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Formula	K <sub>2</sub> (BeS)O <sub>4</sub> F <sub>2</sub>		
Formula weight (amu)	221.27		
Temperature (K)	293(2)		
Wavelength (Å)	1.34139		
Crystal system	Orthorhombic		
Space group	$P2_{1}2_{1}2_{1}$		
a (Å)	4.5337(4)		
b (Å)	5.4828(6)		
c (Å)	12.0877(13)		
α (deg)	90		
β (deg)	90		
γ (deg)	90		
V (Å <sup>3</sup> )	300.47(5)		
Z	2		
Calculated density (g/cm <sup>3</sup> )	2.446		
Absorption coefficient (mm <sup>-1</sup> )	11.362		
F(000)	216		
Theta range $(\theta)$	9.091-60.729		
	-4<=h<=5		
Limiting indices	-6<=k<=7		
	-15<=1<=15		
Reflections collected / unique	1008 / 595		
R <sub>int</sub>	0.0230		
Completeness to $\theta = 53.594^{\circ}(\%)$	96		
GOF on F <sup>2</sup>	1.119		
$R/wR(I>2\sigma(I))$	$R_I = 0.0669$		
10 wR(1-20(1))	$wR_2 = 0.1800$		
R/wR(all data)	$R_I = 0.0700$		
10 with autu)	$wR_2 = 0.1847$		
Absolute structure parameter	0.45(11)		
${}^{a}R_{I} = \sum   \mathbf{F}_{o}  -  \mathbf{F}_{c}   / \sum  \mathbf{F}_{o} $			
${}^{b}_{w}R_{2}(F_{o}^{2}) = \left[\sum w \left(F_{o}^{2} - F_{c}^{2}\right)^{2} / \sum w (F_{o}^{2})^{2}\right]^{1/2}$			

Table S1. Crystal Data and Structure Refinement for  $K_2(BeS)O_4F_2$ .

K <sub>2</sub> ( <b>BC5</b> )04 <sup>1</sup> <sub>2</sub> .				
Atom	Х	у	Z	U(eq)
K(001)	2735(4)	7981(3)	6453(2)	29(1)
O(002)	7639(13)	978(11)	6555(4)	23(1)
O(003)	11653(11)	2743(13)	5404(4)	28(2)
S(004)	8288(9)	2851(9)	5692(4)	41(1)
F(005)	7630(17)	5384(11)	6062(7)	55(2)
Be(0)	8288(9)	2851(9)	5692(4)	41(1)

**Table S2.** Atomic Coordinates (×10<sup>4</sup>) and Equivalent Isotropic Displacement Parameters (Å<sup>2</sup>×10<sup>3</sup>) for  $K_2(BeS)O_4E_2$ .

Table S3. Selected Bond lengths [Å] and angles [°] for  $K_2(BeS)O_4F_2$ .

K(001)-O(002)#1	2.652(6)	O(002)#1-K(001)-O(002)#3	104.90(13)
K(001)-O(002)#2	2.838(6)	O(003)#2-K(001)-O(003)#4	127.18(19)
K(001)-O(002)#3	2.767(6)	F(005)#4-K(001)-O(002)#2	67.86(17)
K(001)-O(003)#4	3.177(7)	K(001)#7-O(002)-K(001)#8	109.32(18)
K(001)-O(003)#2	2.943(7)	O(002)-S(004)-K(001)#11	164.2(3)
K(001)-S(004)#2	3.470(5)	O(002)-S(004)-O(003)	108.7(4)
K(001)-S(004)#1	3.483(5)	O(003)#12-S(004)-K(001)#7	141.8(3)
K(001)-S(004)#5	3.465(5)	F(005)-S(004)-K(001)#9	116.9(4)
K(001)-F(005)#1	3.284(9)	F(005)-S(004)-O(002)	113.1(5)
K(001)-F(005)#5	3.170(9)	K(001)#10-F(005)-K(001)#11	90.3(2)
K(001)-F(005)#4	2.759(7)	K(001)#8-Be(0)-K(001)#9	77.23(10)
K(001)-F(005)	2.679(7)	O(002)-Be(0)-K(001)#7	45.2(3)
O(002)-S(004)	1.493(7)	O(002)-Be(0)-O(003)#12	111.0(4)
O(002)-Be(0)	1.493(7)	O(003)#12-Be(0)-K(001)#11	57.7(3)
O(003)-S(004)#6	1.553(7)	F(005)-Be(0)-K(001)#7	69.9(4)
O(003)-S(004)	1.566(7)	F(005)-Be(0)-O(003)#12	110.9(5)
O(003)-Be(0)	1.566(7)	O(003)#12-Be(0)-O(003)	105.6(3)
S(004)-F(005)	1.489(7)	O(002)-Be(0)-K(001)#8	53.1(3)
F(005)-Be(0)	1.489(7)	K(001)#11-F(005)-K(001)#7	172.5(2)

Table S4. Anisotropic Displacement Parameters (Å $^{2}\times10^{3}$ ) for K<sub>2</sub>(BeS)O<sub>4</sub>F<sub>2</sub>

The Anisotropic displacement factor exponent takes the form:  $-2\pi^2[h^2a^{*2}U_{11}+2hka^*b^*U_{12}+...]$ .

Atom	U <sub>11</sub>	U <sub>22</sub>	U <sub>33</sub>	U <sub>23</sub>	U <sub>13</sub>	U <sub>12</sub>
K(001)	23(1)	24(1)	39(1)	7(1)	0(1)	-1(1)
O(002)	21(3)	26(3)	22(2)	9(2)	4(3)	-4(3)
O(003)	12(2)	49(4)	24(2)	1(3)	-2(2)	2(3)
S(004)	31(2)	45(2)	45(2)	3(2)	0(1)	1(2)
F(005)	27(3)	32(3)	106(5)	-17(3)	-6(4)	3(3)
Be(0)	31(2)	45(2)	45(2)	3(2)	0(1)	1(2)

Table S5.	. The elemental	content ICP	analysis.
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Element	Weight(%)	Atomic ratio
K	30.37	0.7767
Be	3.34	0.3711

## Table S6. The elemental content EA analysis.

Element	Weight(%)
Ν	=<0.3
С	=<0.3
Н	=<0.3

Table S7. Experimental birefringence of  $K_2(BeS)O_4F_2$  at 546.1 nm.

Crystal	$\Delta R (nm)$	Τ (μm)	Δn
K <sub>2</sub> (BeS)O <sub>4</sub> F <sub>2</sub>	516.9	9.22	0.056



Figure S1. Powder XRD patterns of the simulated and experimental for K<sub>2</sub>(BeS)O<sub>4</sub>F<sub>2</sub>



Lsec: 16.9 0 Cnts 0.000 keV Det: Octane Plus Det

Figure S2. EDS analysis of single crystal for  $K_2(BeS)O_4F_2$ 



Figure S3. Polyhedron of K, F and O atoms for  $K_2(BeS)O_4F_2$ 



Figure S4. TG and DTA curves of  $K_2(BeS)O_4F_2$ .



Figure S5. IR transmittance spectra of  $K_2(BeS)O_4F_2$ 



Figure S6. Measurement of birefringence for K<sub>2</sub>(BeS)O<sub>4</sub>F<sub>2</sub>.



Figure S7. Calculated electronic band structure of  $K_2(BeS)O_4F_2$ .



Figure S8. TDOS and PDOS of K<sub>2</sub>(BeS)O<sub>4</sub>F<sub>2</sub>.



Figure S9. The calculated SHG coefficient of  $K_2(BeS)O_4F_2$ .



Figure S10. The identified way about Be and S atoms in calculating part.