Activity and selectivity of N_2 fixation on B doped g-C₉N₁₀: A density functional theory study

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^dResearch Center for Precision Engineering, Graduate School of Engineering, Osaka University, 2-1 Yamada-oka, Suita 565-0871, Osaka, Japan In our work, the phonon contribution of solids to free energy is negligible. To verify this point, we estimated the $\Delta E_{ZPE} - T\Delta S$ term of N₂ +* \rightarrow N₂* process on B_A doped g-C₉N₁₀ with and without phonon contribution using harmonic approximation¹, the equation is as shown in following:²

$$E_{ZPE} = \frac{1}{2} \sum_{i} hv_i$$

$$-TS = k_B T \sum_{i} \ln\left(1 - e^{-\frac{hv_i}{K_B T}}\right) - \sum_{i} hv_i \left(\frac{1}{\frac{hv_i}{k_B T}}\right)$$

$$(1)$$

where h, v_i and k_B are Planck constant, vibrational frequencies and Boltzmann constant, respectively. Vibrational analyses were performed using the finite difference method at the Γ point only.

As shown in Table S1, we found that $\Delta E_{ZPE} - T\Delta S$ values with and without phonon contribution differ by only 40 meV. Therefore, only the calculation of E_{ZPE} and S of reaction intermediates are needed as the contribution of substrate can be offset.

Table S1. Calculated *E*_{ZPE} and *TS* values (in eV) of N₂ adsorbed B_A doped g-C₉N₁₀, B_A doped g-C₉N₁₀ and N₂ gas with and without phonon contribution. Calculated $\Delta E_{ZPE} - T\Delta S \text{ of } N_2 + * \rightarrow N_2*$ process on B_A doped g-C₉N₁₀ with and without phonon contribution.

| | with phonon contribution | | | without phonon contribution | | | | |
|------------------------------------|----------------------------|----------------------------------|--------------------|-----------------------------|------------------------------|----------------|------------------------------|--------------------|
| system | N ₂ adsorbed | B _A doped | N ₂ gas | N ₂ | adsorbed | B _A | doped | N ₂ gas |
| | B _A doped | g-C ₉ N ₁₀ | | B _A | doped | g-C | ₉ N ₁₀ | |
| | $g-C_9N_{10}$ | | | g-C | ₉ N ₁₀ | | | |
| $E_{\rm ZPE}$ | 3.02 | 2.87 | 0.148 | | 0.22 | | 0 | 0.148 |
| TS | 0.64 | 0.74 | 0.593 | | 0 | | 0 | 0.593 |
| process | $N_2 + * \rightarrow N_2*$ | | | $N_2 + * \rightarrow N_2*$ | | | | |
| ΔE_{ZPE} | | | 0.072 | | | | | |
| $T\Delta S$ | | | -0.593 | | | | | |
| $\Delta E_{\rm ZPE}$ – $T\Delta S$ | | | 0.665 | | | | | |
| | | | | | | | | |



Figure S1. Variations of temperature and energy against time for *ab-initio* molecular dynamics (AIMD) simulations of the B_{C1} (a), B_{N1} (b) and B_A doped g- C_9N_{10} (c), and the insets show top and side views of the snapshot of the atomic configuration. The simulation is run at 500 K for 4.8 ps with a time step of 1.2 fs.

To study kinetics of end-on N₂ to side on N₂, rotation process was first calculated using the nudged elastic band (NEB) method³ and the transition state was further refined by using climbing image nudged elastic band (CI-NEB) method^{4,5}. The activation free energy (G_a) can be evaluated by the following equation:

$$G_{\rm a} = G_{\rm TS} - G_{\rm IS}$$

where G_{IS} and G_{TS} stand for the free energy of initial and transition state, respectively.



Figure S2. Free energy barrier diagram of N_2 rotation process on B_A doped g-C₉N₁₀ (end on $N_2^* \rightarrow$ side on N_2^*).



Figure S3. Free energy diagrams for N_2 reduction on B_{N1} doped $g-C_9N_{10}$ through (a) alternating, (b) distal, (c) mixed II and (d) mixed III mechanisms at different applied potentials.



Figure S4. Free energy diagrams for N_2 reduction on B_A doped g- C_9N_{10} through (a) alternating, (b) distal, (c) mixed II and (d) mixed III mechanisms at different applied potentials.

| process | | B _{N1} case |
|-----------------|--|----------------------|
| | | ΔG |
| | | (eV) |
| adsorption | $N_2 + * \rightarrow NN^*$ | -0.90 |
| 1e ⁻ | $NN^* + e^- + H^+ \rightarrow NNH^*$ | 0.62 |
| 2e- | NNH* + e^- + $H^+ \rightarrow NH_2N*$ | -0.75 |
| | NNH* + e^- + $H^+ \rightarrow$ NHNH* | -0.08 |
| 3e ⁻ | $NH_2N^* + e^- + H^+ \rightarrow NH_2NH^*$ | -0.25 |
| | $NH_2N^* + e^- + H^+ \rightarrow N^* + NH_3$ | 0.37 |
| | NHNH* + e^- + $H^+ \rightarrow NH_2NH^*$ | -1.44 |
| 4e- | $NH_2NH^* + e^- + H^+ \rightarrow NH_2NH_2^*$ | -0.44 |
| | $N^* + e^- + H^+ \rightarrow NH^*$ | -0.85 |
| | $NH_2NH^* + e^- + H^+ \rightarrow NH^* + NH_3$ | -0.13 |
| 5e- | $\mathrm{NH}_2\mathrm{NH}_2^*$ + e ⁻ + H ⁺ \rightarrow NH_2^* + NH_2^* | -1.15 |
| | $\rm NH^*$ + e ⁻ + H ⁺ \rightarrow $\rm NH_2^*$ | -1.36 |
| 6e ⁻ | NH_2^* + e ⁻ + H ⁺ \rightarrow NH_3^* | -1.13 |
| desorption | $\rm NH_3^* \rightarrow \rm NH_3$ + * | 2.79 |

Table S2. Calculated free energy of the reaction path followed by N_2RR on B_{N1} doped g- C_9N_{10} .

| process | | B _A case |
|-----------------|---|--------------------------|
| | | $\Delta G (\mathrm{eV})$ |
| adsorption | $N_2 + * \rightarrow NN*$ | -0.85 |
| 1e- | NN* + e^- + $H^+ \rightarrow NNH^*$ | 0.20 |
| 2e⁻ | NNH* + e^- + $H^+ \rightarrow NH_2N^*$ | -0.67 |
| | NNH* + e^- + $H^+ \rightarrow NHNH^*$ | -0.24 |
| 3e ⁻ | $NH_2N^* + e^- + H^+ \rightarrow NH_2NH^*$ | -0.92 |
| | $\rm NH_2N^*$ + e ⁻ + H ⁺ \rightarrow $\rm NNH_3^*$ | 0.1 |
| | NHNH* + e^- + $H^+ \rightarrow NH_2NH^*$ | -1.35 |
| 4e⁻ | $NH_2NH^* + e^- + H^+ \rightarrow NH_2NH_2^*$ | 0.34 |
| | $NNH_3 + e^- + H^+ \rightarrow NH^* + NH_3$ | -0.57 |
| | $\rm NH_2NH^*$ + e ⁻ + H ⁺ \rightarrow $\rm NH^*$ | 0.45 |
| | + NH ₃ | |
| 5e- | $\rm NH_2\rm NH_2^*$ + e ⁻ + H ⁺ \rightarrow | -2.60 |
| | NH ₂ *+NH ₃ | |
| | NH^* + e ⁻ + H ⁺ \rightarrow NH_2^* | -2.71 |
| 6e ⁻ | NH_2 * + e ⁻ + H ⁺ \rightarrow NH_3 * | 0.44 |
| desorption | $\rm NH_3^* \rightarrow \rm NH_3$ + * | 2.85 |

Table S3. Calculated free energy of the reaction path followed by $N_2 RR$ on B_A doped g- $C_9 N_{10}.$



Figure S5. The eight possible H adsorption sites on B_{N1} doped *g*-C₉N₁₀ (a) and B_A doped *g*-C₉N₁₀ (c). The pink, blue, and gray balls denote boron, nitrogen, and carbon atoms, respectively. The Gibbs free energy profile of hydrogen evolution reaction (HER) of B_{N1} doped *g*-C₉N₁₀ (b) and B_A doped *g*-C₉N₁₀ (d). H adsorption on N1 site of B_A doped *g*-C₉N₁₀ broke the structure, so it is not shown in HER diagram.



Figure S6. The band gap, PDOS HOMO and LUMO distributions of B_{N1} doped g-C₉N₁₀ (a), B_A doped g-C₉N₁₀ in spin up channel (b) and spin down channel (c) by using GGA/PBE functional.

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