From the equation (1) and (2)^[10], the formation energy is ΔE , the total energy of solid Li is $E_{Li}(s)$, of gas state O_2 is $E_{O_2}(g)$, of rhombic sulfur is $E_{S_6}(s)$, the calculated theoretical and experimental data are listed in table S1. The formation energy for Li₂O₂, LiO₂ is lower than the previous work due to temperature effect to a certain extent. The low formation energy of Li₂S indicates that Li₂S is easily reproduced during the discharge process.

$$\Delta E = E_{L_{i_x}O_y}(s) - xE_{L_i}(s) - \frac{y}{2}E_{O_2}(g)$$
(1)

$$\Delta E = E_{Li_2S}(s) - 2E_{Li}(s) - \frac{1}{6}E_{S_6}(g)$$
⁽²⁾

Table S1 Predicted standard formation energy and total energies at zero temperature and their comparisons with available experimental and theoretical data at 298.15K

	Li	O_2	S_6	Li ₄ O ₄	LiO ₂	Li_2S
Total energy	-194.8	-867.52	-1823.86	-2532.59	-1063.76	-700.17
Formation				-9.175	-1.44	(50
energy(ΔE)				(-6.569 ^[10] ,-6.557 ^[S1])	$(-3.272^{[10]}, -2.689^{[S2]})$	-0.39

*The Computational methods of Li, O₂, S₆ are consistent with Li₂O₂, LiO₂, and Li₂S.

Method type	Bandgaps (eV)		
	Li ₂ O ₂	Li ₂ S	
GGA-PBE	1.894	3.398	
GGA-WC	1.934	3.212	
HES06	5.040	4.069	
GGA-RPBE(PBE)	1.88(1.99) ^[23,24]		
GGA-PBE, and vdW-DF		3.46 ^[25]	

Table S2 Predicted bandgaps and their comparisons with available theoretical data



Fig. S1 The phonon dispersion of the LiO₂

References:

S1 Chase, M.W. NIST-JANAF Thermochemical Tables, JANAF 4th Ed., Washington D.C.: ACS, AIP, NIST, 1998.

S2 D'Orazio, L.A., Wood, R.H. Thermodynamics of the higher oxides. I, J. Phys. Chem. 1965, 69, 2550-2557