

Supplementary information: Sensitivity of $K\beta$ mainline X-ray emission to structural dynamics in iron photosensitizer

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1 Additional figures

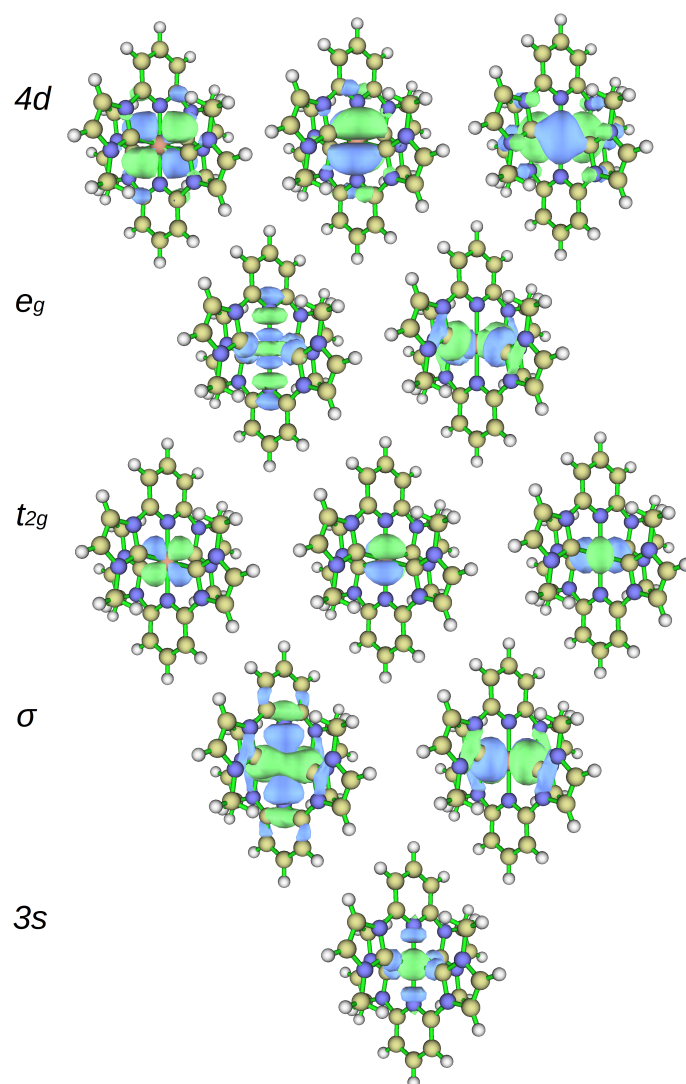


Figure S1: Isodensity plots of the RAS2 active orbitals: $3s$, σ , t_{2g} , e_g and $4d$. The orbitals are from a $1s$ core-hole calculation at the ground state geometry with doublet spin multiplicity.

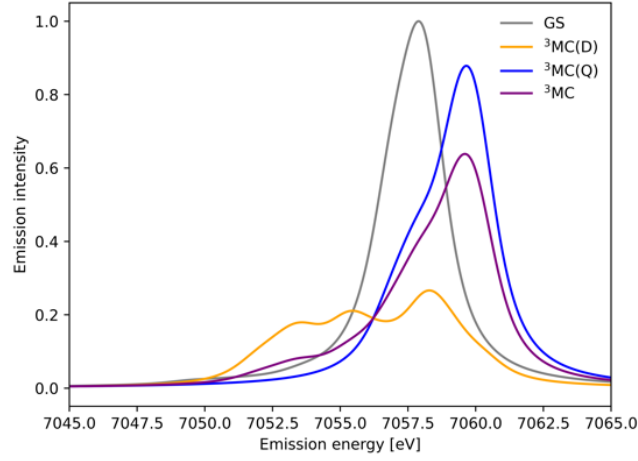


Figure S2: RAS $K\beta$ emission spectra for GS and ^3MC states. The ^3MC spectrum is obtained from the emission from doublet ($^3\text{MC(D)}$) and quartet ($^3\text{MC(Q)}$) $1s$ core-ionized states with a 4:2 ratio. All spectra are simulated using the GS equilibrium geometry.

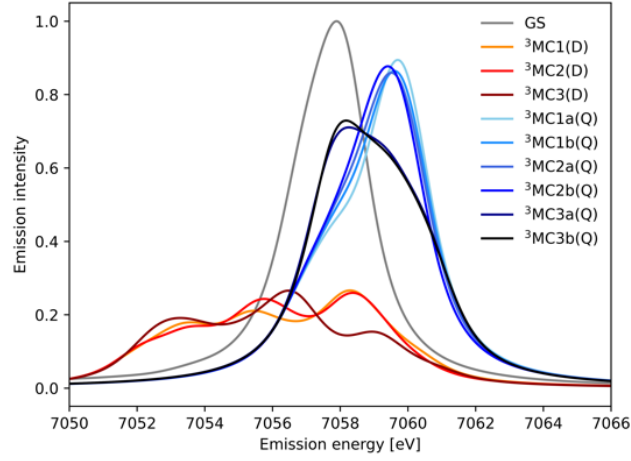


Figure S3: RAS $K\beta$ emission spectra for low-energy ^3MC intermediate ($1s$ core ionized) states calculated for the GS geometry. Quartet states are slit by spin-orbit coupling into groups of close-lying states (a and b). $^3\text{MCX(Q)}$ results are obtained using a 1:1 ratio of $^3\text{MCXa(Q)}$ and $^3\text{MCXb(Q)}$ results.

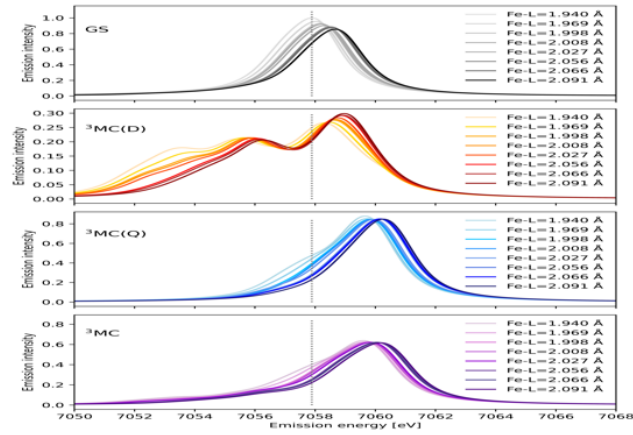


Figure S4: Structural sensitivity of RAS $K\beta$ emission spectra from different core-ionized intermediate states. Data are shown for for GS (top), $^3\text{MC(D)}$ (second top), $^3\text{MC(Q)}$ (second bottom) and the combined ^3MC (bottom) at eight different geometries with increasing Fe-ligand distance. The vertical dashed line represent the maximum emission intensity of the experimental spectra 7057.9 eV. Note the different emission intensity scales of the individual plots.

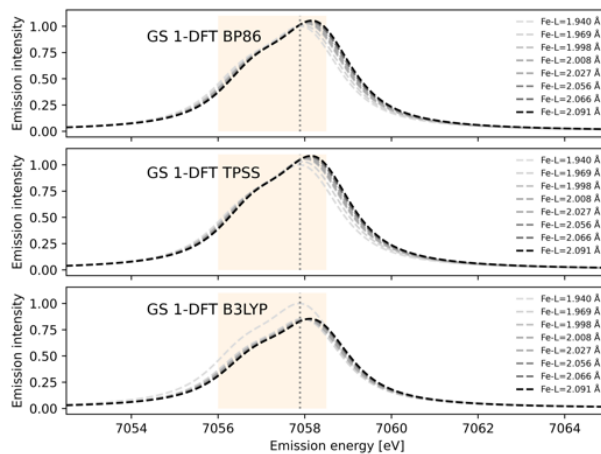


Figure S5: Functional dependence of simulated $K\beta$ emission spectra for the GS electronic state with 1-DFT BP86, B3LYP and TPSS. The grey dotted vertical line at 7057.9 eV represents the maximum emission intensity of the experimental GS spectrum. The yellow area represents the 7056 eV – 7058.5 eV energy range used for the $K\beta$ difference spectrum in reference¹.

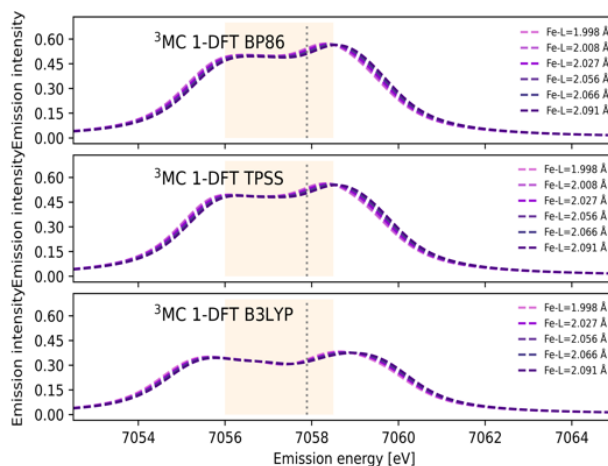


Figure S6: Functional dependence of simulated $K\beta$ emission spectra for the electronic 3MC state with 1-DFT BP86, B3LYP and TPSS. At short Fe-ligand distances the 3MC state is not stable with respect to a 3MLCT state and the corresponding spectra are not included. The grey dotted vertical line at 7057.9 eV represents the maximum emission intensity of the experimental GS spectrum. The yellow area represents the 7056 eV – 7058.5 eV energy range used for the $K\beta$ difference spectrum in reference¹.

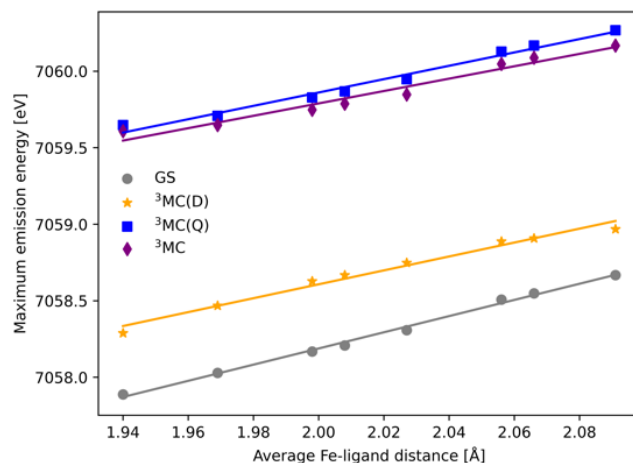


Figure S7: Energies of the RAS $K\beta$ emission maxima as a function of the Fe-ligand distance for the GS, $^3MC(Q)$, $^3MC(D)$ and the combined 3MC states.

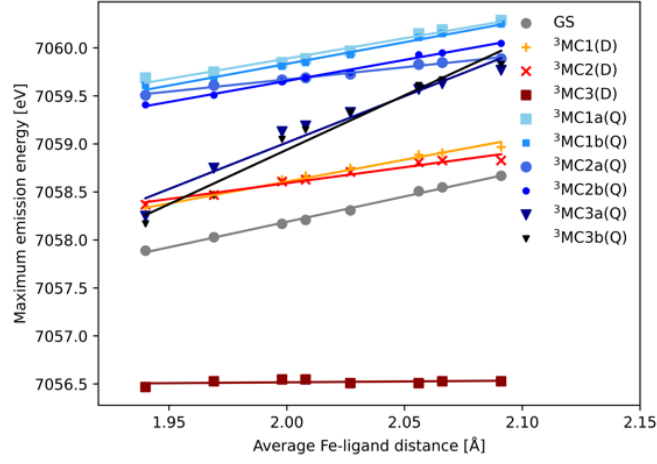


Figure S8: Energies of the RAS $K\beta$ emission maxima as a function of the Fe-ligand distance for the three lowest ${}^3\text{MC}(\text{Q})$ and ${}^3\text{MC}(\text{D})$ energy states. ${}^3\text{MCX}(\text{Q})$ results are obtained using a 1:1 ratio of ${}^3\text{MCXa}(\text{Q})$ and ${}^3\text{MCXb}(\text{Q})$ results.

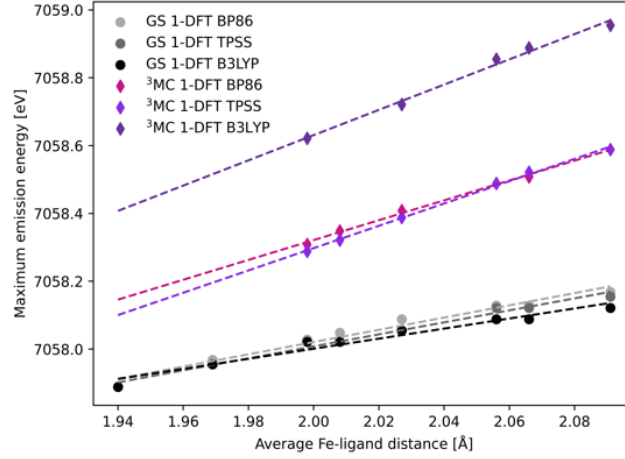


Figure S9: Functional dependence of the energies of the 1-DFT $K\beta$ emission maxima of the ${}^3\text{MC}$ and GS electronic states as a function of the Fe-ligand distance. Linear regression lines were fitted for each set of calculations.

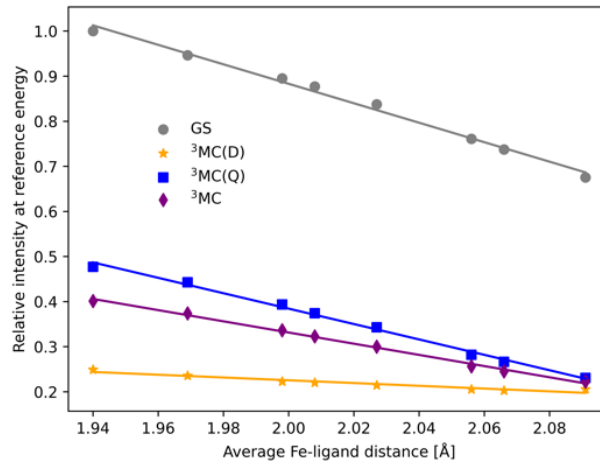


Figure S10: RAS $K\beta$ emission intensities at the GS maximum energy 7057.9 eV, as a function of the Fe-ligand distance for the GS, ${}^3\text{MC}(\text{Q})$, ${}^3\text{MC}(\text{D})$ and the combined ${}^3\text{MC}$ states.

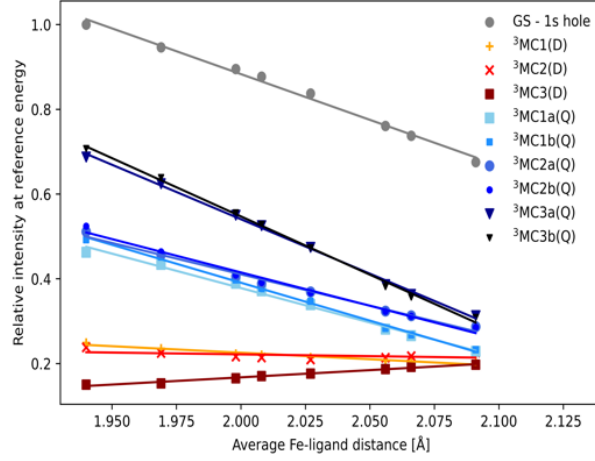


Figure S11: Integrated RAS $K\beta$ emission intensities at the GS maximum energy 7057.9 eV, as a function of the Fe-ligand distance for the GS, $^3\text{MC}(\text{D})$ and $^3\text{MC}(\text{Q})$ states. Quartet states are slit by spin-orbit coupling into groups of close-lying states (a and b). The $^3\text{MCXa}(\text{Q})$ and $^3\text{MCXb}(\text{Q})$ states are combined 1:1 to form the $^3\text{MCX}(\text{Q})$ state.

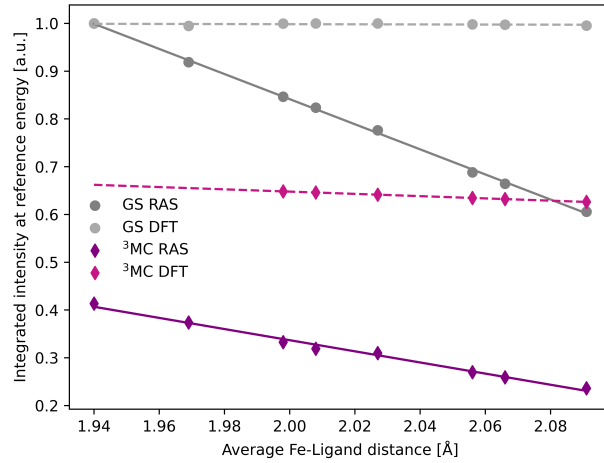


Figure S12: $K\beta$ emission intensities for the 7056-7058.5 eV energy range used in reference¹, as a function of the Fe-ligand distance for the GS and ^3MC states for both RAS and 1-DFT BP86.

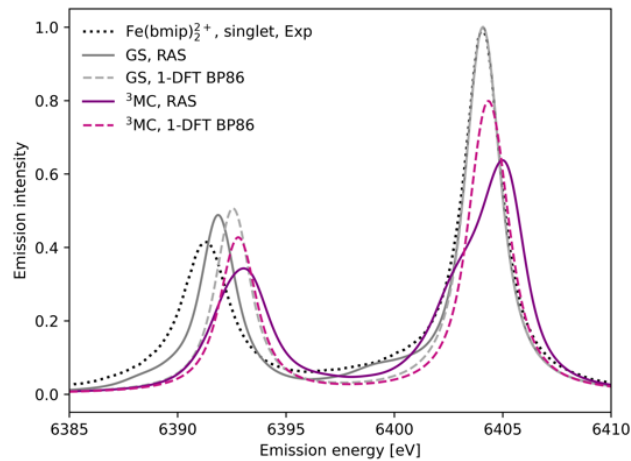


Figure S13: $K\alpha$ x-ray emission spectra from experiment, RAS and 1-DFT BP86 simulations. The GS and ^3MC spectra are calculated at the GS and ^3MC equilibrium geometries respectively. RAS data are taken from reference².

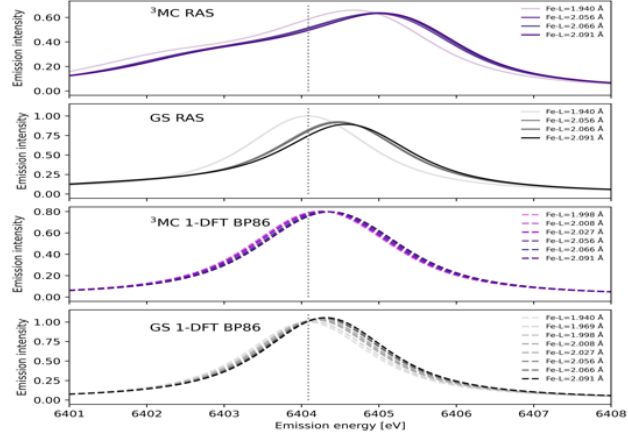


Figure S14: $K\alpha$ emission spectra simulated using RAS and 1-DFT BP86 for GS (top) and 3MC (bottom) electronic structures at different geometries with increasing Fe-ligand distances. The vertical dashed line represent the maximum emission intensity of the experimental spectra 6404.3 eV. RAS data are taken from reference².

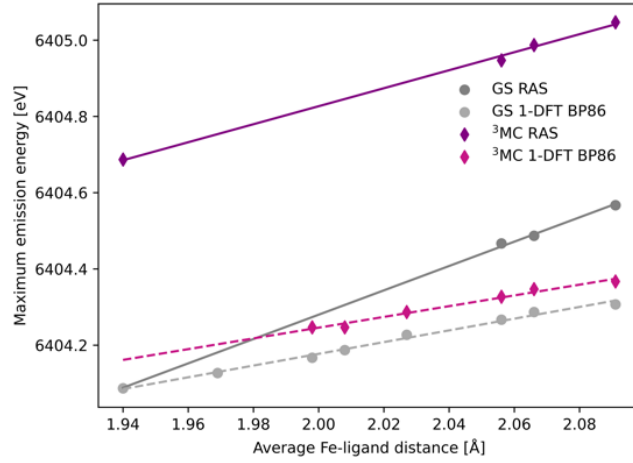


Figure S15: Energies of the $K\alpha$ emission maxima as a function of the Fe-ligand distance for the GS and 3MC from RAS (reference²) and 1-DFT BP86 simulations.

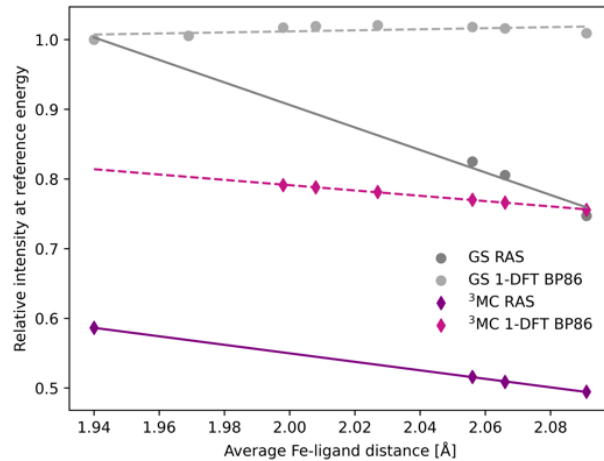


Figure S16: Intensities at the $K\alpha$ GS emission maxima as a function of the Fe-ligand distance for the GS and 3MC from RAS (reference²) and 1-DFT BP86 simulations.

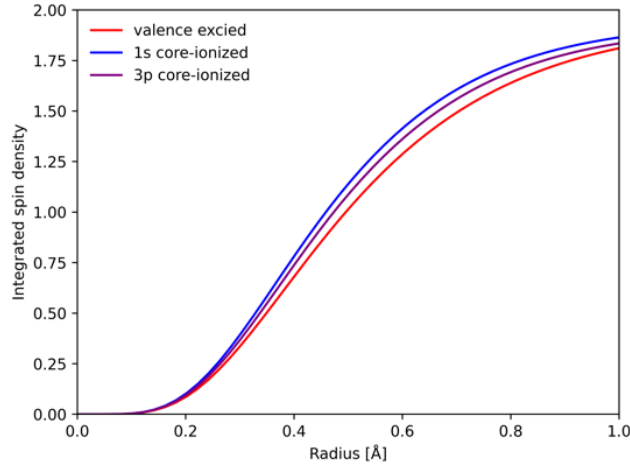


Figure S17: Integrated RAS radial spin density (RSD) plots of the ^3MC valence state, and the corresponding states with $1s$ and $3p$ holes calculated at the ^3MC equilibrium geometry. To avoid effects of changes in core orbital occupation, only the Fe $3d\ t_{2g}$ and e_g orbitals were included.

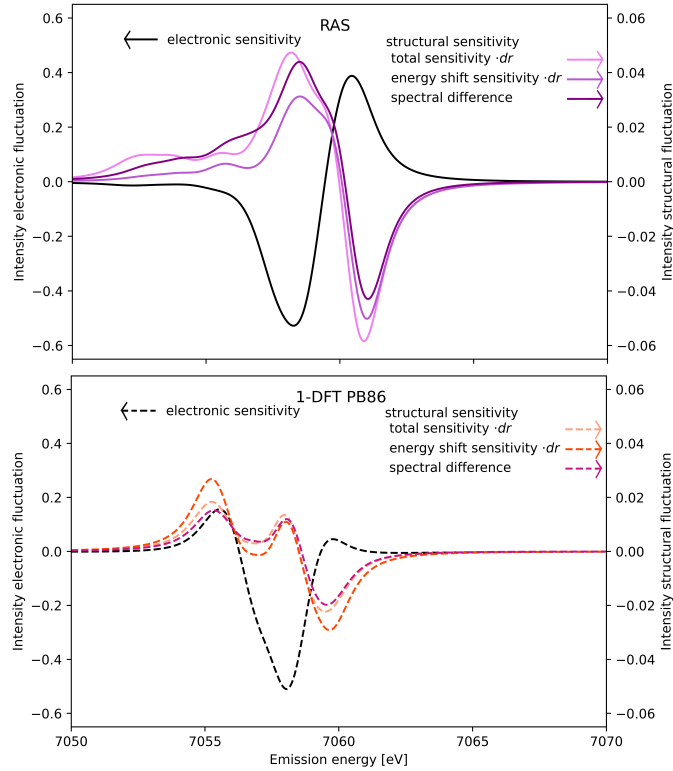


Figure S18: Comparison of three ways to estimate K β structural sensitivity of the ^3MC electronic state as a function of the emission energy. i) Slope of the intensity as a function of Fe-ligand distance (Total intensity) multiplied with the difference in the Fe-L bond length at the turning points in the wavepacket simulations ($\Delta r=0.035\text{ \AA}$) ($dI/dr \cdot \Delta r$). ii) Energy shift sensitivity ($\delta E_{max}/\delta r \cdot dI/dE$) at the ^3MC minimum geometry multiplied with vibrational oscillation (Δr). This is the same method used in reference². iii) Intensity difference between the the turning points in wavepacket simulations (Fe-L distances of 2.056 \AA and 2.091 \AA respectively).

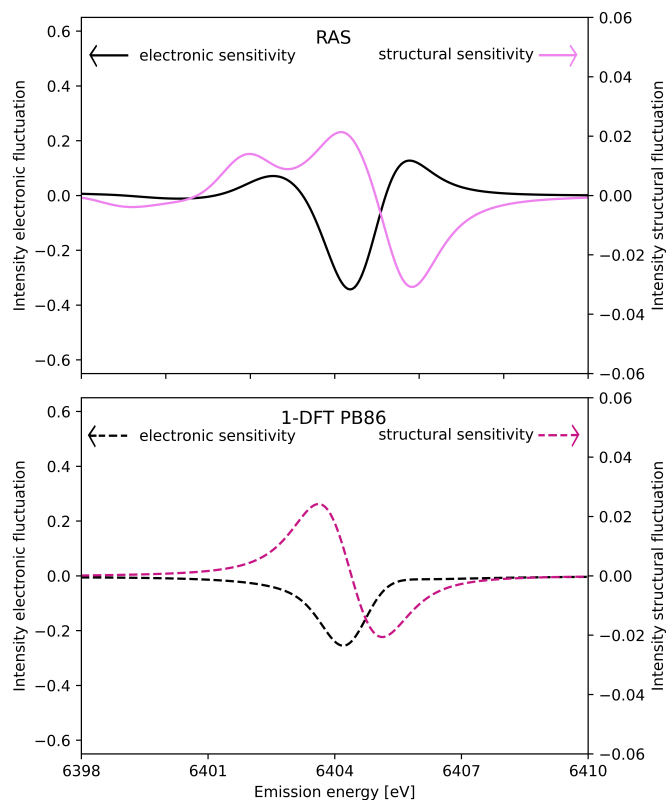


Figure S19: $K\alpha$ sensitivity to electron and structural dynamics as a function of the emission energy from RAS and 1-DFT BP86. Sensitivity to electron dynamics is calculated as the difference in intensity between the ^3MC and GS electronic states at the ^3MC minimum geometry (black curve, left y -axis). Structural sensitivity represents the intensity difference between the turning points in wavepacket simulations (Fe-L distances of 2.056 Å and 2.091 Å respectively) (purple curve, right y -axis), for RAS (top) and 1-DFT PB86 (bottom). Note the different y -scales.

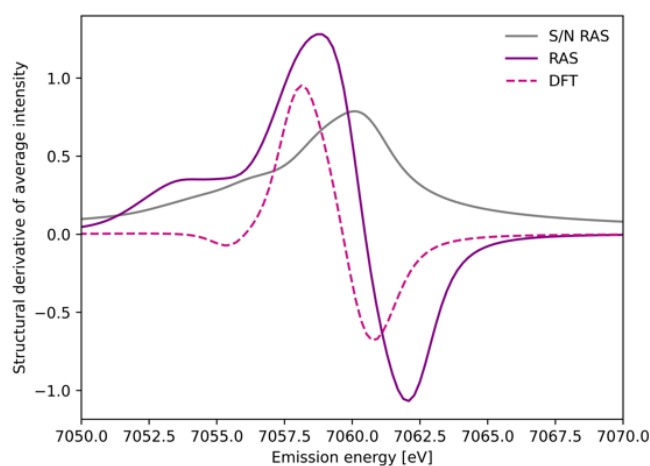


Figure S20: $K\beta$ sensitivity to structural dynamics as a function of the normalized integrated emission energy with RAS and 1-DFT BP86 using the Total sensitivity. Signal to noise (S/N) is calculated as the square root of the ^3MC spectra at the ^3MC minimum geometry for RAS (grey curve). The normalized integrated sensitivity to structural dynamics $\delta I_{\text{area}}/\delta r$ is calculated for the ^3MC electronic states as the negative emission intensity variation integrated over the 7056–7058.5 eV energy range. Calculations include spectra with Fe-ligand distances between 1.998 - 2.091 Å for RAS and 1-DFT (purple curves).

2 Additional tables

Table S1: Orbital energies and electron-nuclei interactions for an iron(II) atomic ion in the ground state (GS) and core-excited (CE) states with $1s$, $2p$ and $3p$ holes.

Orbital	Orbital energy (eV)				Nuclei interaction (eV)			
	GS	CE- $1s$	CE- $2p$	CE- $3p$	GS	CE- $1s$	CE- $2p$	CE- $3p$
$3s$	-134.3	-160.6	-158.5	-157.2	-874.5	-895.8	-890.7	-865.8
$3p$	-93.8	-120.3	-117.6	-114.1	-819.3	-850.1	-842.4	-817.3
$3d$	-34.5	-56.3	-56.9	53.7	-679.4	-738.6	-739.4	-702.3

Table S2: Pairwise interactions (in eV) between M-shell and $1s/2p/3p$ electrons for an iron(II) atomic system in ground state (GS) and core-excited (CE) states.

Orbitals	GS			CE- $1s$			CE- $2p$			CE- $3p$		
	$1s$	$2p$	$3p$	$1s$	$2p$	$3p$	$1s$	$2p$	$3p$	$1s$	$2p$	$3p$
$3s$	43.4	39.6	26.1	45.2	41.3	27.5	44.8	40.8	27.1	43.8	39.9	26.5
$3p$	42.3	38.1	27.4	44.9	40.4	29.2	44.3	39.8	28.7	43.0	38.7	27.9
$3d$	33.8	33.0	24.5	37.9	36.9	27.0	37.9	36.9	26.8	35.9	35.0	25.7

References

- [1] K. Kunnus, M. Vacher, T. C. B. Harlang, K. S. Kjær, K. Haldrup, E. Biasin, T. B. van Driel, M. Pápai, P. Chabera, Y. Liu, H. Tatsuno, C. Timm, E. Källman, M. Delcey, R. W. Hartsock, M. E. Reinhard, S. Koroidov, M. G. Laursen, F. B. Hansen, P. Vester, M. Christensen, L. Sandberg, Z. Németh, D. S. Szemes, É. Bajnóczi, R. Alonso-Mori, J. M. Glowina, S. Nelson, M. Sikorski, D. Sokaras, H. T. Lemke, S. E. Canton, K. B. Møller, M. M. Nielsen, G. Vankó, K. Wärnmark, V. Sundström, P. Persson, M. Lundberg, J. Uhlig and K. J. Gaffney, *Nature Communications*, 2020, **11**, 634.
- [2] M. Vacher, K. Kunnus, M. G. Delcey, K. J. Gaffney and M. Lundberg, *Structural Dynamics*, 2020, **7**, 044102.