

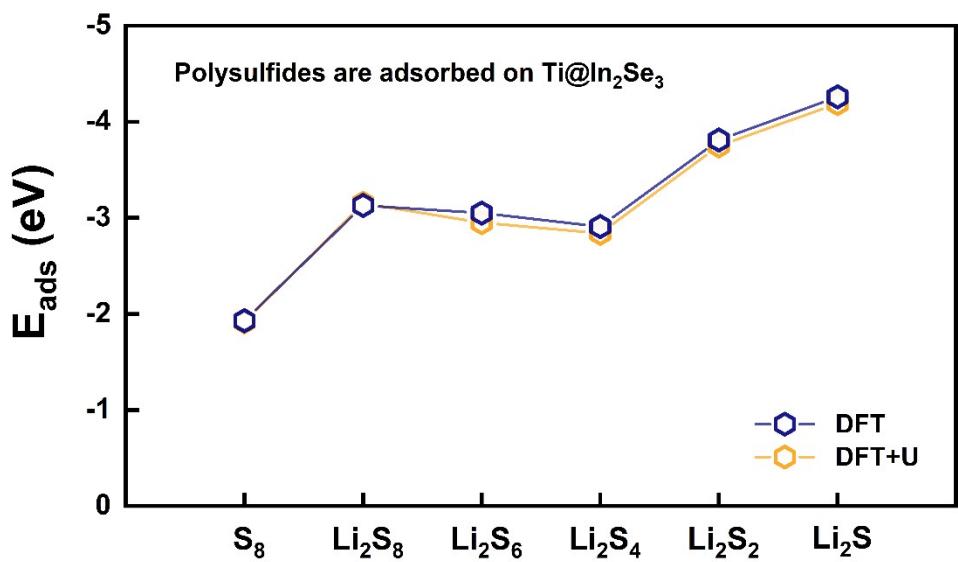
## **Electronic Supplementary Information**

### **Identification of linear scaling relationships in polysulfide conversion on $\alpha$ -In<sub>2</sub>Se<sub>3</sub> supported single-atom catalysts**

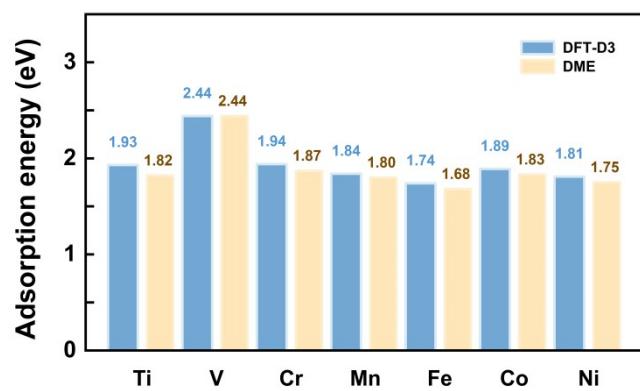
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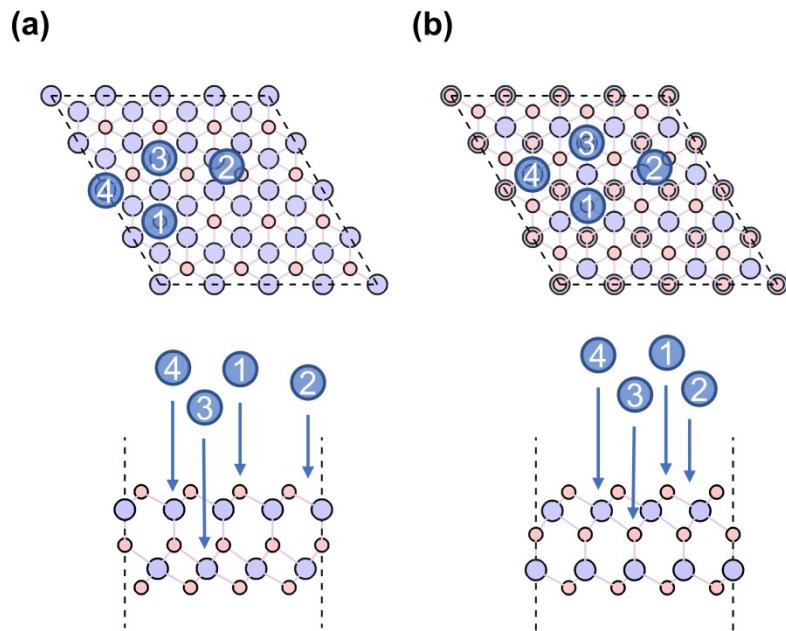
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**Fig. S1** Adsorption energies for Li<sub>2</sub>S<sub>n</sub> via DFT and DFT+U ( $U_{\text{eff}} = 2.58$  eV).



**Fig. S2** Adsorption energies of  $S_8$  with and without consideration of the effect of DME solvent.



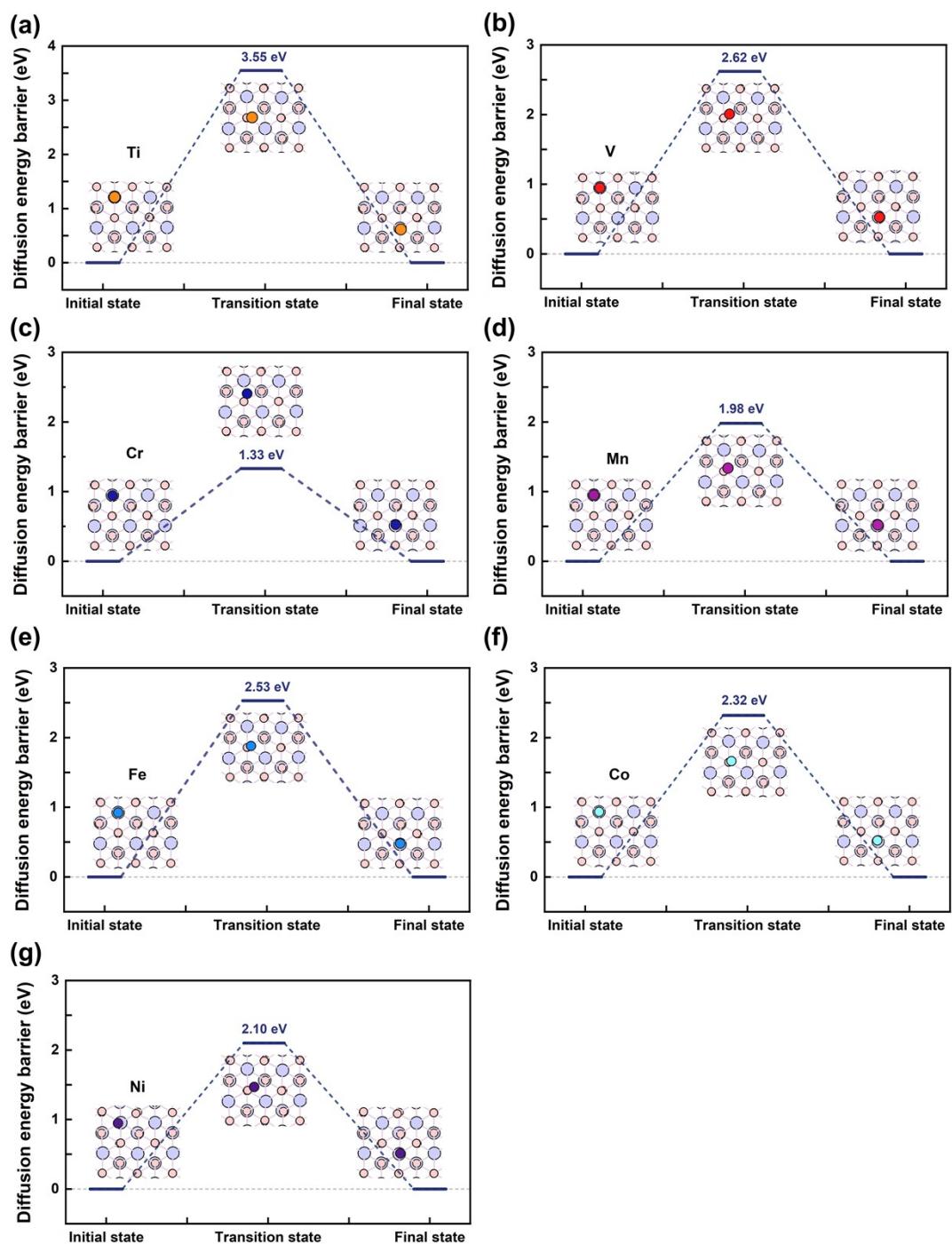
**Fig. S3** Top and side views of (a)  $P_{\uparrow}In_2Se_3$  and (b)  $P_{\downarrow}In_2Se_3$  (color code: pink, Se; purple, In; blue, TM). Four different surface sites, namely, Se top site (site 1), bridge site (site 2), fcc hollow site (site 3), and hcp hollow site (site 4), are labeled.

**Table S1** The values of U parameters for DFT+U calculations (U in eV)

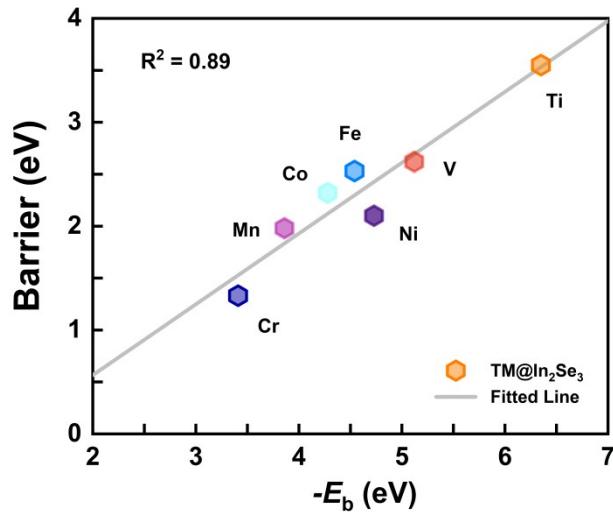
TM	Ti	V	Cr	Mn	Fe	Co	Ni
U	2.58	2.72	2.79	3.06	3.29	3.42	3.40

**Table S2** Binding energies ( $E_b$  in eV) for TM atoms adsorbs on  $P \downarrow In_2Se_3$ 

catalysts	site 1	site 2	site 3	site 4
<b>Ti@In<sub>2</sub>Se<sub>3</sub></b>	-4.98	-5.14	-5.84	-6.35
<b>V@In<sub>2</sub>Se<sub>3</sub></b>	-2.43	-2.52	-4.85	-5.12
<b>Cr@In<sub>2</sub>Se<sub>3</sub></b>	-1.94	-2.14	-3.17	-3.41
<b>Mn@In<sub>2</sub>Se<sub>3</sub></b>	-2.44	-2.45	-3.76	-3.86
<b>Fe@In<sub>2</sub>Se<sub>3</sub></b>	-2.20	-3.10	-4.14	-4.54
<b>Co@In<sub>2</sub>Se<sub>3</sub></b>	-1.95	-1.91	-3.76	-4.28
<b>Ni@In<sub>2</sub>Se<sub>3</sub></b>	-2.55	-2.33	-4.34	-4.73



**Fig. S4** Energy profile and corresponding structures for single TM atom diffusion on  $\text{In}_2\text{Se}_3$  surface.



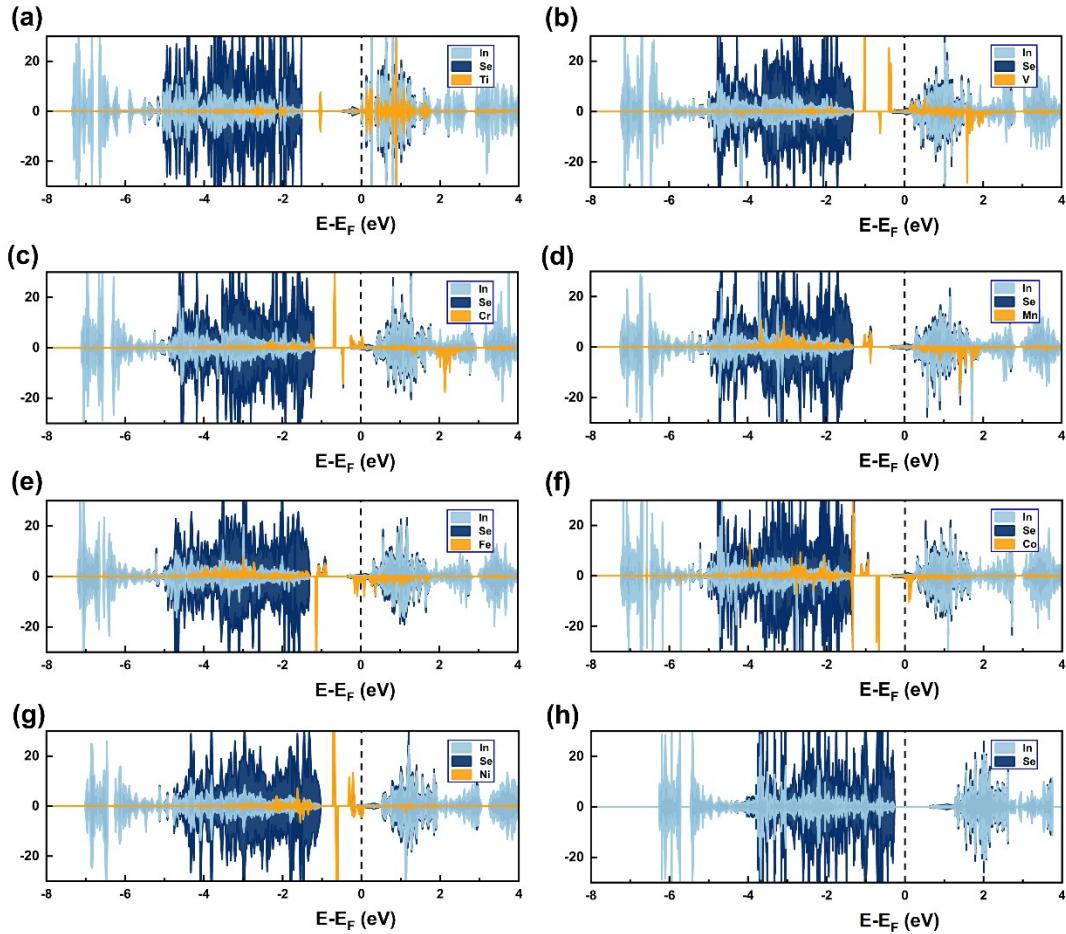
**Fig. S5** Correlation between binding energies ( $E_b$ ) and diffusion barriers (Barrier) for single TM atom absorbed on  $\text{In}_2\text{Se}_3$ .

**Table S3** The binding energies ( $E_b$  in eV) and diffusion barrier (Barrier in eV) for single TM atom on  $\text{In}_2\text{Se}_3$

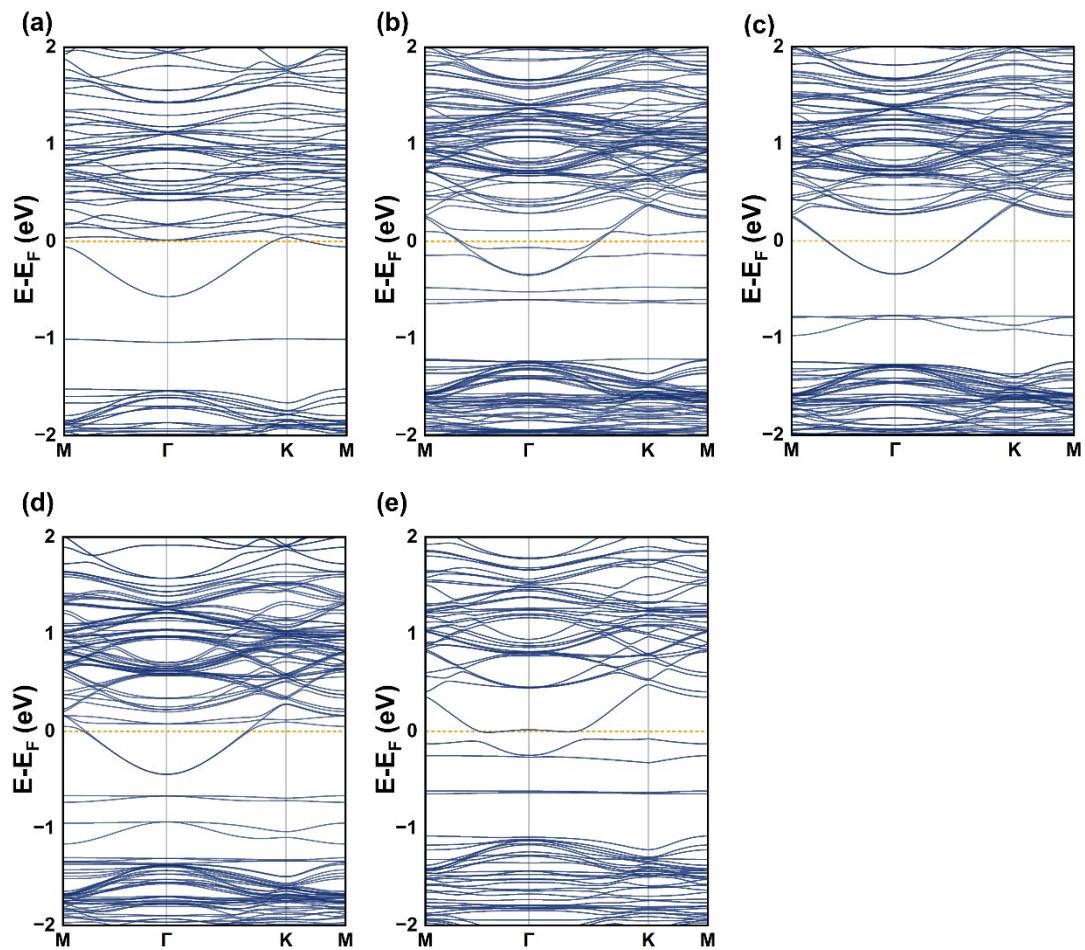
TM	Ti	V	Cr	Mn	Fe	Co	Ni
$E_b$	-6.35	-5.12	-3.41	-3.86	-4.54	-4.28	-4.73
Barrier	3.55	2.62	1.33	1.98	2.53	2.32	2.10

**Table S4** The average electrons transferred from the anchored TM atoms to the  $\text{In}_2\text{Se}_3$  substrate ( $Q$  in e)

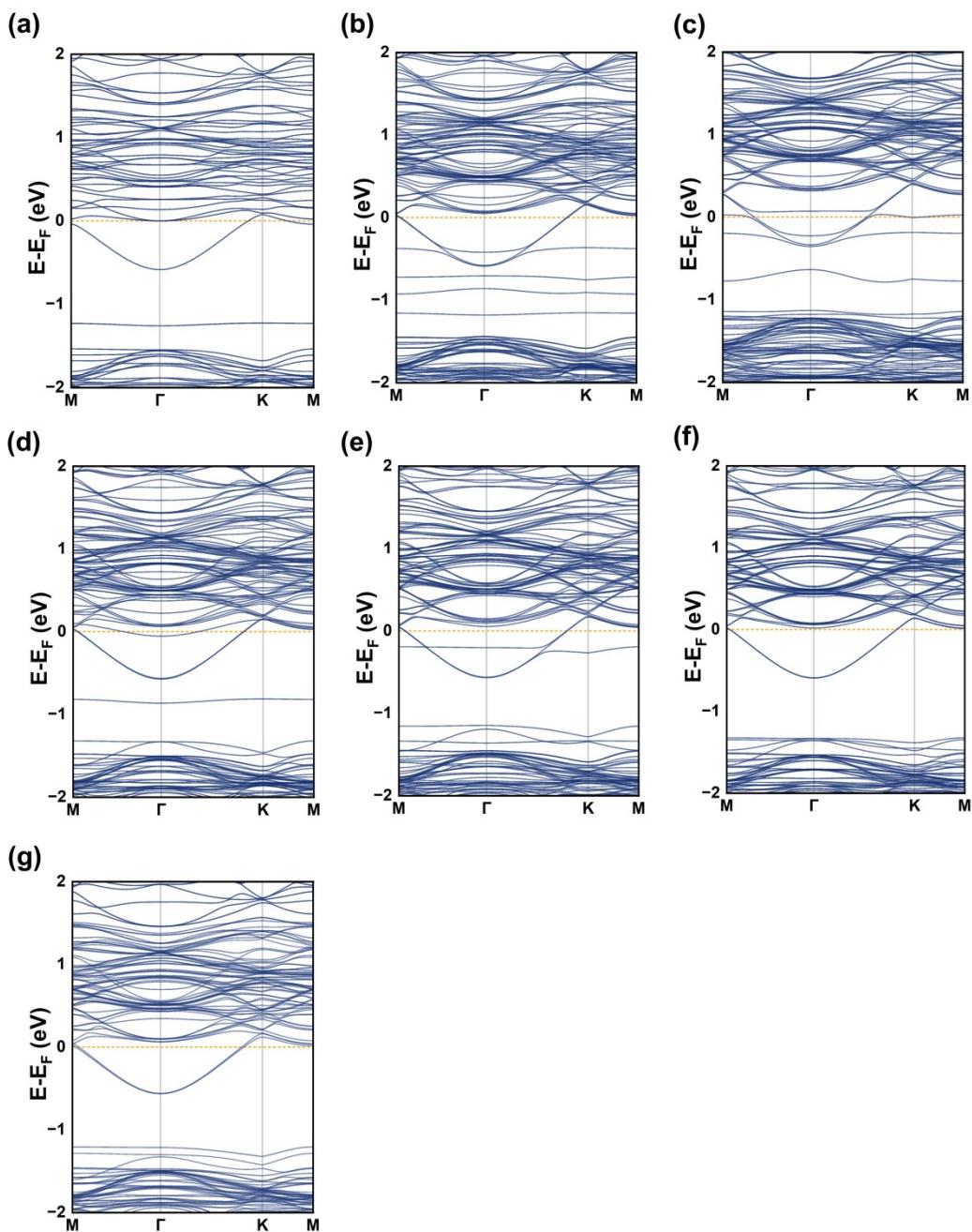
TM	Ti	V	Cr	Mn	Fe	Co	Ni
$Q$	0.88	0.62	0.54	0.63	0.47	0.30	0.03



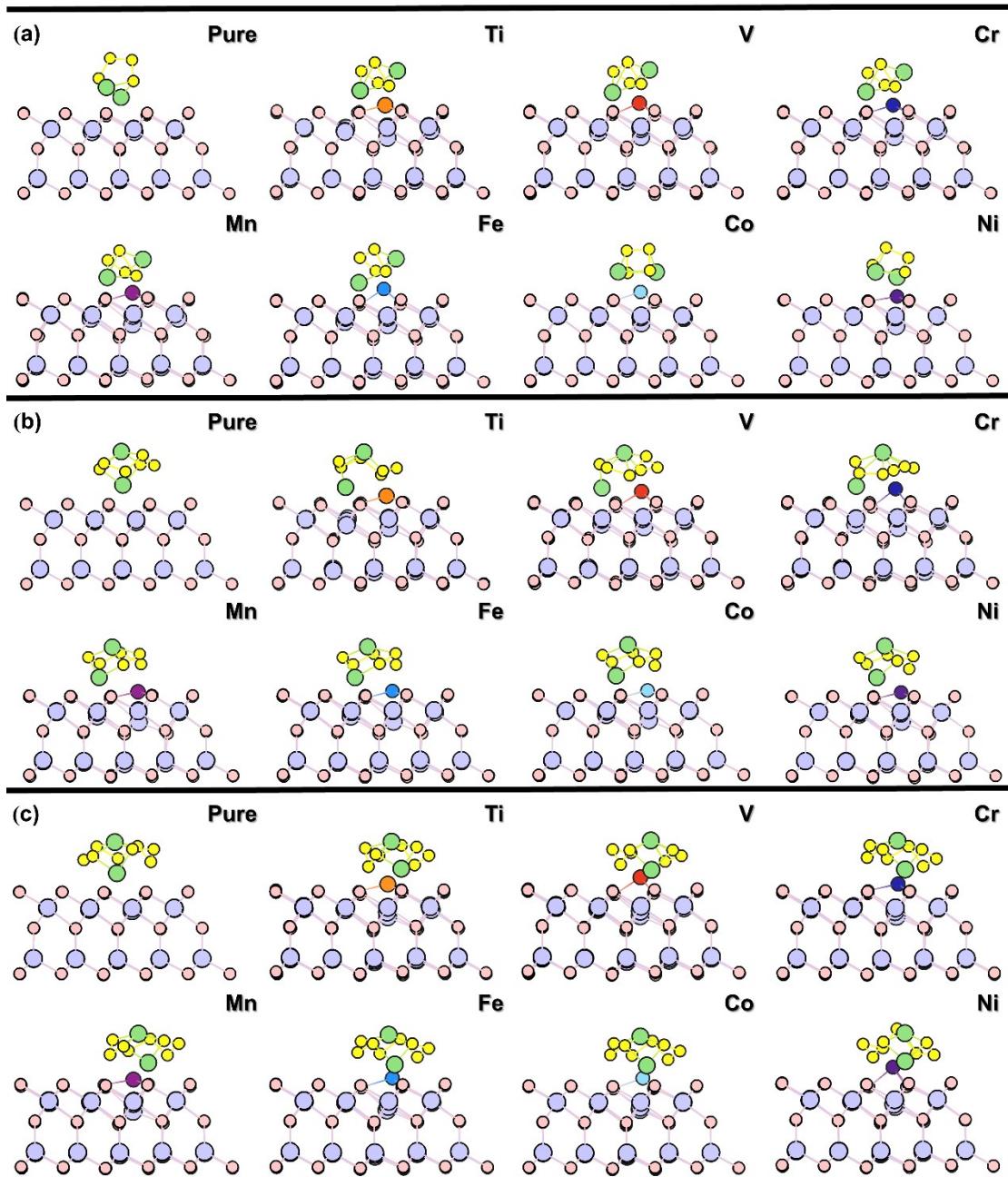
**Fig. S6** Projected density of states (PDOS) of the TM@In<sub>2</sub>Se<sub>3</sub>. (a) Ti@In<sub>2</sub>Se<sub>3</sub>, (b) V@In<sub>2</sub>Se<sub>3</sub>, (c) Cr@In<sub>2</sub>Se<sub>3</sub>, (d) Mn@In<sub>2</sub>Se<sub>3</sub>, (e) Fe@In<sub>2</sub>Se<sub>3</sub>, (f) Co@In<sub>2</sub>Se<sub>3</sub>, (g) Ni@In<sub>2</sub>Se<sub>3</sub>, (h) In<sub>2</sub>Se<sub>3</sub>. The positive and negative values represent the spin-up and spin-down states, respectively. The Fermi level is set to 0 eV.



**Fig. S7** Electronic band structures of TM@In<sub>2</sub>Se<sub>3</sub>. (a)-(e) Represent for Ti@In<sub>2</sub>Se<sub>3</sub>, Cr@In<sub>2</sub>Se<sub>3</sub>, Mn@In<sub>2</sub>Se<sub>3</sub>, Co@In<sub>2</sub>Se<sub>3</sub> and Ni@In<sub>2</sub>Se<sub>3</sub>, respectively.



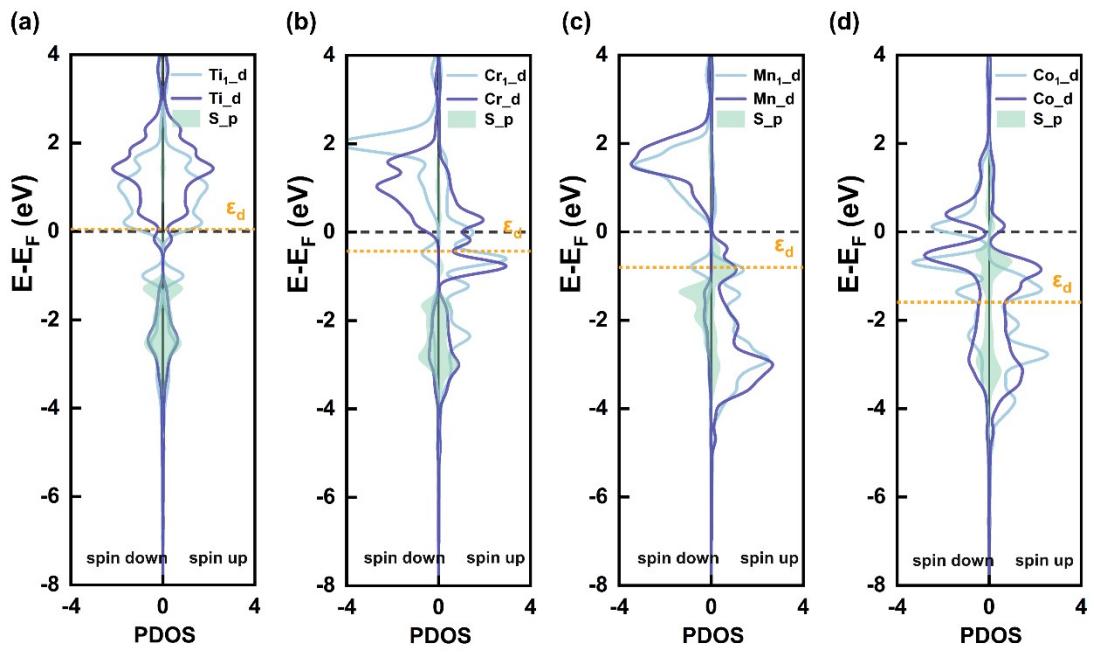
**Fig. S8** Electronic band structures of  $\text{TM}@\text{In}_2\text{Se}_3$  calculated by DFT+U. (a)-(g) Represent for  $\text{Ti}@\text{In}_2\text{Se}_3$ ,  $\text{V}@\text{In}_2\text{Se}_3$ ,  $\text{Cr}@\text{In}_2\text{Se}_3$ ,  $\text{Mn}@\text{In}_2\text{Se}_3$ ,  $\text{Fe}@\text{In}_2\text{Se}_3$ ,  $\text{Co}@\text{In}_2\text{Se}_3$  and  $\text{Ni}@\text{In}_2\text{Se}_3$ , respectively.



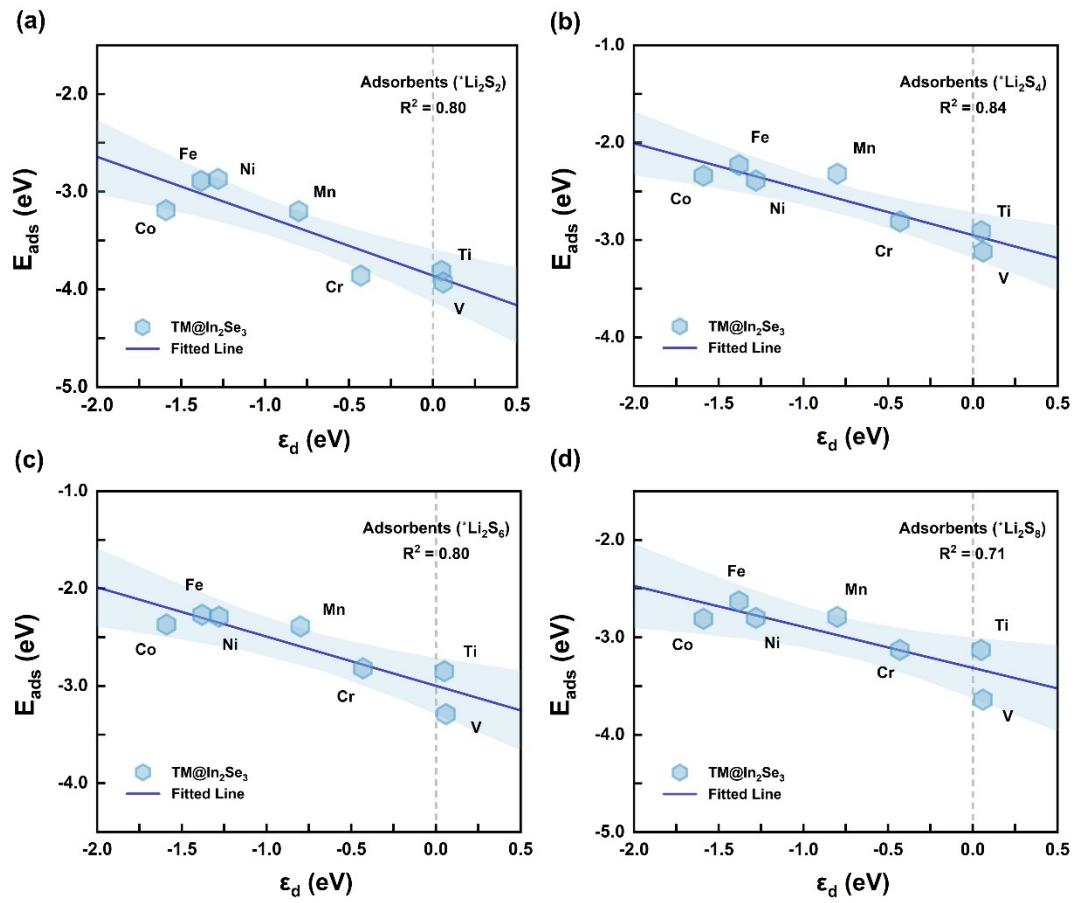
**Fig. S9** Optimized adsorption structures: (a) Li<sub>2</sub>S<sub>4</sub> adsorbs on In<sub>2</sub>Se<sub>3</sub> and TM@In<sub>2</sub>Se<sub>3</sub>, (b) Li<sub>2</sub>S<sub>6</sub> adsorbs on In<sub>2</sub>Se<sub>3</sub> and TM@In<sub>2</sub>Se<sub>3</sub>, (c) Li<sub>2</sub>S<sub>8</sub> adsorbs on In<sub>2</sub>Se<sub>3</sub> and TM@In<sub>2</sub>Se<sub>3</sub> (color code: pink, Se; purple, In; yellow, S; green, Li; other colors, TM)

**Table S5** Adsorption energies for Li<sub>2</sub>S<sub>n</sub> on TM@In<sub>2</sub>Se<sub>3</sub>

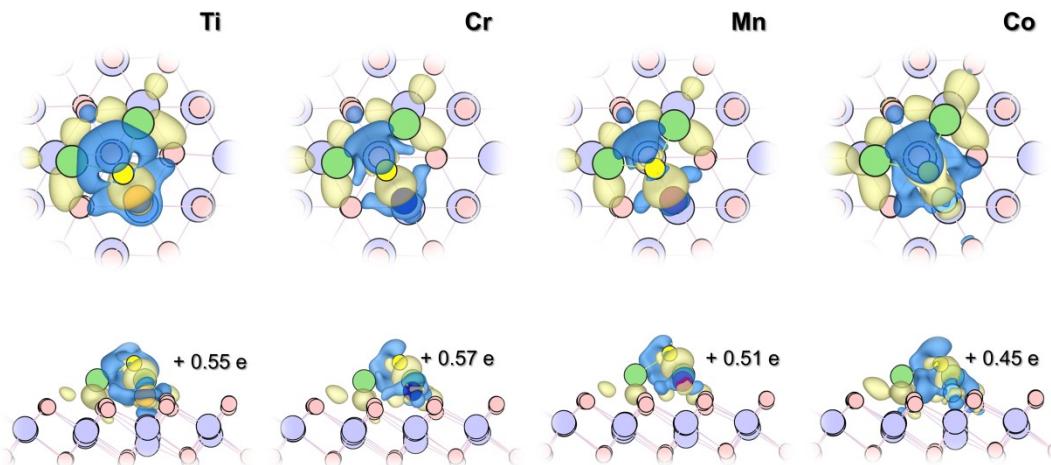
Catalyst \ <i>E<sub>ads</sub></i> (eV)	Li <sub>2</sub> S	Li <sub>2</sub> S <sub>2</sub>	Li <sub>2</sub> S <sub>4</sub>	Li <sub>2</sub> S <sub>6</sub>	Li <sub>2</sub> S <sub>8</sub>	S <sub>8</sub>
Catalyst	Li <sub>2</sub> S	Li <sub>2</sub> S <sub>2</sub>	Li <sub>2</sub> S <sub>4</sub>	Li <sub>2</sub> S <sub>6</sub>	Li <sub>2</sub> S <sub>8</sub>	S <sub>8</sub>
In <sub>2</sub> Se <sub>3</sub>	-3.3	-2.33	-1.69	-1.71	-2.19	-1.46
Ti@In <sub>2</sub> Se <sub>3</sub>	-4.26	-3.81	-2.91	-2.85	-3.13	-1.93
V@In <sub>2</sub> Se <sub>3</sub>	-4.36	-3.93	-3.12	-3.29	-3.64	-2.44
Cr@In <sub>2</sub> Se <sub>3</sub>	-4.19	-3.86	-2.81	-2.82	-3.13	-1.94
Mn@In <sub>2</sub> Se <sub>3</sub>	-3.74	-3.2	-2.32	-2.39	-2.79	-1.84
Fe@In <sub>2</sub> Se <sub>3</sub>	-3.53	-2.89	-2.23	-2.27	-2.63	-1.74
Co@In <sub>2</sub> Se <sub>3</sub>	-3.59	-3.19	-2.34	-2.37	-2.81	-1.89
Ni@In <sub>2</sub> Se <sub>3</sub>	-3.38	-2.87	-2.39	-2.29	-2.8	-1.81



**Fig. S10** (a)-(d) Projected density of states (PDOS) for  $\text{Li}_2\text{S}$  adsorbed on  $\text{Ti}@\text{In}_2\text{Se}_3$ ,  $\text{Cr}@\text{In}_2\text{Se}_3$ ,  $\text{Mn}@\text{In}_2\text{Se}_3$ , and  $\text{Co}@\text{In}_2\text{Se}_3$ , respectively.



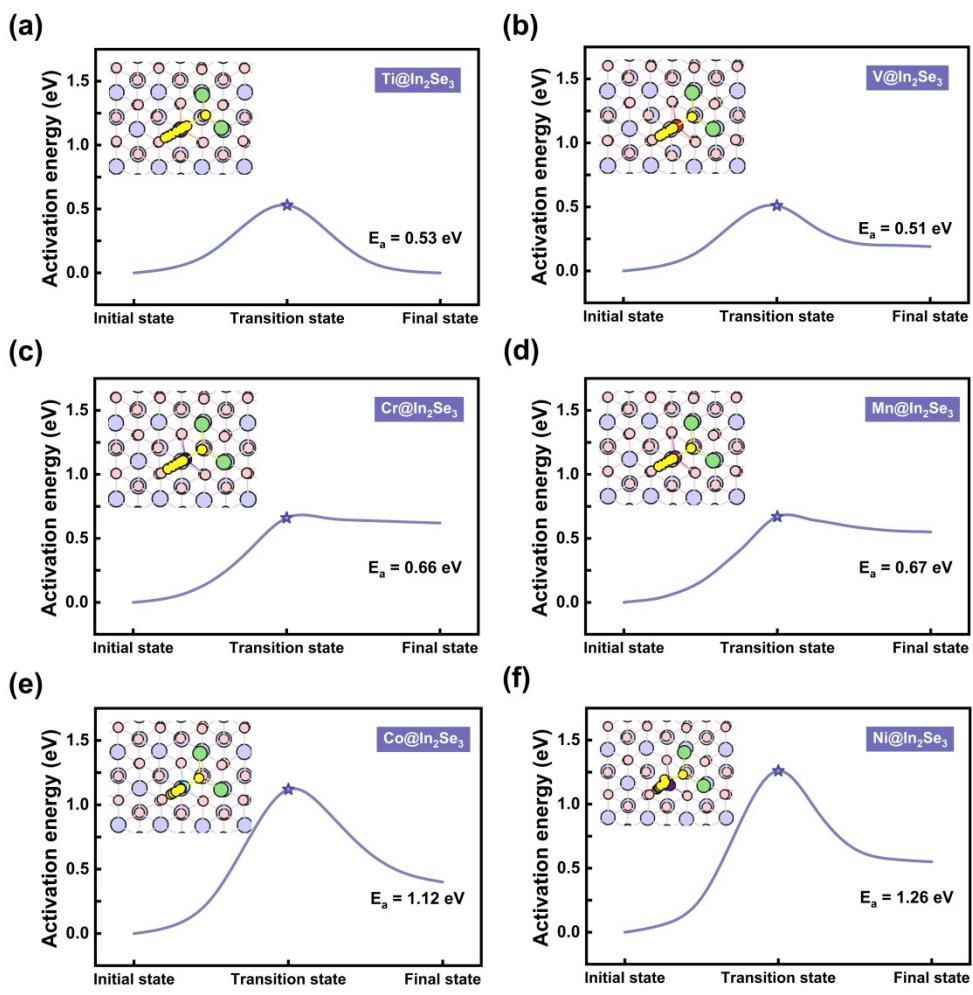
**Fig. S11** (a)-(d) The correlation between  $\epsilon_d$  of the adsorbed TM atoms and  $E_{\text{ads}}$  for  $\text{Li}_2\text{S}_2$ ,  $\text{Li}_2\text{S}_4$ ,  $\text{Li}_2\text{S}_6$ , and  $\text{Li}_2\text{S}_8$  adsorption.



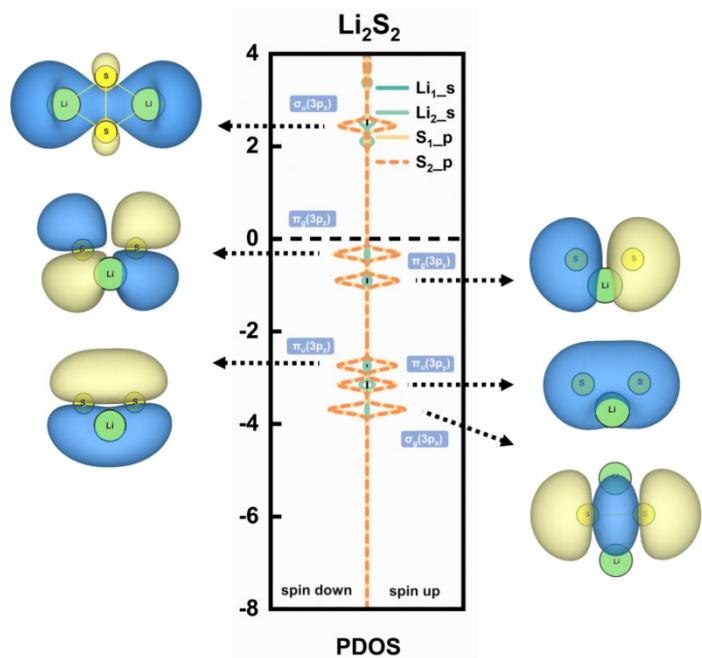
**Fig. S12** Top view and side view of charge density differences for  $\text{Li}_2\text{S}$  adsorbed on  $\text{Ti}@\text{In}_2\text{Se}_3$ ,  $\text{Cr}@\text{In}_2\text{Se}_3$ ,  $\text{Mn}@\text{In}_2\text{Se}_3$ , and  $\text{Co}@\text{In}_2\text{Se}_3$ . Yellow and blue states represent the charge accumulation and loss, respectively. The isosurface is set to be  $0.003 \text{ e}/\text{bohr}^3$ . The amount of charge accumulated on S of the adsorbed  $\text{Li}_2\text{S}$  is presented.

**Table S6** The average Li-S bond length ( $d_{\text{Li-S}}$  in Å) and S-S bond length ( $d_{\text{S-S}}$  in Å) for  $\text{Li}_2\text{S}_2$  absorbed on  $\text{In}_2\text{Se}_3$  and TM@ $\text{In}_2\text{Se}_3$

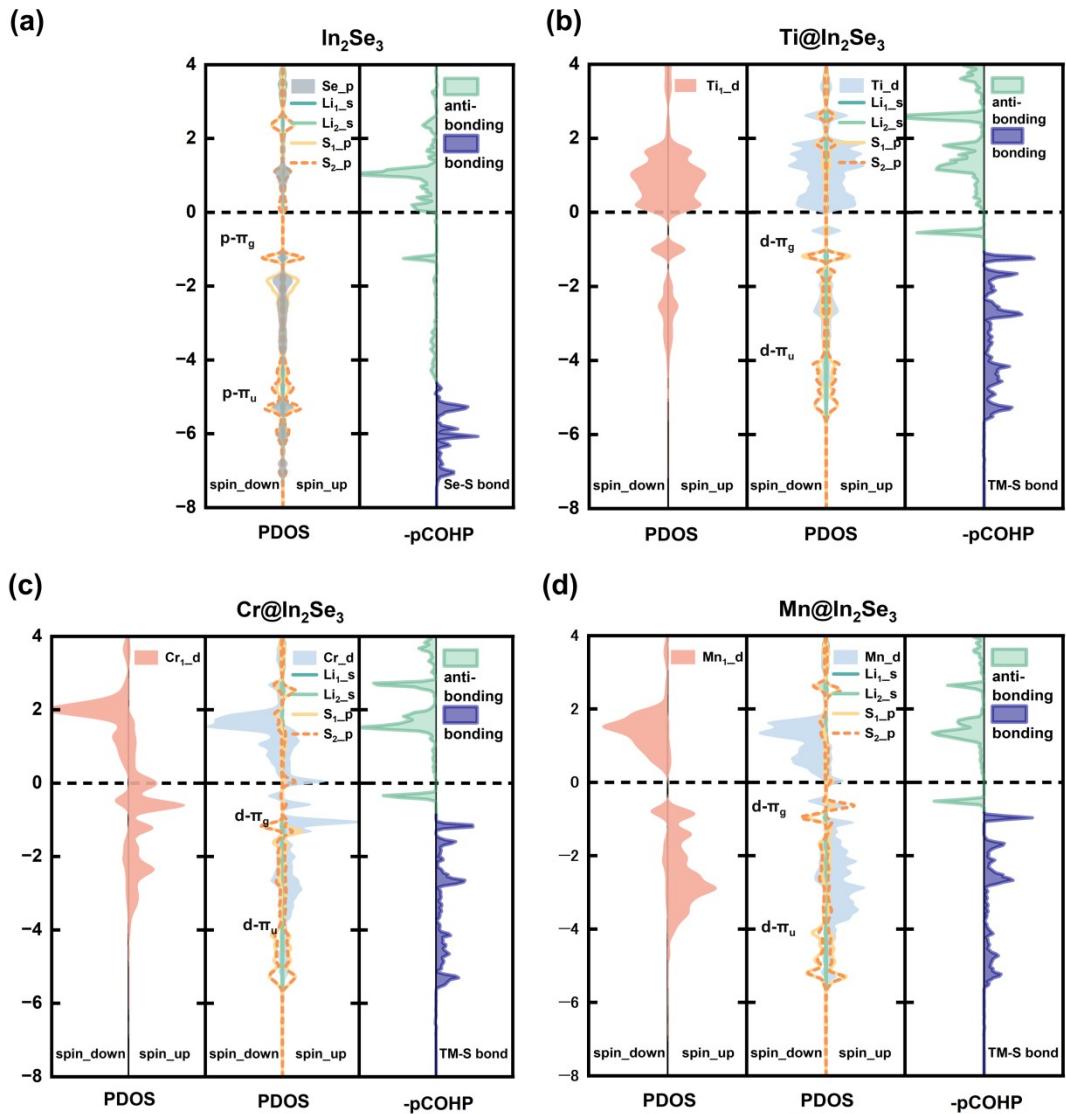
<b>TM</b>	<b>Pure</b>	<b>Ti</b>	<b>V</b>	<b>Cr</b>	<b>Mn</b>	<b>Fe</b>	<b>Co</b>	<b>Ni</b>
$d_{\text{Li-S}}$	2.39	2.48	2.48	2.49	2.52	2.51	2.50	2.51
$d_{\text{S-S}}$	2.05	2.09	2.08	2.06	2.05	2.04	2.03	2.03



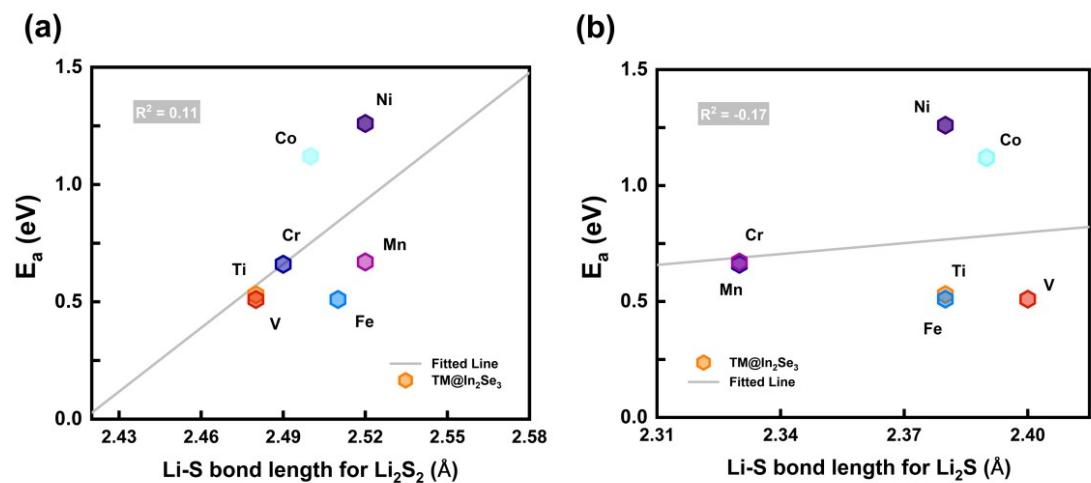
**Fig. S13** (a)-(f) Energy profiles and corresponding structures for Li<sub>2</sub>S<sub>2</sub> dissociation on Ti@In<sub>2</sub>Se<sub>3</sub>, V@In<sub>2</sub>Se<sub>3</sub>, Cr@In<sub>2</sub>Se<sub>3</sub>, Mn@In<sub>2</sub>Se<sub>3</sub>, Co@In<sub>2</sub>Se<sub>3</sub>, and Ni@In<sub>2</sub>Se<sub>3</sub>.



**Fig. S14** Molecular orbitals of gas-phase  $\text{Li}_2\text{S}_2$ .



**Fig. S15** Projected density of states (PDOS) and projected crystal orbital Hamilton population (pCOHP) for  $\text{Li}_2\text{S}_2$  adsorbed on (a)  $\text{In}_2\text{Se}_3$ , (b)  $\text{Ti}@\text{In}_2\text{Se}_3$ , (c)  $\text{Cr}@\text{In}_2\text{Se}_3$ , (d)  $\text{Mn}@\text{In}_2\text{Se}_3$ .



**Fig. S16** Correlation between activation energy and Li-S bond length for (a) the adsorbed  $\text{Li}_2\text{S}_2$  and the adsorbed  $\text{Li}_2\text{S}$ .