## **Electronic Supplementary Information**

### Large-scale benchmarks of the Time-Warp/Graph-Theoretical Kinetic Monte Carlo approach for distributed on-lattice simulations of catalytic kinetics

# Giannis D. Savva,<sup>*ab*‡</sup> Raz L. Benson,<sup>*a*‡</sup> Ilektra A. Christidi,<sup>*c*</sup> and Michail Stamatakis<sup>\**a*</sup>

<sup>a</sup> Department of Chemical Engineering, University College London, Torrington place, London, WC1E 7JE, United Kingdom.

<sup>b</sup> Theory and Simulation of Materials (THEOS), École Polytechnique Fédérale de Lausanne, 1015 Lausanne, Switzerland.

<sup>c</sup> Research Software Development Group, Advanced Research Computing Centre, University College London, Gower Street, London, WC1E 6BT, United Kingdom.

<sup>‡</sup> These authors contributed equally to this work.

\* Corresponding author. E-mail: m.stamatakis@ucl.ac.uk.

#### Weak-scaling results

In Fig. S1 we reproduce the weak-scaling results of ref. 1 for distributed runs of Systems 1 and 2. The weak-scaling efficiency,  $\eta_{WS}$ , is plotted against the number of lattice sites,  $n_{sites}$ . Using the notation introduced in Section 3.2 of the main text, the weak-scaling efficiency can be defined as

$$\eta_{\rm WS} = \tau_{\rm serial}^* / \tau^*, \tag{S1}$$

where  $\tau_{\text{serial}}^*$  is the elapsed clock time per unit of KMC time for a serial run of a 100 × 100 lattice (i.e., the size of one subdomain in the distributed runs).



**Figure S1** Weak-scaling results from Ref. 1 for distributed runs of (a) System 1 and (b) System 2, as defined in the main text. Desirable behaviour is represented by a constant weak-scaling efficiency,  $\eta_{WS}$ , such that no overheads are incurred as more processors are utilised to simulate progressively larger lattices. For both systems, we observe that a roughly constant efficiency is reached for sufficiently large runs, employing about 60 processors. The data points that correspond to the lattices used in the present study ( $200 \times 200$  and  $1200 \times 1200$ ) are plotted using blue filled squares.

### References

[1] S. Ravipati, G. D. Savva, I.-A. Christidi, R. Guichard, J. Nielsen, R. Réocreux and M. Stamatakis, *Comput. Phys. Commun.*, 2022, **270**, 108148.