

## Supporting Information

### **Thermal Conductivity of Ethylene Glycol and Propylene Glycol Nanofluids with Boron Nitride Nano-barbs**

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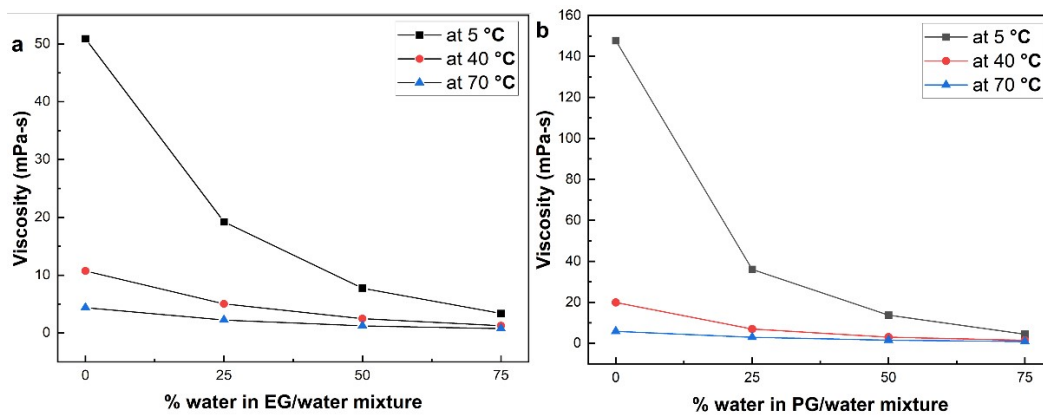
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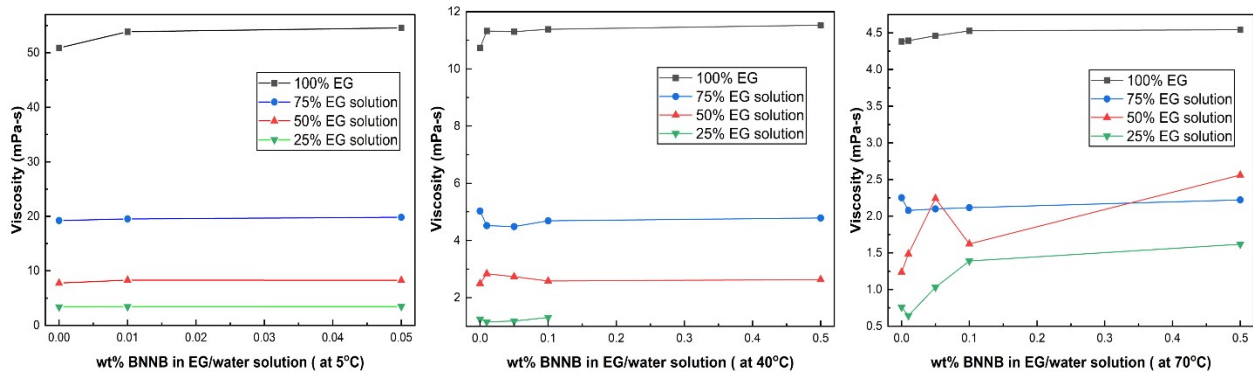
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SI 1: Dilution chart for the 10wt% BNNB ethylene- and propylene-glycol stock solution.

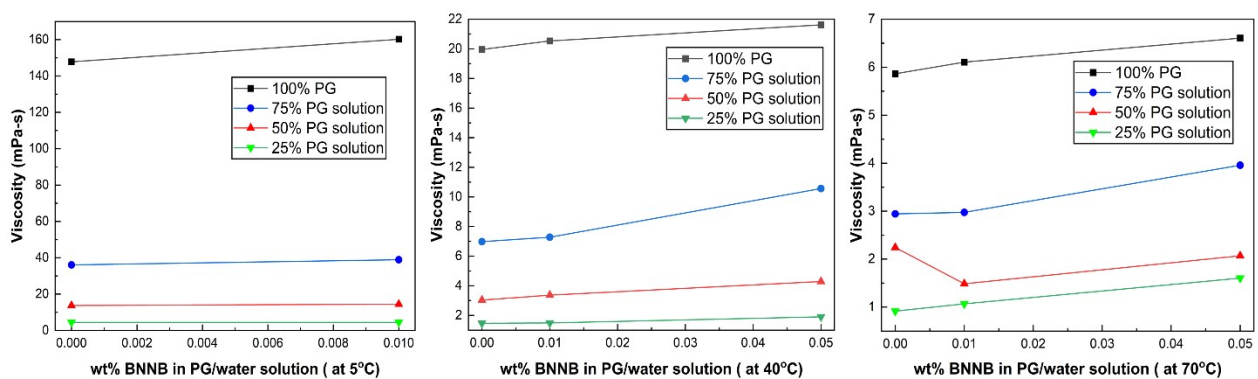
|                            |                      | concentration | Sample creation | NB stock | Previous sample | Ethylene glycol | DI water | 75:25 EG:DI | 50:50 EG:DI | 25:75 EG:DI |
|----------------------------|----------------------|---------------|-----------------|----------|-----------------|-----------------|----------|-------------|-------------|-------------|
|                            | Stock solution in EG | 10            |                 |          |                 |                 |          |             |             |             |
| EG dispersion              | EG1                  | 5             |                 | 5        |                 | 5               |          |             |             |             |
|                            | EG2                  | 1             |                 |          | 2               | 8               |          |             |             |             |
|                            | EG3                  | 0.5           |                 |          | 5               | 5               |          |             |             |             |
|                            | EG4                  | 0.1           |                 |          | 2               | 8               |          |             |             |             |
|                            | EG5                  | 0.05          |                 |          | 5               | 5               |          |             |             |             |
|                            | EG6                  | 0.01          |                 |          | 2               | 8               |          |             |             |             |
|                            | EG0                  | 0             |                 |          | 0               | 10              |          |             |             |             |
| 50:50 EG: water dispersion | 50EG1                | 5             |                 | 5        |                 |                 | 5        |             |             |             |
|                            | 50EG2                | 1             |                 |          | 2               |                 |          |             | 8           |             |
|                            | 50EG3                | 0.5           |                 |          | 5               |                 |          |             | 5           |             |
|                            | 50EG4                | 0.1           |                 |          | 2               |                 |          |             | 8           |             |
|                            | 50EG5                | 0.05          |                 |          | 5               |                 |          |             | 5           |             |
|                            | 50EG6                | 0.01          |                 |          | 2               |                 |          |             | 8           |             |
|                            | 50EG0                | 0             |                 |          | 0               |                 |          |             | 10          |             |
| 25:75 EG: water dispersion | 25EG1                | 2.5           |                 | 1        |                 |                 | 3        |             |             |             |
|                            | 25EG2                | 1             |                 | 1        |                 |                 | 3        |             |             | 6           |
|                            | 25EG3                | 0.5           |                 |          | 5               |                 |          |             |             | 5           |
|                            | 25EG4                | 0.1           |                 |          | 2               |                 |          |             |             | 8           |
|                            | 25EG5                | 0.05          |                 |          | 5               |                 |          |             |             | 5           |
|                            | 25EG6                | 0.01          |                 |          | 2               |                 |          |             |             | 8           |
|                            | 25EG0                | 0             |                 |          | 0               |                 |          |             |             | 10          |
| 75:25 EG: water dispersion | 75EG1                | 5             |                 | 5        |                 | 2.5             | 2.5      |             |             |             |
|                            | 75EG2                | 1             |                 |          | 2               |                 |          | 8           |             |             |
|                            | 75EG3                | 0.5           |                 |          | 5               |                 |          | 5           |             |             |
|                            | 75EG4                | 0.1           |                 |          | 2               |                 |          | 8           |             |             |
|                            | 75EG5                | 0.05          |                 |          | 5               |                 |          | 5           |             |             |
|                            | 75EG6                | 0.01          |                 |          | 2               |                 |          | 8           |             |             |
|                            | 75EG0                | 0             |                 |          | 0               |                 |          | 10          |             |             |



SI 2: Thermal conductivity measurement of a. ethylene glycol/ water mixture b. propylene glycol/ water mixture



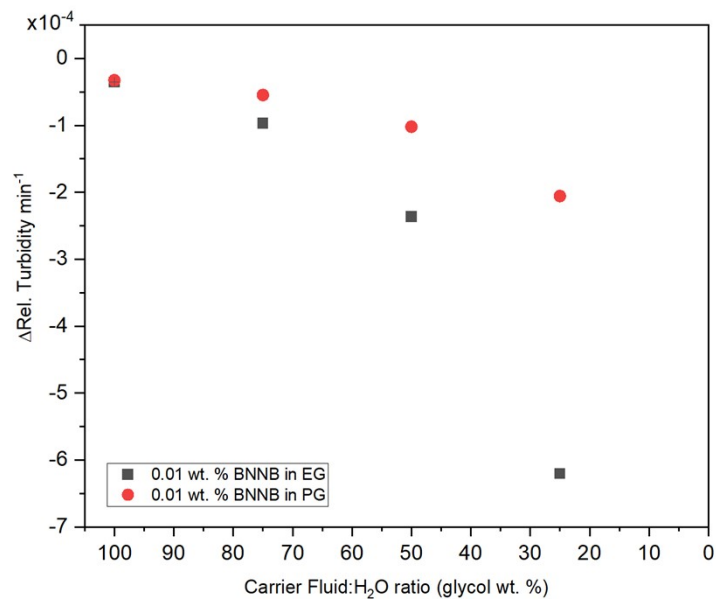
SI 3: Viscosity measurements of ethylene glycol/water mixture boron nitride nano-barbs nanofluids at 5, 40 and 70 °C



SI 4: Viscosity measurements of propylene glycol/water mixture boron nitride nano-barbs nanofluids at 5, 40 and 70 °C

*SI 5: Slope values of the relative turbidity data against time at 475 nm of ethylene glycol/water mixture and propylene glycol/water mixture BNNB nanofluids*

|                                 | Slope                                      | R square |
|---------------------------------|--------------------------------------------|----------|
| <b>Ethylene Glycol - Water</b>  |                                            |          |
| 0.01 wt% 100% EG                | $-3.5458\text{E-}5 \pm 1.21017\text{E-}7$  | 0.99892  |
| 0.01 wt% 75% EG                 | $-9.6823\text{E-}5 \pm 6.65092\text{E-}7$  | 0.99563  |
| 0.01 wt% 50% EG                 | $-2.3635\text{E-}4 \pm 1.89974\text{E-}6$  | 0.99403  |
| 0.01 wt% 25% EG                 | $-6.203\text{E-}4 \pm 2.68798\text{E-}6$   | 0.99826  |
| <b>Propylene Glycol - Water</b> |                                            |          |
| 0.01 wt% 100% PG                | $-3.28761\text{E-}5 \pm 1.11497\text{E-}6$ | 0.90337  |
| 0.01 wt% 75% PG                 | $-5.49009\text{E-}5 \pm 1.30176\text{E-}6$ | 0.95031  |
| 0.01 wt% 50% PG                 | $-1.02154\text{E-}4 \pm 2.11978\text{E-}6$ | 0.9615   |
| 0.01 wt% 25% PG                 | $-2.05853\text{E-}4 \pm 3.19707\text{E-}6$ | 0.97806  |



*SI 6: Experimental value for the thermal conductivity of ethylene and propylene glycol – water BNNB nanofluids.*

| % Water in EG/water solution | 0 °C  | Standard Deviation (±) | 40 °C   | Standard Deviation (±) | % Water in PG/water solution | 0 °C    | Standard Deviation (±) | 40 °C   | Standard Deviation (±) |
|------------------------------|-------|------------------------|---------|------------------------|------------------------------|---------|------------------------|---------|------------------------|
| <b>0</b>                     | 0.254 | 0.0079                 | 0.25825 | 0.01287                | <b>0</b>                     | 0.21075 | 0.07298                | 0.21054 | 0.01323                |
| <b>25</b>                    | 0.303 | 0.0165                 | 0.32021 | 0.02371                | <b>25</b>                    | 0.28146 | 0.05264                | 0.28207 | 0.01269                |
| <b>50</b>                    | 0.373 | 0.02872                | 0.38525 | 0.02691                | <b>50</b>                    | 0.37    | 0.0364                 | 0.38226 | 0.02276                |
| <b>75</b>                    | 0.449 | 0.0131                 | 0.49202 | 0.02367                | <b>75</b>                    | 0.442   | 0.0352                 | 0.48268 | 0.02684                |

| wt% BNNB in EG/water solution (at 40 °C) | Ethylene Glycol (k (W m <sup>-1</sup> K <sup>-1</sup> )) | Standard Deviation (±) | 75% EG (k (W m <sup>-1</sup> K <sup>-1</sup> )) | Standard Deviation (±) | 50% EG (k (W m <sup>-1</sup> K <sup>-1</sup> )) | Standard Deviation (±) |             | 25% EG (k (W m <sup>-1</sup> K <sup>-1</sup> )) | Standard Deviation (±) |
|------------------------------------------|----------------------------------------------------------|------------------------|-------------------------------------------------|------------------------|-------------------------------------------------|------------------------|-------------|-------------------------------------------------|------------------------|
| <b>10</b>                                | 0.37382                                                  | 0.02353                |                                                 |                        |                                                 |                        |             |                                                 |                        |
| <b>5</b>                                 | 0.28963                                                  | 0.01853                | 0.38716                                         | 0.0161                 | 0.4322                                          | 0.01466                | <b>2.5</b>  | 0.52537                                         | 0.04516                |
| <b>1</b>                                 | 0.26932                                                  | 0.01048                | 0.34081                                         | 0.01133                | 0.40953                                         | 0.01789                | <b>1</b>    | 0.51652                                         | 0.03043                |
| <b>0.5</b>                               | 0.26748                                                  | 0.01385                | 0.33094                                         | 0.01867                | 0.39872                                         | 0.01346                | <b>0.5</b>  | 0.5136                                          | 0.05356                |
| <b>0.1</b>                               | 0.26366                                                  | 0.0129                 | 0.32872                                         | 0.02722                | 0.39773                                         | 0.01368                | <b>0.1</b>  | 0.50871                                         | 0.04417                |
| <b>0.05</b>                              | 0.26197                                                  | 0.01297                | 0.32524                                         | 0.01902                | 0.39469                                         | 0.01941                | <b>0.05</b> | 0.50445                                         | 0.0473                 |
| <b>0.01</b>                              | 0.26097                                                  | 0.01419                | 0.32431                                         | 0.0304                 | 0.39102                                         | 0.02058                | <b>0.01</b> | 0.50184                                         | 0.02629                |
| <b>0</b>                                 | 0.25825                                                  | 0.01287                | 0.32021                                         | 0.02371                | 0.38525                                         | 0.02691                | <b>0</b>    | 0.49202                                         | 0.02367                |

| wt% BNNB in PG/water solution (at 40 °C) | Propylene Glycol (k (W m <sup>-1</sup> K <sup>-1</sup> )) | Standard Deviation (±) | 75% PG (k (W m <sup>-1</sup> K <sup>-1</sup> )) | Standard Deviation (±) | 50% PG (k (W m <sup>-1</sup> K <sup>-1</sup> )) | Standard Deviation (±) |             | 25% PG (k (W m <sup>-1</sup> K <sup>-1</sup> )) | Standard Deviation (±) |
|------------------------------------------|-----------------------------------------------------------|------------------------|-------------------------------------------------|------------------------|-------------------------------------------------|------------------------|-------------|-------------------------------------------------|------------------------|
| <b>10</b>                                | 0.29101                                                   | 0.00741                |                                                 |                        |                                                 |                        |             |                                                 |                        |
| <b>5</b>                                 | 0.25325                                                   | 0.01125                | 0.33498                                         | 0.02127                | 0.42046                                         | 0.0238                 | <b>2.5</b>  | 0.51888                                         | 0.04298                |
| <b>1</b>                                 | 0.2227                                                    | 0.01512                | 0.29964                                         | 0.02052                | 0.39965                                         | 0.03524                | <b>1</b>    | 0.51118                                         | 0.0293                 |
| <b>0.5</b>                               | 0.2217                                                    | 0.00968                | 0.29484                                         | 0.0154                 | 0.3928                                          | 0.02378                | <b>0.5</b>  | 0.50911                                         | 0.04161                |
| <b>0.1</b>                               | 0.21267                                                   | 0.01041                | 0.2903                                          | 0.01419                | 0.38978                                         | 0.04054                | <b>0.1</b>  | 0.50158                                         | 0.01477                |
| <b>0.05</b>                              | 0.21328                                                   | 0.01677                | 0.28745                                         | 0.01881                | 0.38871                                         | 0.02893                | <b>0.05</b> | 0.49601                                         | 0.04416                |
| <b>0.01</b>                              | 0.21167                                                   | 0.0171                 | 0.28558                                         | 0.02026                | 0.38638                                         | 0.03683                | <b>0.01</b> | 0.48766                                         | 0.0284                 |
| <b>0</b>                                 | 0.21054                                                   | 0.01323                | 0.28207                                         | 0.01269                | 0.38226                                         | 0.02276                | <b>0</b>    | 0.48268                                         | 0.02684                |

## Hansen Solubility Parameter Discussion

Hansen Solubility Parameters (HSP) are a set of three values that represent the relative energy contributions from dispersion forces ( $\delta_D$ ), polar forces ( $\delta_P$ ), and hydrogen bonding ( $\delta_H$ ) in a solvent or mixture. These parameters can help predict the solubility of various substances in a given solvent or solvent mixture. When mixing two solvents, the HSP values of the mixture can be calculated as a weighted average of the individual solvents' HSP values based on their respective volume fractions.

First, consider the HSP values of pure water, ethylene glycol (EG), and propylene glycol (PG):

|                             | Hansen solubility<br>parameters (MPa <sup>0.5</sup> ) |            |            |
|-----------------------------|-------------------------------------------------------|------------|------------|
|                             | $\delta_D$                                            | $\delta_P$ | $\delta_H$ |
| Ethylene glycol<br>[37, 38] | 17                                                    | 11         | 26         |
| Propylene glycol<br>[37]    | 16.8                                                  | 9.4        | 23.3       |
| Water                       | 15.1                                                  | 20.4       | 42.3       |

1. Water:  $\delta_D = 15.1 \text{ MPa}^{0.5}$ ,  $\delta_P = 20.4 \text{ MPa}^{0.5}$ ,  $\delta_H = 42.3 \text{ MPa}^{0.5}$
2. Ethylene Glycol:  $\delta_D = 17.0 \text{ MPa}^{0.5}$ ,  $\delta_P = 11.0 \text{ MPa}^{0.5}$ ,  $\delta_H = 26.0 \text{ MPa}^{0.5}$
3. Propylene Glycol:  $\delta_D = 16.8 \text{ MPa}^{0.5}$ ,  $\delta_P = 9.4 \text{ MPa}^{0.5}$ ,  $\delta_H = 23.3 \text{ MPa}^{0.5}$

Then we recalculate the HSP values for each mixture of water and ethylene glycol or propylene glycol at the specified concentrations:

### 25% water in ethylene glycol:

$$\delta_D = (0.25 \times 15.1) + (0.75 \times 17.0) = 16.525 \text{ MPa}^{0.5} \quad \delta_P = (0.25 \times 20.4) + (0.75 \times 11.0) = 13.35 \text{ MPa}^{0.5} \quad \delta_H = (0.25 \times 42.3) + (0.75 \times 26.0) = 30.075 \text{ MPa}^{0.5}$$

### 50% water in ethylene glycol:

$$\delta_D = (0.5 \times 15.1) + (0.5 \times 17.0) = 16.05 \text{ MPa}^{0.5} \quad \delta_P = (0.5 \times 20.4) + (0.5 \times 11.0) = 15.7 \text{ MPa}^{0.5} \quad \delta_H = (0.5 \times 42.3) + (0.5 \times 26.0) = 34.15 \text{ MPa}^{0.5}$$

### 75% water in ethylene glycol:

$$\delta_D = (0.75 \times 15.1) + (0.25 \times 17.0) = 15.575 \text{ MPa}^{0.5} \quad \delta_P = (0.75 \times 20.4) + (0.25 \times 11.0) = 18.05 \text{ MPa}^{0.5} \quad \delta_H = (0.75 \times 42.3) + (0.25 \times 26.0) = 38.225 \text{ MPa}^{0.5}$$

**25% water in propylene glycol:**

$$\delta D = (0.25 \times 15.1) + (0.75 \times 16.8) = 16.375 \text{ MPa}^{0.5} \quad \delta P = (0.25 \times 20.4) + (0.75 \times 9.4) = 12.15 \text{ MPa}^{0.5}$$
$$\delta H = (0.25 \times 42.3) + (0.75 \times 23.3) = 28.05 \text{ MPa}^{0.5}$$

**50% water in propylene glycol:**

$$\delta D = (0.5 \times 15.1) + (0.5 \times 16.8) = 15.95 \text{ MPa}^{0.5} \quad \delta P = (0.5 \times 20.4) + (0.5 \times 9.4) = 14.9 \text{ MPa}^{0.5}$$
$$\delta H = (0.5 \times 42.3) + (0.5 \times 23.3) = 32.8 \text{ MPa}^{0.5}$$

**75% water in propylene glycol:**

$$\delta D = (0.75 \times 15.1) + (0.25 \times 16.8) = 15.525 \text{ MPa}^{0.5} \quad \delta P = (0.75 \times 20.4) + (0.25 \times 9.4) = 17.65 \text{ MPa}^{0.5}$$
$$\delta H = (0.75 \times 42.3) + (0.25 \times 23.3) = 37.55 \text{ MPa}^{0.5}$$