

Electronic Supplementary Information (ESI) for
Efficient Asymmetrical Silicon-Metal Dimer Electrocatalysts for Nitrogen
Reduction Reaction

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1. Catalysts models

A 2D (2×2) supercell of $g\text{-C}_3\text{N}_4$ was built and then optimized to the stable structure ($a = 14.36$, $b = 14.35$, $\alpha = \beta = 90^\circ$, $\gamma = 120^\circ$), including the lattice constant. Then, heteroatom (Si or Metal) was substituted into the N_{v1} site and the optimized catalysts models were denoted as $\text{Si}@C_3N_4$ (shown in Fig. 1a) and $M@C_3N_4$ (including $\text{Mo}@C_3N_4$ and $\text{Ru}@C_3N_4$ as shown in Fig. S8). Additionally, Si and Metal were both substituted into two N_{v1} sites to build asymmetrical dimer catalysts and the optimized catalyst models were denoted as $\text{SiM}@C_3N_4$. The vacuum thickness of catalyst models along the z direction is set to 20 Å to avoid false interactions between periodic structures during geometry optimizations.

2. Scheme of ENRR on $\text{Si}@C_3N_4$

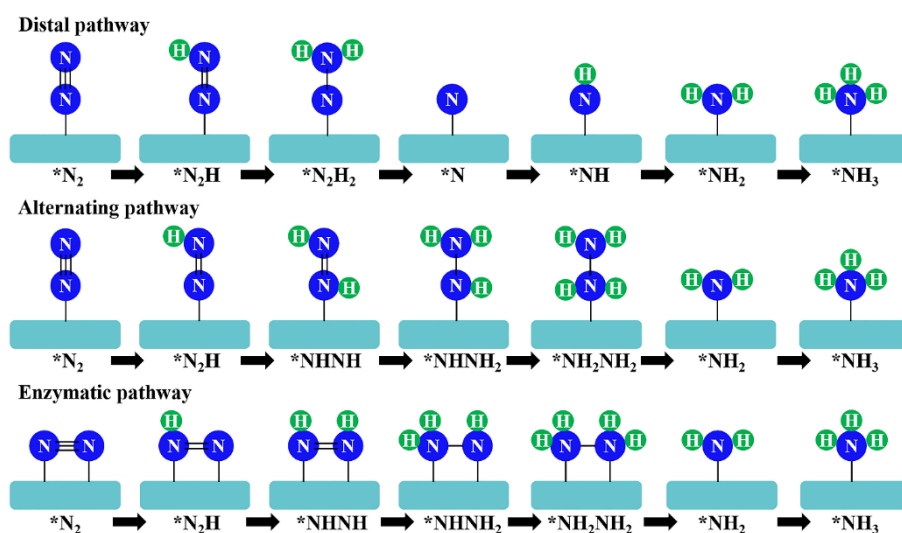


Fig. S1 The widely-proposed ENRR mechanisms, including distal, alternating and enzymatic ones.

3. Interstitial Si-doping into $g\text{-C}_3\text{N}_4$

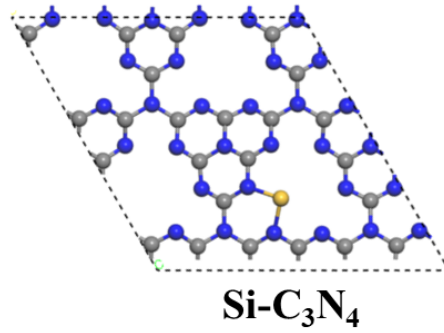


Fig. S2 The configuration of optimized Si-C₃N₄.

The formation energy of the configuration of Si-C₃N₄ is -0.02 eV, derived from the $E_f = E_{\text{Si-C}_3\text{N}_4} - \mu_{\text{Si}} - E_{g\text{-C}_3\text{N}_4}$, where $E_{\text{Si-C}_3\text{N}_4}$, and $E_{g\text{-C}_3\text{N}_4}$ represent the electronic energies of the catalyst and the pristine $g\text{-C}_3\text{N}_4$ substrate, and μ_{Si} refers to the chemical potential of Si, obtained by $1/n * E_{\text{Si-cell}}$. In comparison with the above configuration, the Si-doping into the Nv site (N_{v1}), named as Si@C₃N₄, is more energetically favorable.

4. SiM@C₃N₄ models

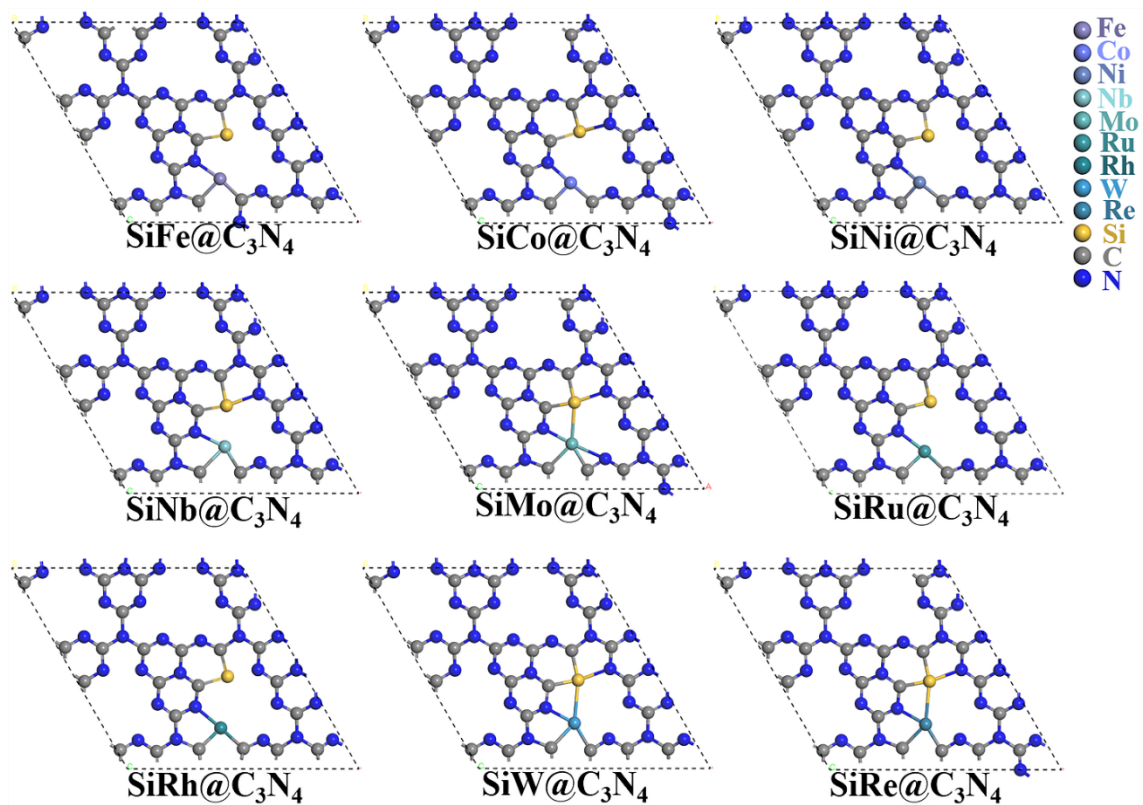


Fig. S3 The concept catalysts of SiM@C₃N₄.

5. Characteristics of SiM@C₃N₄

Table S1 Characteristics of SiM@C₃N₄.

| Catalysts | Adsorption energy | | Binding energies of dopants, E_b /eV | Cohesive energies, E_{co} /eV | Si-M bond length/Å |
|------------------------------------|-------------------|---------|---|------------------------------------|-----------------------|
| | E_{ads} /eV | | | | |
| | end-on | side-on | | | |
| Si@C ₃ N ₄ | 0.54 | 1.09 | -6.51 | -4.55 ($E_{co,Si}$) | — |
| Mo@C ₃ N ₄ | -0.77 | 0.01 | -6.98 | -5.86 ($E_{co,Mo}$) | — |
| Ru@C ₃ N ₄ | -0.24 | — | -7.95 | -6.77 ($E_{co,Ru}$) | — |
| SiFe@C ₃ N ₄ | — | 0.16 | -13.51 | -5.14 ($E_{co,Fe}$) | 2.82 |
| SiCo@C ₃ N ₄ | — | -0.04 | -13.91 | -5.02 ($E_{co,Co}$) | 3.23 |
| SiNi@C ₃ N ₄ | — | 0.43 | -14.08 | -4.70 ($E_{co,Ni}$) | 2.99 |
| SiNb@C ₃ N ₄ | — | 0.12 | -15.44 | -6.78 ($E_{co,Nb}$) | 2.86 |
| SiMo@C ₃ N ₄ | — | -0.38 | -14.18 | -5.86 ($E_{co,Mo}$) | 2.67 |
| SiRu@C ₃ N ₄ | — | -0.29 | -14.53 | -6.77 ($E_{co,Ru}$) | 3.11 |
| SiRh@C ₃ N ₄ | — | 0.34 | -14.31 | -5.66 ($E_{co,Rh}$) | 3.24 |
| SiW@C ₃ N ₄ | — | 0.06 | -15.58 | -8.59 ($E_{co,W}$) | 2.68 |
| SiRe@C ₃ N ₄ | — | — | -15.09 | -7.80 ($E_{co,Re}$) | 2.67 |

6. N₂ adsorption on SiRe@C₃N₄ model

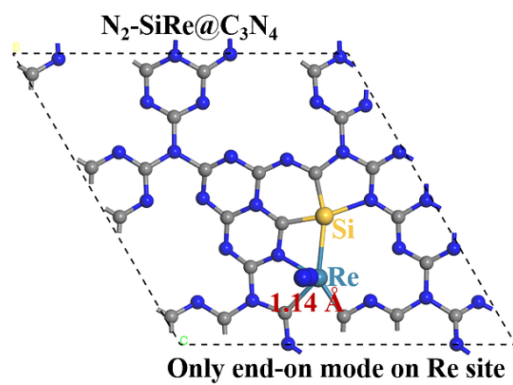


Fig. S4 N₂ adsorption on SiRe@C₃N₄.

7. Adsorption kinetics of N_2 on $SiM@C_3N_4$

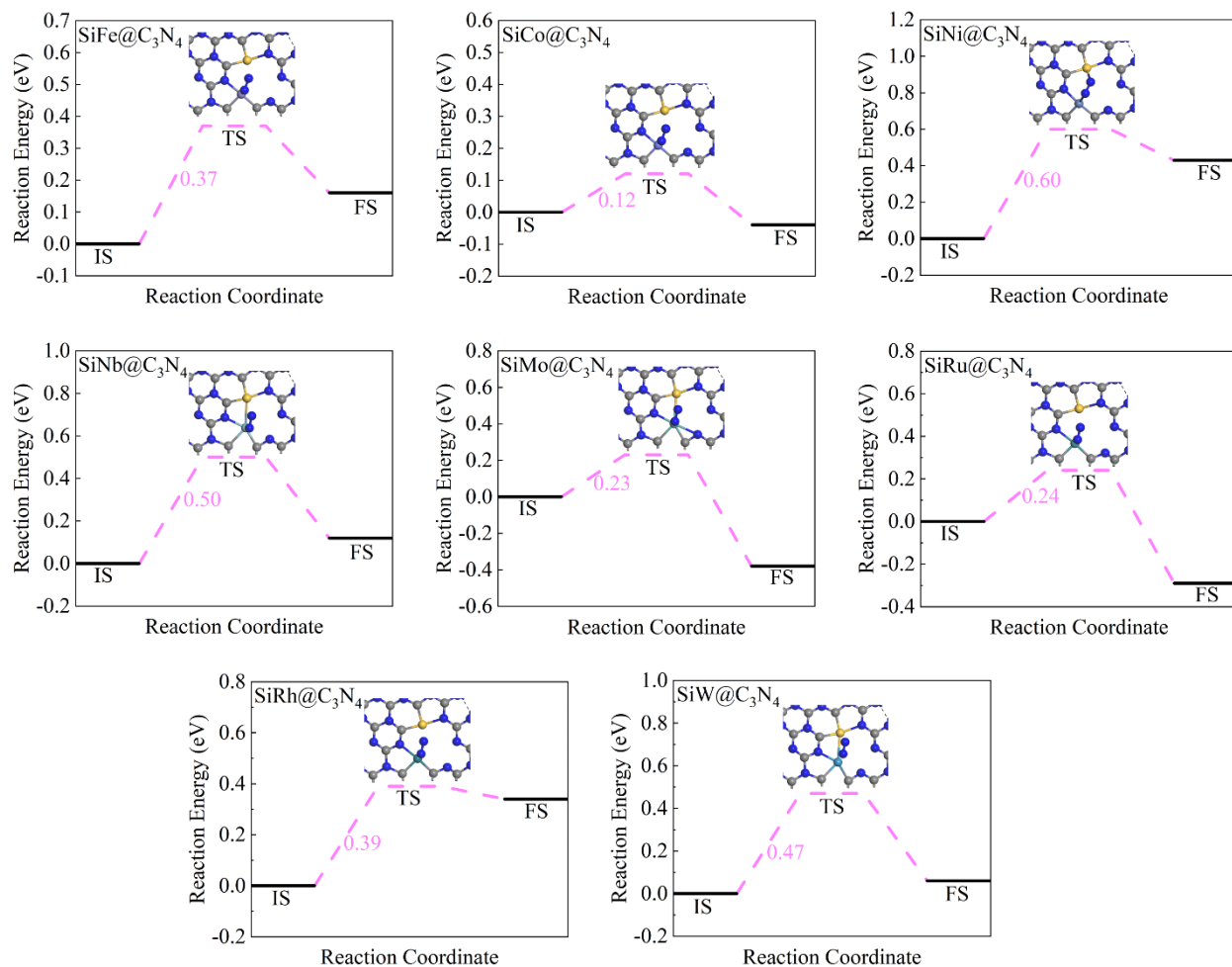


Fig. S5 The kinetics analysis of N_2 adsorption on $SiM@C_3N_4$ (inserts are the transition states). It is noticed that the TS was not analyzed for $SRe@C_3N_4$ because N_2 can merely be activated in the end-on configuration. The 'IS' and 'FS' terms refer to the initial and final states during the adsorption.

8. ENRR mechanisms on dimer catalysts

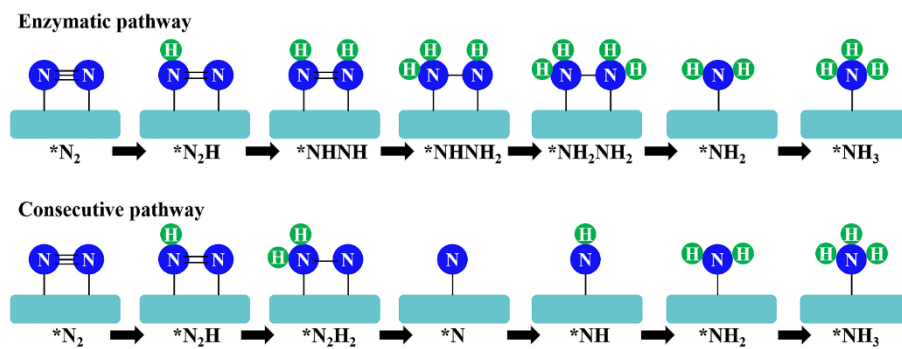


Fig. S6 The ENRR mechanisms on dimer catalysts.

9. ENRR pathways on SiRu@C₃N₄

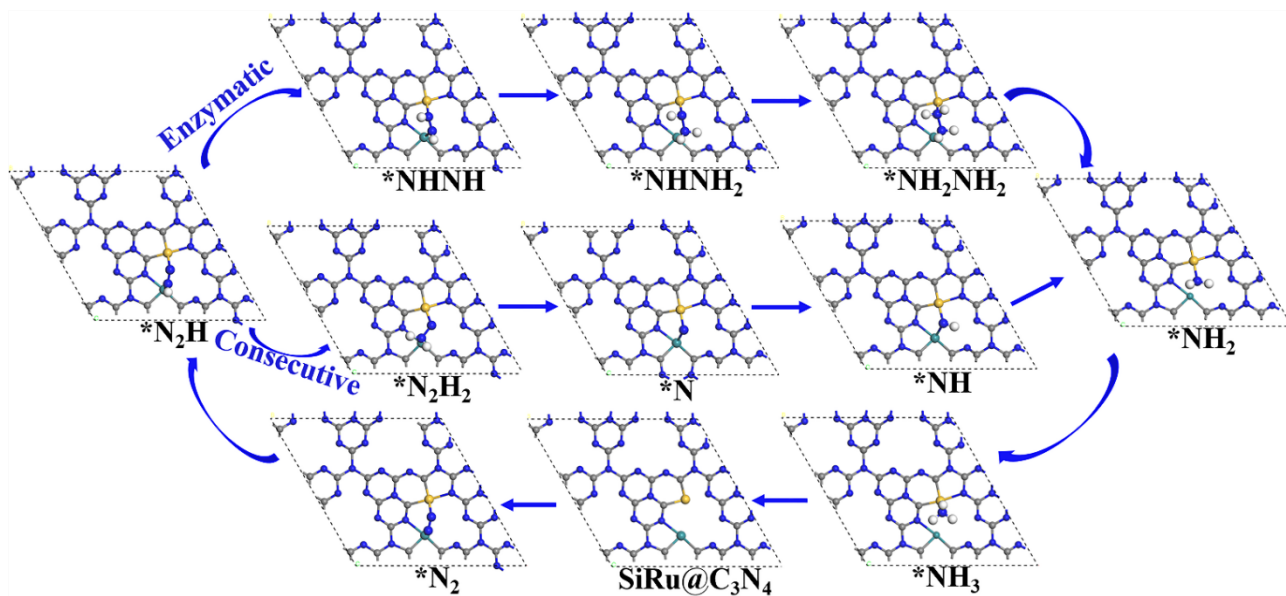


Fig. S7 ENRR enzymatic and consecutive pathways on SiRu@C₃N₄.

10. *N_2H on $SiMo@C_3N_4$ and $SiRu@C_3N_4$

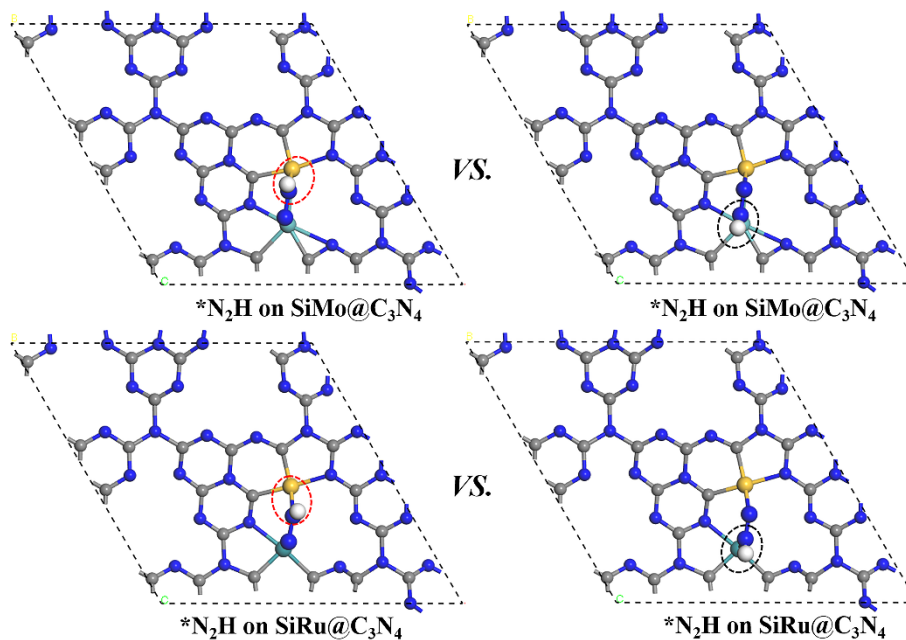


Fig. S8 The Si site *VS.* metal site (Mo/Ru) for the adsorption of *N_2H : the H^+/e^- pair tends to attack the N adatoms bound to the metal site energetically. The dash circles indicate different H adsorption sites on N adatom.

11. Mo@C₃N₄ and Ru@C₃N₄

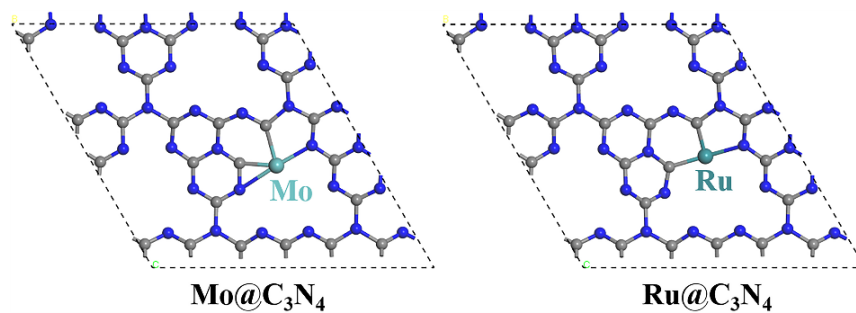


Fig. S9 The single-atom Mo/Ru catalysts supported on *g*-C₃N₄, named Mo@C₃N₄ and Ru@C₃N₄.

12. N₂ adsorption on Mo@C₃N₄ and Ru@C₃N₄

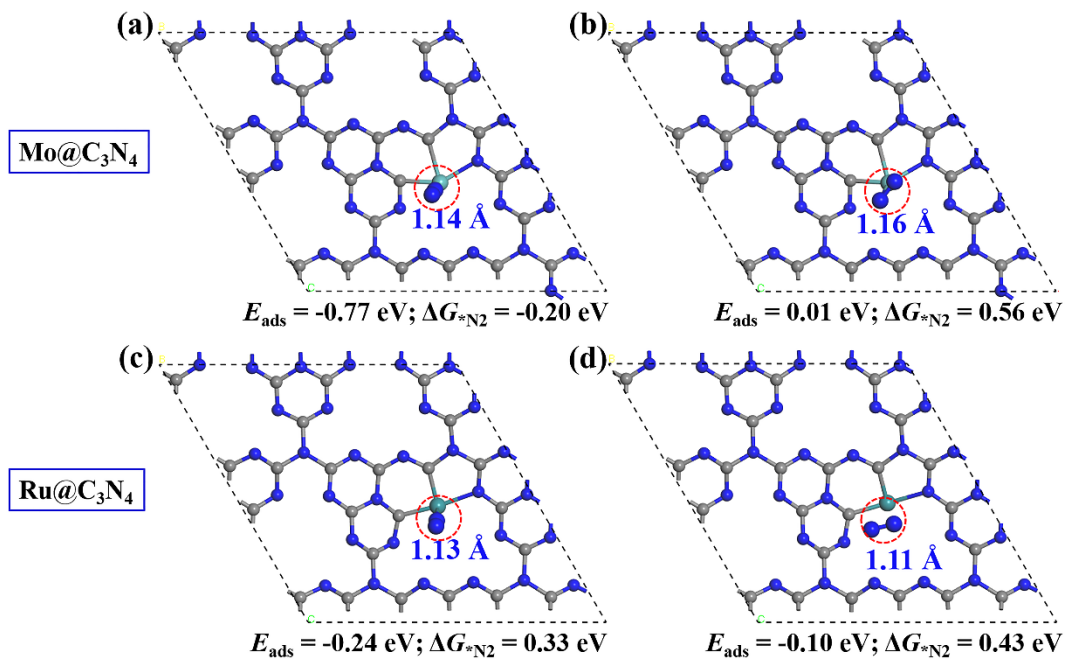
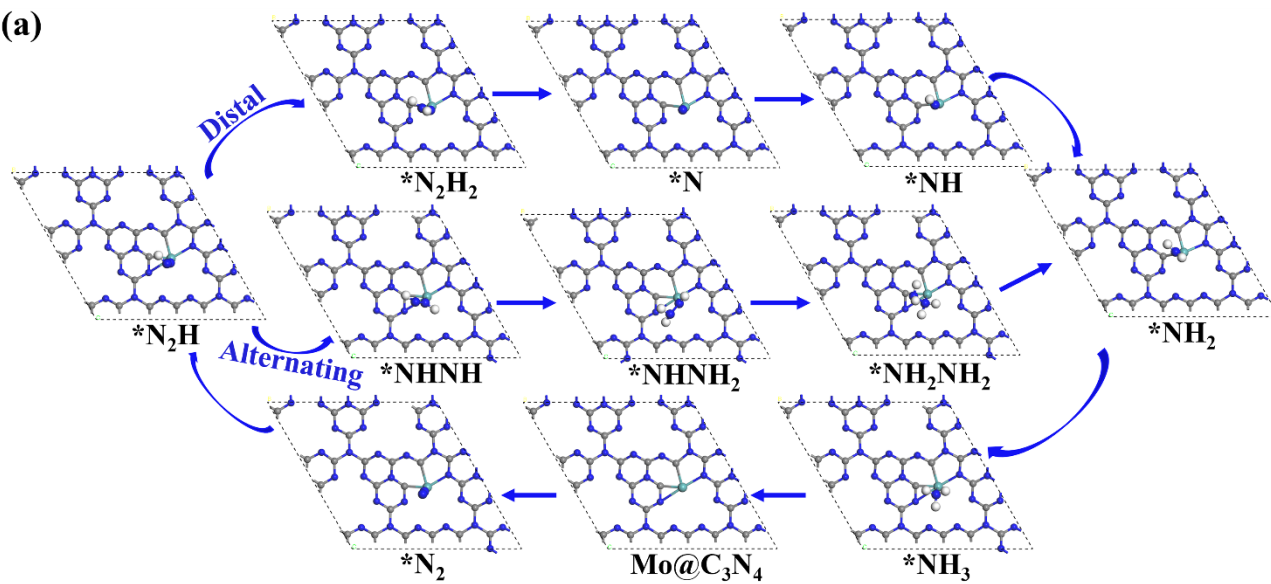


Fig. S10 The adsorption configurations of *N₂ on Mo@C₃N₄ and Ru@C₃N₄ with N-N bond lengths and energy changes.

13. ENRR on $\text{Mo@C}_3\text{N}_4$ and $\text{Ru@C}_3\text{N}_4$

(a)



(b)

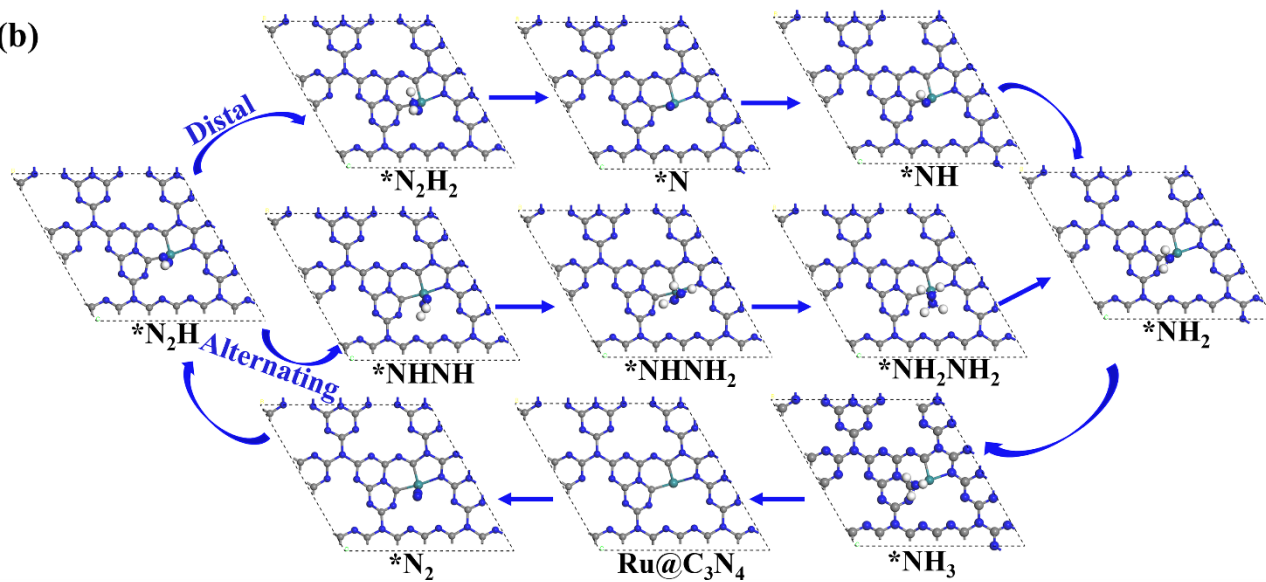


Fig. S11 ENRR intermediates along the distal and alternating pathways on (a) $\text{Mo@C}_3\text{N}_4$ and (b) $\text{Ru@C}_3\text{N}_4$.

14. Hirshfeld charge and N-N bond length analyses

Table S2 The Hirshfeld charge and N-N bond length analyses towards *N₂.

| Catalysts | N-N bond/Å | | Hirshfeld charges/e | |
|------------------------------------|------------|---------|---------------------|---------|
| | End-on | Side-on | End-on | Side-on |
| Si@C ₃ N ₄ | 1.13 | 1.21 | 0.06 | -0.14 |
| Mo@C ₃ N ₄ | 1.14 | 1.16 | -0.13 | — |
| Ru@C ₃ N ₄ | 1.13 | — | -0.01 | — |
| SiMo@C ₃ N ₄ | — | 1.21 | — | -0.20 |
| SiRu@C ₃ N ₄ | — | 1.20 | — | -0.18 |

15. DOS and orbital analyses for N₂

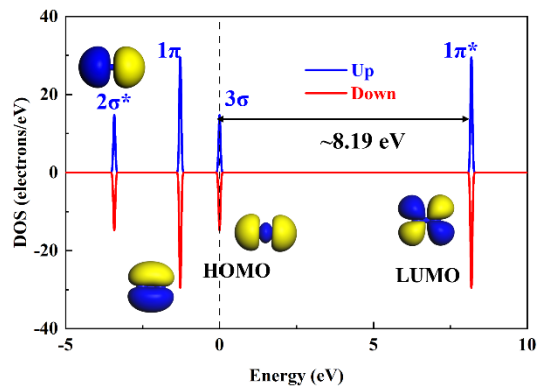


Fig. S12 DOS and orbital analyses for N₂.

From the above DOS image, it is noticed that the 3σ molecular orbital (MO) crosses the Fermi level. This image is produced by DMol³ package, where the HOMO level is automatically corrected to the Fermi level. Therefore, it does not indicate that N₂ possesses metallic properties. Also, we did the orbital analysis shown in the above image, again evidencing the accuracy of DOS collected.

16. Evolution of Hirshfeld charges

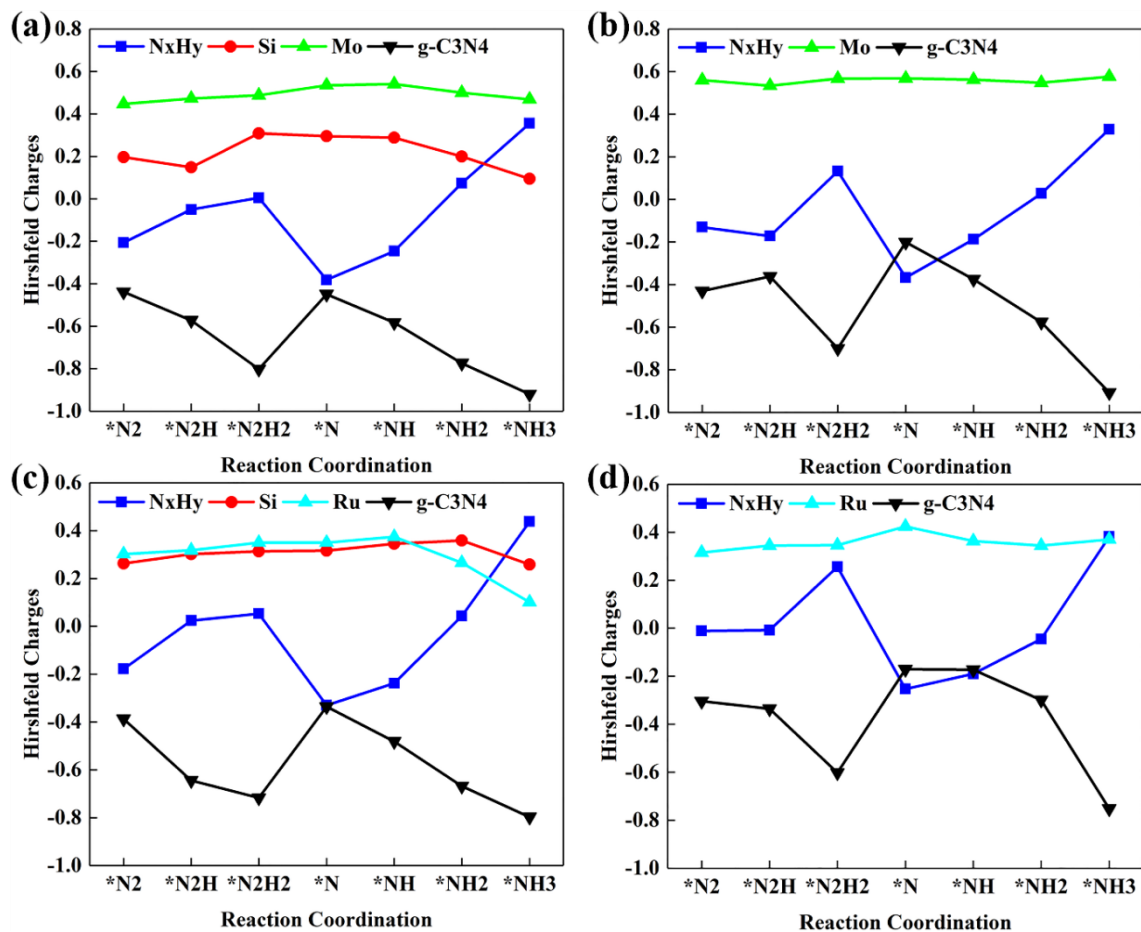


Fig. S13 (a, c) Evolution of Hirshfeld charges on SiMo@C₃N₄ and SiRu@C₃N₄ along the consecutive pathways; (b, d) Evolution of Hirshfeld charges on Mo@C₃N₄ and Ru@C₃N₄ along the distal pathway.

17. Energetically favorable configuration of dual Si-M dimer catalysts

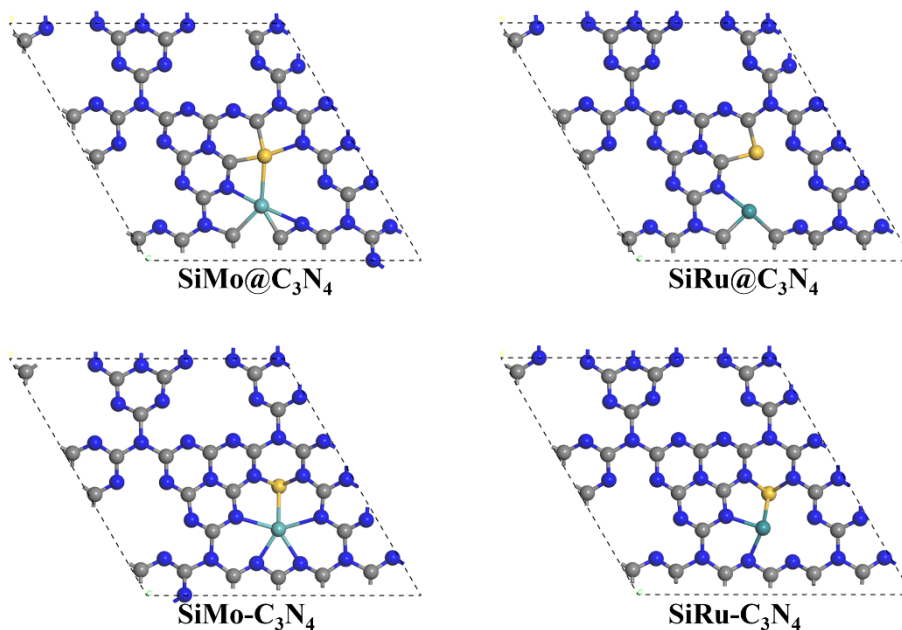


Fig. S14 Configurations of SiMo@C₃N₄ and SiRu@C₃N₄ vs. SiMo-C₃N₄ and SiRu-C₃N₄.

Here, we analyzed the formation energies of the above catalysts to evaluate the synthetic availability in labs. The dual-atom SiMo@C₃N₄ and SiRu@C₃N₄ catalysts designed by doping two dopant atoms into Nv1 vacancies are more energetically favorable than directly embedded into the hole of g-C₃N₄.

Table S3 Analyses of formation energies.

| Concept-catalysts | Si@C ₃ N ₄ | Si-C ₃ N ₄ | SiMo@C ₃ N ₄ | SiRu@C ₃ N ₄ | SiMo-C ₃ N ₄ | SiRu-C ₃ N ₄ |
|----------------------------|----------------------------------|----------------------------------|------------------------------------|------------------------------------|------------------------------------|------------------------------------|
| Formation energy/eV | -0.08 | -0.02 | 2.19 | 1.36 | 4.04 | 3.44 |

18. Thermodynamics calculated by DFT

Table S4 Thermodynamic quantities for H₂, N₂, and NH₃ gases at standard conditions (N₂ + 3H₂ → 2NH₃).

| Gases | E_{DFT}/eV | ZPE/eV | $\int C_p dT$ | TS/eV | G/eV |
|-----------------|----------------------------|--------|---------------|-------|----------|
| H ₂ | -32.07 | 0.27 | 0.09 | 0.40 | -32.11 |
| N ₂ | -2981.80 | 0.15 | 0.09 | 0.59 | -2982.15 |
| NH ₃ | -1539.82 | 0.89 | 0.10 | 0.60 | -1539.43 |

For the gas molecules, the Gibbs free energy calculation should be performed as follows:

$$\mu = E_{\text{DFT}} + \text{ZPE} + \int C_p dT - \text{TS}, \text{ where } \mu, E, \text{ and } C_p \text{ denote the chemical potential, electronic energy, and heat capacity, respectively.}$$

Table S5 Calculated data for ENRR.

| Intermediates | Catalysts (SiMo@C ₃ N ₄) | | Catalysts (SiRu@C ₃ N ₄) | | Catalysts (Mo@C ₃ N ₄) | | Catalysts (Ru@C ₃ N ₄) | |
|----------------------------------|---|--------|---|--------|---|--------|---|--------|
| | <i>E</i> _{DFT} /eV | ZPE/eV | <i>E</i> _{DFT} /eV | ZPE/eV | <i>E</i> _{DFT} /eV | ZPE/eV | <i>E</i> _{DFT} /eV | ZPE/eV |
| *N ₂ | -83069.63 | 0.20 | -83898.67 | 0.22 | -76683.90 | 0.22 | -77512.97 | 0.22 |
| *N ₂ H | -83085.84 | 0.55 | -83914.68 | 0.56 | -76699.45 | 0.50 | -77528.42 | 0.51 |
| *N ₂ H ₂ | -83102.79 | 0.91 | -83931.17 | 0.91 | -76715.83 | 0.84 | -77544.55 | 0.84 |
| *N | -81579.12 | 0.11 | -82407.32 | 0.095 | -75192.60 | 0.10 | -76020.32 | 0.09 |
| *NH | -81595.77 | 0.40 | -82425.16 | 0.43 | -75209.12 | 0.37 | -76037.32 | 0.36 |
| *NH ₂ | -81612.72 | 0.53 | -82442.03 | 0.75 | -75225.72 | 0.68 | -76054.91 | 0.70 |
| *NH ₃ | -81629.54 | 1.08 | -82457.92 | 0.90 | -75242.59 | 1.06 | -76071.55 | 1.08 |
| *NHNH | -83102.39 | 0.86 | -83931.14 | 0.86 | -76715.42 | 0.86 | -77544.53 | 0.66 |
| *NHNH ₂ | -83118.94 | 1.22 | -83947.86 | 1.24 | -76732.20 | 0.99 | -77561.17 | 1.18 |
| *NH ₂ NH ₂ | -83135.28 | 1.37 | -83963.92 | 1.38 | -76748.51 | 1.54 | -77577.83 | 1.34 |