## Supporting information

# Understanding the Role of Flux, Pressure and Temperature on Polymorphism in $\mathrm{ThB}_{2} \mathrm{O}_{5}$ 



Figure S1. SEM image and EDS measurement for $\beta-\mathrm{ThB}_{2} \mathrm{O}_{5}$

Table S1. Selected Important Bond Lengths (angstroms) for $\beta-\mathrm{ThB}_{2} \mathrm{O}_{5}$.

| $\mathrm{Th}(1)-\mathrm{O}(3) \# 1$ | $2.302(5)$ | $\mathrm{Th}(1)-\mathrm{O}(3) \# 2$ | $2.302(5)$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{Th}(1)-\mathrm{O}(2) \# 3$ | $2.370(6)$ | $\mathrm{Th}(1)-\mathrm{O}(1)$ | $2.583(6)$ |
| $\mathrm{Th}(1)-\mathrm{O}(4) \# 4$ | $2.520(7)$ | $\mathrm{Th}(1)-\mathrm{O}(2)$ | $2.514(6)$ |
| $\mathrm{Th}(1)-\mathrm{O}(3) \# 5$ | $2.539(5)$ | $\mathrm{Th}(1)-\mathrm{O}(3) \# 6$ | $2.539(5)$ |
| $\mathrm{Th}(1)-\mathrm{O}(3)$ | $3.067(6)$ | $\mathrm{Th}(1)-\mathrm{O}(3)$ | $3.067(6)$ |
|  |  |  |  |
| $\mathrm{B}(1)-\mathrm{O}(1)$ | $1.472(11)$ | $\mathrm{B}(1)-\mathrm{O}(3)$ | $1.455(7)$ |
| $\mathrm{B}(1)-\mathrm{O}(4)$ | $1.471(11)$ | $\mathrm{B}(1)-\mathrm{O}(3) \# 7$ | $1.455(7)$ |
| $\mathrm{B}(2)-\mathrm{O}(2)$ | $1.356(11)$ | $\mathrm{B}(2)-\mathrm{O}(1)$ | $1.380(11)$ |
| $\mathrm{B}(2)-\mathrm{O}(4) \# 3$ | $1.390(11)$ |  |  |

Symmetry transformations used to generate equivalent atoms:
$\# 1-x,-y,-z+2, \# 2-x, y+1 / 2,-z+2, \# 3 x-1, y, z, \# 4 x+1, y, z+1, \# 5 x,-y+1 / 2, z+1, \# 6 x, y, z+1$, \#7 x, $-\mathrm{y}+1 / 2$, z .


Figure S2. PXRD patterns of High-Pressured (4GPa) phase of $\mathrm{ThB}_{2} \mathrm{O}_{5}$, calculated $\alpha-, \beta-\mathrm{ThB}_{2} \mathrm{O}_{5}$ and the mixture of $\alpha$ - and $\beta-\mathrm{ThB}_{2} \mathrm{O}_{5}$.


Figure S3. Thermal dependence of the $a, b, c$ and $\beta$ lattice parameters of $a-\mathrm{ThB}_{2} \mathrm{O}_{5}$ determined from refinements against in situ PXRD data using the Le Bail method.


Figure S4. Thermal dependence of the lattice volume normalized per formula unite.


Figure S5. HT-PXRD pattern of a mixture of $\alpha-(34 \%), \beta-\mathrm{ThB}_{2} \mathrm{O}_{5}(66 \%)$ and PXRD pattern of calculated $\mathrm{ThO}_{2}$.


Figure S6. The Th-coordination environment with Th-O bond lengths in the structure of $\beta-\mathrm{ThB}_{2} \mathrm{O}_{5}$.
Thorium atom, B1 atom are shown in yellow and cyan, oxygen atoms in red.


Figure S7. The 3D Th borate framework formed by B-O chains link the 2D Th-based sheets in $\beta$ ThB ${ }_{2} \mathrm{O}_{5}$, through corner $\left(\mathrm{BO}_{4}\right)$, edge $\left(\mathrm{BO}_{3}\right)$, and face $\left(\mathrm{BO}_{4}\right)$ sharing. Thorium polyhedra, $\mathrm{BO}_{3}$ triangles and $\mathrm{BO}_{4}$ tetrahedra are shown in yellow, green and cyan.


Figure S8. Four membered rings along the $a$-axis in the structure of $\beta$ - $\operatorname{ThB}_{2} \mathrm{O}_{5}$.


Figure S9. Representation of the $\alpha-\mathrm{ThB}_{2} \mathrm{O}_{5}$ structure. A one-capped distorted thorium pentagonal bipyramid (a), a four-fold Th-coordinated thorium polyhedron (b), the 3D thorium network structure along the $b$-axis (c), a $\mathrm{B}_{2} \mathrm{O}_{5}$ dimer (d), the 3D thorium borate framework structure along the $b$-axis (e). $\mathrm{ThO}_{8}$ polyhedra and $\mathrm{BO}_{3}$ triangles are shown in yellow and green, O atoms are shown in red.


Figure S10. Schlegel projections of the Voronoi-Dirichlet polyhedral (VDP) with $4^{5} \cdot 5^{2} \cdot 6^{5}$ ( $\beta$ $\left.\mathrm{ThB}_{2} \mathrm{O}_{5}\right)$ and $3^{4} \cdot 4^{4} \cdot 5^{8} \cdot 10^{4}\left(\alpha-\mathrm{ThB}_{2} \mathrm{O}_{5}\right)$ combinatorial-topological types (CTTs).


Figure S11. Cationic topology representation of $\beta-\mathrm{ThB}_{2} \mathrm{O}_{5}$. (a) A zigzag boron chain $\cdots$ B1B2B1B2B1 $\cdots$ along the $a$-axis, (b) a 2D $\left\{3^{6}\right\}$ Th-sheet parallel to the $a b$-plain, (c) Topological view of the 3D new 3 -nodal cation network along $a$-axis with a point symbol of $\left\{3^{4}, 4^{10}, 5^{10}\right.$, $\left.6^{4}\right\}\left\{3^{4}, 4^{10}, 5^{6}, 6\right\}\left\{3^{4}, 4^{4}, 5^{2}\right\}$. The Th cations are shown as 8 -connected nodes with blackballs, B1 and B2 are 7 and 5-connected nodes as hollow balls.


Figure S12. TG and DSC curves of $\alpha-\mathrm{ThB}_{2} \mathrm{O}_{5}$ from 200 to $1200^{\circ} \mathrm{C}$.


Figure S13. Raman spectra of compound $\beta-\operatorname{ThB}_{2} \mathrm{O}_{5}$ (a) and $\alpha-\mathrm{ThB}_{2} \mathrm{O}_{5}$ (b) presented in the range 100 to $1500 \mu \mathrm{~m}$.

Table S2. The lattice parameters of $\alpha-\mathrm{ThB}_{2} \mathrm{O}_{5}$ and $\beta-\mathrm{ThB}_{2} \mathrm{O}_{5}$ obtained by DFT studies. In parentheses we report the offset from the measured values.

|  | $\beta-\mathrm{ThB}_{2} \mathrm{O}_{5}$ | $\alpha-\mathrm{ThB}_{2} \mathrm{O}_{5}$ |
| :--- | :--- | :--- |
| A | $4.239(-0.014)$ | $11.643(+0.098)$ |
| B | $6.934(+0.061)$ | $7.037(+0.100)$ |
| C | $6.339(+0.015)$ | $10.258(-0.005)$ |
| Alpaha | 90 | 90 |
| Betha | $106.69(+0.374)$ | 90 |
| Gamma | 90 | $825.96(+20.52)$ |
| Vol | $178.47(+1.03)$ |  |

Table S3.Computed and measured IR bands positions. The frequencies are reported in $\mathbf{c m}^{-}$ ${ }^{1}$.

| $\beta-\mathrm{ThB}_{2} \mathrm{O}_{5}$ |  | $\alpha-\mathrm{ThB}_{2} \mathrm{O}_{5}$ |  |
| :--- | :--- | :--- | :--- |
| computed | experimental | computed | experimental |
| 1411 | 1438,1385 | 1400 | 1414 |
| 1294 | 1268 | 1250,1252 | 1257 |
| 1078 | 1072 | 1028 | 1027 |
| $990,945,914$ | 928 | $634,630,618$ | 652 |
| 790 | 807 | $513,508,505$ | 529 |
| 715 | 652 |  |  |
| 628 | 580,557 |  |  |
| 562,543 |  |  |  |

