

# Materials design, synthesis, and transport properties of disordered rare-earth Zintl bismuthides with the *anti*-Th<sub>3</sub>P<sub>4</sub> structure type

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**Table S1.** Fractional Atomic Coordinates and Equivalent Isotropic Displacement Parameters ( $\text{\AA}^2$ ) for  $\text{Ca}_{3.33(1)}\text{Ce}_{0.67}\text{Bi}_3$ .  $U_{eq}$  is defined as 1/3 of the trace of the orthogonalized  $U_{ij}$  tensor.

Atom	Site	$x$	$y$	$z$	$U_{eq}$
Ca1/Ce1 <sup>a</sup>	16c	0.07103(5)	$x$	$x$	0.0113(4)
Sb1	12a	3/8	0	1/4	0.0100(2)

<sup>a</sup>Atomic occupancies according to refinement: Ca1/Ce1 = 0.822(7)Ca + 0.178Ce.

**Table S2.** Fractional Atomic Coordinates and Equivalent Isotropic Displacement Parameters ( $\text{\AA}^2$ ) for  $\text{Ca}_{3.35(1)}\text{Pr}_{0.66}\text{Bi}_3$ .  $U_{eq}$  is defined as 1/3 of the trace of the orthogonalized  $U_{ij}$  tensor.

Atom	Site	$x$	$y$	$z$	$U_{eq}$
Ca1/Pr1 <sup>a</sup>	16c	0.0721(1)	$x$	$x$	0.0067(9)
Bi1	12a	3/8	0	1/4	0.0068(3)

<sup>a</sup>Atomic occupancies according to refinement: Ca1/Pr1 = 0.836(8)Ca + 0.164Pr.

**Table S3.** Fractional Atomic Coordinates and Equivalent Isotropic Displacement Parameters ( $\text{\AA}^2$ ) for  $\text{Ca}_{3.33(1)}\text{Nd}_{0.67}\text{Bi}_3$ .  $U_{eq}$  is defined as 1/3 of the trace of the orthogonalized  $U_{ij}$  tensor.

Atom	Site	$x$	$y$	$z$	$U_{eq}$
Ca1/Nd1 <sup>a</sup>	16c	0.0719(2)	$x$	$x$	0.0084(8)
Bi1	12a	3/8	0	1/4	0.0084(2)

<sup>a</sup>Atomic occupancies according to refinement: Ca1/Nd1 = 0.833(6)Ca + 0.167Nd.

**Table S4.** Fractional Atomic Coordinates and Equivalent Isotropic Displacement Parameters ( $\text{\AA}^2$ ) for  $\text{Ca}_{3.23(1)}\text{Sm}_{0.77}\text{Bi}_3$ .  $U_{eq}$  is defined as 1/3 of the trace of the orthogonalized  $U_{ij}$  tensor.

Atom	Site	$x$	$y$	$z$	$U_{eq}$
Ca1/Sm1 <sup>a</sup>	16c	0.0719(1)	$x$	$x$	0.0087(7)
Bi1	12a	3/8	0	1/4	0.0083(2)

<sup>a</sup>Atomic occupancies according to refinement: Ca1/Sm1 = 0.807(6)Ca + 0.193Sm.

**Table S5.** Fractional Atomic Coordinates and Equivalent Isotropic Displacement Parameters ( $\text{\AA}^2$ ) for  $\text{Ca}_{3.23(1)}\text{Gd}_{0.77}\text{Bi}_3$ .  $U_{eq}$  is defined as 1/3 of the trace of the orthogonalized  $U_{ij}$  tensor.

Atom	Site	$x$	$y$	$z$	$U_{eq}$
Ca1/Gd1 <sup>a</sup>	16c	0.0723(1)	$x$	$x$	0.0073(7)
Bi1	12a	3/8	0	1/4	0.0065(2)

<sup>a</sup>Atomic occupancies according to refinement: Ca1/Gd1 = 0.808(7)Ca + 0.192Gd.

**Table S6.** Fractional Atomic Coordinates and Equivalent Isotropic Displacement Parameters ( $\text{\AA}^2$ ) for  $\text{Ca}_{3.35(1)}\text{Tb}_{0.65}\text{Bi}_3$ .  $U_{eq}$  is defined as 1/3 of the trace of the orthogonalized  $U_{ij}$  tensor.

Atom	Site	$x$	$y$	$z$	$U_{eq}$
Ca1/Tb1 <sup>a</sup>	16c	0.0725(1)	$x$	$x$	0.011(1)
Bi1	12a	3/8	0	1/4	0.010(1)

<sup>a</sup>Atomic occupancies according to refinement: Ca1/Tb1 = 0.837(10)Ca + 0.163Tb.



**Table S7.** Fractional Atomic Coordinates and Equivalent Isotropic Displacement Parameters ( $\text{\AA}^2$ ) for  $\text{Ca}_{3.33(1)}\text{Dy}_{0.67}\text{Bi}_3$ .  $U_{eq}$  is defined as 1/3 of the trace of the orthogonalized  $U_{ij}$  tensor.

Atom	Site	$x$	$y$	$z$	$U_{eq}$
Ca1/Dy1 <sup>a</sup>	16c	0.0724(1)	$x$	$x$	0.0090(7)
Bi1	12a	3/8	0	1/4	0.0096(2)

<sup>a</sup>Atomic occupancies according to refinement: Ca1/Dy1 = 0.833(4)Ca + 0.167Dy

**Table S8.** Fractional Atomic Coordinates and Equivalent Isotropic Displacement Parameters ( $\text{\AA}^2$ ) for  $\text{Ca}_{3.38(1)}\text{Ho}_{0.62}\text{Bi}_3$ .  $U_{eq}$  is defined as 1/3 of the trace of the orthogonalized  $U_{ij}$  tensor.

Atom	Site	$x$	$y$	$z$	$U_{eq}$
Ca1/Ho1 <sup>a</sup>	16c	0.07252(9)	$x$	$x$	0.0095(6)
Bi1	12a	3/8	0	1/4	0.0097(2)

<sup>a</sup>Atomic occupancies according to refinement: Ca1/Ho1 = 0.844(5)Ca + 0.156Ho.

**Table S9.** Fractional Atomic Coordinates and Equivalent Isotropic Displacement Parameters ( $\text{\AA}^2$ ) for  $\text{Ca}_{3.27(1)}\text{Er}_{0.73}\text{Bi}_3$ .  $U_{eq}$  is defined as 1/3 of the trace of the orthogonalized  $U_{ij}$  tensor.

Atom	Site	$x$	$y$	$z$	$U_{eq}$
Ca1/Er1 <sup>a</sup>	16c	0.0727(2)	$x$	$x$	0.011(1)
Bi1	12a	3/8	0	1/4	0.010(1)

<sup>a</sup>Atomic occupancies according to refinement: Ca1/Er1 = 0.818(8)Ca + 0.182Er.

**Table S10.** Fractional Atomic Coordinates and Equivalent Isotropic Displacement Parameters ( $\text{\AA}^2$ ) for  $\text{Ca}_{3.25(1)}\text{Tm}_{0.75}\text{Bi}_3$ .  $U_{eq}$  is defined as 1/3 of the trace of the orthogonalized  $U_{ij}$  tensor.

Atom	Site	$x$	$y$	$z$	$U_{eq}$
Ca1/Tm1 <sup>a</sup>	16c	0.0725(1)	$x$	$x$	0.0091(9)
Bi1	12a	3/8	0	1/4	0.0106(3)

<sup>a</sup>Atomic occupancies according to refinement: Ca1/Tm1 = 0.813(7)Ca + 0.187Tm.

**Table S11.** Fractional Atomic Coordinates and Equivalent Isotropic Displacement Parameters ( $\text{\AA}^2$ ) for  $\text{Ca}_{3.47(1)}\text{Lu}_{0.5}\text{Bi}_3$ .  $U_{eq}$  is defined as 1/3 of the trace of the orthogonalized  $U_{ij}$  tensor.

Atom	Site	$x$	$y$	$z$	$U_{eq}$
Ca1/Lu1 <sup>a</sup>	16c	0.07235(9)	$x$	$x$	0.0116(5)
Bi1	12a	3/8	0	1/4	0.0151(3)

<sup>a</sup>Atomic occupancies according to refinement: Ca1/Lu1 = 0.865(6)Ca + 0.135Lu.

**Table S12.** Fractional Atomic Coordinates and Equivalent Isotropic Displacement Parameters ( $\text{\AA}^2$ ) for  $\text{Ca}_{3.29(1)}\text{Y}_{0.71}\text{Bi}_3$ .  $U_{eq}$  is defined as 1/3 of the trace of the orthogonalized  $U_{ij}$  tensor.

Atom	Site	$x$	$y$	$z$	$U_{eq}$
Ca1/Y1 <sup>a</sup>	16c	0.0728(2)	$x$	$x$	0.011(1)
Bi1	12a	3/8	0	1/4	0.0096(2)

<sup>a</sup>Atomic occupancies according to refinement: Ca1/Y1 = 0.823(18)Ca + 0.177Y.

**Table S13.** Fractional Atomic Coordinates and Equivalent Isotropic Displacement Parameters ( $\text{\AA}^2$ ) for  $\text{Ca}_{3.2}\text{Ho}_{0.8}\text{Bi}_{1.67(1)}\text{Sb}_{1.33}$ .  $U_{eq}$  is defined as 1/3 of the trace of the orthogonalized  $U_{ij}$  tensor.

Atom	Site	$x$	$y$	$z$	$U_{eq}$
Ca1/Ho1 <sup>a</sup>	16c	0.07250(2)	$x$	$x$	0.009(1)
Bi1/Sb1 <sup>b</sup>	12a	3/8	0	1/4	0.009(1)

<sup>a</sup>Atomic occupancies of Ca and Ho were fixed according to the ratio  $\text{Ca}/\text{Ho} = 0.8\text{Ca} + 0.2\text{Ho}$ .

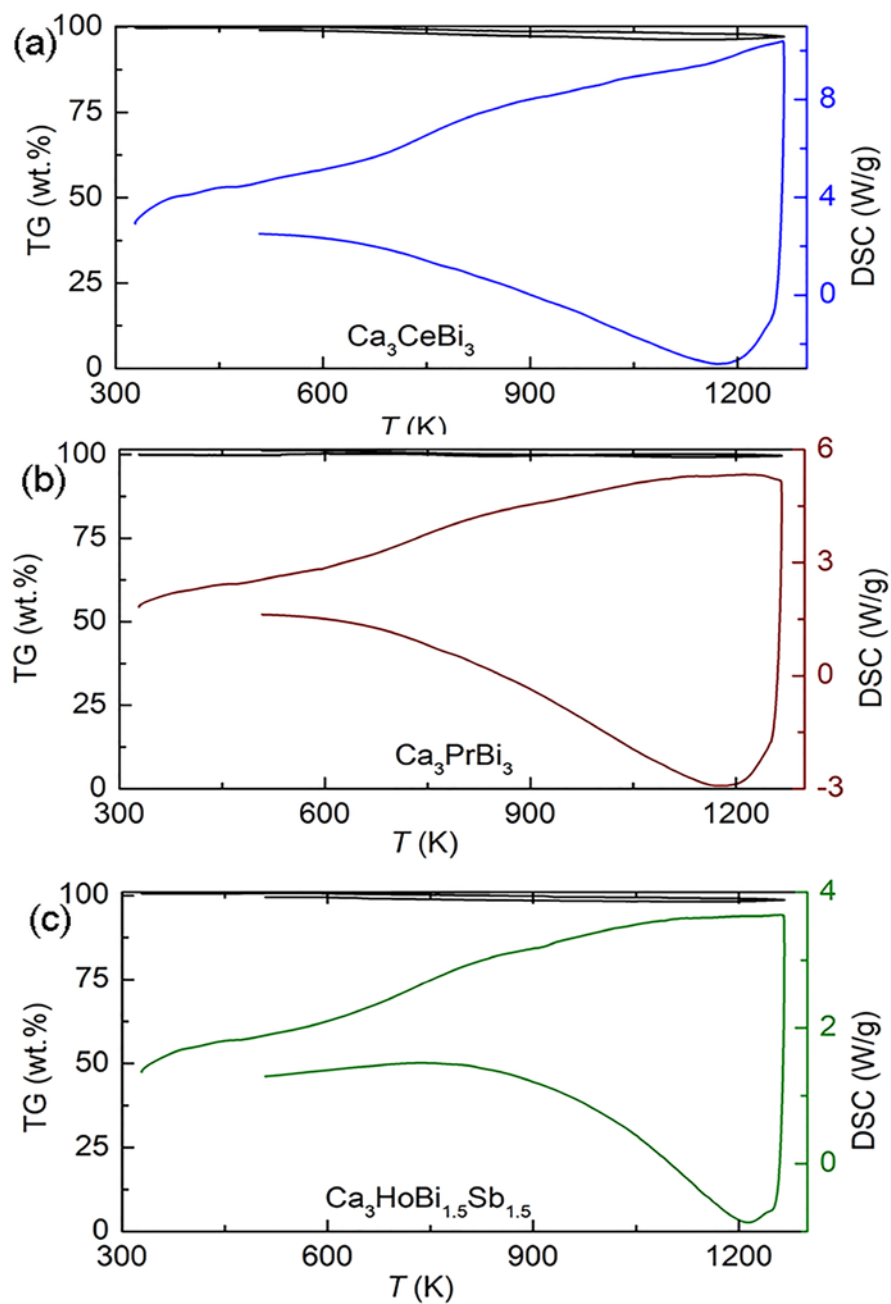
<sup>b</sup>Atomic occupancies according to refinement:  $\text{Bi1}/\text{Sb1} = 0.56(4)\text{Bi} + 0.44(4)\text{Sb}$ .

**Table S14.** Selected crystallographic data of  $\text{Ca}_3\text{HoBi}_{1.5}\text{Sb}_{1.5}$ , measured at 200(2) K, space group  $I\bar{4}3d$ ,  $Z = 4$ , Mo  $K\alpha$  radiation  $\lambda = 0.71073 \text{ \AA}$ .

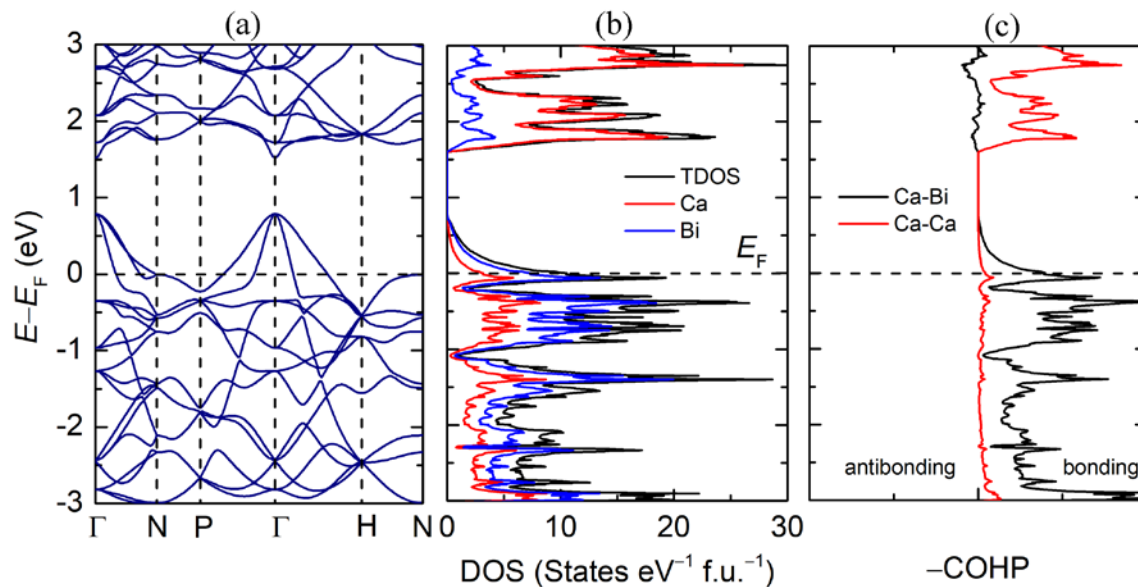
refined formula	$\text{Ca}_{3.2}\text{Ho}_{0.8}\text{Bi}_{1.67(1)}\text{Sb}_{1.33}$
formula wt.	771.12
$a/\text{\AA}$	9.4530(17)
$V/\text{\AA}^3$	844.7(4)
$\rho_{\text{cal}}/\text{g cm}^{-3}$	6.06
$\mu/\text{cm}^{-1}$	481.5
$R_1 (I \geq 2\sigma_I)^a$	0.0376
$wR_2 (I \geq 2\sigma_I)^a$	0.0768
$R_1$ (all data) <sup>a</sup>	0.0403
$wR_2$ (all data) <sup>a</sup>	0.0775
largest diff. peak and hole	2.69; -1.25

<sup>a</sup>  $R_1 = \sum ||F_o| - |F_c|| / \sum |F_o|$ ;  $wR_2 = [\sum [w(F_o^2 - F_c^2)^2] / \sum [w(F_o^2)]]^{1/2}$ , where  $w = 1 / [\sigma^2 F_o^2 + (0.0236P)^2 + (83.284P)]$ , and  $P = (F_o^2 + 2F_c^2) / 3$ .

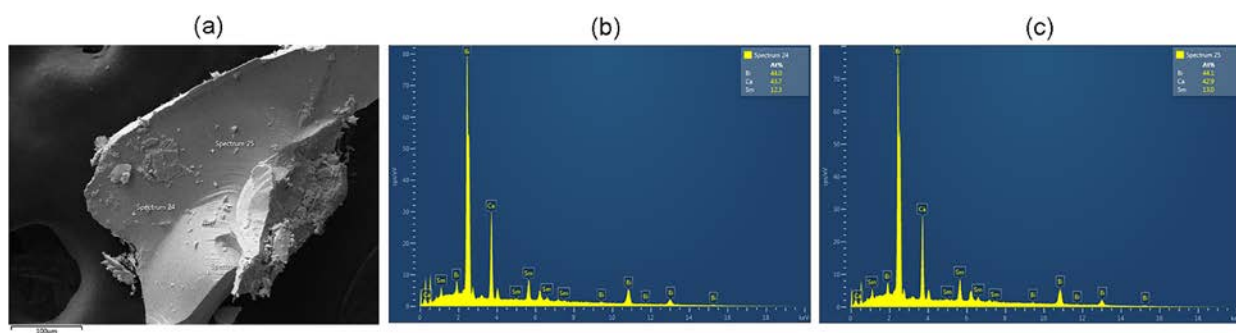




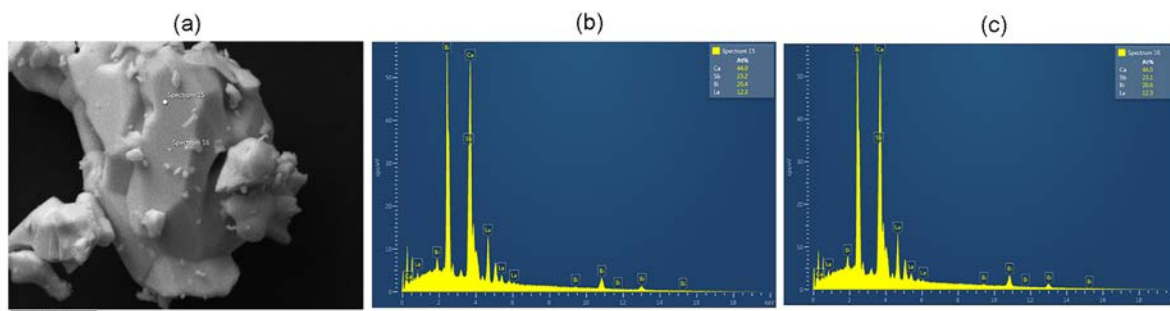
**Figure S1.** Plots of TG/DSC analysis for (a)  $\text{Ca}_3\text{LaBi}_3$  (b)  $\text{Ca}_3\text{PrBi}_3$  and (c)  $\text{Ca}_3\text{HoBi}_{1.5}\text{Sb}_{1.5}$  samples. The weight (wt.) % and heat flows are represented as blue, brown, and green lines, respectively.



**Figure S2.** (a) Electronic band structure of  $\text{Ca}_4\text{Bi}_3$ . (b) Total density of states (TDOS) and orbital resolved DOS of  $\text{Ca}_4\text{Bi}_3$ . (c) calculated COHP curves for Ca–Bi and Ca–Ca interactions for  $\text{Ca}_4\text{Bi}_3$ . COHP are showing the bonding and antibonding states as indicated. The Fermi energy is set as a reference point at 0 eV.



**Figure S3.** (a) SEM image of single crystal of  $\text{Ca}_3\text{SmBi}_3$ . (b) and (c) Representative histograms from EDS analysis of  $\text{Ca}_3\text{SmBi}_3$  under high magnification.



**Figure S4.** (a) SEM image of single crystal of  $\text{Ca}_3\text{LaBi}_{1.5}\text{Sb}_{1.5}$ . (b) and (c) Representative histograms from EDS analysis of  $\text{Ca}_3\text{SmBi}_3$  under high magnification.