

Combination of Explainable Machine Learning and Conceptual Density Functional Theory: Applications for the Study of Key Solvation Mechanisms

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Correlation Coefficients - Numerical Values

| | ΔE_{CS} | ΔE_{AS} | ΔE_{CA} | $\Delta \Delta E_{sol}$ | $\Sigma \Delta E_{ASCS}$ | $\Delta \Delta E_{ASCS}$ | E_{HOMO}^S | E_{LUMO}^S | χ_S | η_S | E_{HOMO}^C | E_{LUMO}^C | χ_C | η_C | E_{HOMO}^A | E_{LUMO}^A | χ_A | η_A |
|--------------------------|-----------------|-----------------|-----------------|-------------------------|--------------------------|--------------------------|--------------|--------------|----------|----------|--------------|--------------|----------|----------|--------------|--------------|----------|----------|
| ΔE_{CS} | 1.00 | 0.02 | 0.63 | -0.40 | 0.99 | -0.99 | -0.13 | -0.13 | 0.13 | 0.12 | 0.99 | 0.82 | -0.99 | -0.99 | -0.03 | -0.06 | 0.05 | -0.03 |
| ΔE_{AS} | 0.02 | 1.00 | 0.71 | -0.82 | 0.18 | 0.14 | 0.23 | 0.14 | -0.19 | -0.32 | 0.05 | 0.07 | -0.05 | -0.05 | -0.88 | -0.77 | 0.93 | -0.02 |
| ΔE_{CA} | 0.63 | 0.71 | 1.00 | -0.97 | 0.73 | -0.51 | 0.01 | -0.01 | -0.00 | -0.04 | 0.63 | 0.57 | -0.63 | -0.62 | -0.64 | -0.70 | 0.76 | -0.17 |
| $\Delta \Delta E_{sol}$ | -0.40 | -0.82 | -0.97 | 1.00 | -0.53 | 0.27 | -0.05 | -0.02 | 0.04 | 0.07 | -0.41 | -0.40 | 0.41 | 0.40 | 0.73 | 0.80 | -0.87 | 0.20 |
| $\Sigma \Delta E_{ASCS}$ | 0.99 | 0.18 | 0.73 | -0.53 | 1.00 | -0.95 | -0.09 | -0.10 | 0.10 | 0.07 | 0.99 | 0.82 | -0.99 | -0.98 | -0.17 | -0.18 | 0.20 | -0.03 |
| $\Delta \Delta E_{ASCS}$ | -0.99 | 0.14 | -0.51 | 0.27 | -0.95 | 1.00 | 0.17 | 0.15 | -0.16 | -0.17 | -0.98 | -0.80 | 0.98 | 0.97 | -0.11 | -0.06 | 0.10 | 0.03 |
| E_{HOMO}^S | -0.13 | 0.23 | 0.01 | -0.05 | -0.09 | 0.17 | 1.00 | 0.96 | -0.99 | -0.91 | -0.07 | -0.11 | 0.08 | 0.07 | -0.05 | -0.07 | 0.07 | -0.03 |
| E_{LUMO}^S | -0.13 | 0.14 | -0.01 | -0.02 | -0.10 | 0.15 | 0.96 | 1.00 | -0.98 | -0.75 | -0.09 | -0.12 | 0.10 | 0.09 | -0.04 | -0.06 | 0.06 | -0.02 |
| χ_S | 0.13 | -0.19 | -0.00 | 0.04 | 0.10 | -0.16 | -0.99 | -0.98 | 1.00 | 0.86 | 0.08 | 0.12 | -0.09 | -0.08 | 0.05 | 0.07 | -0.06 | 0.03 |
| η_S | 0.12 | -0.32 | -0.04 | 0.07 | 0.07 | -0.17 | -0.91 | -0.75 | 0.86 | 1.00 | 0.03 | 0.07 | -0.03 | -0.03 | 0.05 | 0.08 | -0.07 | 0.04 |
| E_{HOMO}^C | 0.99 | 0.05 | 0.63 | -0.41 | 0.99 | -0.98 | -0.07 | -0.09 | 0.08 | 0.03 | 1.00 | 0.79 | -1.00 | -1.00 | -0.04 | -0.06 | 0.05 | -0.03 |
| E_{LUMO}^C | 0.82 | 0.07 | 0.57 | -0.40 | 0.82 | -0.80 | -0.11 | -0.12 | 0.12 | 0.07 | 0.79 | 1.00 | -0.81 | -0.76 | -0.06 | -0.10 | 0.09 | -0.06 |
| χ_C | -0.99 | -0.05 | -0.63 | 0.41 | -0.99 | 0.98 | 0.08 | 0.10 | -0.09 | -0.03 | -1.00 | -0.81 | 1.00 | 1.00 | 0.04 | 0.06 | -0.06 | 0.03 |
| η_C | -0.99 | -0.05 | -0.62 | 0.40 | -0.98 | 0.97 | 0.07 | 0.09 | -0.08 | -0.03 | -1.00 | -0.76 | 1.00 | 1.00 | 0.03 | 0.05 | -0.05 | 0.03 |
| E_{HOMO}^A | -0.03 | -0.88 | -0.64 | 0.73 | -0.17 | -0.11 | -0.05 | -0.04 | 0.05 | 0.05 | -0.04 | -0.06 | 0.04 | 0.03 | 1.00 | 0.54 | -0.86 | -0.35 |
| E_{LUMO}^A | -0.06 | -0.77 | -0.70 | 0.80 | -0.18 | -0.06 | -0.07 | -0.06 | 0.07 | 0.08 | -0.06 | -0.10 | 0.06 | 0.05 | 0.54 | 1.00 | -0.90 | 0.60 |
| χ_A | 0.05 | 0.93 | 0.76 | -0.87 | 0.20 | 0.10 | 0.07 | 0.06 | -0.06 | -0.07 | 0.05 | 0.09 | -0.06 | -0.05 | -0.86 | -0.90 | 1.00 | -0.19 |
| η_A | -0.03 | -0.02 | -0.17 | 0.20 | -0.03 | 0.03 | -0.03 | -0.02 | 0.03 | 0.04 | -0.03 | -0.06 | 0.03 | 0.03 | -0.35 | 0.60 | -0.19 | 1.00 |

Figure 1: Correlation coefficients for feature set.

Correlation Coefficients - Heatmap

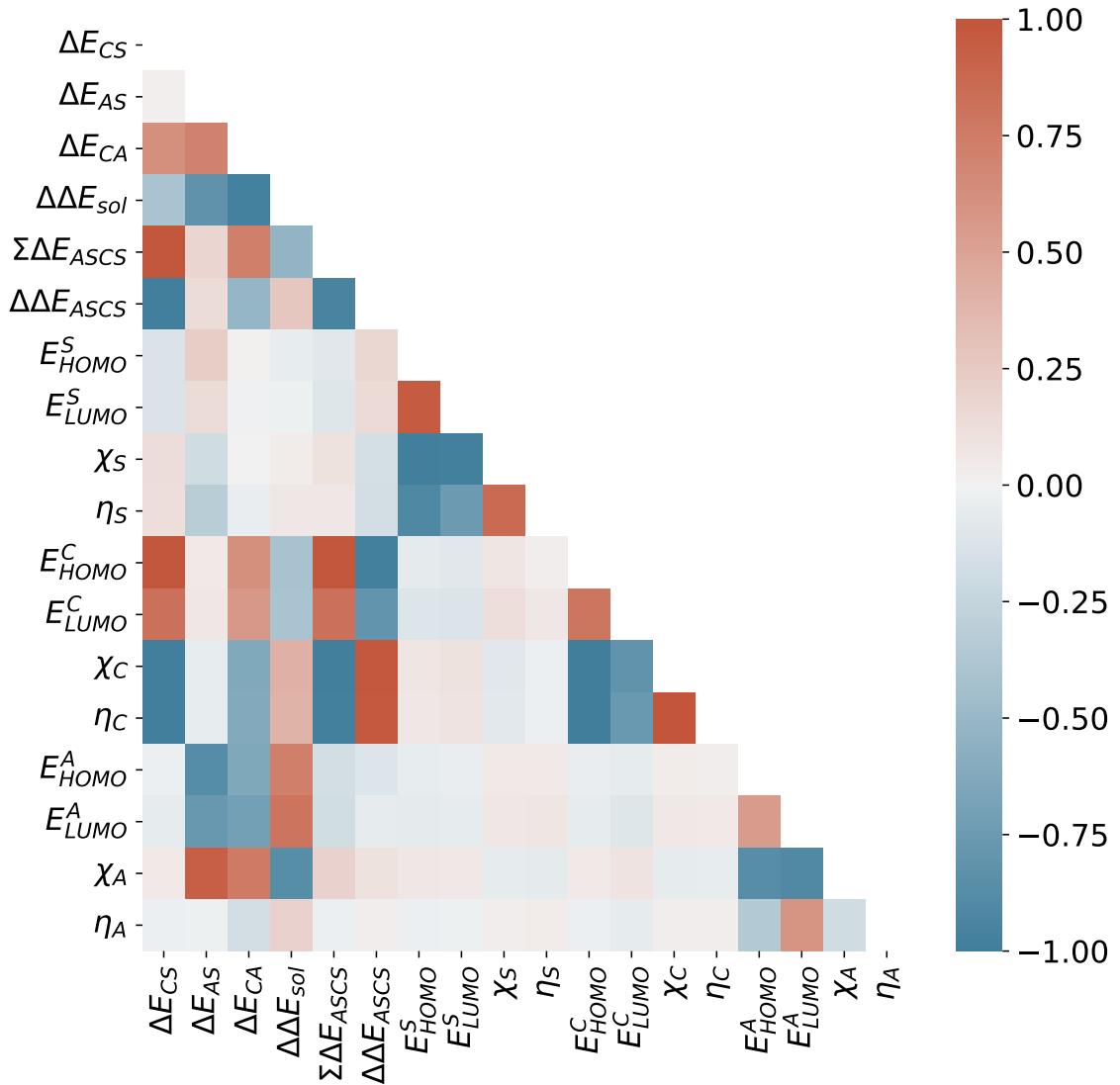


Figure 2: Correlation coefficients for feature set as heatmap.

Free Energy Calculations - Reduced XGB Model

Goodness of fit plot

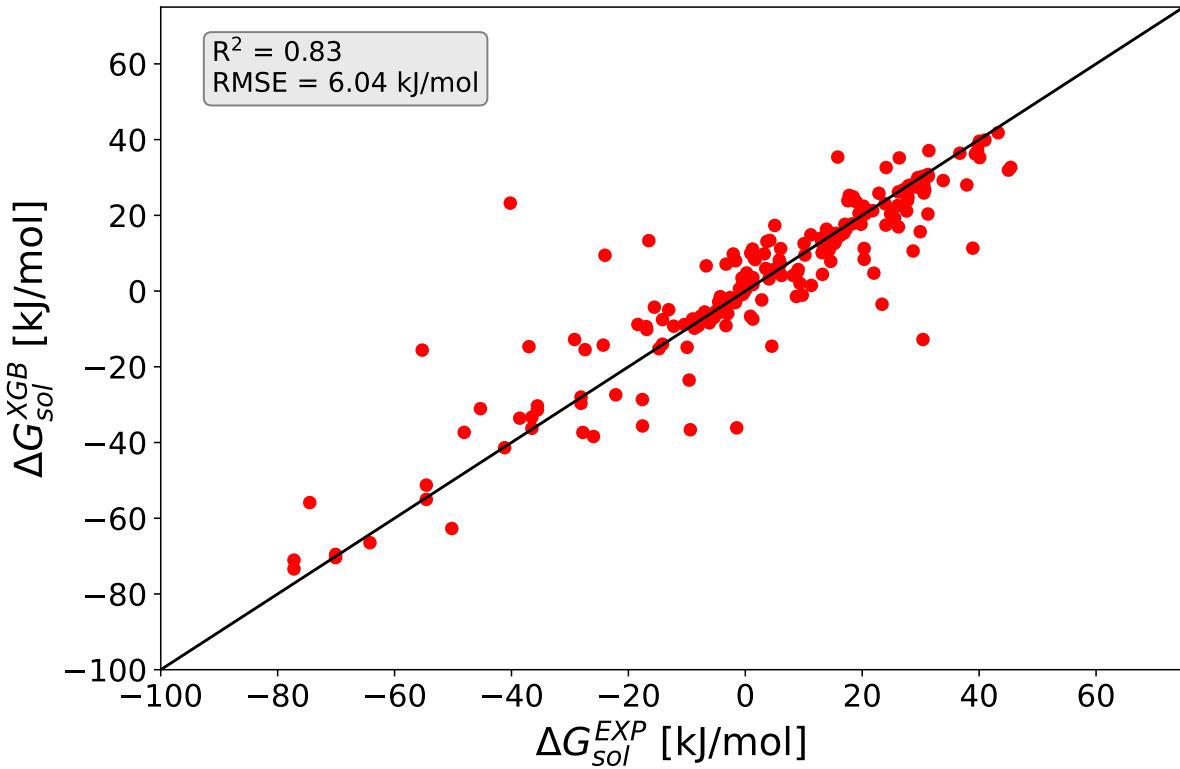


Figure 3: Goodness of fit plots for predicted (subscript XGB) and experimental values (subscript EXP) for ΔG_{sol} regarding the reduced XGB model. The straight black lines highlight a full coincidence.

SHAP analysis

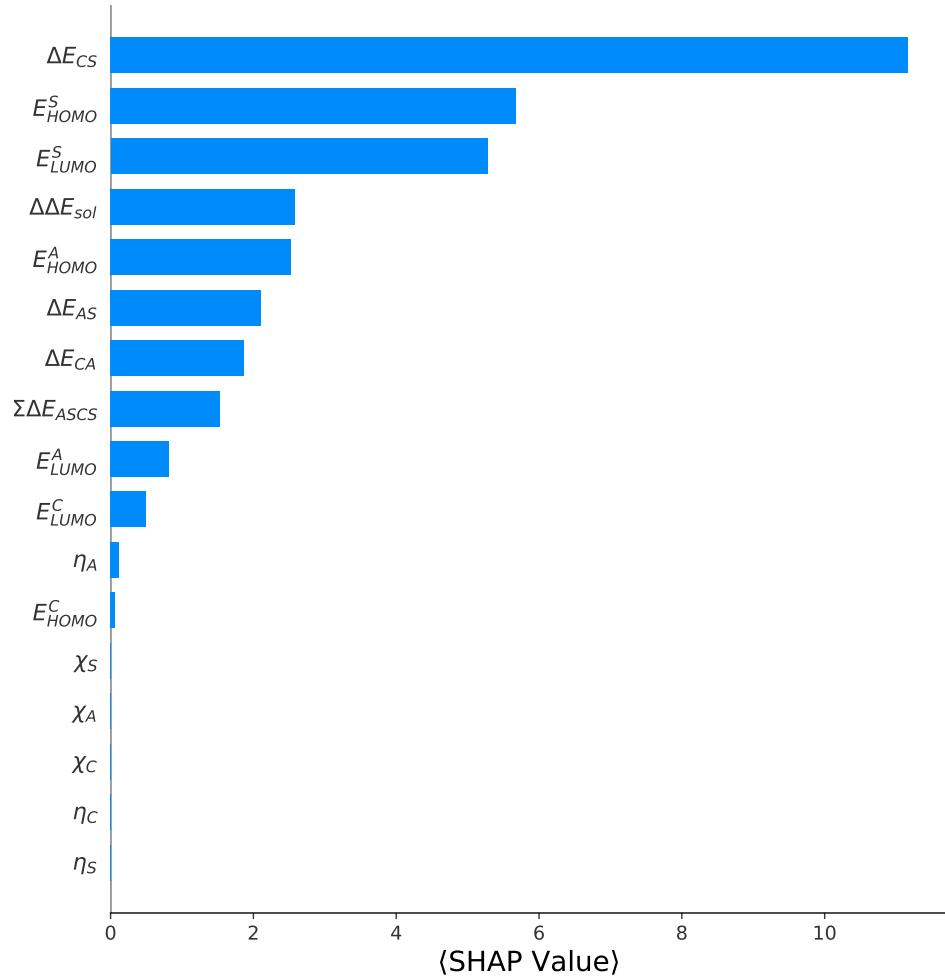


Figure 4: Net SHAP values for feature ranking of the reduced XGB model for the prediction of ΔG_{sol} .

Free Enthalpy Calculations - Reduced XGB Model

Goodness of fit plot

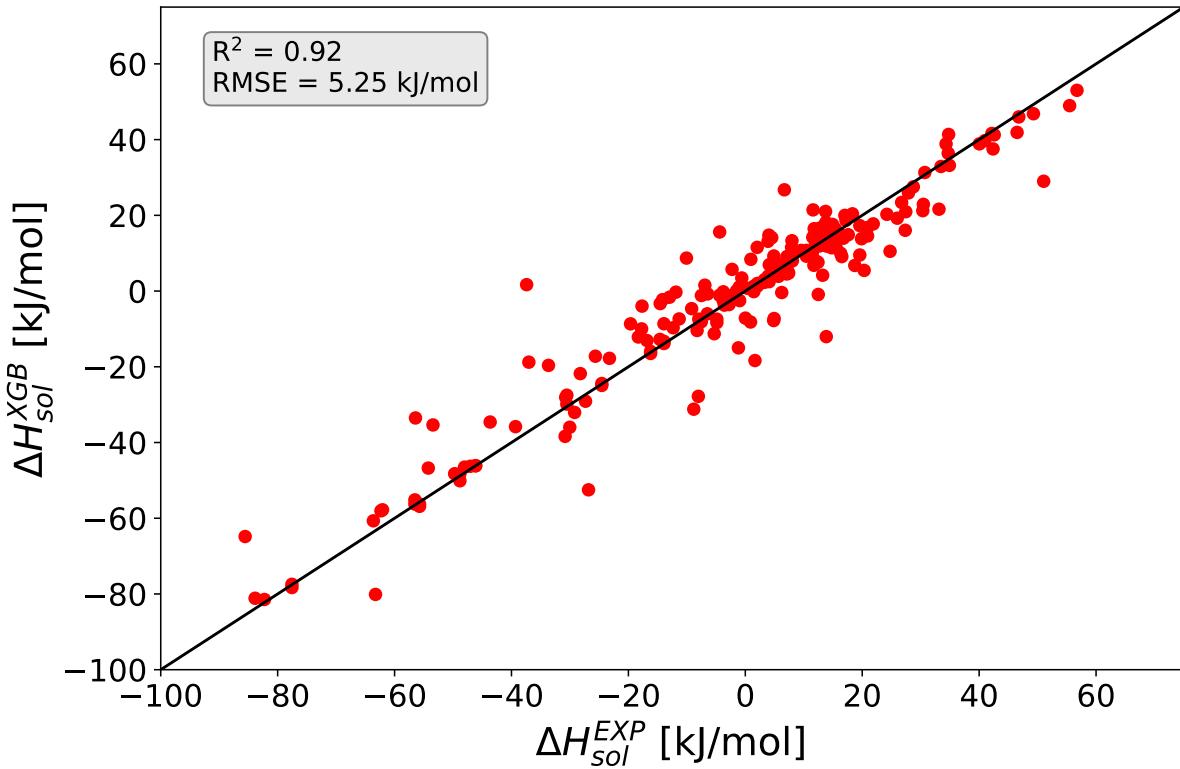


Figure 5: Goodness of fit plots for predicted (subscript XGB) and experimental values (subscript EXP) for ΔH_{sol} regarding the reduced XGB model. The straight black lines highlight a full coincidence.

SHAP analysis

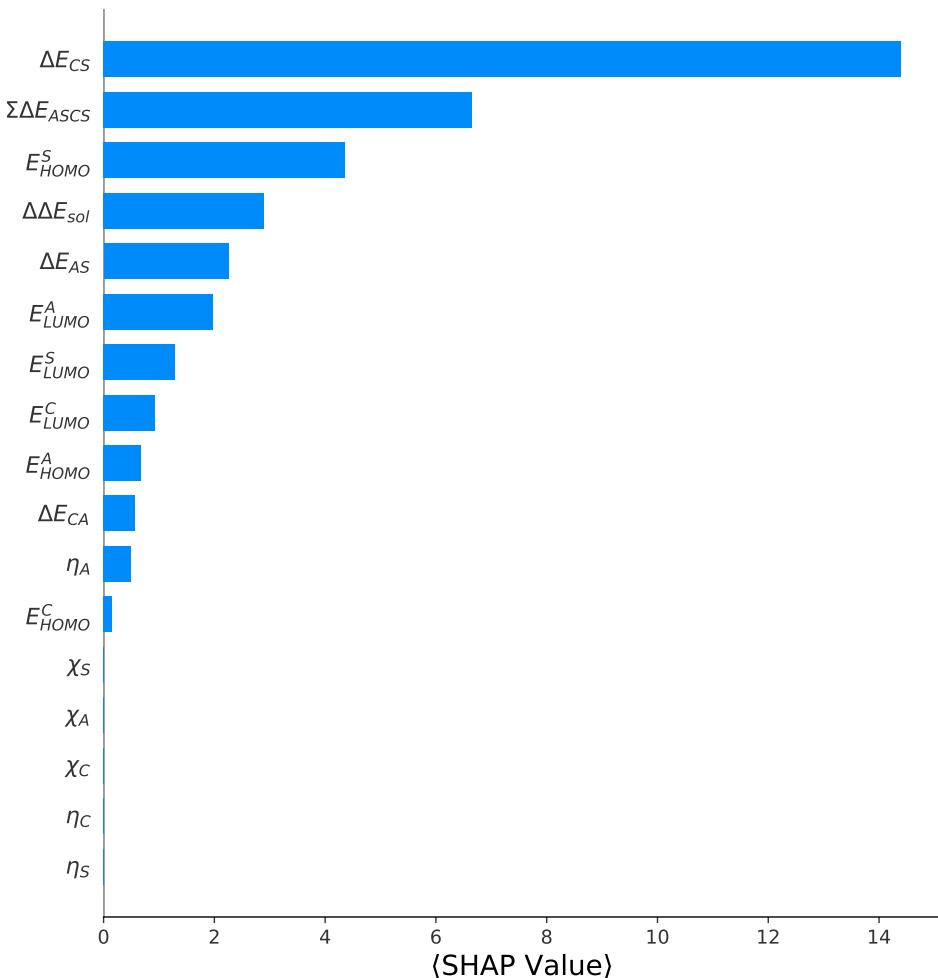


Figure 6: Net SHAP values for feature ranking of the reduced XGB model for the prediction of ΔH_{sol} .

Free Entropy Calculations - Reduced ET Model

Goodness of fit plot

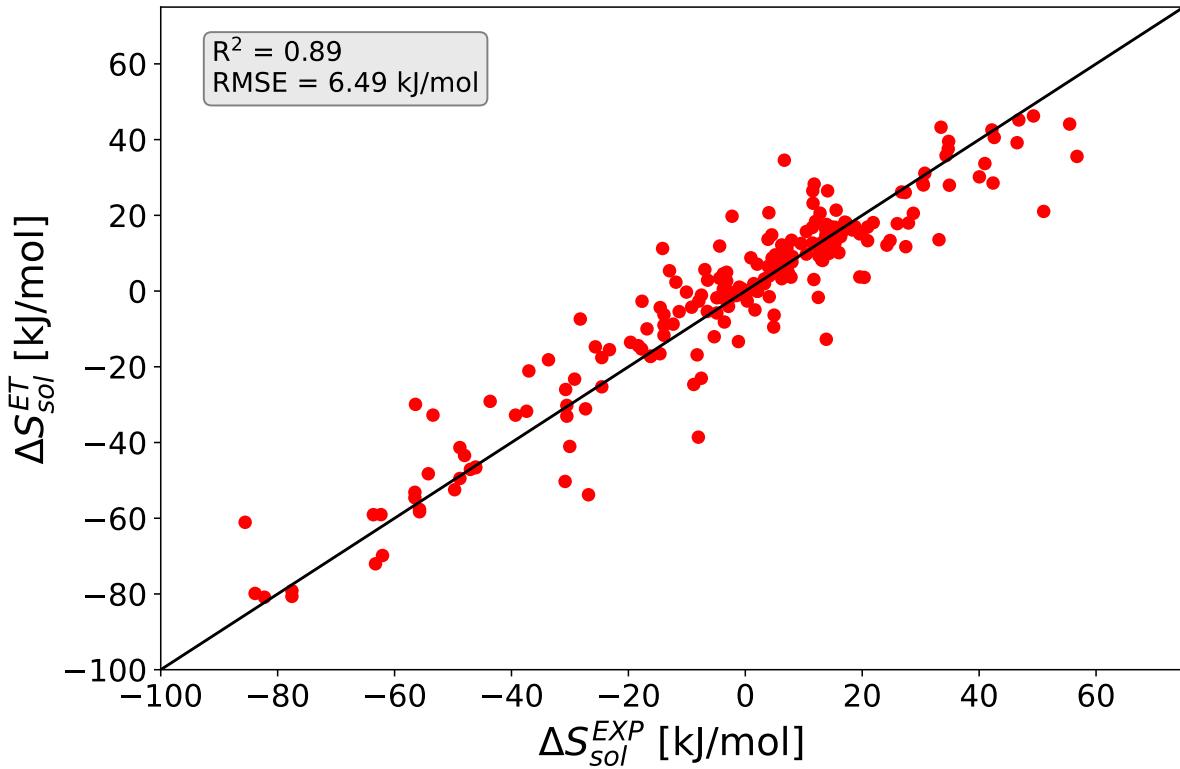


Figure 7: Goodness of fit plots for predicted (subscript XGB) and experimental values (subscript EXP) for ΔS_{sol} regarding the reduced ET model. The straight black lines highlight a full coincidence.

SHAP analysis

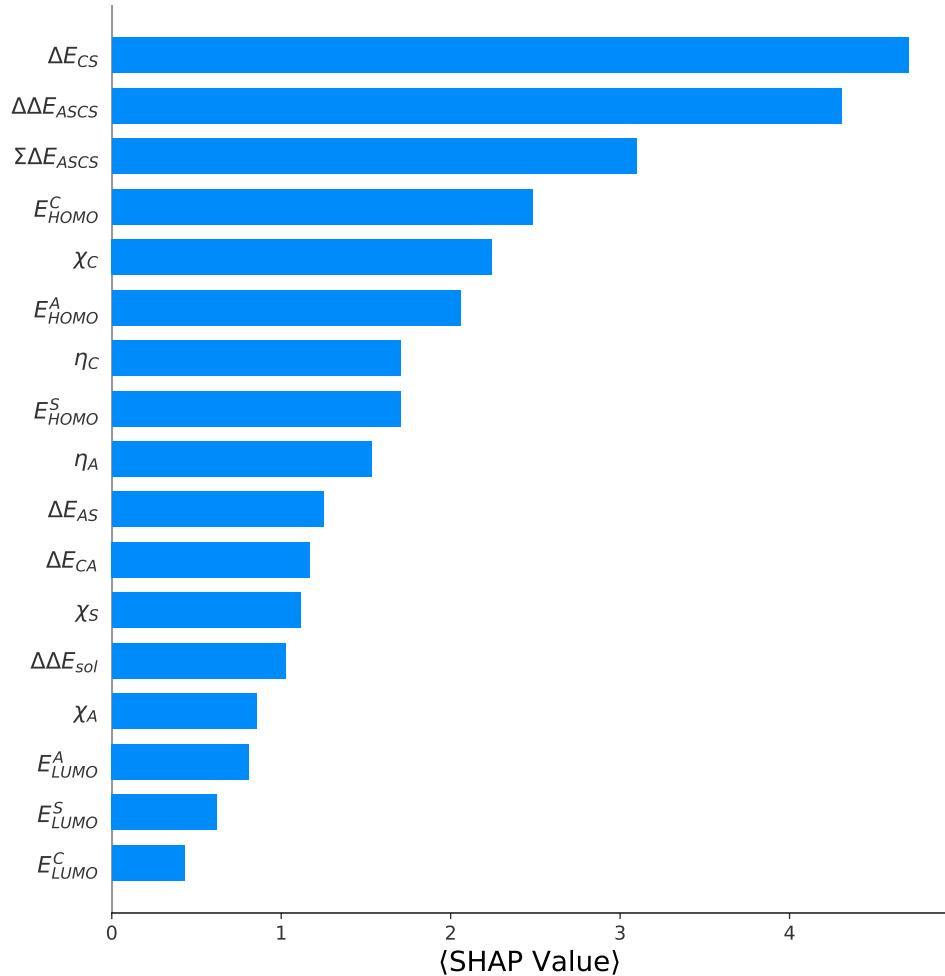


Figure 8: Net SHAP values for feature ranking of the reduced ET model for the prediction of ΔS_{sol} .