

Supplementary Materials for

Automated biophysical classification of apoptotic pancreatic cancer cell subpopulations by using machine learning approaches with impedance cytometry

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A. Supplementary Results

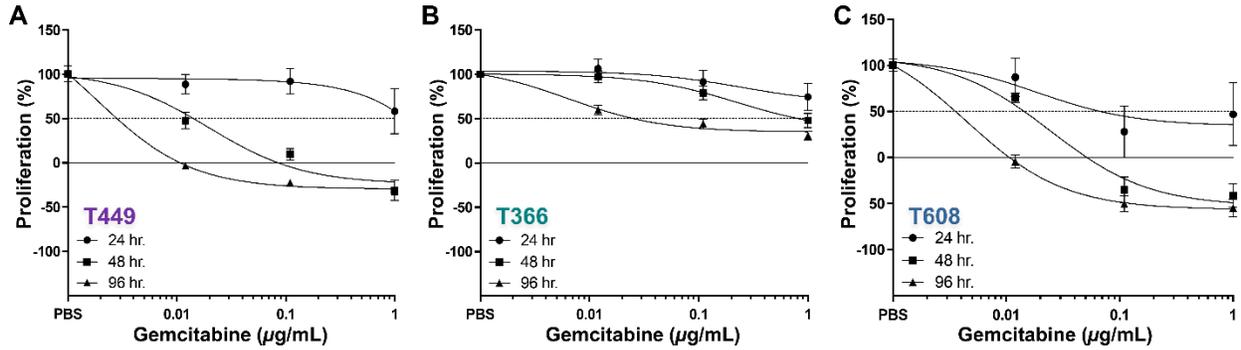


Figure S1: Proliferation studies on PDAC cell lines: A - T449, B – T366, and C – T608. Cell cultures were exposed to varying concentrations of gemcitabine (0.01, 0.1, and 1 $\mu\text{g mL}^{-1}$) for: 24 h (circle), 48 h (square) and 96 h (triangle). Proliferation (%) is calculated as the relative proliferation under each treated condition compared with untreated for each exposure period and gemcitabine concentration.

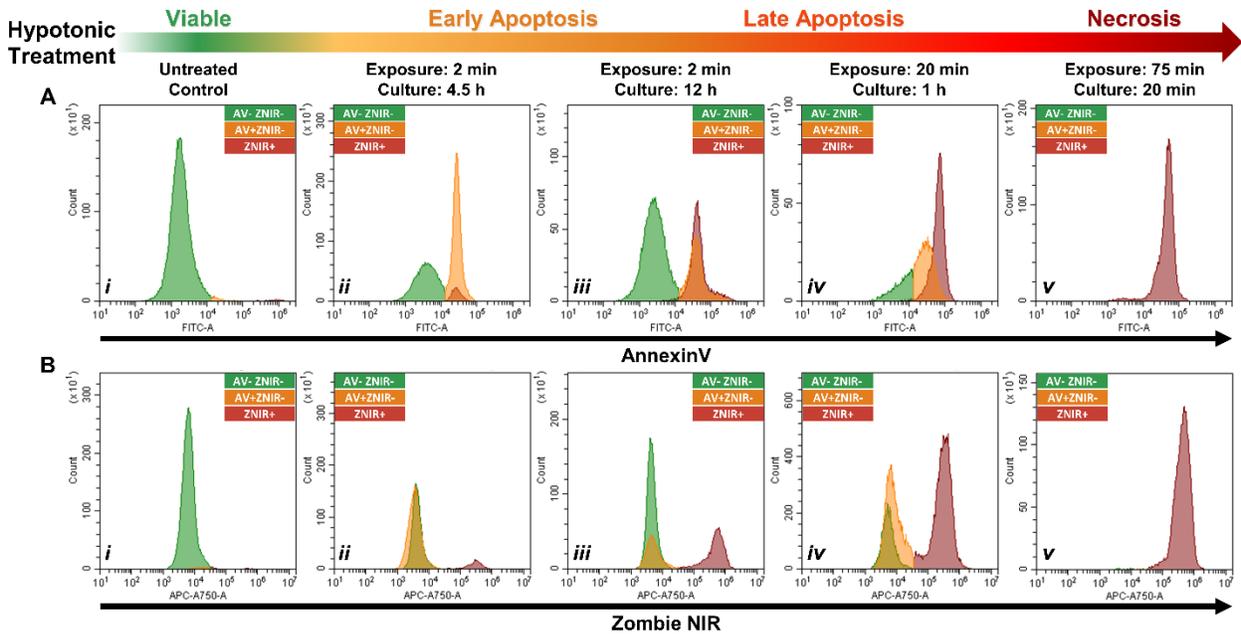


Figure S2: Hypotonic treatment studies on PDAC T449 cell line. Histograms A – Annexin V (AV) and B – Zombie Near-Infrared (ZNIR) show that exposing cell cultures to DI water for increasing periods of time induces cells towards apoptosis and necrosis pathways.

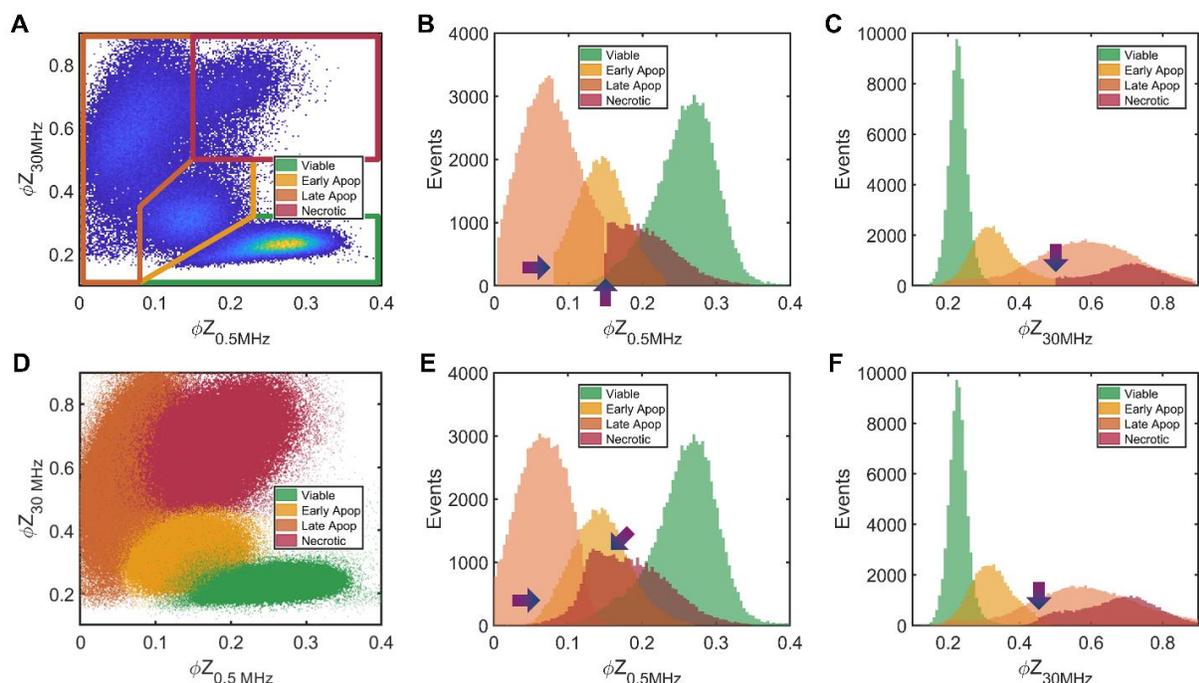


Figure S3: Manual gating versus clustering with unsupervised learning. A – Manual gates for each viability subpopulation applied to the density scatter plot of impedance phase at 0.5 MHz ($\phi Z_{0.5\text{MHz}}$) versus impedance phase at 30 MHz ($\phi Z_{30\text{MHz}}$) for merged data from the different hypotonic treatment samples. Histograms for B – $\phi Z_{0.5\text{MHz}}$ and C – $\phi Z_{30\text{MHz}}$ of the manually gated subpopulations. D – A Gaussian Mixture Model (GMM), with $k = 4$ clusters, applied to cluster each viability subpopulation in the density scatter plot of impedance phase at 0.5 MHz ($\phi Z_{0.5\text{MHz}}$) versus impedance phase at 30 MHz ($\phi Z_{30\text{MHz}}$) for merged data from the different hypotonic treatment samples. Histograms for E – $\phi Z_{0.5\text{MHz}}$ and F – $\phi Z_{30\text{MHz}}$ of the machine learning gated subpopulations.

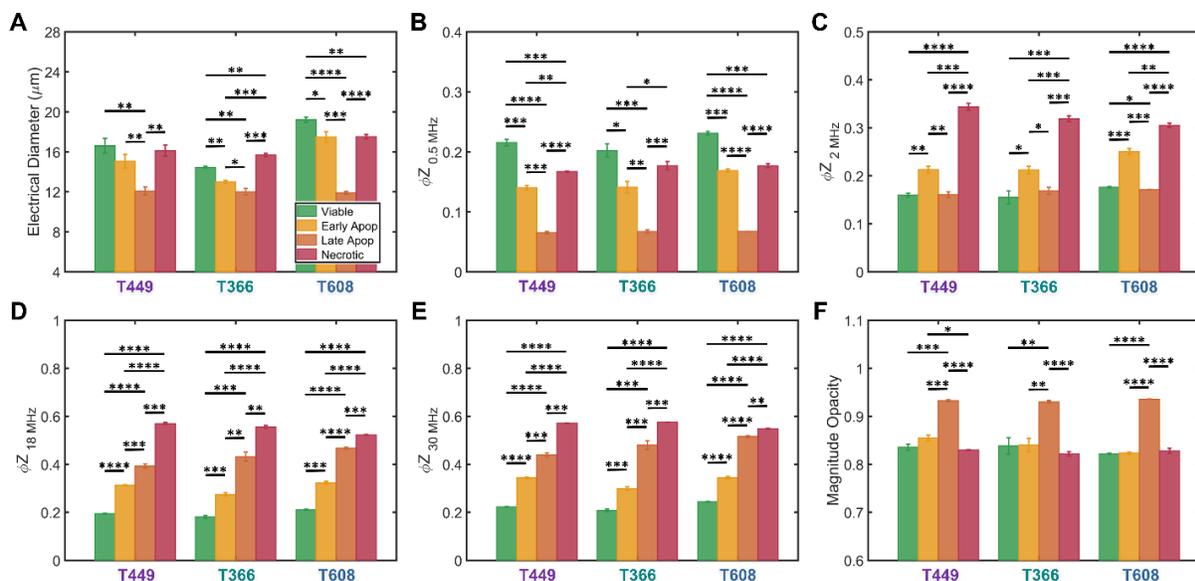


Figure S4: Comparison of the impedance cytometry biometrics of electrical diameter (A), impedance phase at 0.5 MHz ($\phi Z_{0.5\text{MHz}}$, B), at 2 MHz ($\phi Z_{2\text{MHz}}$, C), at 18 MHz ($\phi Z_{18\text{MHz}}$, D) and

at 30 MHz ($\phi Z_{30\text{MHz}}$, E), and magnitude opacity ($|Z|_{2\text{MHz}} / |Z|_{0.5\text{MHz}}$, F) for each untreated PDAC cell line (n = 3). Statistical significance: *p ≤ 0.05 ; **p ≤ 0.01, ***p ≤ 0.001 and ****p ≤ 0.00001.

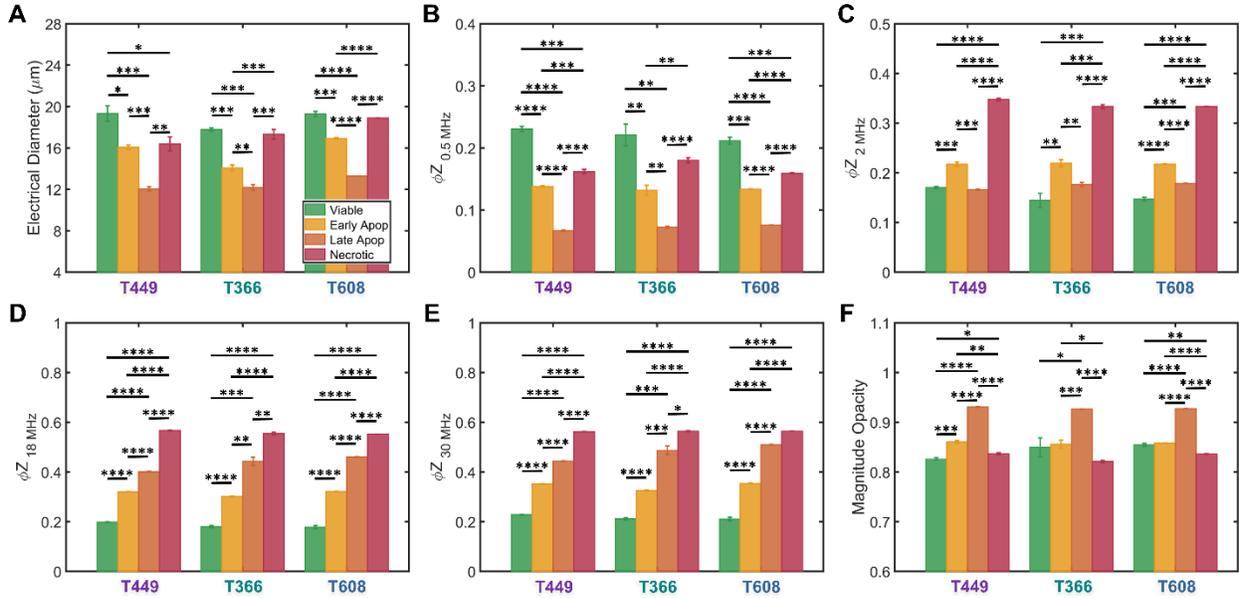


Figure S5: Comparison of the impedance cytometry biometrics of electrical diameter (A), impedance phase at 0.5 MHz ($\phi Z_{0.5\text{MHz}}$, B), at 2 MHz ($\phi Z_{2\text{MHz}}$, C), at 18 MHz ($\phi Z_{18\text{MHz}}$, D) and at 30 MHz ($\phi Z_{30\text{MHz}}$, E), and magnitude opacity ($|Z|_{2\text{MHz}} / |Z|_{0.5\text{MHz}}$, F) for each gemcitabine-treated PDAC cell line (n = 3). Statistical significance: *p ≤ 0.05 ; **p ≤ 0.01, ***p ≤ 0.001 and ****p ≤ 0.00001.

B. Supplementary Methods

Dielectric Shell Modelling

For the case where a particle is suspended in a dielectric medium, dielectric spectroscopy can be used to measure the dielectric properties of the suspension¹. This mixture of particle and medium can be approximated to that of a single dispersion using Maxwell's mixture theory (MMT)². MMT can be used to combine the dielectric properties of all parts into an overall complex permittivity of the mixture ($\tilde{\epsilon}_{mix}$):

$$\tilde{\epsilon}_{mix} = \tilde{\epsilon}_{medium}(1 + 3\varphi \tilde{f}_{CM,mix}) \quad (\text{S1})$$

where $\tilde{\epsilon}_{medium}$ is the complex permittivity of the suspending medium, φ the volume fraction of the particle in the medium, and $\tilde{f}_{CM,mix}$ the Clausius–Mossotti factor of the cell in the mixture. In practical terms, $\tilde{\epsilon}_{mix}$ describes the change in the medium permittivity, due to the presence of a particle of a given volume and can only be used if the volume fraction is small, *i.e.*, $\varphi \ll 1$. For the case of a cell in suspending medium, MMT-based, shell models can be used to retrieve the dielectric properties of the cell^{3–5}. While cells have an intricate internal structure surrounded by a membrane, a simplified approximation can be used based on shell models, wherein a cell is described as a series of n concentric shells with defined dielectric properties (**Figure S6A**). In a standard single-model, there are two dispersions, corresponding to the existing interfaces, *i.e.* medium-membrane and membrane-interior.

For a shell model, the Clausius–Mossotti factor of the cell in the mixture is given by:

$$\tilde{f}_{CM,mix} = \frac{\tilde{\epsilon}_{particle} - \tilde{\epsilon}_{medium}}{\tilde{\epsilon}_{particle} + 2\tilde{\epsilon}_{medium}} \quad (S2)$$

The complex permittivity of the cell, $\tilde{\epsilon}_{particle}$, is an aggregation of the complex permittivities of all the n shells modelled for the particle, and represents the final dispersion, typically corresponding to medium and cell membrane. The complex permittivity of any dispersion can be calculated as:

$$\tilde{\epsilon}_{n,n+1} = \tilde{\epsilon}_n \frac{\gamma_{n-1,n}^3 + 2\left(\frac{\tilde{\epsilon}_{n+1} - \tilde{\epsilon}_n}{\tilde{\epsilon}_{n+1} + 2\tilde{\epsilon}_n}\right)}{\gamma_{n-1,n}^3 - \left(\frac{\tilde{\epsilon}_{n+1} - \tilde{\epsilon}_n}{\tilde{\epsilon}_{n+1} + 2\tilde{\epsilon}_n}\right)} \quad (S3)$$

with,

$$\gamma_{n-1,n} = \frac{r_{n-1}}{r_n} \quad (S4)$$

where r is the radius of the shell being modeled. The complex permittivities of each specific shell can in turn be calculated using:

$$\tilde{\epsilon}_n = \epsilon_0 \epsilon_n - i \frac{\sigma_n}{\omega} \quad (S5)$$

where ϵ_n and σ_n can be ranges of permittivities and conductivities, respectively, being tested with the model for each n shell; while ϵ_0 is the constant vacuum permittivity ($8.85 \times 10^{-12} \text{ F m}^{-1}$) and ω is the angular frequency along the frequency spectrum measured. By calculating of each shell, and using **Equation S1**, it is then possible to calculate the dielectric decrement due to the presence of the particle in the suspending medium between the measurement electrodes. Thus, the impedance of the mixture (\tilde{Z}_{mix}) can be obtained:

$$\tilde{Z}_{mix} = 1 / i\omega \tilde{\epsilon}_{mix} G_f \quad (S6)$$

where $i^2 = -1$, ω is the angular frequency, and G_f is the geometric constant of the system. For an ideal parallel plate electrode system, G_f is simplified to $A_{electrode} / d_{electrode}$, where $A_{electrode}$ is the electrode surface area and $d_{electrode}$ is the separation distance between electrodes.

Given the frequency-dependence of \tilde{Z}_{mix} , relaxation curves for the impedance magnitude and phase can be calculated using:

$$|\tilde{Z}_{mix}| = \sqrt{\text{Re}(\tilde{Z}_{mix})^2 + \text{Im}(\tilde{Z}_{mix})^2} \quad (S7)$$

$$\phi_{\tilde{Z}_{mix}} = \arctan\left(\frac{\text{Im}(\tilde{Z}_{mix})}{\text{Re}(\tilde{Z}_{mix})}\right) \quad (S8)$$

An iterative algorithm can be implemented to calculate these curves for a wide spectrum of combinations between different electrophysiology metrics (e.g. varying particle size, membrane conductivity or internal conductivity; **Figure S6B-F**).

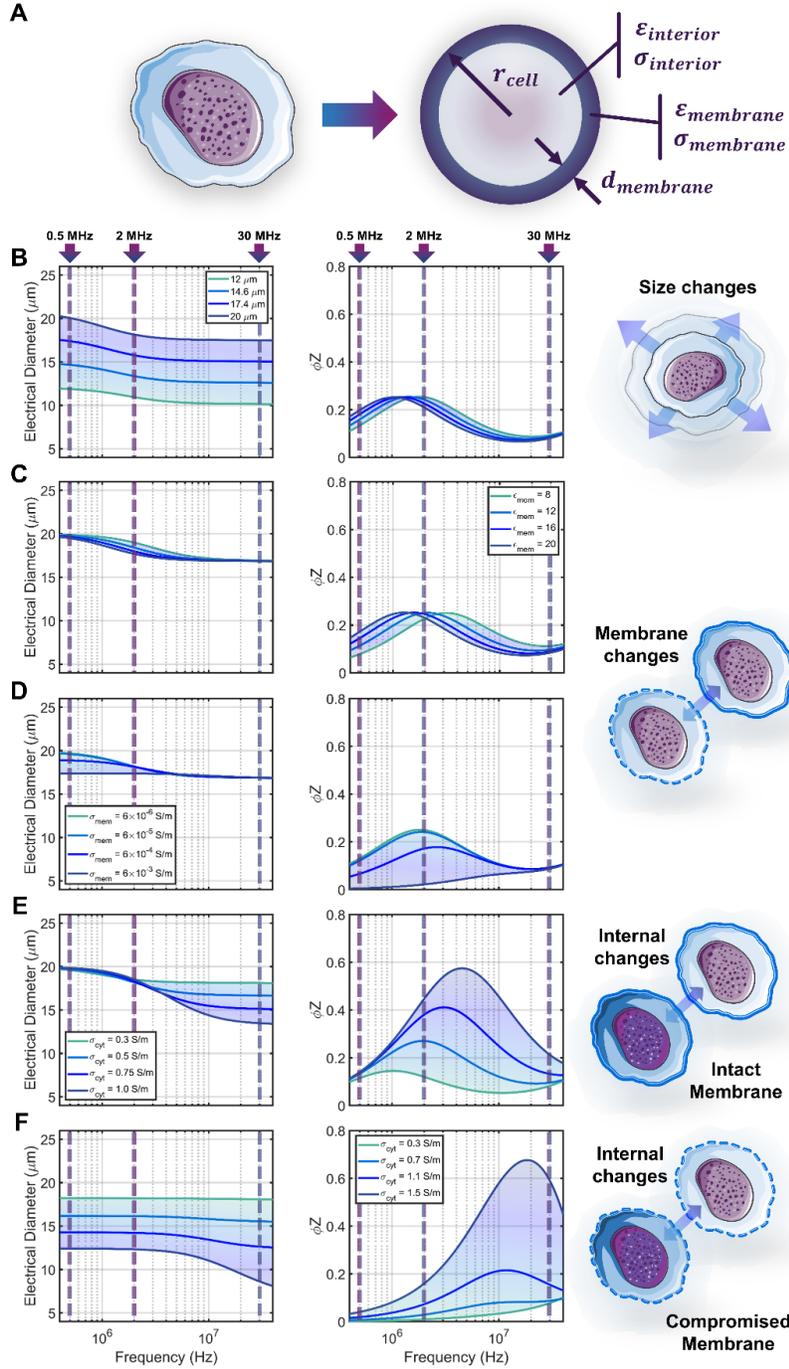


Figure S6: Dielectric shell modelling. A – An equivalent single-shell model of a biological cell in a suspending medium, obtained through Maxwell’s mixture theory. Modelled electrical diameter and impedance phase (ϕZ) for a variety of different alterations to the dielectric properties: B – cell size (r_{cell} from 6 to 10 μm , C – membrane permittivity (ϵ_{mem} from 8 to 20), D – membrane conductivity (σ_{mem} from 6×10^{-6} to 6×10^{-3}), E – internal conductivity (σ_{int} from 0.3 to 1.0 S m^{-1} , assuming $\epsilon_{mem} = 14$ and $\sigma_{mem} < 1 \times 10^{-6}$ S m^{-1}), and F – internal conductivity (σ_{int} from 0.3 to 1.5 S m^{-1} , assuming $\epsilon_{mem} = 14$ and $\sigma_{mem} = 6 \times 10^{-3}$ S m^{-1}). Cells modelled using a single-shell model with the following set of dielectric properties (if not being varied at each

individual sub-figure case): $d_{mem} = 10 \text{ nm}$, $\epsilon_{mem} = 14$, $\sigma_{mem} < 1 \times 10^{-6} \text{ S m}^{-1}$, $\epsilon_{int} = 60$, $\sigma_{int} = 0.5 \text{ S m}^{-1}$, $\epsilon_{medium} = 80$, $\sigma_{medium} = 1.6 \text{ S m}^{-1}$, $d_{electrode} = 50 \text{ }\mu\text{m}$, $A_{electrode} = 2.5 \times 10^{-9} \text{ m}^2$.

References

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3. Hanai, T., Koizumi, N. & Irimajiri, A. A method for determining the dielectric constant and the conductivity of membrane-bounded particles of biological relevance. *Biophys. Struct. Mech.* **1**, 285–294 (1975).
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5. Irimajiri, A., Hanai, T. & Inouye, A. A dielectric theory of ‘multi-stratified shell’ model with its application to a lymphoma cell. *J. Theor. Biol.* **78**, 251–269 (1979).