## Antiferromagnetic ordering in the TM-adsorbed AlN monolayer (TM = V and Cr)

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Figure S1: Spin-resolved band structure (Black line: spin-up; Red line: spin-down; E<sub>g</sub>: electronic band gap; M: metallic nature) of the V- and Cr-adsorbed AlN monolayer calculated by DFT-D3 with coverage of (a)-(d) 0.25 ML; (b)-(e) 0.5 ML; and (e)-(f) 1.0 ML.



Fig.S2: Energy of magnetic transition of (a) V- and (b) Cr-adsorbed AlN monolayer in a 4×4×1 supercell.



Fig.S3: Fluctuation of temperature as a function of molecular dynamics simulation steps at 300 K of Vand Cr-adsorbed AlN monolayer with coverage of (a-d) 0.25 ML, (b-e) 0.50 ML, and (c-f) 1.0 ML.