

**Nitric Oxide Reduction Reaction for Efficient Ammonia Synthesis on
Topological Nodal-Line Semimetal Cu₂Si Monolayer**

Zebin Ren, Haona Zhang, Shuhua Wang, Baibiao Huang, Ying Dai* and Wei Wei*

School of Physics, State Key Laboratory of Crystal Materials, Shandong University,

Jinan 250100, China

* Corresponding authors: daiy60@sdu.edu.cn (Y. Dai), weiw@sdu.edu.cn (W. Wei)

Table S1 Elementary reactions for all the considered pathways for NORR towards NH₃ synthesis.

End-on	
N-distal	N-alternating
$\text{NO (g)} + * \rightarrow * \text{NO}$	$\text{NO (g)} + * \rightarrow * \text{NO}$
$* \text{NO} + \text{H}^+ + \text{e}^- \rightarrow * \text{HNO}$	$* \text{NO} + \text{H}^+ + \text{e}^- \rightarrow * \text{HNO}$
$* \text{HNO} + \text{H}^+ + \text{e}^- \rightarrow * \text{H}_2\text{NO}$	$* \text{HNO} + \text{H}^+ + \text{e}^- \rightarrow * \text{HNOH}$
$* \text{H}_2\text{NO} + \text{H}^+ + \text{e}^- \rightarrow * \text{H}_2\text{NOH}$	$* \text{HNOH} + \text{H}^+ + \text{e}^- \rightarrow * \text{H}_2\text{NOH}$
$* \text{H}_2\text{NOH} + \text{H}^+ + \text{e}^- \rightarrow * \text{NH}_2 + \text{H}_2\text{O}$	$* \text{H}_2\text{NOH} + \text{H}^+ + \text{e}^- \rightarrow * \text{NH}_2 + \text{H}_2\text{O}$
$* \text{NH}_2 + \text{H}^+ + \text{e}^- \rightarrow * \text{NH}_3$	$* \text{NH}_2 + \text{H}^+ + \text{e}^- \rightarrow * \text{NH}_3$
<hr/>	
O-alternating	O-distal
$\text{NO (g)} + * \rightarrow * \text{NO}$	$\text{NO (g)} + * \rightarrow * \text{NO}$
$* \text{NO} + \text{H}^+ + \text{e}^- \rightarrow * \text{NOH}$	$* \text{NO} + \text{H}^+ + \text{e}^- \rightarrow * \text{NOH}$
$* \text{NOH} + \text{H}^+ + \text{e}^- \rightarrow * \text{HNOH}$	$* \text{NOH} + \text{H}^+ + \text{e}^- \rightarrow * \text{N} + \text{H}_2\text{O}$
$* \text{HNOH} + \text{H}^+ + \text{e}^- \rightarrow * \text{NH} + \text{H}_2\text{O}$	$* \text{N} + \text{H}^+ + \text{e}^- \rightarrow * \text{NH}$
$* \text{NH} + \text{H}^+ + \text{e}^- \rightarrow * \text{NH}_2$	$* \text{NH} + \text{H}^+ + \text{e}^- \rightarrow * \text{NH}_2$
$* \text{NH}_2 + \text{H}^+ + \text{e}^- \rightarrow * \text{NH}_3$	$* \text{NH}_2 + \text{H}^+ + \text{e}^- \rightarrow * \text{NH}_3$
<hr/>	
Side-on	
O-first	O-enzymatic
$\text{NO (g)} + * \rightarrow * \text{NO}$	$\text{NO (g)} + * \rightarrow * \text{NO}$
$* \text{NO} + \text{H}^+ + \text{e}^- \rightarrow * \text{NOH}$	$* \text{NO} + \text{H}^+ + \text{e}^- \rightarrow * \text{NOH}$
$* \text{NOH} + \text{H}^+ + \text{e}^- \rightarrow * \text{N} + \text{H}_2\text{O}$	$* \text{NOH} + \text{H}^+ + \text{e}^- \rightarrow * \text{HNOH}$
$* \text{N} + \text{H}^+ + \text{e}^- \rightarrow * \text{NH}$	$* \text{HNOH} + \text{H}^+ + \text{e}^- \rightarrow * \text{NH} + \text{H}_2\text{O}$
$* \text{NH} + \text{H}^+ + \text{e}^- \rightarrow * \text{NH}_2$	$* \text{NH} + \text{H}^+ + \text{e}^- \rightarrow * \text{NH}_2$
$* \text{NH}_2 + \text{H}^+ + \text{e}^- \rightarrow * \text{NH}_3$	$* \text{NH}_2 + \text{H}^+ + \text{e}^- \rightarrow * \text{NH}_3$
<hr/>	
N-enzymatic	N-first
$\text{NO (g)} + * \rightarrow * \text{NO}$	$\text{NO (g)} + * \rightarrow * \text{NO}$
$* \text{NO} + \text{H}^+ + \text{e}^- \rightarrow * \text{HNO}$	$* \text{NO} + \text{H}^+ + \text{e}^- \rightarrow * \text{HNO}$
$* \text{HNO} + \text{H}^+ + \text{e}^- \rightarrow * \text{HNOH}$	$* \text{HNO} + \text{H}^+ + \text{e}^- \rightarrow * \text{H}_2\text{NO}$
$* \text{HNOH} + \text{H}^+ + \text{e}^- \rightarrow * \text{H}_2\text{NOH}$	$* \text{H}_2\text{NO} + \text{H}^+ + \text{e}^- \rightarrow * \text{O} + \text{NH}_3$
$* \text{H}_2\text{NOH} + \text{H}^+ + \text{e}^- \rightarrow * \text{NH}_2 + \text{H}_2\text{O}$	$* \text{O} + \text{H}^+ + \text{e}^- \rightarrow * \text{OH}$
$* \text{NH}_2 + \text{H}^+ + \text{e}^- \rightarrow * \text{NH}_3$	$* \text{OH} + \text{H}^+ + \text{e}^- \rightarrow * \text{H}_2\text{O}$

Table S2 Computed total energies (E), zero-point energies (E_{ZPE}) and entropy (TS) of NORR intermediates on Cu–Si-bridge site with N-end configuration of NO adsorption.

	E (eV)	E_{ZPE} (eV)	TS (eV)	G (eV)
*NO	-121.20	0.18	0.13	-121.15
*NOH	-124.85	0.47	0.15	-124.52
*HNOH	-129.41	0.75	0.18	-128.84
*NH	-119.79	0.38	0.04	-119.45
*NH ₂	-124.42	0.72	0.07	-123.77
*NH ₃	-128.41	1.03	0.15	-127.53

Table S3 Computed total energies (E), zero-point energies (E_{ZPE}) and entropy (TS) of NORR intermediates on Cu–Si-bridge site with NO-side configuration of NO adsorption.

	E (eV)	E_{ZPE} (eV)	TS (eV)	G (eV)
*NO	-120.57	0.16	0.11	-120.52
*HNO	-125.27	0.47	0.13	-124.89
*H ₂ NO	-129.99	0.84	0.14	-129.29
*HNOH	-128.53	0.78	0.15	-127.89
*O	-114.78	0.07	0.06	-114.77
*H ₂ NOH	-132.76	1.09	0.26	-131.92
*NH	-119.79	0.38	0.04	-119.45
*OH	-119.40	0.34	0.14	-119.20
*H ₂ O	-122.49	0.65	0.17	-122.02

Table S4 Computed total energies (E), zero-point energies (E_{ZPE}) and entropy (TS) of NORR intermediates on Si site with N-end configuration of NO adsorption.

	E (eV)	E_{ZPE} (eV)	TS (eV)	G (eV)
*NO	-121.04	0.17	0.18	-121.04
*HNO	-125.15	0.47	0.21	-124.89
*HNOH	-129.31	0.78	0.22	-128.75
*H ₂ NOH	-133.52	1.13	0.21	-132.60
*NH ₂	-124.36	0.65	0.16	-123.86
*NH ₃	-128.41	1.03	0.15	-127.53

Table S5 Computed total energies (E), zero-point energies (E_{ZPE}) and entropy (TS) of NORR intermediates on Si site with N-end configuration of NO adsorption by DFT + U method.

	E (eV)	E_{ZPE} (eV)	TS (eV)	G (eV)
*NO	-96.82	0.18	0.16	-96.80
*HNO	-100.85	0.47	0.20	-100.58
*HNOH	-104.94	0.77	0.25	-104.41
*H ₂ NOH	-109.14	1.13	0.21	-108.21
*NH ₂	-99.98	0.66	0.15	-99.48
*NH ₃	-104.03	1.03	0.14	-103.14

Table S6 Computed total energies (E), zero-point energies (E_{ZPE}) and entropy (TS) of NORR intermediates on Si site with N-end configuration of NO adsorption, using a 4×4 supercell.

	E (eV)	E_{ZPE} (eV)	TS (eV)	G (eV)
*NO	-204.74	0.18	0.17	-204.73
*HNO	-208.89	0.47	0.18	-208.6
*HNOH	-213.00	0.77	0.21	-212.43
*H ₂ NOH	-217.24	1.13	0.21	-216.32
*NH ₂	-208.06	0.65	0.17	-207.58
*NH ₃	-212.13	1.03	0.15	-211.25

Table S7 Computed total energies (E), zero-point energies (E_{ZPE}) and entropy (TS) of NORR intermediates on Si site with N-end configuration of NO adsorption after including the solvation effects.

	E (eV)	E_{ZPE} (eV)	TS (eV)	G (eV)
*NO	-120.98	0.16	0.18	-121.00
*HNO	-125.26	0.47	0.14	-124.93
*HNOH	-129.45	0.78	0.22	-128.90
*H ₂ NOH	-133.86	1.15	0.19	-132.90
*NH ₂	-124.41	0.64	0.08	-123.85
*NH ₃	-128.93	1.06	0.11	-127.98

Table S8 Computed NORR free energy changes (ΔG) of elementary steps for NORR

on Si site along the N-alternating pathway under different calculation conditions. The unit is eV.

Elementary Reactions	DFT	DFT + U	DFT	DFT + solvation
	3×3	3×3	4×4	3×3
$\text{NO (g)} + * \rightarrow *\text{NO}$	-0.5	-0.66	-0.46	-0.53
$*\text{NO} + \text{H}^+ + \text{e}^- \rightarrow *\text{HNO}$	-0.4	-0.34	-0.43	-0.48
$*\text{HNO} + \text{H}^+ + \text{e}^- \rightarrow *\text{HNOH}$	-0.42	-0.39	-0.39	-0.52
$*\text{HNOH} + \text{H}^+ + \text{e}^- \rightarrow *\text{H}_2\text{NOH}$	-0.4	-0.36	-0.44	-0.56
$*\text{H}_2\text{NOH} + \text{H}^+ + \text{e}^- \rightarrow *\text{NH}_2 + \text{H}_2\text{O}$	-2.04	-2.04	-2.04	-1.72
$*\text{NH}_2 + \text{H}^+ + \text{e}^- \rightarrow *\text{NH}_3$	-0.23	-0.21	-0.22	-0.68

Table S9 Computed total energies (E), zero-point energies (E_{ZPE}) and entropy (TS) of NORR intermediates on pure Cu(111) surface.

E (eV)	E_{ZPE} (eV)	TS (eV)	G (eV)
----------	-----------------------	-----------	----------

*NO	-196.20	0.16	0.13	-196.17
*NOH	-199.63	0.45	0.16	-199.33
*N	-189.42	0.08	0.03	-189.37
*NH	-194.42	0.29	0.01	-194.14
*NH ₂	-198.61	0.69	0.08	-197.99
*NH ₃	-202.80	1.01	0.18	-201.97

Table S10 Computed total energies (E), zero-point energies (E_{ZPE}) and entropy (TS) of NORR intermediates on Si@Cu(111) surface.

	E (eV)	E_{ZPE} (eV)	TS (eV)	G (eV)
N-alternating				
*NO	-198.05	0.16	0.19	-198.07

*HNO	-201.97	0.46	0.14	-201.65
*HNOH	-206.14	0.75	0.26	-205.65
*H ₂ NOH	-210.29	1.11	0.23	-209.41
*NH ₂	-201.17	0.65	0.15	-200.64
*NH ₃	-205.11	1.01	0.18	-204.27
O-distal				
*NO	-198.37	0.16	0.13	-198.35
*NOH	-202.31	0.47	0.14	-201.97
*N	-192.60	0.09	0.03	-192.54
*NH	-197.28	0.39	0.04	-196.93
*NH ₂	-201.17	0.65	0.15	-200.64
*NH ₃	-205.11	1.01	0.18	-204.27

Table S11 Computed total energies (E), zero-point energies (E_{ZPE}) and entropy (TS) of the intermediates for N₂ synthesis on Cu₂Si monolayer.

	E (eV)	E_{ZPE} (eV)	TS (eV)	G (eV)
*NONO	-134.84	0.39	0.25	-134.70
*NONOH	-138.98	0.73	0.29	-138.55
*NNO	-128.62	0.29	0.18	-128.51
*NNOH	-132.95	0.59	0.21	-132.57
* + N ₂	-124.01	0.15	0.59	-124.44

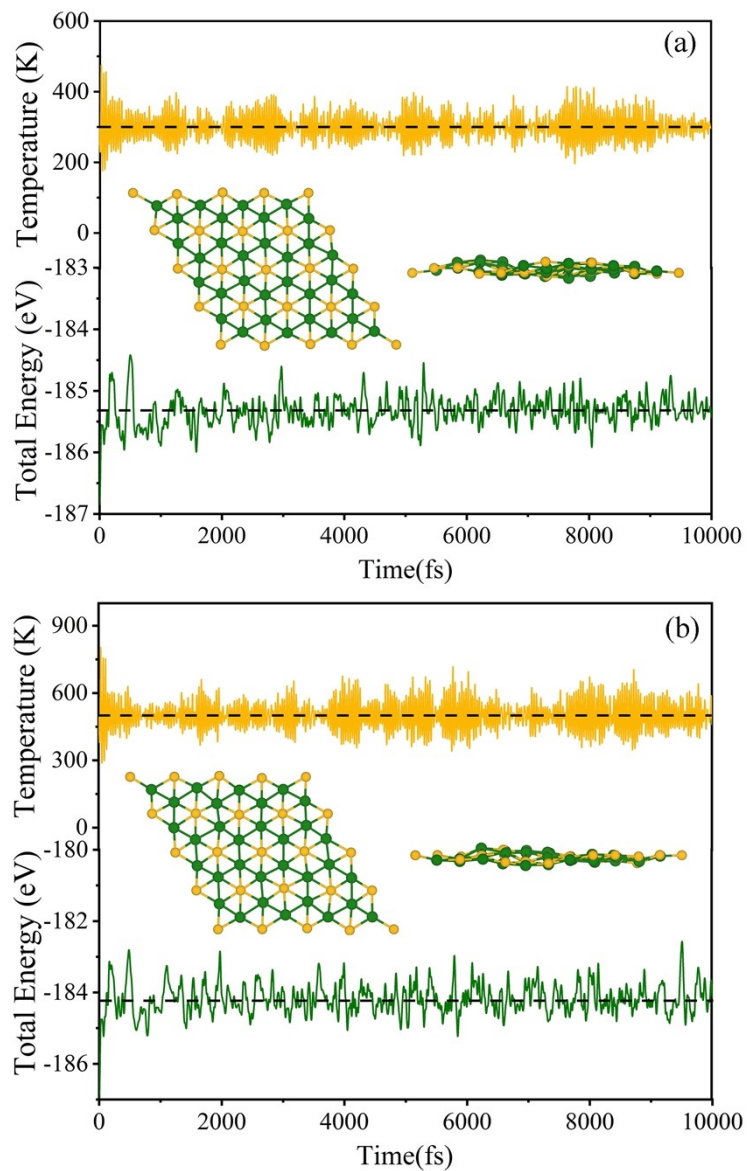


Fig. S1 Variation of total energy and temperature versus the AIMD simulation time for Cu_2Si monolayer at (a) 300 K and (b) 500 K. Insets denote the top and side views of Cu_2Si structure as the AIMD simulations lasted for 10 ps.

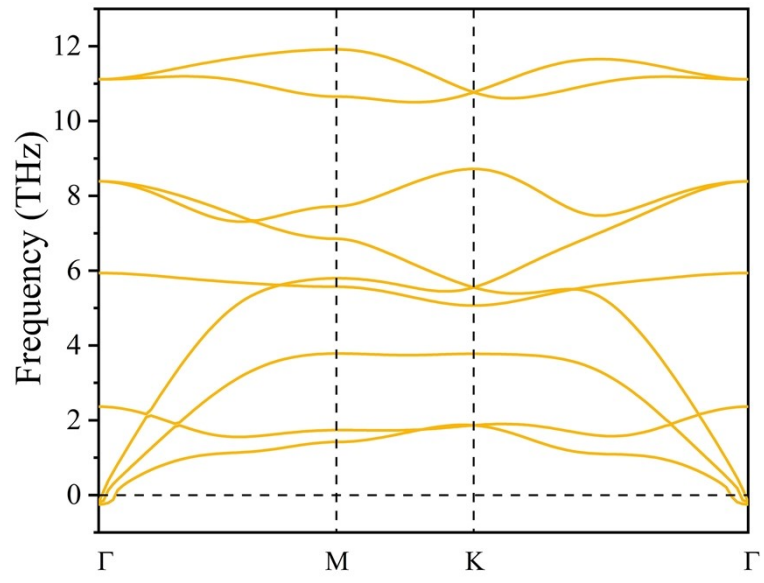


Fig. S2 Phonon dispersion spectrum of Cu₂Si monolayer.

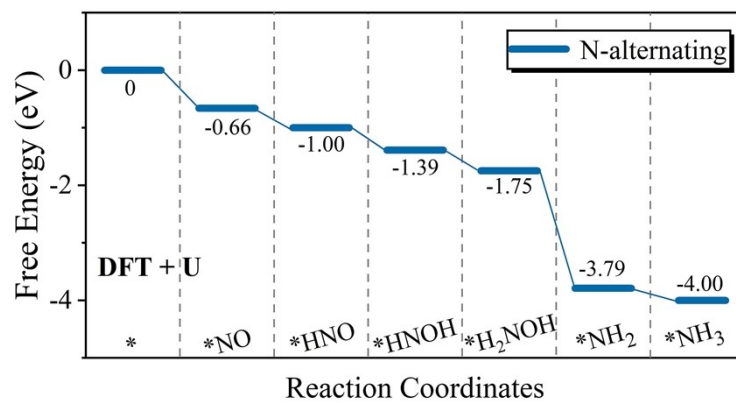


Fig. S3 Free energy diagram for NORR toward NH₃ on Si site by DFT + *U* method.

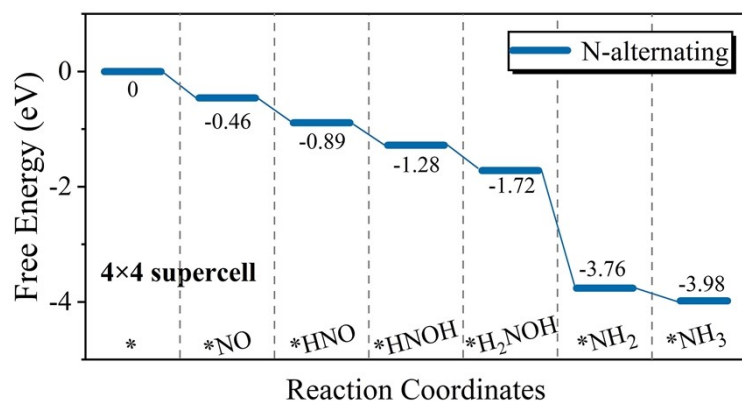


Fig. S4 Free energy diagram for NORR toward NH₃ on Si site using a 4x4 Cu₂Si supercell.

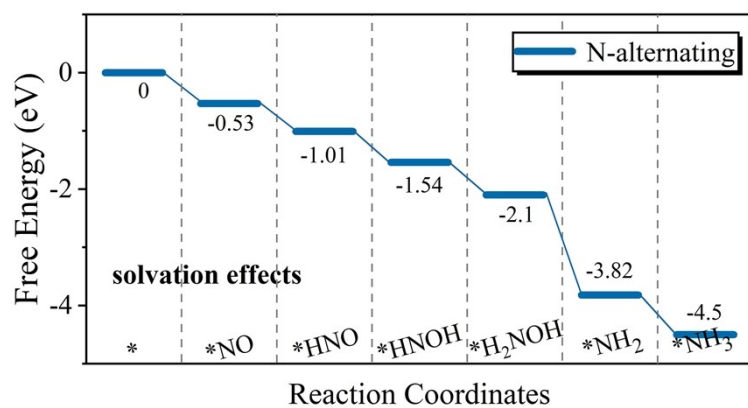


Fig. S5 Free energy diagram for NORR toward NH₃ on Si site using implicit solvation model.