## Supporting information for

## "Structural, electronic phase transitions and thermal spin transport properties in 2D NbSe<sub>2</sub> and NbS<sub>2</sub>: A first-principles study"

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**Fig. S1** The optimized lattice constants for 2H- and 1T-NbSe<sub>2</sub> (a) and NbS<sub>2</sub> (b) monolayers within PBE with different U values.



Fig. S2 The structural phase transition diagrams of (a) NbSe<sub>2</sub> and NbS<sub>2</sub> (b) within LDA with different U values. The total energy difference per formula unit  $\Delta E = E_{1T}-E_{2H}$ .



Fig. S3 The structural phase transition diagrams of (a) NbSe<sub>2</sub> and NbS<sub>2</sub> (b) within PBE with different U values. The Gibbs free energy difference per formula unit  $\Delta G = G_{1T}-G_{2H}$ .



Fig. S4 The structural phase transition diagrams of (a) NbSe<sub>2</sub> and NbS<sub>2</sub> (b) within LDA with different U values. The Gibbs free energy difference per formula unit  $\Delta G = G_{1T}-G_{2H}$ .



Fig. S5 The spin structures of 2H-Nb $X_2$  (X=Se, S) with FM (a) and AFM (b) states and 1T-Nb $X_2$  with FM (c) and AFM (d) states.



Fig. S6 The strain-dependent total energy per formula unit (a) and Nb atomic magnetic moment (b) in the FM and AFM states within PBE+U ( $U_{eff}$ =4.0 eV) for NbSe<sub>2</sub> monolayer.



**Fig. S7** The spin density within PBE+U ( $U_{eff}$ =4.0 eV) for NbSe<sub>2</sub> monolayer in the 2H (a,b) and 1T (c,d) phases. (a, c) and (b,d) represent without and with 15% tensile strain, respectively. The pink and blue isosurfaces represent the positive and negative spin densities (0.012 e/Å<sup>2</sup>) respectively.



**Fig. S8** Tensile strain effect on spin-polarized band structures for 2H-NbS<sub>2</sub> monolayer within PBE+U. The Fermi level is indicated by the blue dashed line.



Fig. S9 Spin-dependent partial density of states (DOS) within PBE and PBE+U ( $U_{eff}$ =4.0 eV) for 2H-NbSe<sub>2</sub> monolayer with tensile strain.



Fig. S10 Spin-dependent partial density of states (DOS) within PBE and PBE+U ( $U_{eff}$ =4.0 eV) for 1T-NbSe<sub>2</sub> monolayer with tensile strain.



Fig. S11 Tensile strain effect on spin-polarized band structures for  $1T-NbS_2$  monolayer with PBE+U ( $U_{eff}=0, 4 \text{ eV}$ ).



**Fig. S12** Spin-polarized band structures with hybrid Heyd-Scuseria-Ernzerhof functional and PBE+U ( $U_{eff}$ = 4.0 eV) for NbSe<sub>2</sub> and NbS<sub>2</sub> monolayers in 2H and 1T phases.



Fig. S13 Spin-polarized band structures for 2H-NbSe<sub>2</sub> bulk within PBE+U (U=0, 1, 2, 3, 4 eV).



Fig. S14 Spin-polarized band structures for 2H-NbSe<sub>2</sub> monolayer within PBE+U (U=0, 1, 2, 3, 4 eV).



Fig. S15 Spin-polarized band structures for 2H-NbS<sub>2</sub> bulk within PBE+U (U=0, 1, 2, 3, 4 eV).



Fig. S16 Spin-polarized band structures for 2H-NbS<sub>2</sub> monolayer within PBE+U (U=0, 1, 2, 3, 4 eV).