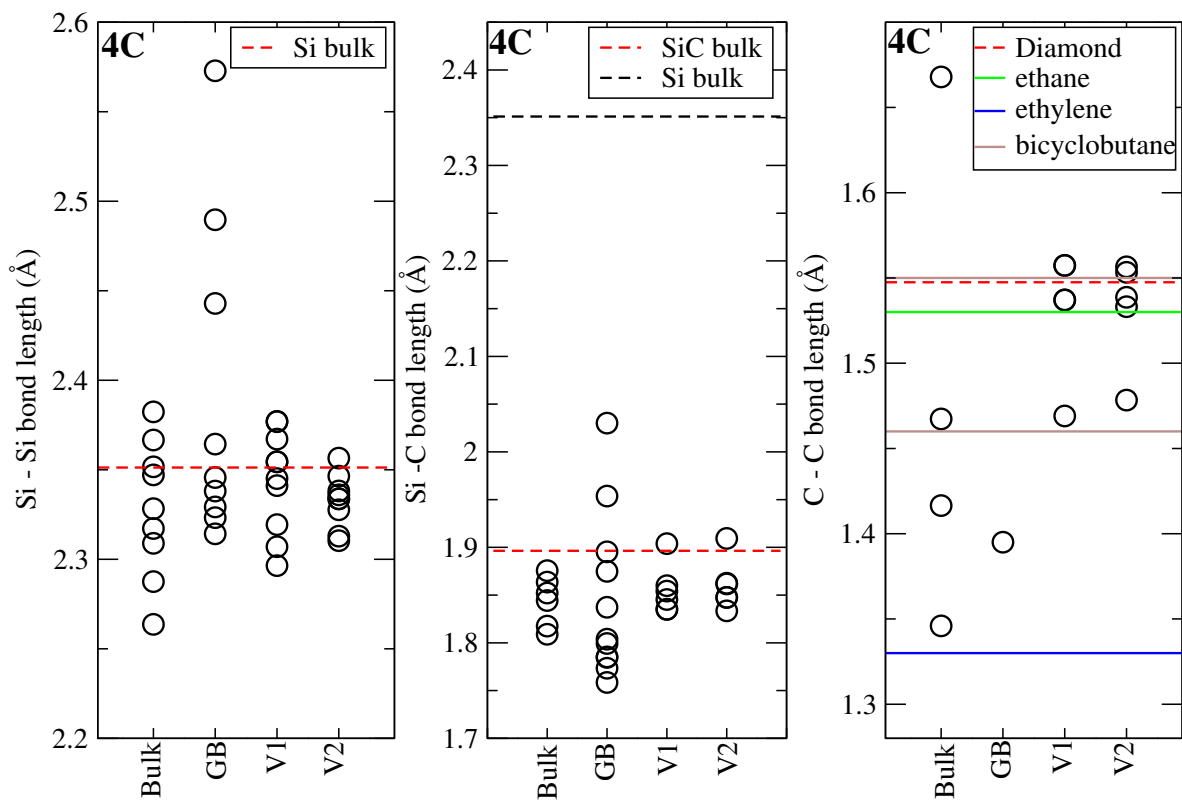


Figure 12: Bond length variation of Si-Si, Si-C and C-C for the inclusion of four carbon atoms in Si-bulk, Si-GB and in presence of vacancy V1 and V2. As a reference, Si-Si/Si-C/C-C bond length from bulk phases of Si, SiC, diamond and molecular systems ethylene, ethane, and bicyclobutane are marked in the inset of respective plots

6.2 Nitrogen

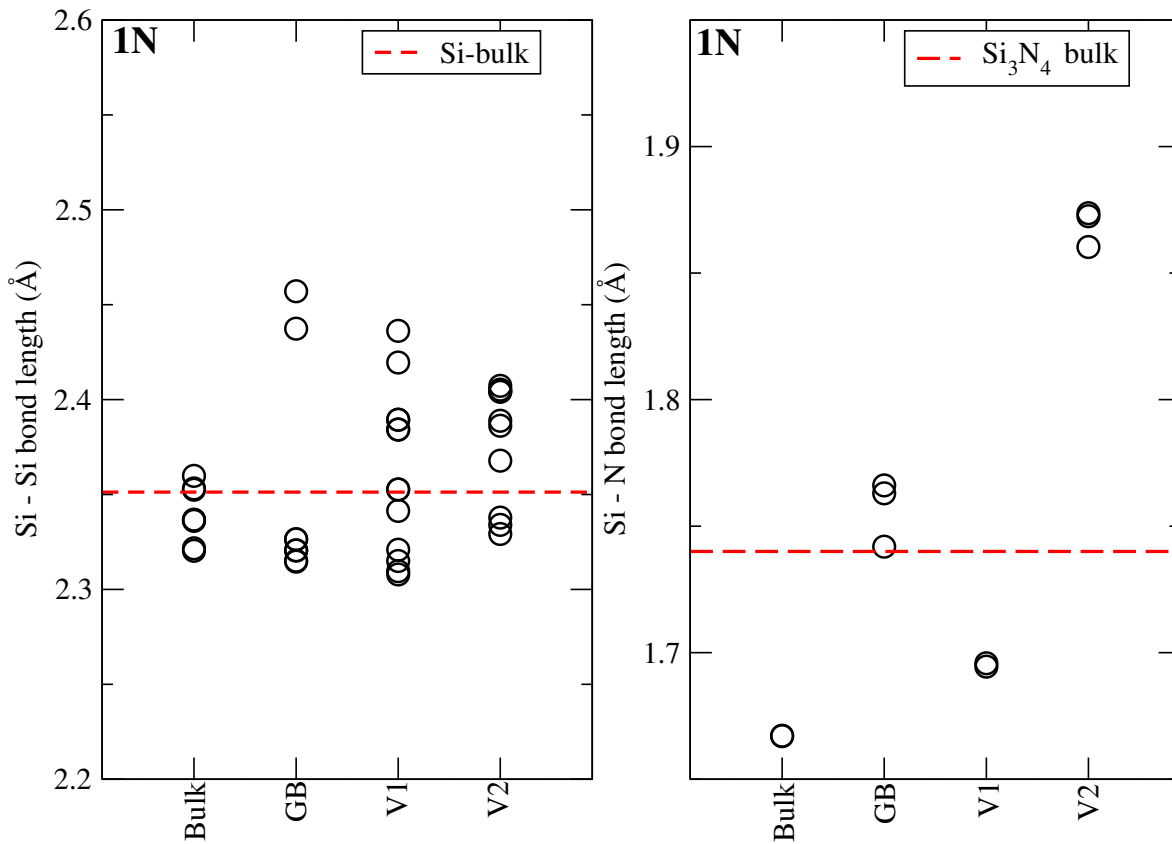


Figure 13: Bond length variation of Si-Si and Si-N for the inclusion of one nitrogen atom in Si-bulk, Si-GB and in presence of vacancy V1 and V2. As a reference, Si-Si/Si-N bond length from bulk phases of Si, Si₃N₄ are marked in the inset of respective plots.

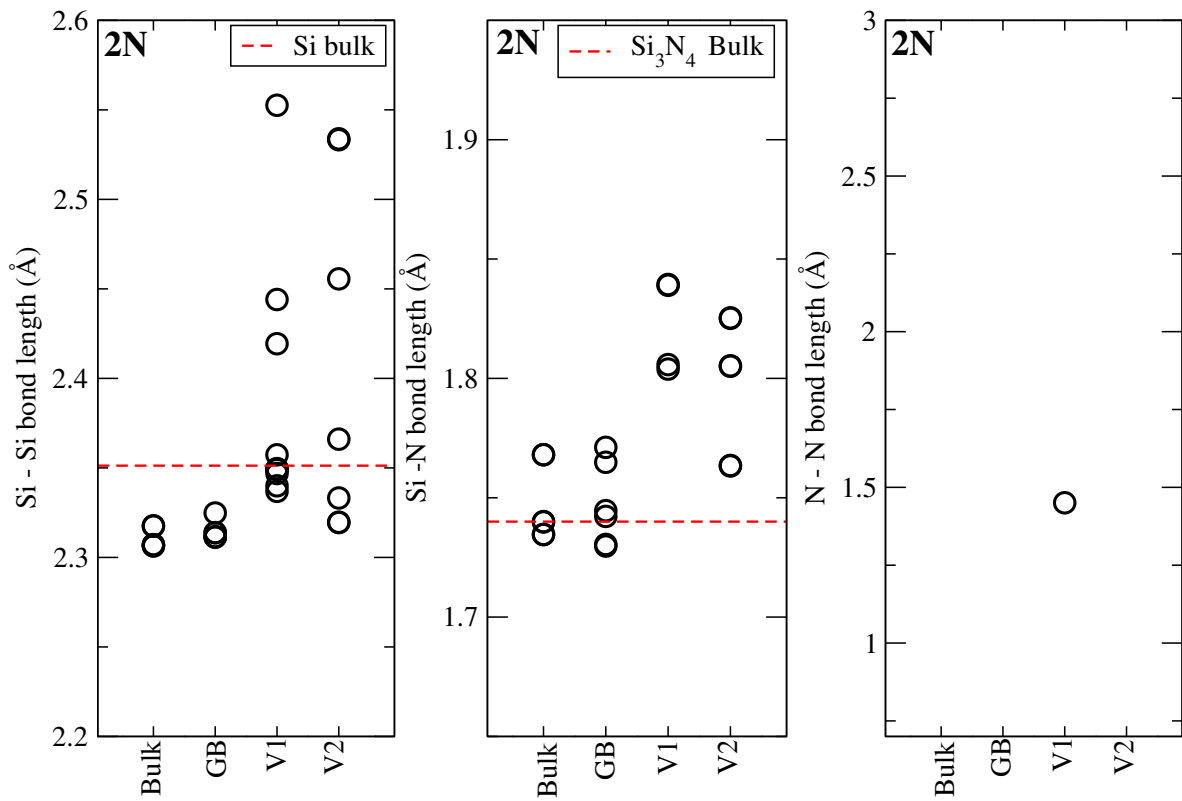


Figure 14: Bond length variation of Si-Si, Si-N and N-N for the inclusion of two nitrogen atoms in Si-bulk, Si-GB and in presence of vacancy V1 and V2. As a reference, Si-Si/Si-N bond length from bulk phases of Si, Si₃N₄ are marked in the inset of respective plots.

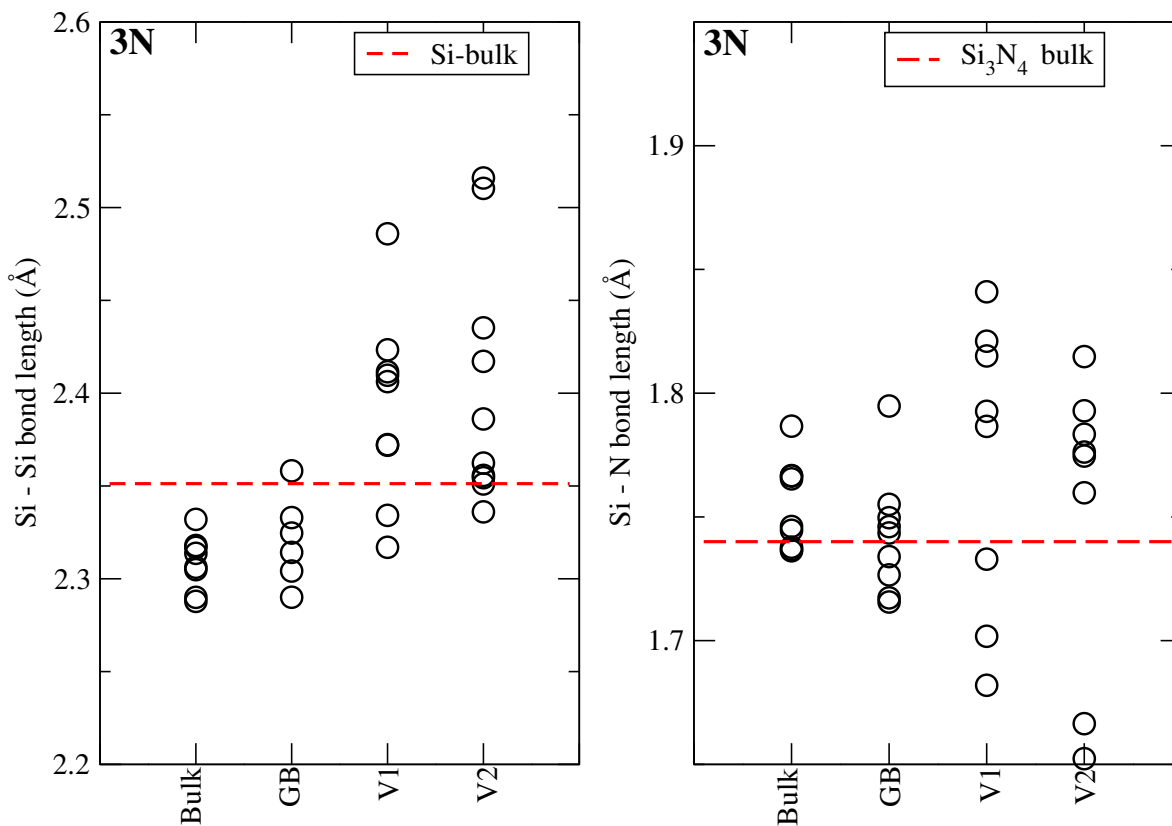


Figure 15: Bond length variation of Si-Si and Si-N for the inclusion of three nitrogen atom in Si-bulk, Si-GB and in presence of vacancy V1 and V2. As a reference, Si-Si/Si-N bond length from bulk phases of Si, Si₃N₄ are marked in the inset of respective plots.

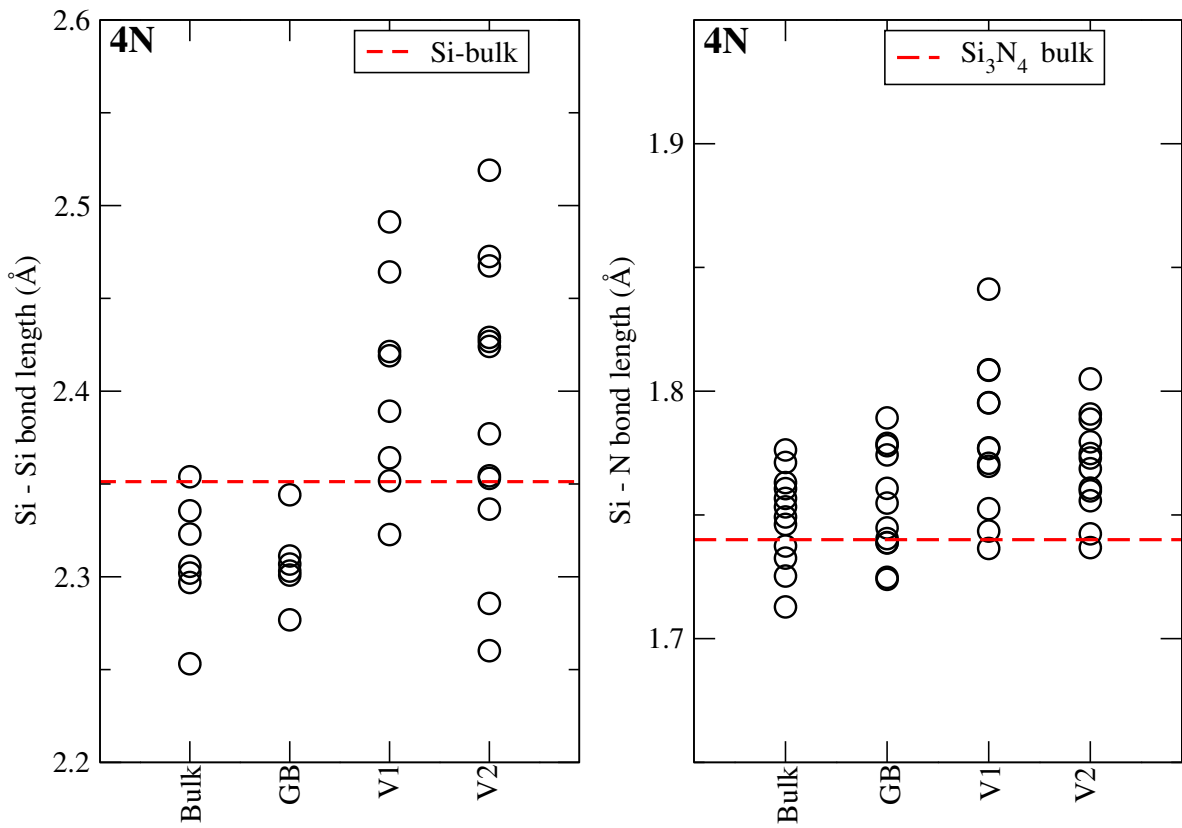


Figure 16: Bond length variation of Si-Si and Si-N for the inclusion of four nitrogen atom in Si-bulk, Si-GB and in presence of vacancy V1 and V2. As a reference, Si-Si/Si-N bond length from bulk phases of Si, Si₃N₄ are marked in the inset of respective plots.

6.3 Oxygen

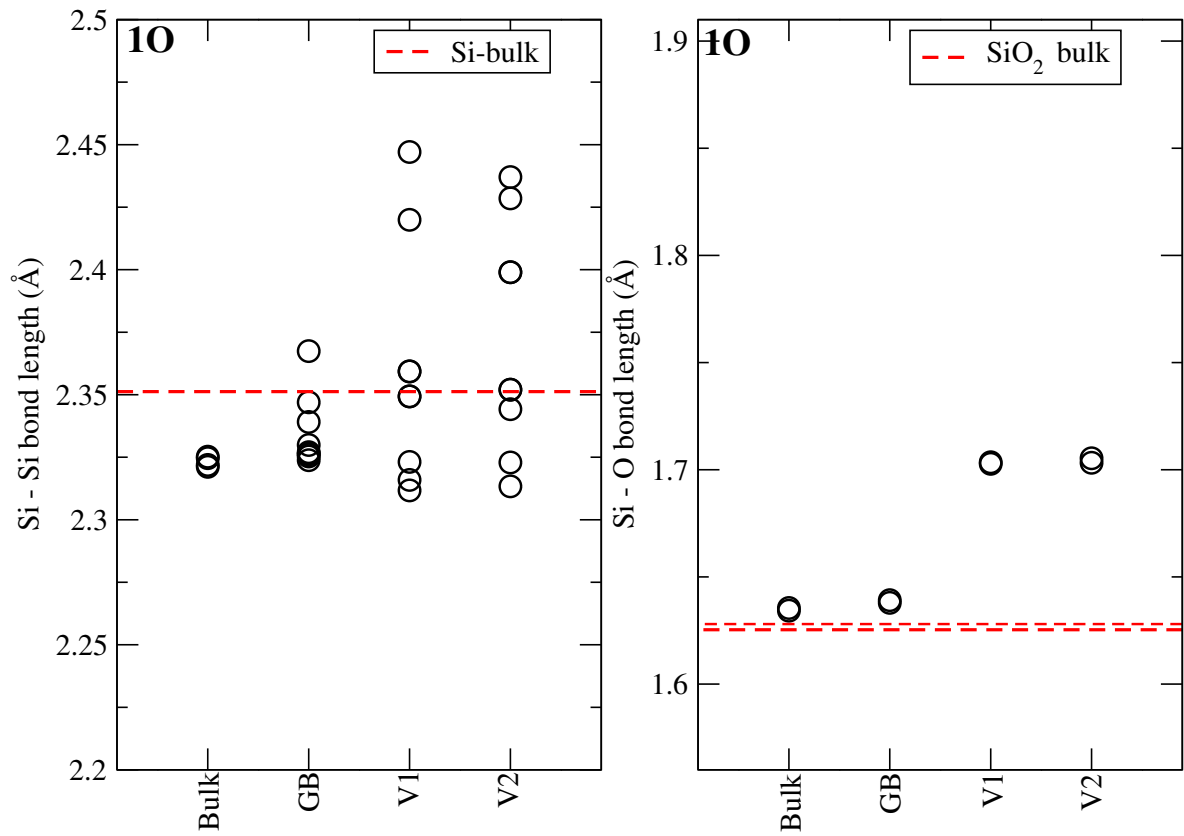


Figure 17: Bond length variation of Si-Si and Si-O for the inclusion of one oxygen atom in Si-bulk, Si-GB and in presence of vacancy V1 and V2. As a reference, Si-Si/Si-O bond length from bulk phases of Si, SiO₂ are marked in the inset of respective plots.

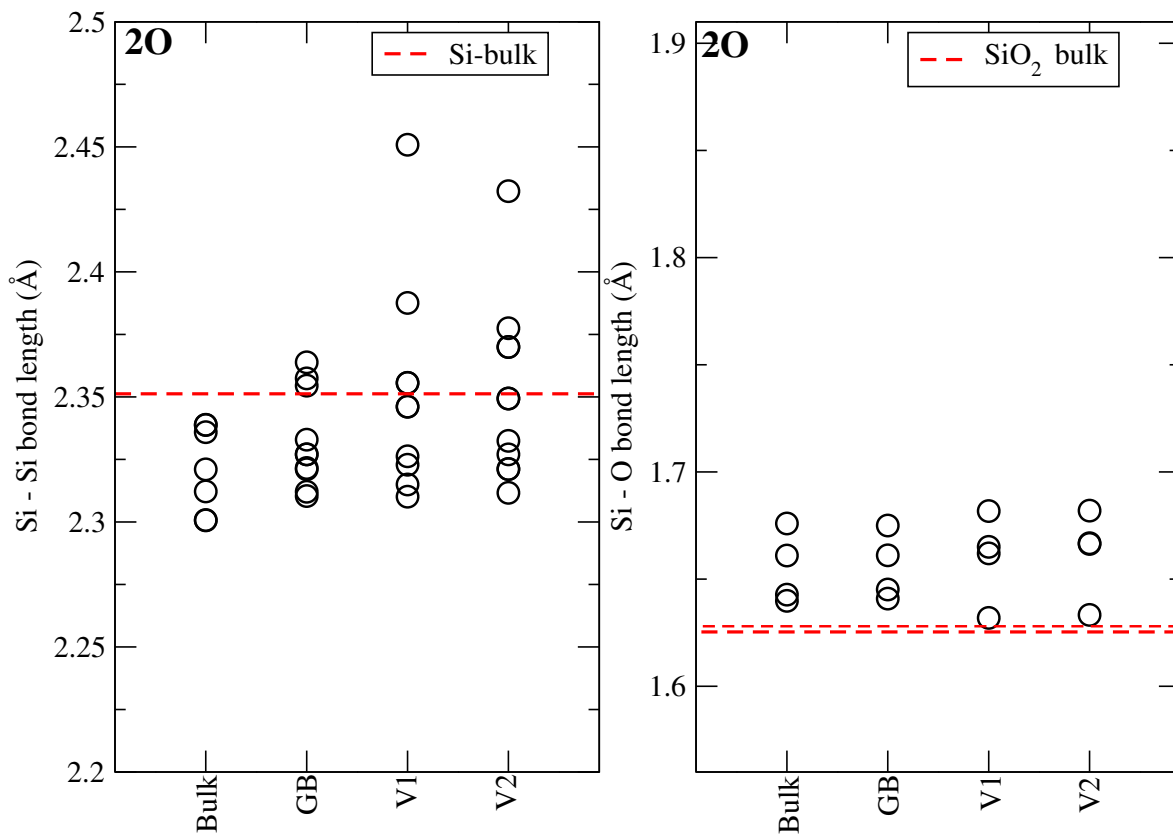


Figure 18: Bond length variation of Si-Si and Si-O for the inclusion of two oxygen atoms in Si-bulk, Si-GB and in presence of vacancy V1 and V2. As a reference, Si-Si/Si-O bond length from bulk phases of Si, SiO₂ are marked in the inset of respective plots.

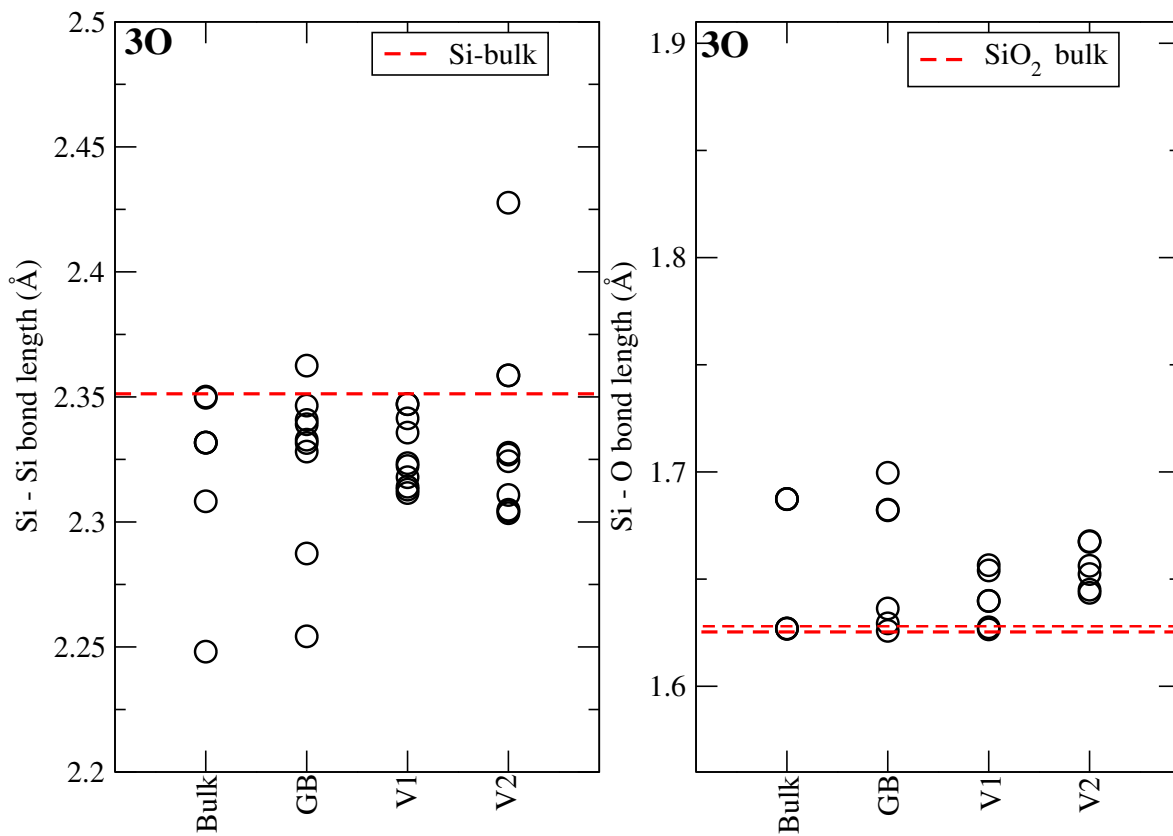


Figure 19: Bond length variation of Si-Si and Si-O for the inclusion of three oxygen atoms in Si-bulk, Si-GB and in presence of vacancy V1 and V2. As a reference, Si-Si/Si-O bond length from bulk phases of Si, SiO₂ are marked in the inset of respective plots.

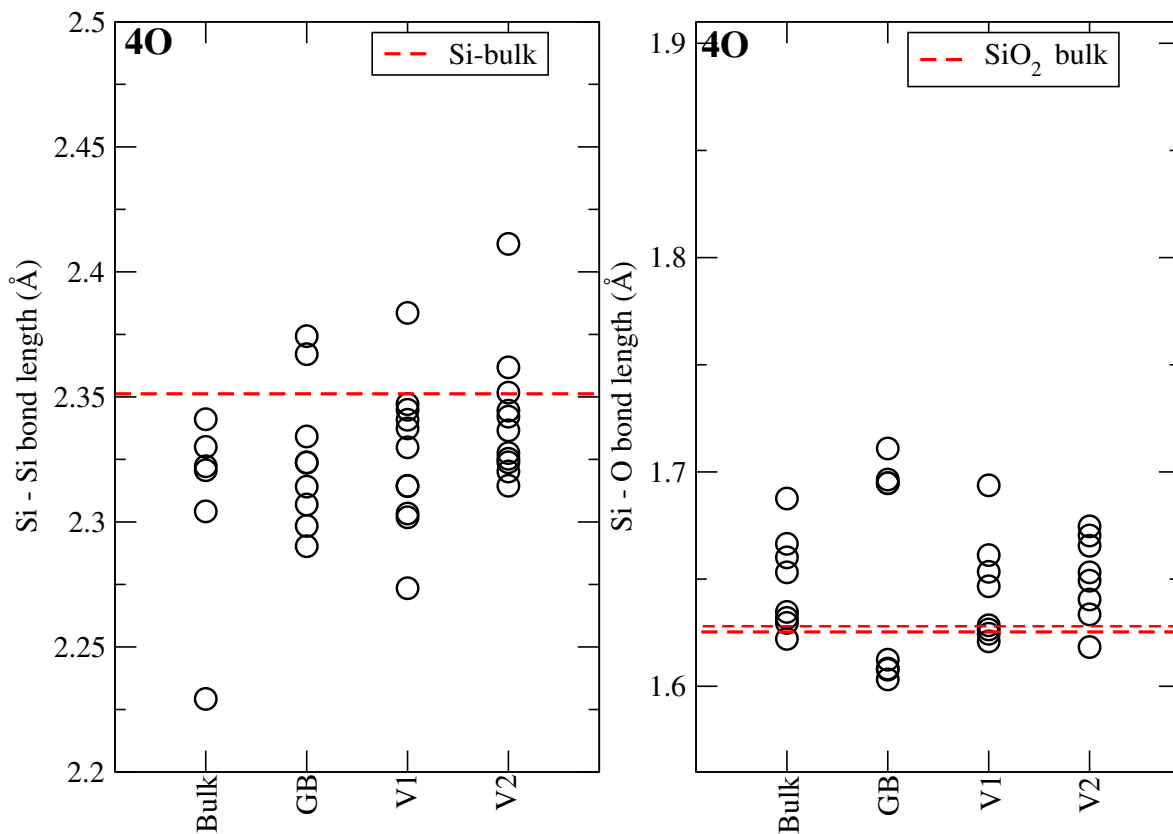


Figure 20: Bond length variation of Si-Si and Si-O for the inclusion of four oxygen atoms in Si-bulk, Si-GB and in presence of vacancy V1 and V2. As a reference, Si-Si/Si-O bond length from bulk phases of Si, SiO₂ are marked in the inset of respective plots.