

## The role of the A monovalent cation in the $AVF_3$ perovskite series. A quantum mechanical investigation.

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In this section, complementary material for the discussion in the main text is provided:

1. Table I provides the contribution of the polarization functions on the 5 A cations. For Li, Na, and K, then, the effect of adding a d shell is shown. For Rb and Cs, the energy lowering is due to the addition of a f shell. For Li, Na and K the d shell is added both in the cubic (Cs and Rb), and in the tetragonal (K) or orthorhombic (Li, Na) equilibrium geometries. Data refer to B3LYP, FM solution. In all cases the added shell contains a single Gaussian. The exponent of the polarization function has been optimized in the bulk.
2. Tables II, III, IV, V VI show the optimized Li, Na, K, Rb and Cs basis sets; the optimization is

performed in the bulk, with B3LYP, for the FM solution. The V and F basis set has been optimized in  $KVF_3$  bulk, and used as such for the other four systems.

3. Table VII reports the core and valence (and the lowest conduction) eigenvalues for the three kinds of atoms of the five systems, evaluated with B3LYP for the FM solution, at the equilibrium geometry of the most stable structure: cubic (Rb, Cs), or tetragonal (K), or orthorhombic (Na, Li). The width of the bands ( $\delta$ ) and the energy difference between the  $\alpha$  and  $\beta$  eigenvalues ( $\Delta$ ) is also shown. Obviously, most of the *bands* are actually levels with width smaller than 0.1 eV.

All tables are referred to and commented in the main text.

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TABLE I. Effect of adding d (A=Li, Na, K) and f (Rb and Cs) polarization orbitals.  $\Delta E$  is the total energy difference obtained with and without the polarization functions at fixed optimized geometry. The data to the left refer to the cubic structure; to the right, to the most stable space group (see text). The exponents of the optimized polarization shell is shown in the following tables. Q is the Mulliken population of the polarization shell. Energies are in  $E_h$ ,  $\Delta E$  in  $\mu E_h$ . Population in  $|e|$ .

	Pm $\bar{3}$ (221)			Pnma (62)		
	E	Q	$\Delta E$	E	Q	$\Delta E$
Li	-1251.276144	0.007	-1.3	-1251.324773	0.021	-1.0
Na	-1406.053857	0.013	-2.1	-1406.072297	0.017	-1.3
K	-1843.669071	0.038	-5.9	-1843.669146	0.039	-5.8
Rb	-4183.658627	0.004	-0.9			
Cs	-8800.175405	0.007	-1.9			

TABLE II. The K, V and F basis sets optimized (numerically) in  $\text{KVF}_3$ . The optimization process stops when a full cycle of optimization lowers the total energy of the bulk by less than  $1 \mu E_h$ ; optimization performed for space group P6mm (four formula units).

19	6	0	0	8	2.0	1.0000
				170602.10967	0.00022	
				23423.76869	0.00201	
				4918.08613	0.01147	
				1305.24945	0.04985	
				404.40909	0.16260	
				142.61932	0.35178	
				55.32332	0.40572	
				22.35979	0.14772	
		0	1	6	8.0	1.0000
				471.67766	-0.00467	0.00626
				113.04226	-0.05669	0.04548
				36.60891	-0.14039	0.17447
				13.65432	0.21493	0.37601
				5.42563	0.71855	0.41160
				2.02585	0.32366	0.16604
		0	1	5	8.0	1.0000
				18.87356	-0.00342	-0.02775
				6.48435	-0.27631	-0.06849
				2.78914	-0.60990	0.24189
				1.15389	1.07001	1.38192
				0.42253	1.18745	1.27860
		0	1	1	0.0	1.0000
				0.51160	1.00000	1.00000
		0	1	1	0.0	1.0000
				0.15452	1.00000	1.00000
		0	3	1	0.0	1.0000
				0.30473	1.00000	
23	7	0	0	8	2.0	1.0000
				243610.31337	0.00023	
				33706.54271	0.00204	
				7132.80340	0.01157	
				1906.39231	0.04990	
				592.63885	0.16306	
				209.18489	0.35407	
				81.52253	0.40504	
				33.04397	0.14371	
		0	1	6	8.0	1.0000
				714.98240	-0.00449	0.00660
				171.50341	-0.05530	0.04806
				56.07125	-0.14050	0.18607
				21.21413	0.19583	0.40012
				8.74267	0.70802	0.41590
				3.60772	0.29757	0.13522
		0	1	4	8.0	1.0000
				34.02706	0.01132	-0.02251
				11.21250	-0.30640	-0.08367
				4.81204	-0.76077	0.23245
				2.04920	1.13284	1.22344
		0	1	1	0.0	1.0000
				0.85592	1.00000	1.00000
		0	1	1	0.0	1.0000
				0.32795	1.00000	1.00000
		0	3	4	3.0	1.0000
				23.97650	0.03669	
				6.47729	0.18401	
				2.12869	0.42845	
				0.72089	0.51429	
		0	3	1	0.0	1.0000
				0.23477	1.00000	
9	4	0	0	7	2.0	1.0000
				10139.60067	0.00110	
				1517.42324	0.00850	
				348.08291	0.04183	
				100.56220	0.14604	
				33.74770	0.33609	
				12.83710	0.40569	
				5.27944	0.16871	
		0	1	3	8.0	1.0000
				39.45194	-0.06901	0.07752
				9.17932	-0.39853	0.45487
				2.75061	0.48002	1.30646
		0	1	1	0.0	1.0000
				0.86820	1.00000	1.00000
		0	1	1	0.0	1.0000
				0.24838	1.00000	1.00000

TABLE III. The Li basis set optimized in  $\text{LiVF}_3$ 

3 4			
0 0	5	2.0	1.0000
	1207.38010	0.00155	
	201.18462	0.00992	
	45.76816	0.05585	
	11.54912	0.24230	
	3.11940	0.66414	
0 1	1	0.0	1.0000
	0.87435	1.00000	1.00000
0 1	1	0.0	1.0000
	0.14960	1.00000	1.00000
0 3	1	0.0	1.0000
	0.40845	1.00000	

TABLE IV. The Na basis set optimized in  $\text{NaVF}_3$ 

11 5			
0 0	8	2.0	1.0000
	55701.72042	0.00023	
	7945.78669	0.00194	
	1683.28885	0.01119	
	439.65696	0.05018	
	133.30567	0.16677	
	45.99796	0.36134	
	17.66780	0.40167	
	7.22365	0.14933	
0 1	5	8.0	1.0000
	108.46506	-0.00738	0.00871
	26.10566	-0.07257	0.05648
	8.40948	-0.08722	0.18921
	3.10995	0.31845	0.35247
	1.20577	0.61033	0.38252
0 1	1	0.0	1.0000
	0.46702	1.00000	1.00000
0 1	1	0.0	1.0000
	0.11512	1.00000	1.00000
0 3	1	0.0	1.0000
	0.35851	1.00000	

TABLE V. The Rb basis set optimized in RbVF<sub>3</sub>

37	10			
0	0	8	2.0	1.0000
		2850858.11809	0.00003	
		415753.92550	0.00030	
		71313.36763	0.00255	
		15645.53008	0.01409	
		4206.42720	0.06098	
		1279.89992	0.20518	
		422.60980	0.44897	
		146.09441	0.38337	
0	1	6	8.0	1.0000
		4625.18760	-0.00033	0.00169
		1083.11959	-0.01075	0.01465
		341.74990	-0.07128	0.07645
		125.29215	-0.12744	0.25406
		49.98883	0.35681	0.48209
		20.61764	0.77457	0.38454
0	1	5	8.0	1.0000
		75.50906	0.00116	-0.01604
		21.23088	-0.05942	-0.07551
		16.67282	-0.04588	0.14150
		8.08641	352.52995	0.62583
		5.32950	106.92995	0.61211
0	1	3	8.0	1.0000
		7.11540	0.74932	-0.45559
		2.66216	0.19118	0.19639
		1.46383	0.02213	0.06671
0	1	1	0.0	1.0000
		0.72691	1.00000	1.00000
0	1	1	0.0	1.0000
		0.25325	1.00000	1.00000
0	3	5	10.0	1.0000
		250.04613	0.00610	
		72.91736	0.04837	
		26.51837	0.19051	
		10.46395	0.41558	
		4.13361	0.47976	
0	3	1	0.0	1.0000
		1.57935	0.99925	
0	3	1	0.0	1.0000
		0.49255	0.99925	
0	4	1	0.0	1.0000
		0.46697	1.00000	

TABLE VI. The Cs basi set optimized in CsVF<sub>3</sub>

55 11				
0 0	9	2.0	1.0000	
	5371058.30078	0.00005		
	780235.96199	0.00040		
	166217.96247	0.00238		
	43056.24088	0.01130		
	12690.32695	0.04565		
	4128.37094	0.15065		
	1472.59933	0.35821		
	570.80952	0.48513		
	232.15700	0.23063		
0 1	7	8.0	1.0000	
	14813.73771	-0.00037	0.00115	
	3459.82498	-0.00650	0.01026	
	1091.07743	-0.05024	0.05724	
	401.23611	-0.14503	0.21166	
	165.00542	0.06736	0.47093	
	74.12614	0.66416	0.52596	
	34.75478	0.50279	0.22665	
0 1	6	8.0	1.0000	
	362.87245	0.00616	-0.01286	
	139.34470	-0.02466	-0.06984	
	56.94712	-0.30068	-0.00730	
	26.91024	-0.09427	0.77239	
	12.80035	0.86557	1.36381	
	6.28899	0.59226	0.53691	
0 3	6	10.0	1.0000	
	444.19163	0.01298		
	133.01663	0.09115		
	50.23551	0.29264		
	21.15547	0.45088		
	9.49038	0.30392		
	4.13882	0.05614		
0 1	3	8.0	1.0000	
	10.22516	0.55576	-0.12044	
	6.16664	0.24266	0.25117	
	3.54524	0.04065	0.29157	
0 3	3	10.0	1.0000	
	8.30737	0.19298		
	3.35715	0.54189		
	1.34214	0.42631		
0 3	1	0.0	1.0000	
	0.45394	1.00000		
0 1	3	8.0	1.0000	
	7.35954	0.10108	0.02690	
	2.59709	0.88418	0.37490	
	1.26647	0.61672	0.24353	
0 1	1	0.0	1.0000	
	0.47820	1.00000	1.00000	
0 1	1	0.0	1.0000	
	0.17933	1.00000	1.00000	
0 4	1	0.0	1.0000	
	0.45425	1.00000		

	Li			Na			K			Rb			Cs		
	$E_a$	$\delta$	$\Delta$	$E_a$	$\delta$	$\Delta$	$E_a$	$\delta$	$\Delta$	$E_a$	$\delta$	$\Delta$	$E_a$	$\delta$	$\Delta$
Cs 1s													-34305.5	0.0	0.0
Rb 1s										-14790.2	0.0	0.0			
V 1s	-5350.8	0.0	0.0	-5350.9	0.0	0.0	-5350.9	0.0	0.0	-5351.1	0.0	0.0	-5350.9	0.0	0.0
K 1s							-3525.9	0.0	0.0						
Cs 2s													-5254.6	0.0	0.0
Cs 2p													-4949.6	0.0	0.0
Na 1s				-1040.8	0.0	0.0									
Rb 2s										-1956.8	0.0	0.0			
Rb 2p										-1775.7	0.0	0.0			
Cs 3s													-1093.9	0.0	0.0
Cs 3p													-963.7	0.0	0.0
Cs 3d													-721.9	0.0	0.0
F 1s	-666.0	0.3	0.0	-665.8	0.0	0.0	-665.7	0.0	0.0	-665.6	0.0	0.0	-665.0	0.0	0.0
V 2s	-599.0	0.0	1.0	-599.0	0.0	1.0	-599.0	0.0	1.0	-599.0	0.0	1.0	-599.0	0.0	1.0
V 2p	-503.7	0.0	0.8	-503.8	0.0	0.8	-503.8	0.0	0.8	-503.8	0.0	0.8	-503.8	0.0	0.8
Rb 3s										-289.1	0.0	0.0			
K 2s							-353.8	0.0	0.0						
K 2p							-281.4	0.0	0.0						
Rb 3p										-223.9	0.0	0.0			
Cs 4s													-203.1	0.0	0.0
Cs 4p													-155.8	0.0	0.0
Rb 3d										-105.2	0.0	0.0			
Cs 4d													-73.5	0.0	0.0
Na 2s				-54.9	0.0	0.0									
Li 1s	-48.5	0.0	0.0												
V 3s	-66.5	0.0	3.2	-66.5	0.0	3.2	-66.5	0.0	3.2	-66.5	0.0	3.2	-66.5	0.0	3.2
V 3p	-40.3	0.1	3.2	-40.3	0.1	3.3	-40.3	0.0	3.3	-40.3	0.0	3.4	-40.2	0.0	3.4
K 3s							-32.2	0.0	0.0						
Rb 4s										-27.3	0.2	0.0			
F 2s	-26.6	0.6	0.1	-26.6	0.5	0.0	-26.3	0.4	0.1	-26.1	0.4	0.1	-25.6	0.4	0.1
Na 2p				-26.6	0.5	0.0									
Cs 5s													-19.9	0.2	0.0
K 3p							-15.1	0.2	0.0						
Rb 4p										-12.0	0.6	0.0			
Cs 5p													-9.3	1.5	0.1
F 2p	-8.4	2.7	0.1	-8.3	2.5	0.1	-8.6	2.9	0.1	-8.5	2.9	0.1	-9.3	4.5	0.1
V t2g	-0.7	0.7	5.9	-0.8	0.8	5.1	-1.0	1.0	8.7	-1.0	1.0	7.6	-0.8	0.8	7.4
V eg	4.5	0.5	8.8	4.1	1.0	4.1	4.3	0.9	11.7	4.2	0.9	6.2	4.2	0.9	5.8
Na 3s				4.1	3.5	-2.0									
Li 2s	6.1	1.8	-1.0												
F 3s	6.1	1.8	0.3	5.6	2.0	5.7	6.0	2.6	0.9	9.3	1.5	0.7	8.9	1.5	0.6
Rb 5s										12.1	1.5	-0.7			
Cs 5s													8.9	1.5	0.6

TABLE VII. B3LYP FM core and valence eigenvalues (and lowest conduction ones) for the [Li-Cs]VF<sub>3</sub> system in the most stable structure.  $\delta$  is the width of the band.  $\Delta$  (in  $\mu E_h$ ) is the maximum difference between the  $\beta$  and  $\alpha$  eigenvalues. The horizontal line separates the occupied from the virtual levels.