Electronic Supplementary Material (ESI) for Journal of Materials Chemistry C. This journal is © The Royal Society of Chemistry 2022

## Supporting Information

## Note S1. Stokes shift fitting method.

The stokes shift of QTPA1 and QTPA2 as a function of polarity of solvent is given in Figure 1(C), which is fitted by linear function of

$$
\begin{gathered}
\Delta \bar{v}\left(v_{a b s}^{-}-\overline{v_{e m}}\right)=\frac{2 \Delta \mu^{2} \Delta f}{h c a^{3}}+\text { const } . \\
\Delta f=\frac{\varepsilon-1}{2 \varepsilon+1}-\frac{n^{2}-1}{2 n^{2}+1}
\end{gathered}
$$

where $\varepsilon$ and $n$ are the dielectric constant and the refractive index of the solvents, respectively; ${ }^{v}\left(v_{f}\right)$ is the wavenumber $\left(\mathrm{cm}^{-1}\right)$ of the absorption (emission) maximum, $h\left(6.6 \times 10^{-34} \mathrm{~J} \cdot \mathrm{~s}\right)$ is the Planck constant, $c\left(3.00 \times 10^{8} \mathrm{~m} \cdot \mathrm{~s}^{-1}\right)$ is the light velocity, $\varepsilon_{0}$ $\left(8.85 \times 10^{-12} \mathrm{C} \cdot \mathrm{V}^{-1} \cdot \mathrm{~m}^{-1}\right)$ is the vacuum permittivity and $\Delta \mu\left(=\mu_{e}-\mu_{g}\right)$ is the dipole moment difference of the solute between $S_{0}$ and $S_{1}$ state.

Note S2. Calculation Details of nonlinear absorption coefficient ( $\boldsymbol{\beta}$ ) and the twophoton absorption cross section ( $\sigma$ ).

The influence of the solvent nonlinearity could be excluded. The two-photon absorption (TPA) coefficient $\beta$ of TOND in three solvents can be obtained by fitting the experimental results with equation:
$T(z, S=1)=\sum_{m=0}^{\infty} \frac{\left(-q_{0}(z, 0)\right)^{m}}{(m+1)^{3 / 2}}$
where $^{q_{0}(z)=\beta I_{0} /\left(1+z^{2} / z_{0}{ }^{2}\right)} ; z_{0}=k \omega^{2} / 2_{\text {is the Rayleigh length, }} k=2 \pi / \lambda$ is the wave vector, ${ }^{\omega}{ }_{0}$ is beam waist radius of Gaussian pulse, and $I_{0 \text { is the pulse irradiance. }}$. The TPA coefficient $\beta$ is related to the TPA cross section $\sigma$ by using
$\sigma=\frac{\beta h v 10^{3}}{N c}$
where N is Avogadro's number, $c$ is the concentration, $h$ is Planck's constant, and $v$ is the laser frequency. In this experiment, the concentration of QTPA is $5 \times 10^{-4} \mathrm{M} . \sigma$ is expressed in Göppert-Mayer units (GM), with $1 \mathrm{GM}=1 \times 10^{-50} \mathrm{~cm}^{4} \mathrm{~s}$ molecule ${ }^{-1}$
photon ${ }^{-1}$.

## Note S3. Calculation Details of Temperature-Dependent PL Quantum Yield.

The PL quantum yield can be defined as the ratio of the number of emitted photons to the number of absorbed photons by a luminescent material:
$P L Q Y=\frac{N_{e m}}{N_{a b s}}$
The most straightforward method for the determination of PLQY values presents the absolute measurement of $N_{a b s}$ and $N_{e m}$ with an integrating sphere setup. The PLQY of QTPA1 and QTPA2 film at room temperature can be described by:
$P L Q Y=\frac{\int \frac{\lambda}{h c}\left(I_{e m}^{\text {sample }}(\lambda)-I_{e m}(\lambda)\right) d \lambda}{\int \frac{\lambda}{h c}\left(I_{e x}(\lambda)-I_{e x}^{\text {sample }}(\lambda)\right) d \lambda}$
and $\lambda$ is the wavelength; $h$ is Planck's constant; $c$ is the velocity of light; $I_{e x}^{\text {sample }}$ and $I_{e x}$ are the integrated intensities of the excitation light with and without a sample, respectively.

After obtaining the temperature-dependent absorption and PL spectra of the sample, the quantum yield at different temperatures $Q Y_{2}$ can be obtained from $Q Y_{1}$. The general equation used in the determination of relative quantum yields is given in
$\frac{Q Y_{2}}{Q Y_{1}}=\frac{I_{e m 2}}{I_{e m 1}} \times \frac{A_{1}}{A_{2}} \times \frac{\lambda_{e x 1}}{\lambda_{e x 2}} \times \frac{\eta_{2}}{\eta_{1}}$
Among them, $I_{e m}$ is the integrated area under the corrected emission spectrum; $A$ is absorbance at the excitation wavelength; $\lambda_{e x}$ is the excitation wavelength; $\eta$ is the collection efficiency of the system. In our experiments, the system and test conditions are unchanged, which means that $\eta_{2} / \eta_{1} \approx 1$, and the excitation wavelength remains the same.

Note S4. Calculation Details of the Radiative Lifetime.
The PL decay can be described by:

$$
I_{P L}(t)=\sum_{i=1}^{n} k_{i} \exp \left(-t / \tau_{X}^{i}\right)
$$

where $\tau_{X}^{i}$ is the effective single-exciton lifetime given by

$$
\tau_{X}^{i}=\tau_{r, X} \tau_{n r, X}^{i} /\left(\tau_{r, X}+\tau_{n r, X}^{i}\right)
$$

and $k_{i}$ is the relative fraction of the QDs in the i-th sub-ensemble; the $k_{i}$ coefficients are normalized such as $\sum_{i=1}^{n} k_{i}=1$.The PL quantum yield(QY) of the individual subensemble is given by:

$$
q_{i}=\tau_{X}^{i} / \tau_{r, X}
$$

And the total PL QY of the entire QD sample( Q ) can be expressed as:

$$
Q=\sum_{i=1}^{n} k_{i} q_{i}=\tau_{r, X}^{-1} \sum_{i=1}^{n} k_{i} \tau_{X}^{i}
$$

This lead to the following expression for the radiative lifetime:

$$
\tau_{r, X}=Q^{-1} \sum_{i=1}^{n} k_{i} \tau_{X}^{i}=Q^{-1}\left\langle\tau_{X}\right\rangle
$$

Where $\left\langle\tau_{X}\right\rangle_{\text {, is the average exciton lifetime in the } \mathrm{QD} \text { ensemble expressed as: }}$
$\left\langle\tau_{X}\right\rangle=\sum_{i=1}^{n} k_{i} \tau_{X}^{i}$

|  | QTPA1 |  | QTPA2 |  |
| :---: | :---: | :---: | :---: | :---: |
|  | abs (nm) | PL (nm) | abs (nm) | PL (nm) |
| CHX | 413 | 484 | 414 | 483 |
| TOL | 422 | 508 | 422 | 506 |
| o-dichlorobenzene | 425 | 541 | 425 | 555 |
| DCM | 429 | 555 | 430 | 566 |
| THF | 430 | 573 | 431 | 586 |
| TCM | 431 | 581 | 432 | 607 |
| EToH | 432 | 609 | 433 | 617 |
| ACE | 433 | 623 | 434 | 623 |
| DMF | 435 | 631 | 436 | 642 |
| DMSO | 438 | 643 | 438 | 658 |

Table S1. The relevant data of solution absorption and photoluminescence emission spectra of QTPA1 and QTPA2.


Figure S1. Two-photon fluorescence (TPF) spectra of QTPA1 in TOL (A) and DMF (B).


Figure S2. Temperature-dependent fluorescence lifetime of QTPA2.

