

**Supplemental Material for
Easy axis rotation in ferromagnetic monolayer CrN induced by fluorine and chlorine
functionalization**

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I. STRUCTURAL PARAMETERS

TABLE SI: The Hubbard-U parameter (U), atomic distance and angles, buckling parameter (Δ), formation energy (E_f) and charge transfer between CrN monolayer and halide atom (Q_{CrN}).

	U (eV)	a (\AA)	d_{Cr-N} (\AA)	d_{Cr-X} (\AA)	$\angle Cr - N$ (°)	$\angle Cr - X$ (°)	Δ (\AA)	E_f (eV/atom)	Q_{CrN} (e)	$Q_X(e)$
CrN	4.10	3.29	1.90	—	120	—	0	—	—	—
F-CrN	3.50	3.10	1.89	1.76	110.55	108.37	0.59	-2.88	0.51	-0.51
Cl-CrN	4.10	3.22	1.92	2.22	114.10	104.32	0.47	-0.84	0.33	-0.33

II. ANISOTROPIC SPIN MODEL

A. In-plane easy axis

$$H = - \sum_{i,j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j - \sum_i A_i (\mathbf{S}_i \cdot \mathbf{z}_i)^2 - \sum_{i,j} \delta_{ij} S_i^z S_j^z - \sum_{i,j} \Gamma_{ij} (S_i^x S_j^x - S_i^y S_j^y)$$

where $J_{ij} \equiv J(\mathbf{R}_{ij})$ is the Heisenberg exchange interaction between spins \mathbf{S}_i and \mathbf{S}_j , A_i is the single-ion magnetic anisotropy at spin \mathbf{S}_i , δ_{ij} is the anisotropic exchange interaction, Γ_{ij} describes the inter-site magnetic anisotropy within the xy -plane, and \mathbf{z}_i is the unit vector pointing in the direction of the easy magnetization axis. The Holstein-Primakoff transformation can be applied to Eq. (S.1) which transforms the spin Hamiltonian to the bosonic Hamiltonian. In the linear Holstein-Primakoff approximation, spin operators are given as $S_i^+ \approx \sqrt{2S}a_i^\dagger$ and $S_i^- \approx \sqrt{2S}a_i$. After the Fourier transformation, the resulting Hamiltonian can be written as,

$$H = \sum_{\mathbf{k}} \hbar \omega_{\mathbf{k}} a_{\mathbf{k}}^\dagger a_{\mathbf{k}} + \sum_{\mathbf{k}} \Delta_{\mathbf{k}} (a_{\mathbf{k}} a_{-\mathbf{k}} + a_{\mathbf{k}}^\dagger a_{-\mathbf{k}}^\dagger), \quad (\text{S.1})$$

where

$$\hbar \omega_{\mathbf{k}} = 6S(2J + 2\Gamma - \frac{A}{6}) - S(4J - 2\Gamma + 2\delta)f(\mathbf{k})$$

and

$$\Delta_{\mathbf{k}} = -S \left[(\delta + \Gamma)f(\mathbf{k}) + \frac{A}{2} \right]$$

are diagonal and off diagonal parts of the bosonic Hamiltonian. In Eq. (S.1), $f(\mathbf{k}) = \cos k_x a + 2 \cos(\frac{1}{2}k_x a) \cos(\frac{\sqrt{3}}{2}k_y a)$ is the structure factor of a hexagonal lattice. The total Hamiltonian given by Eq. (S.1) can be diagonalized by using the coupled oscillator type unitary transformation [1] to obtain spin-wave spectrum. Similar treatment is followed in Ref.2. Consequently, the spin-wave spectrum can be written as

$$E_{\mathbf{k}}^{in} = \sqrt{(\hbar \omega_{\mathbf{k}})^2 - 4(\Delta_{\mathbf{k}})^2}. \quad (\text{S.2})$$

In the hexagonal lattice each Cr atom has six nearest neighbor Cr atoms. According to this model, the exchange coupling parameters can be expressed as

$$E_{FM_x} = -6JS^2 - 6\Gamma S^2$$

$$E_{FM_y} = -6JS^2 + 6\Gamma S^2$$

$$E_{FM_z} = -6JS^2 - AS^2 - 6\delta S^2$$

$$E_{AFM_x} = 2JS^2 + 2\Gamma S^2$$

$$E_{AFM_z} = 2JS^2 - AS^2 + 2\delta S^2$$

$$J = (3E_{AFM_z} - 2E_{FM_y} - E_{FM_x})/48S^2$$

$$A = (3E_{AFM_x} - 3E_{AFM_z} + E_{FM_x} - E_{FM_z})/4S^2$$

$$\delta = (3E_{AFM_x} - 3E_{AFM_z} - 3E_{FM_z} + E_{FM_x} + 2E_{FM_y})/48S^2 \quad (\text{S.3})$$

$$\Gamma = (E_{FM_y} - E_{FM_x})/16S^2 \quad (\text{S.4})$$

B. Out-of-plane easy axis

The DFT results can be mapped onto the anisotropic classical spin model,

$$H = - \sum_{i,j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j - \sum_i A_i (\mathbf{S}_i \cdot \mathbf{z}_i)^2 - \sum_{i,j} \delta_{ij} S_i^z S_j^z. \quad (\text{S.5})$$

Similarly, the linear Holstein-Primakoff transformation is applied to the Hamiltonian. After the Fourier transformation, the resulting Hamiltonian can be written in a diagonal form as,

$$H = \sum_{\mathbf{k}} \hbar \omega_{\mathbf{k}} a_{\mathbf{k}}^\dagger a_{\mathbf{k}}, \quad (\text{S.6})$$

where

$$\hbar \omega_{\mathbf{k}} = S(12J + 12\delta - 2A) - 4SJf(\mathbf{k}),$$

i.e. $\hbar \omega_{\mathbf{k}} = E_{\mathbf{k}}^{out}$. The spin-wave dispersion can be expanded in the vicinity of Γ point, $E_{\mathbf{k}}^{out/in}(\mathbf{k}) \simeq \epsilon_0 + \rho k^2$ where ϵ_0 and ρ are spin-wave gap and spin stiffness, respectively. Strictly speaking, Eq. (S.5) is justified for the atomic limit, i.e. when the Coulomb interaction between the Cr 3d electrons is larger compared to the 3d band width. Similarly, the exchange coupling parameters can be written as

$$E_{FM_x} = -6JS^2$$

$$E_{FM_z} = -6JS^2 - AS^2 - 6\delta S^2$$

$$E_{AFM_x} = 2JS^2$$

$$E_{AFM_z} = 2JS^2 - AS^2 + 2\delta S^2$$

$$J = (E_{AFM_x} - E_{FM_x})/16S^2$$

$$A = (3E_{AFM_x} - 3E_{AFM_z} + E_{FM_x} - E_{FM_z})/4S^2$$

$$\delta = (E_{AFM_x} - E_{AFM_z} - E_{FM_z} + E_{FM_x})/16S^2 \quad (\text{S.7})$$

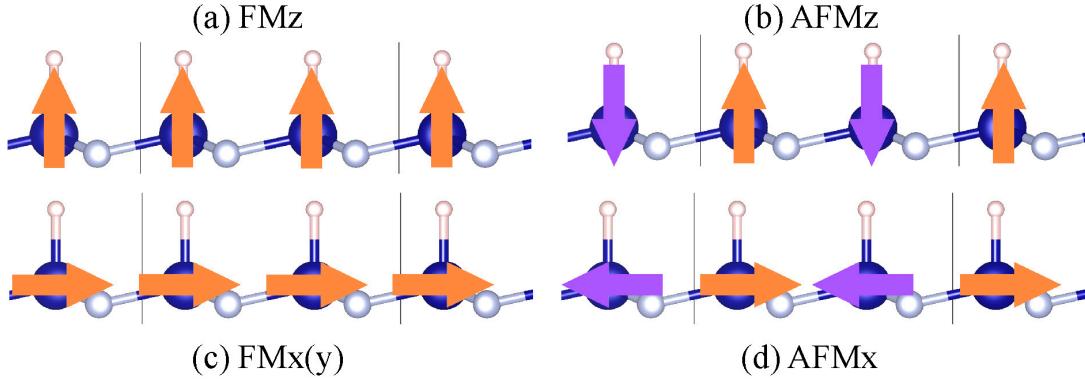


FIG. S1: The ferromagnetic (FM) configurations along (a) z and (c) x/y. The antiferromagnetic (AFM) configurations along (b) z and (d) x.

TABLE SII: The Hubbard parameter (U), net magnetic moment (M), spin stiffness (ρ), easy axis direction, magnetic exchange (J), site magnetic anisotropy (A), inter-site magnetic anisotropy (δ), inside the plane magnetic anisotropy (Γ) and Curie temperature T_C for pristine CrN monolayer and after adsorption of F and Cl atoms.

	U (eV)	M (μ_B)	ρ (meVÅ 2)	Easy Axis	J (meV)	A (meV)	δ (meV)	$\Gamma(\mu eV)$	T_C (K)
CrN	4.10	3.00	496	out-of-plane	10.73	0.25	0.03	-	910
F-CrN	3.50	2.00	510	in-plane	19.84	-0.07	-0.02	0.05	650
Cl-CrN	4.10	2.00	784	in-plane	26.08	-0.06	-0.01	0.01	800

III. CALCULATION OF THE CRITICAL TEMPERATURE

The critical temperature of magnetic ordering can be calculated within the random phase approximation (RPA) [3], which is a minimal approximation that takes long-range spin fluctuations into account. In case of a ferromagnet with one magnetic sublattice, the Curie temperature can be expressed as,

$$k_B T_c = \frac{2}{3} \frac{S(S+1)}{\langle S^z \rangle} \left\{ \frac{1}{\Omega} \int d\mathbf{k} \left[\left(E^{out/in}(\mathbf{k}) \right)^{-1} \right] \right\}^{-1}, \quad (\text{S.8})$$

where $\Omega = 8\pi^2/\sqrt{3}a^2$ is the Brillouin zone area. $E^{out/in}(\mathbf{k})$ is the spin-wave dispersion for out-of-plane/in-plane easy axis. The thermal average of magnetization can be calculated within the random phase approximation and using magnon excited states [3].

IV. CALCULATION OF MAGNETIC MOMENT AS A FUNCTION OF TEMPERATURE

The thermal average of spin magnetic moment is calculated by using the following equation for the single sublattice of CrN monolayer [3].

$$\langle S \rangle = \frac{(S - \lambda)(1 + \lambda)^{2S+1} + (S + 1 + \lambda)\lambda^{2S+1}}{(1 + \lambda)^{2S+1} - \lambda^{2S+1}} \quad (\text{S.9})$$

where λ is a temperature dependent parameter defined as,

$$\lambda = -\frac{2\hbar}{\Omega} \int d\omega \int dk \text{Im} \left(\left[\hbar\omega - E^{out/in}(\mathbf{k}) + i0^+ \right]^{-1} \right) (e^{\beta\hbar\omega} - 1)^{-1}. \quad (\text{S.10})$$

Here the expectation value of S in Eq. (S.9) and magnon energy spectrum in the whole Brillouin zone are solved self-consistently.

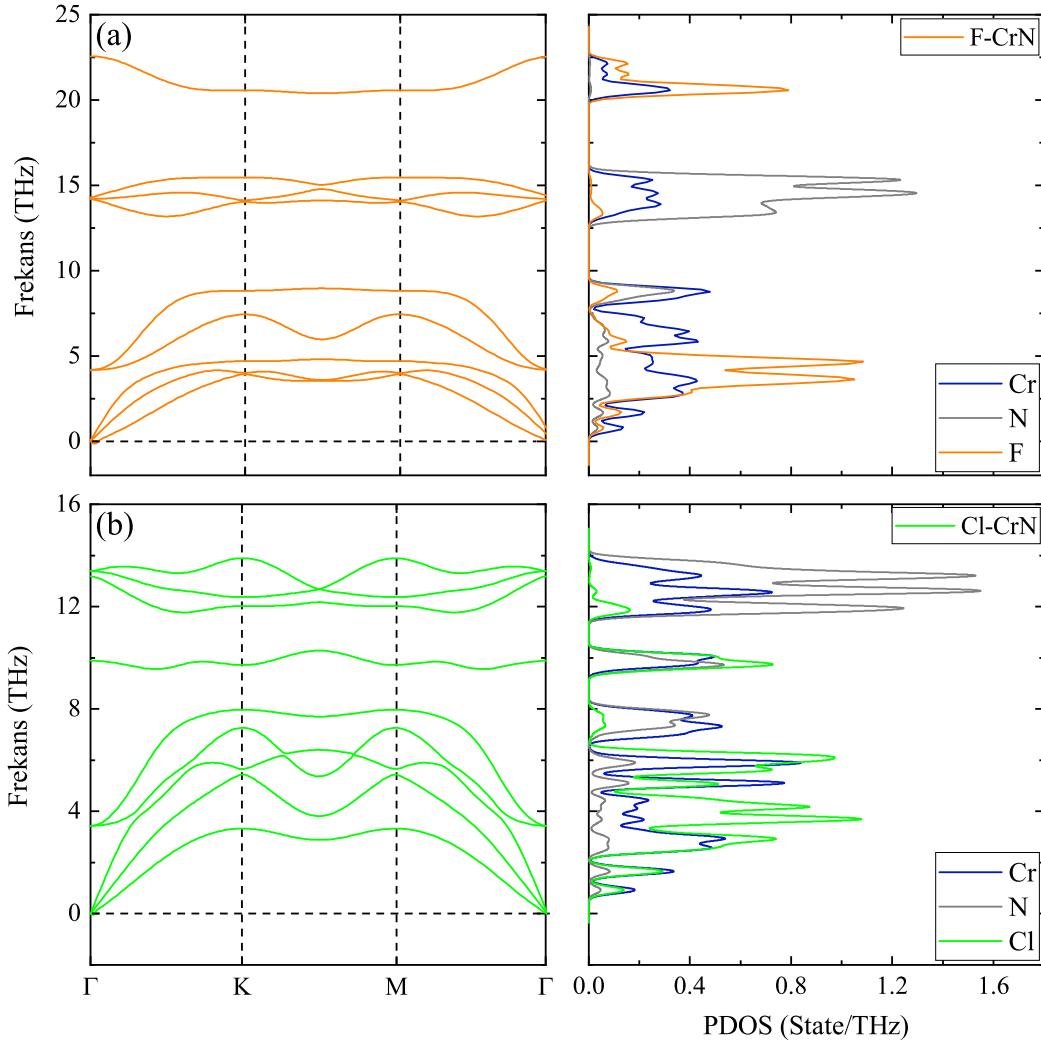


FIG. S2: The phonon spectra of (a) F-CrN (b) Cl-CrN with phonon projected density of states (right panel)

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- [1] M. Wagner, *Unitary Transformations in Solid State Physics*, Modern problems in condensed matter sciences (North-Holland, 1986).
 - [2] S. Memarzadeh, M. R. Roknabadi, M. Modarresi, A. Mogulkoc, and A. N. Rudenko, *2D Mater.* **8**, 035022 (2021).
 - [3] J. Rusz, I. Turek, and M. Diviš, *Phys. Rev. B* **71**, 174408 (2005).

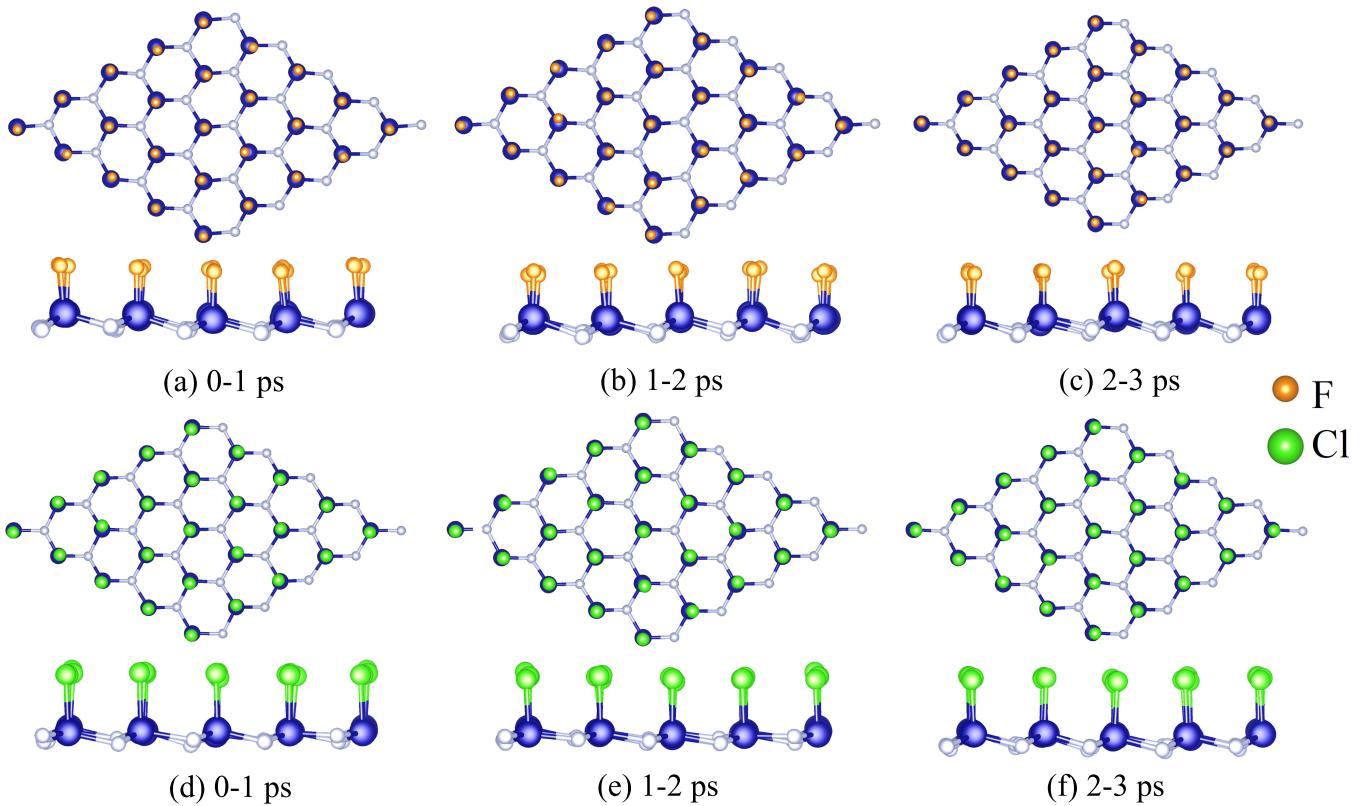


FIG. S3: The snapshots of AIMD simulations for (a)-(c) F-CrN and (d)-(f) Cl-CrN at 300 K with total simulation time of 3 ps.

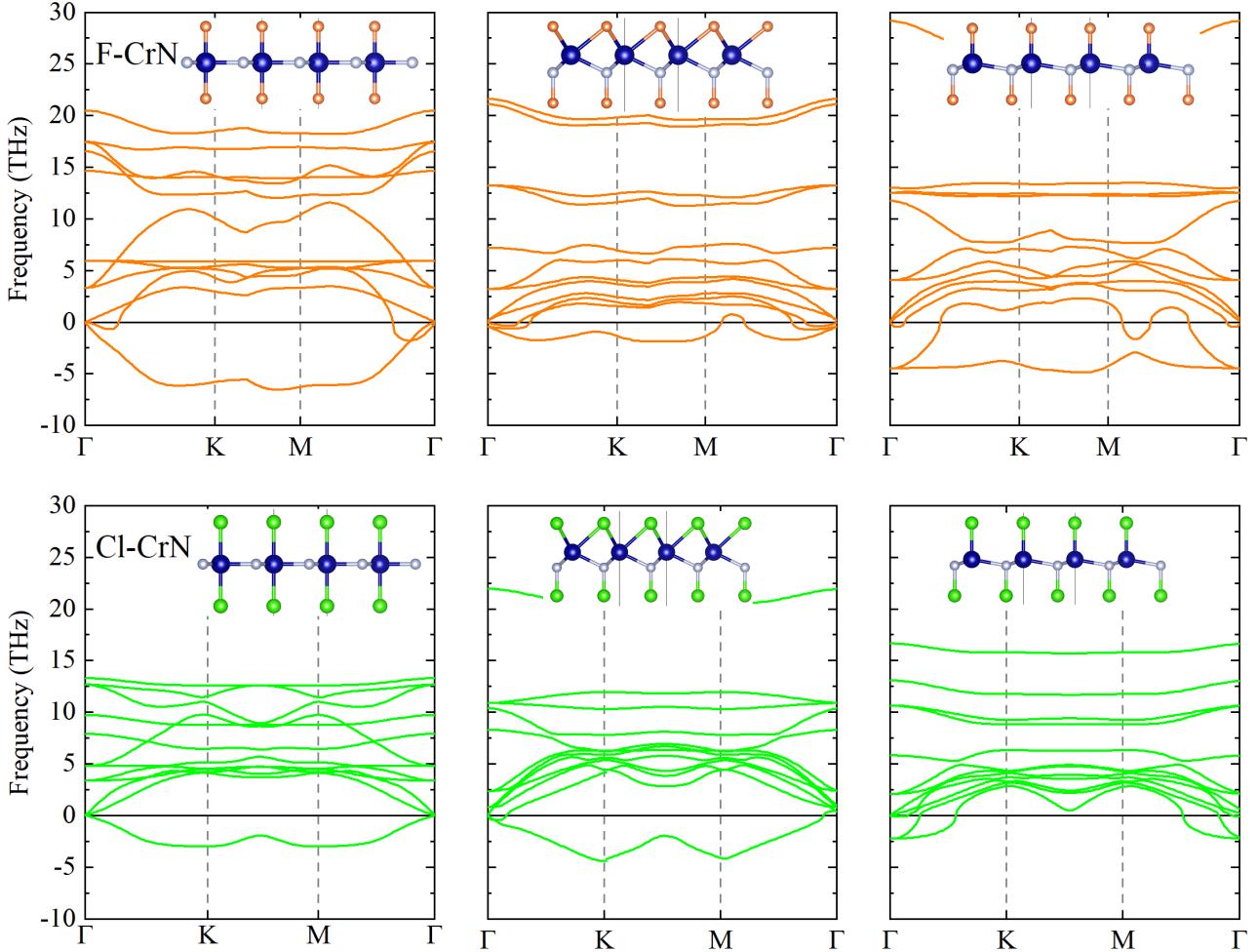


FIG. S4: Phonon spectra of the CrN monolayer functionalized by F and Cl atom on both sides, demonstrating dynamical instability of double-side functionalization.

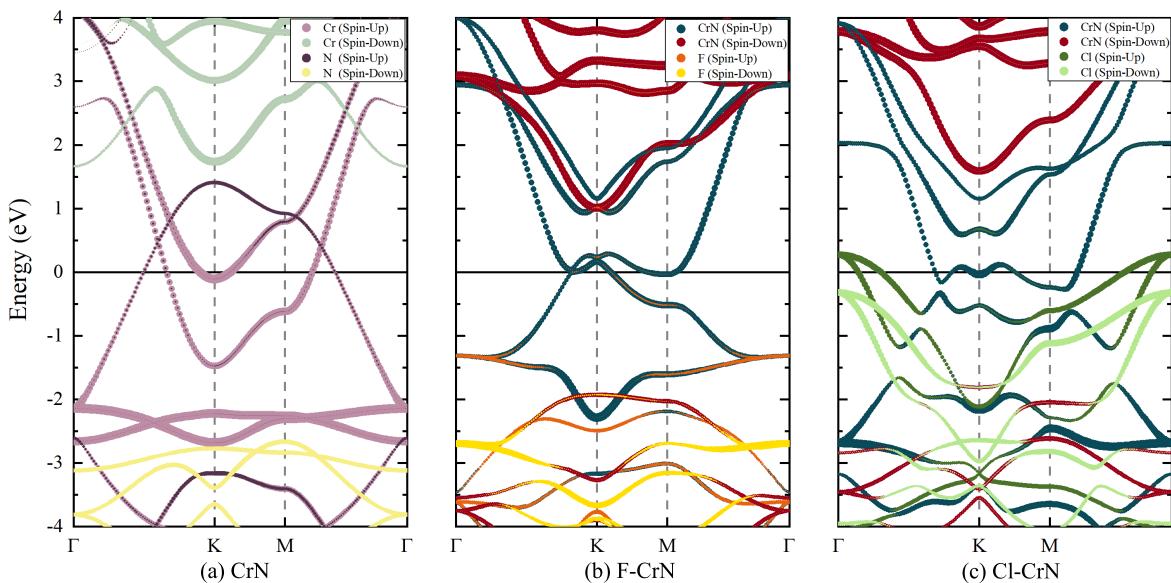


FIG. S5: The spin resolved partial bands of pristine CrN and F/Cl-CrN monolayers.

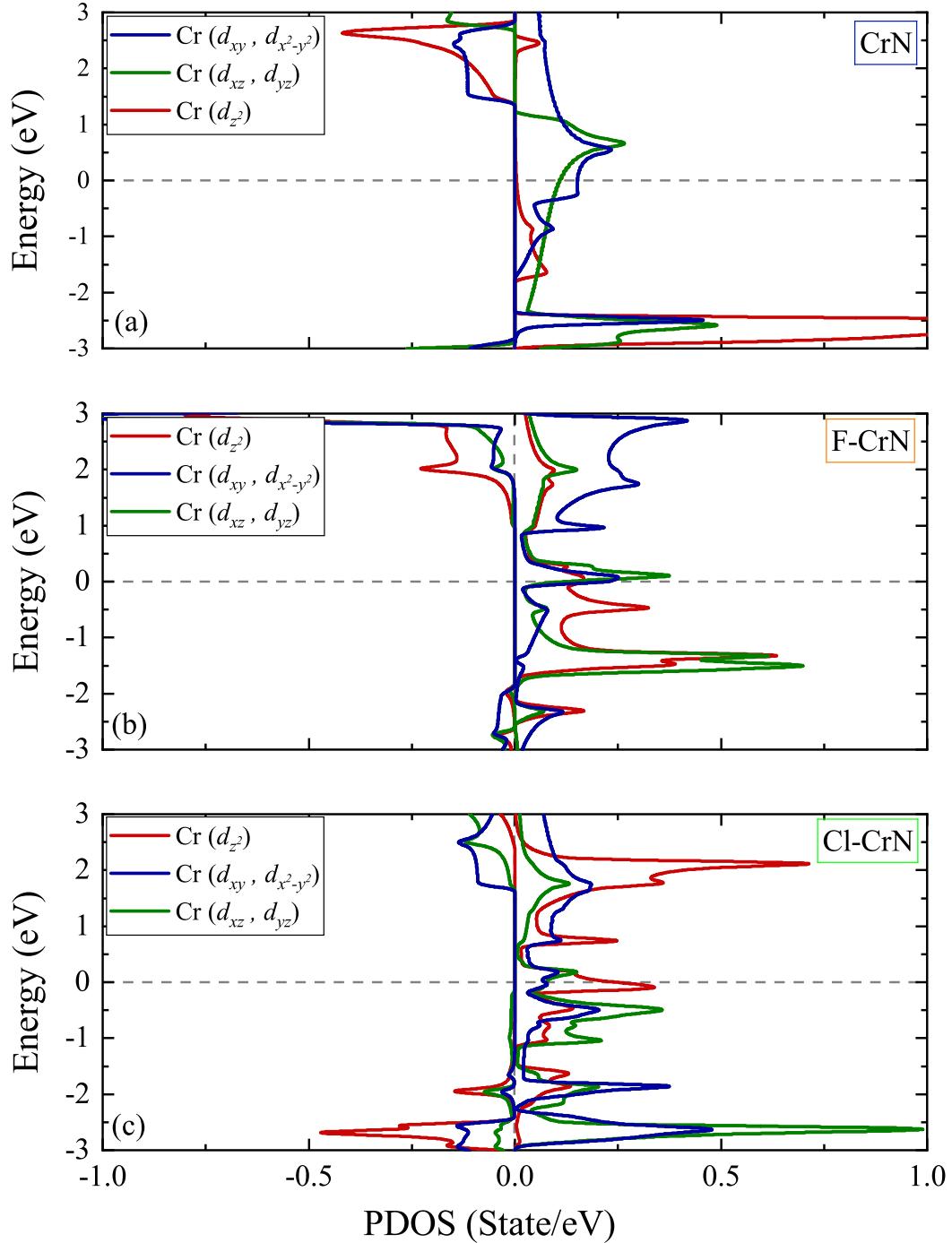


FIG. S6: Partial density of states (PDOS) of Cr *d* orbitals for (a) pristine CrN, (b) F-CrN and (c) Cl-CrN. The Fermi level is set to be zero