Supporting Information: Electric-field induced second harmonic generation responses of push–pull polyenic dyes: Experimental and theoretical characterizations

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1 Synthesis

Polyenals of series I and II were obtained from the corresponding generic aldehydes via a sequential protocol based upon Wittig oxyprenylation followed by acidic hydrolysis.^{S1} Synthesis of intermediate compounds I-Pyr[n] and I-Quin[n] (resp. II-Pyr[n] and II-Quin) was carried out by reacting I[n-1] (resp. II[n-1]) with one equivalent of HE1 or HE2 in anhydrous THF in the presence of a catalytic amount of 18-O-6 crown ether and 1.5 equivalent of NaH. After vigorous stirring at room temperature for 16h, a small amount of water was added to quench the NaH excess and the solvent was evaporated. The reaction mixture was dissolved in dichloromethane and washed with water. After drying the organic phase on Na₂SO₄, the solvent was evaporated and the crude compounds were then purified by column chromatography on silica gel eluting with a 8/2 dichloromethane/ethyl acetate mixture. The intermediate compounds I-Pyr[n] and I-Quin[n] (resp. II-Pyr[n] and II-Quin) were then dissolved in pure methyl iodide. After stirring for one hour, the excess MeI was evaporated and the solids were washed with ether then dried under vacuum. Compounds A-D[n] were characterized by HRMS and ¹H NMR. Elementary analyses (EA) were also conducted for compounds B and C1-3.

B1

NMR ¹**H** (200.13 MHz, CDCl₃): $\delta = 9.55$ (d, J = 6.2Hz, 1H), 8.61 (d, J = 8.0 Hz, 1H), 8.03 (m, 3H), 7.77-8.03 (m, 1H), 7.73 (d, J = 15.4Hz, 1H), 7.64 (d, J = 8.5Hz, 2H), 7.51 (d, J = 15.4Hz, 1H), 6.67 (d, J = 8.5Hz, 2H), 4.50 (s, 3H), 3.37 (m, 4H), 1.66 (m, 4H), 1.39 (m, 4H), 0.92 (t, J = 7.0Hz, 6H). **HRMS** (LSIMS): [C⁺] m/z theo. for C₂₆H₃₃N₂: 373.2644, exp. : 373.2647. **EA**: % theo. for C₂₆H₃₃N₂I+2/3 H₂O: C, 60.94; H, 6.75; N, 5.47, % exp.: C, 60.75; H, 6.87; N, 5.35.

$\mathbf{B2}$

NMR ¹**H** (200.13 MHz, CDCl₃): $\delta = 9.76$ (d, J = 6.0 Hz, 1H), 8.59 (d, J = 8.6 Hz, 1H), 8.08 (m, 3H), 7.93 (m, 1H), 7.93 (m, 1H), 7.69 (m, 1H), 7.47 (d, J = 8.6 Hz, 2H), 7.34 (d, J = 16,7Hz 1H), 7.05 (m, 2H), 6.67 (d, J = 8.4 Hz, 2H), 4.59 (s, 3H), 3.38 (t, J = 7.1Hz, 4H),

1.64 (m, 4H), 1.43 (m, 4H), 1.02 (t, J=7.1Hz, 6H). **HRMS** (LSIMS): [C +] m/z theo. for C₂₈H₃₅N₂: 399.2800, exp.: 399.2797. **EA**: % theo. for C₂₈H₃₅N₂I + H₂O: C, 61.76; H, 6.85; N, 5.14, % exp.: C, 61.55; H, 6.70; N, 4.96.

$\mathbf{B3}$

NMR ¹**H** (200.13 MHz, CDCl₃): $\delta = 9.79$ (d, J = 6.7Hz, 1H), 8.55 (d, J = 8.9 Hz, 1H), 8.13 (m, 3H), 7.89 (m, 1H), 7.71 (dd, J = 14.6 Hz, J = 11.0 Hz, 1H), 7.38 (d, J = 8.9Hz, 2H), 7.31 (d, J = 14.7 Hz, 1H), 6.99 (m, 1H), 6.77 (m, 2H), 6.68-6.62(m, 1H), 6.64 (d, J = 9.0 Hz, 2H), 4.63 (s, 3H), 3.36 (t, J = 7.4Hz, 4H), 1.63 (m, 4H), 1.41 (m, 4H), 1.01 (t, J = 7.2Hz, 6H). **HRMS** (LSIMS): [C⁺] m/z theo. for C₃₀H₃₇N₂: 425.2957, exp.: 425.2961. **EA**: % theo. for C₃₀H₃₇N₂I + 1.5 H₂O: C, 62.17; H, 6.96; N, 4.83, % exp.: C, 62.03; H, 6.84; N, 4.96.

$\mathbf{B4}$

NMR ¹**H** (200.13 MHz, CDCl₃): $\delta = 9.87$ (d, J = 6.5Hz, 1H), 8.54 (d, J = 8.4 Hz, 1H), 8.16 (m, 3H), 7.94 (m, 1H), 7.70 (dd, J=15.9 Hz, J=11.1 Hz, 1H), 7.35 (d, J=8.9Hz, 2H), 7.32 (d, J=11.1 Hz,1H), 6.95 (dd, J=15.9 Hz, J=10.9 Hz, 1H), 6.77-6.61 (m, 4H), 6.63 (d, J=8.9 Hz, 2H), 6.45 (dd, J=14.9 Hz, J=11.1 Hz, 1H), 4.66 (s, 3H), 3.34 (t, J=7.6Hz, 4H), 1.60 (m, 4H), 1.40 (t, 4H), 1.00 (t, J=7.2Hz, 6H). **HRMS** (LSIMS): [C⁺] m/z theo. for C₃₂H₃₉N₂: 451.3113, exp.: 451.3114. **EA**: % theo. for C₃₂H₃₉N₂I + H₂O: C, 64.42; H, 6.93; N, 4.70, % exp.: C, 64.58; H, 6.79; N, 4.56.

$\mathbf{B5}$

NMR ¹**H** (200.13 MHz, CDCl₃): $\delta = 9.86$ (m, 1H), 8.54 (d, J = 8.8 Hz, 1H), 8.15 (m, 3H), 7.94 (m, 1H), 7.69 (dd, J=15.6 Hz, J=10.7 Hz, 1H), 7.36 (d, J=8.8Hz, 2H), 7.33 (m, 4H), 6.93 (m, 1H), 6.75 (m, 3H), 6.63 (d, J = 9.5Hz, 2H), 6.45 (m, 1H), 4.66 (s, 3H), 3.33 (t, J =7.4Hz, 4H), 1.62 (m, 4H), 1.37 (m, 4H), 0.97 (t, J=7.2Hz, 6H). **HRMS** (LSIMS): [C⁺] m/ztheo. for C₃₄H₄₁N₂: 477.3270, exp.: 477.3271. **EA**: % theo. for C₃₄H₄₁N₂I + H₂O: C, 65.59; H, 6.96; N, 4.50, % exp.: C, 65.63; H, 6.77; N, 4.08.

C1

NMR ¹**H** (200.13 MHz, CDCl₃): $\delta = 8.50$ (d, J = 6.8 Hz, 2H), 7.74 (d, J = 14.9 Hz,

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1H), 7.54 (d, J = 6.8 Hz, 2H), 7.25 (d, J = 4.4 Hz, 1H), 6.14 (d, J = 14.9 Hz, 1H), 5.90 (d, J = 4.4 Hz, 1H), 4.28 (s, 3H), 3.36 (m, 4H), 1.64 (m, 4H), 1.34 (m, 4H), 0.98 (m, 6H). **HRMS** (LSIMS): [C⁺] m/z theo. for C₂₀H₂₉N₂S: 329.2051, exp. : 329.2054. **EA**: % theo. for C₂₀H₂₉IN₂S + H₂O : C, 50.63; H, 6.59; N, 5.90, % exp.: C, 50.83; H, 6.24; N, 5.87.

$\mathbf{C2}$

NMR ¹**H** (200.13 MHz, CDCl₃): $\delta = 8.63$ (d, J = 7.2 Hz, 2H), 7.63 (d, J = 7.2 Hz, 2H), 7.47 (dd, J = 14.9 Hz, J = 10.9 Hz, 1H), 7.10 (d, J = 14.1 Hz, 1H), 7.00 (d, J = 4.2 Hz, 1H), 6.31 (d, J = 14.9 Hz, 1H), 6.30 (dd, J = 14.1 Hz, J = 10.9 Hz, 1H), 5.80 (d, J = 4.2 Hz, 1H), 4.35 (s, 3H), 3.30 (m, 4H), 1.63 (m, 4H), 1.33 (m, 12H), 0.91 (m, 6H). **HRMS** (LSIMS): [C⁺] m/z theo. for C₂₆H₃₉N₂S: 411.2834, exp.: 411.2831. **EA**: % theo. for C₂₆H₃₉IN₂S : C, 57.98; H, 7.30; N, 5.20, % exp.: C, 57.67; H, 7.39; N, 4.93.

C3

NMR ¹**H** (300.13 MHz, CDCl₃): $\delta = 8.73$ (d, J = 6.8 Hz, 2H), 7.69 (dd, J = 15.1 Hz, J = 11.4Hz, 1H), 6.88-6.80 (m, 3H), 6.85 (d, J = 4.1 Hz, 1H), 6.41-6.22 (m, 4H), 4.40 (s, 3H), 3.27 (m, 4H), 1.65 (m, 4H), 1.32 (m, 12H), 0.91 (6H). NMR 13C (75.47 MHz, CDCl₃): $\delta = 160.5, 153.4, 145.5, 144.0, 143.7, 134.1, 132.9, 126.7, 124.7, 122.3, 121.5, 120.7, 102.0, 53.7, 47.6, 31.5, 27.1, 26.7, 22.6, 14.0.$ **HRMS**(LSIMS): [C⁺] <math>m/z theo. for C₂₈H₄₁N₂S : 437.2991, exp.: 437.2986. **EA**: % theo. for C₂₈H₄₁IN₂S: C, 59.56; H, 7.32; N, 4.96, % exp.: C, 59.3; H, 7.35; N, 4.79.

C4

NMR ¹**H** (300.13 MHz, CDCl₃): $\delta = 8.78$ (d, J = 4.5 Hz, 2H), 7.73 (d, J = 4.5 Hz, 2H), 7.46 (m, 1H), 6.78-6.32 (m, 8H), 5.70 (m, 1H), 4.43 (s, 3H), 3.25 (m, 4H), 1.60 (m, 4H), 1.32 (m, 12H), 0.91 (m, 6H). **HRMS** (LSIMS): [C⁺] m/z theo. for C₃₀H₄₃N₂S : 463.3147, exp.: 463.3142.

D1

NMR ¹**H** (200.13 MHz, CDCl₃): $\delta = 9.25$ (d, J = 6.9 Hz, 1H), 8.38 (d, J = 8.3 Hz, 1H), 8.12 (d, J = 14.5 Hz, 1H), 7.95-7.86 (m, 2H), 7.92 (d, J = 6.9 Hz, 1H), 7.73 (m, 1H), 7.48

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(d, J = 4.4 Hz, 1H), 6.87 (d, J = 14.5 Hz, 1H), 6.05 (d, J = 4.4 Hz, 1H), 4.40 (s, 3H), 3.42 (m, 4H), 1.66 (m, 4H), 1.34 (m, 12H), 0.93 (m, 6H). **HRMS** (LSIMS): [C⁺] m/z theo. for C₂₈H₃₉N₂S : 435.2834, exp.: 435.2841.

D2

NMR ¹**H** (200.13 MHz, CDCl₃): $\delta = 9.49$ (d, J = 7.2 Hz, 1H), 8.38 (d, 8.3 Hz, 1H), 7.98 (d, J = 7.2 Hz, 1H), 7.94 (m, 2H), 7.78 (m, 2H), 7.11 (d, J = 4.6 Hz, 1H), 7.08 (m, 2H), 6.52 (m, 1H), 5.91 (d, J = 4.6 Hz, 1H), 4.48 (s, 3H), 3.36 (t, 4H), 1.62 (m, 4H), 1.34 (m, 12 H), 0.92 (m, 6H). **HRMS** (LSIMS): [C⁺] m/z theo. for C₃₀H₄₁N₂S: 461.2991, exp.: 461.2992. **D3**

NMR ¹**H** (300.13 MHz, CDCl₃): $\delta = 9.61$ (d, J = 6.8 Hz, 1H), 8.40 (d, J = 8.3 Hz, 1H), 8.02 (m, 2H), 7.83 (m, 2H), 7.70 (m, 1H), 7.10 (d, J = 14.9Hz, 1H), 6.90 (m, 3H), 6.53 (dd, J = 14.1Hz, J = 11.2 Hz, 1H), 6.30 (dd, J = 14.1Hz, J = 11.2 Hz, 1H), 5.80 (6.53 (d, J = 4.0Hz, 1H), 4.55 (s, 3H), 3.32 (m, 4H), 1.52 (m, 4H), 1.40 (m, 12H), 0.92 (m, 6H). **HRMS** (ESI): [C⁺] m/z theo. for C₃₂H₄₃N₂S: 487.31415, exp.: 487.31239.

D4

NMR ¹**H** (300.13 MHz, CDCl₃): $\delta = 9.69$ (d, J = 6.6Hz, 1H), 8.38 (d, J = 8.3 Hz, 1H), 8.00 (m, 3H), 7.80 (d, J = 4.8 Hz, 1H), 7.60 (dd, J = 14.1Hz, J = 11.2 Hz, 1H), 7.16 (m, 3H), 6.87 (d, J = 3.9 Hz, 1H), 6.62 (m, 4H), 5.65 (d, J = 3.9Hz, 1H), 4.50 (s, 3H), 3.23 (m, 4H), 1.62 (m, 4H), 1.34 (m, 12H), 0.93 (m, 6H). **HRMS** (ESI): [C⁺] m/z theo. for C₃₄H₄₅N₂S: 513.32980, exp.: 513.32818. **EA**: % theo. for C₃₄H₄₅IN₂S: C, 61.15; H, 7.24; N, 4.19; S, 4.80, % exp.: C, 61.23; H, 6.88; N, 4.52; S, 4.91

D5

NMR ¹**H** (600 MHz, DMSO-d6): $\delta = 9.15$ (d, J=6.5Hz, 1H), 8.77 (d, J=8.4Hz, 1H), 8.36 (d, J=8.8Hz, 1H), 8.30 (s, 1H), 8.20 (m, 1H), 8.21 (m, 3H), 7.72 (d, J=14.2Hz, 1H), 6.97 (m, 1H), 6.84 (s, 1H), 6.77 (m, 2H), 6.59 (m, 1H), 6.50 (m, 1H), 6.40 (m, 1H), 6.23 (m, 1H), 5.79 (s, 1H), 4.46 (s, 3H), 3.32 (m, 4H), 1.56 (m, 4H), 1.28 (m, 12H), 0.87 (m, 6H). **HRMS** (ESI): [C⁺] m/z theo. for C₃₆H₄₇N₂S: 539.34545, exp.: 539.34368.

2 Definition of the geometrical parameters

2.1 Bond length alternation

The bond length alternation (BLA) along the conjugated polyenic bridge connecting the donor and acceptor units is calculated as:

$$BLA = \frac{1}{N-2} \sum_{i=1}^{N-2} (-1)^{i+1} (d_{i+1,i+2} - d_{i,i+1})$$
(1)

where N is the total number of carbon atoms in the π -conjugated chain and $d_{i,j}$ is the interatomic distance between carbons i and j. According to the 2-state resonance picture schematized in Figure S1 for **D3**, a negative (positive) value of the BLA calculated along the C₁-C₈ chain indicates that the ground-state electronic structure is dominated by structure 1 (2). A value equal to zero indicates that the two resonance forms equivalently contribute to the ground state.



Figure S1: Resonance structures of **D3** and labels of atoms (1-8) used to calculate the bond length alternation.

2.2 Torsional angles

Angle	atoms
θ_1	$S-C-N-C_{But}$
θ_2	a-1-2-3
$ heta_3$	6-7-8-S
$ heta_4$	1 - 2 - 3 - 4
$ heta_5$	5-6-7-8
$ heta_6$	2 - 3 - 4 - 5
θ_7	4-5-6-7
$ heta_8$	3-4-5-6

Table S1: Definition of the dihedral angles θ_1 - θ_8 schematized in Figure S2b. See Figure S1 for atom labels.

3 Derivation of an optimal force field for the D3 dye

3.1 Iterative parameterization of bond lengths and torsional potentials

At the DFT level, the BLA along the polyenic bridge amounts to -0.043 Å while the original GAFF (Generalized Amber Force Field) relaxed geometry yields a value of -0.054 Å due to the limited number of atom types used (ca and c2). Besides, the planarity of the DFT structure is not well reproduced, with out-of-plane deviations of up to 14°. These discrepancies in the molecular structure with respect to DFT expectedly translate into poor estimations of the first hyperpolarizability, namely $\beta_{tot}(\text{GAFF}) = 2.269 \ 10^5$ a.u. against 1.924 10^5 a.u. with the reference DFT geometry.

To achieve a more accurate description of the molecular geometry, we derived new parameters for both bonds and torsional potentials using a simplified structure of the **D3** molecule, in which butyl chains were removed from the chromophore and replaced by methyl groups (Figure S2). Practically, several new atom types were added to the original GAFF (Figure S2a) to properly reproduce the bond lengths and thus, the BLA. The torsional potentials around the dihedral angles θ_1 - θ_5 were fitted on relaxed potential energy scans performed at the M06-2X/6-311G(d) level in the gas phase (Figure S3). The FF potentials are freeenergy profiles obtained using the adapting biasing force (ABF) method considering the chromophore inside a box with 40 Ar atoms at the temperature of 298.15 K. Note that the torsional potentials around the θ_6 - θ_8 angles were described using standard GAFF in all MD simulations. Parameters for bonds and torsions were derived iteratively and converged values were used as starting point to describe the whole **D3** molecule, including butyl chains. A final refinement of the bonds was done so as to reproduce accurately the DFT geometry of the whole system and proper description of the dihedrals was checked.



Figure S2: Geometry of the fragment employed in the optimization of the AMBER force field. (a) Atom types defined in the modified GAFF, (b) The reparameterized dihedrals are θ_{1-5} . The torsional potentials around θ_6 - θ_8 (in blue) were not reparameterized.



Figure S3: Relaxed potential energy scans calculated at the M06-2X/6-311G(d) level (red) and force field fitted potentials (blue) for the **D3** dye.

3.2 Assessment of the quality of the modified force field

In order to assess the quality of the reparameterized force field, the geometry of the **D3** molecule was optimized using molecular mechanics (MM) with the original and systemspecific derived force fields and compared to the geometry optimized using the reference DFT level. Results gathered in Table S3 show that MM calculations using the reparameterized GAFF reproduce well the BLA along the π -conjugated bridge, while they give rise to a slightly less planar structure compared to DFT, with differences in the θ_2 and θ_5 dihedrals of the order of 10°. Note that the deviation from planarity resulting from the MM optimization is canceled out by the subsequent MD simulations, which predict a strictly planar average structure (Table S4).

Table S2: Values of the bond distances d_{ij} and BLA (Å), and of dihedrals (degrees) optimized at the DFT and MM levels with the original and reparameterized GAFF for the **D3** chromophore. Absolute differences with DFT values are also reported.

Parameters	DFT	MM (GAFF rep.)	Diff.	MM (GAFF orig.)	Diff.
d_{12}	1.424	1.423	-0.001	1.506	0.082
d_{23}	1.372	1.373	0.001	1.334	-0.038
d_{34}	1.411	1.411	0.000	1.332	-0.079
d_{45}	1.372	1.374	0.002	1.330	-0.042
d_{56}	1.412	1.411	-0.001	1.331	-0.081
d_{67}	1.370	1.371	0.001	1.333	-0.036
d_{78}	1.415	1.416	0.001	1.490	0.075
BLA	-0.043	-0.041	0.002	-0.054	-0.011
$ heta_1$	1.4	4.6	3.3	-4.6	3.2
$ heta_2$	2.8	14.0	11.2	16.9	14.1
$ heta_3$	-178.9	-176.8	2.0	-179.9	1.1
$ heta_4$	-179.3	179.7	0.4	179.8	0.6
$ heta_5$	179.9	171.8	8.0	180.0	0.1
$ heta_6$	-179.3	-179.3	0.1	-179.3	0.0
$ heta_7$	179.8	179.0	0.8	179.9	0.1
$ heta_8$	179.9	179.4	0.5	179.9	0.0

To assess the impact of the geometry mismatches on the NLO responses, β_{tot} has been computed at the IEF-PCM/M06-2X/6-311+G(d) level by using both the DFT and MM geometries (Table S3). Using the MM structure optimized with the original GAFF provides a β_{tot} value overestimated by more than 15%, while the overestimation is reduced to about 7% with the reparameterized force field. Note that fixing all dihedral angles to their DFToptimized values only slightly reduces the overestimation of β_{\parallel} , indicating that the difference can only be partly ascribed to the deviation from planarity of the MM geometry.

Table S3: Static β_{tot} values (a.u.) calculated at the IEF-PCM/M06-2X/6-311+G(d) level in chloroform using the DFT and MM geometries, and using the MM geometry while fixing all dihedral angles listed in Table S2 to their DFT-optimized values. Deviations (in %) with respect to values computed using the DFT geometry are listed in the last column.

Geometry	$\beta_{tot}(0;0,0)$	% wrt DFT
DFT	1.92E + 05	-
MM (GAFF original)	2.27E + 05	15.2
MM (GAFF reparameterized)	2.08E + 05	7.3
MM (GAFF rep. + DFT dihedrals)	2.05E + 05	6.0

3.3 Assessment of the quality of the force field used for chloroform

The quality of the solvent description using standard GAFF parameters and DFT-derived charges has been verified by comparing the calculated mass density with the experimental one (1.468 g/cm⁻³). For this purpose we performed an NpT simulation on 1600 chloroform molecules at 1 atm and 298.15 K obtaining a density of 1.415 g/cm⁻³.

4 MD simulations on the D3/iodide complex

4.1 Probability distributions of geometrical parameters

The distributions of different geometrical parameters characterizing the **D3**/iodide complex have been calculated for the 20000 frames extracted from each NVT simulation starting at two different initial values of the dihedral θ_3 , *i.e.* for 40000 geometrical structures. Namely, the distributions of i) the dihedral angles θ_i along the π -conjugated linker, ii) the average bond length alternation (BLA), iii) the average distance (d_{NI}) between the counterion I⁻ and the nitrogen of the quinolinium group and iv) the dihedral angle θ_{PhI} between the terminal phenyl and the anion are reported in Figures S4, S5, S7, S8 and S9, respectively. They are compared to the distributions obtained using the 400 geometries used for computing the NLO properties. The average values of the geometrical parameters, extracted from the full and reduced sets of structures, are reported in Table S4. The correlation of the results show that the 400 snapshots selected for calculating the NLO properties are representative of the

dynamics of the system.

Table S4: Values of geometrical parameters of the **D3**/iodide complex (BLA and d_{NI} in Å, and dihedral angles θ_i in degrees) averaged over 40000 structures and over the 400 snapshots selected for calculation of the NLO properties.

Property	MD (40000 snapshots)	MD (400 snapshots)
BLA	-0.042 ± 0.022	-0.045 ± 0.023
dyr	456 ± 0.48	457 ± 0.020
θ_{I}	-0.4 ± 14.1	0.4 + 12.9
θ_1	-0.4 ± 14.1	0.4 ± 12.5 0.7 ± 14.6
θ_2	0.0 ± 14.1 180 1 \pm 11 1	-0.7 ± 14.0 180 1 \pm 10 1
$\theta_3 (\sin 1)$	100.1 ± 11.1	100.1 ± 10.1 0.2 \pm 10.5
$\theta_3 (\text{SIII } 2)$	0.0 ± 9.4	-0.3 ± 10.3
θ_4	180.0 ± 8.9	100.4 ± 0.0
θ_5	180.0 ± 10.2	$1/9.4 \pm 10.5$
θ_6	180.0 ± 6.3	180.3 ± 6.5
θ_7	180.0 ± 6.1	179.9 ± 6.1
θ_8	180.0 ± 6.4	180.2 ± 6.3
θ_{PhI}	177.5 ± 39.3	175.1 ± 45.9



Figure S4: Potential energy curves associated to the rotation of the dihedrals θ_1 , θ_2 and θ_3 in **D3** (left), and probability distributions of θ_1 , θ_2 and θ_3 in the **D3**/iodide complex obtained using 40000 structures (middle) and the selected 400 structural snapshots (right) extracted from the MD trajectories. The two colors in the distributions of θ_3 (plots (h) and (i)) correspond to two different trajectories starting from $\theta_3 = 0^\circ$ (purple) and $\theta_3 = 180^\circ$ (blue).



Figure S5: Potential energy curves associated to the rotation of the dihedrals θ_4 and θ_5 in **D3** (left), and probability distributions of θ_4 and θ_5 in the **D3**/iodide complex obtained using 40000 structures (middle) and the selected 400 structural snapshots (right) extracted from the MD trajectories.



Figure S6: Probability distributions associated to the rotation around the internal dihedrals θ_6 , θ_7 and θ_8 of **D3** in the **D3**/iodide complex.



Figure S7: Probability distributions of the BLA along the conjugated bridge of D3 in the D3/iodide complex, obtained using 40000 structures (left) and the selected 400 structural snapshots (right) extracted from the MD trajectories.



Figure S8: Probability distributions of the distances between the nitrogen of the quinolinium group and the iodine atom in the $\mathbf{D3}$ /iodide complex, obtained using 40000 structures (left) and the selected 400 structural snapshots (right) extracted from the MD trajectories.



Figure S9: Probability distributions of the dihedral angle $\theta_{PhI} = (\text{I-b-N-c})$ (see Figure S1 for atom labels) in the **D3**/iodide complex, obtained using 40000 structures (left) and the selected 400 structural snapshots (right) extracted from the MD trajectories.

4.2 Time evolution of the EFISH properties over the MD trajec-



Figure S10: Time evolution along the MD trajectories of the EFISH properties of the **D3**/iodide complex.

tories

4.3 Structure - NLO properties relationships



Figure S11: Evolution of the θ angle (degrees) between the $\vec{\mu}$ and $\vec{\beta}$ vectors with respect to the bond length alternation (Å) in the **D3**/iodide complex.



Figure S12: Evolution of β_{tot} values (in 10⁴ a.u.) calculated for the **D3**/iodide complex with respect to those calculated for the same geometries of the **D3** chromophore only (after removing the anion).



Figure S13: Evolution of the optical quantities with respect to the θ angle (degrees) between the $\vec{\mu}$ and $\vec{\beta}$ vectors in the **D3**/iodide complex: (a) dipole moment (a.u.), (b) isotropic polarizability (α_{iso} , a.u.), β_{\parallel} (10⁴ a.u.), β_{tot} (10⁴ a.u.), and γ_{\parallel} (10⁷ a.u.).



Figure S14: Evolution of the optical quantities with respect to the bond length alternation (Å) in the **D3**/iodide complex: (a) dipole moment (a.u.), (b) isotropic polarizability (α_{iso} , a.u.), $\beta_{||}$ (10⁴ a.u.), β_{tot} (10⁴ a.u.), and $\gamma_{||}$ (10⁷ a.u.).

5 Assessment of the DFT approximation for computing NLO properties

5.1 Performance of M06-2X with respect to MP2

To assess the reliability of the selected exchange-correlation functional, the static first hyperpolarizabilities β_{tot} of compounds of series **D** were calculated at the M06-2X/6-311+G(d) level (in vacuum) and compared to MP2 calculations carried out with the same basis set. As shown in Figure S15, the very good correlation observed for the two sets of values validates the suitability of the M06-2X exchange-correlation functional for the series of investigated systems.



Figure S15: Comparison of static first hyperpolarizabilities ($\beta = \beta_{tot}$, in a.u.) of compounds of series **D**, computed at the M06-2X and MP2 levels using the 6-311+G(d) basis set. The geometries of the compounds have been optimized at the IEF-PCM/M06-2X/6-311+G(d) level.

5.2 Impact of the basis set

Three basis sets of increasing size (6-311+G(d), aug-cc-pVDZ and aug-cc-pVTZ) have been tested for molecules of series **D**, by calculating their static first hyperpolarizabilities at the

M06-2X level. The results displayed in Figure S16 show that the two smaller basis sets (6-311+G(d) and aug-cc-pVDZ) provide similar results to the ones obtained using aug-cc-pVTZ, validating the choice of 6-311+G(d) for the calculation of the NLO properties of the dyes.



Figure S16: Comparison of static first hyperpolarizabilities ($\beta = \beta_{tot}$, in a.u.) of compounds **D1-D4**, calculated at the TD-DFT/M06-2X level using different basis sets. The geometries of the compounds have been optimized at the IEF-PCM/M06-2X/6-311+G(d) level.

Three basis set used for describing the iodide counterion were also evaluated, by calculating the static first hyperpolarizability of the **D3**/iodide complex. In these tests the 6-311+G(d) basis set was used for the dye. The results collected in Table S5 show that varying the basis set for iodine atom does not impact significantly the values of β .

Table S5: Static first hyperpolarizabilities (β_{tot} , in 10⁴ a.u.) of the **D3**/iodide complex as a function of the basis set used for describing the iodide anion (by using geometries optimized at the IEF-PCM/M06-2X/6-311+G(d) level). These computations have been performed on 24 cpus on a Xeon node with 64 Gb of RAM. The total number N_{basis} of basis functions and the computation time (min) are also provided.

Dye basis	Iodine basis	β_{tot}	N_{basis}	Time
6-311+G(d)	6-311G(d)	16.1	857	18
6-311+G(d)	aug-cc-pvdz(PP)	16.1	827	18
6-311+G(d)	aug-cc-pvtz(PP)	16.1	850	32

6 Optimized structures of the dye/iodide complexes



Figure S17: Optimized structures of the dye/iodide complexes for dyes of series **A** with the orientation of the (normalized) $\vec{\mu}$ (red) and $\vec{\beta}$ (blue) vectors.





(e) n = 5

Figure S18: Optimized structures of the dye/iodide complexes for dyes of series **B** with the orientation of the (normalized) $\vec{\mu}$ (red) and $\vec{\beta}$ (blue) vectors.



Figure S19: Optimized structures of the dye/iodide complexes for dyes of series **C** with the orientation of the (normalized) $\vec{\mu}$ (red) and $\vec{\beta}$ (blue) vectors.



(c) n = 3 (d) n = 4

(e) n = 5

Figure S20: Optimized structures of the dye/iodide complexes for dyes of series **D** with the orientation of the (normalized) $\vec{\mu}$ (red) and $\vec{\beta}$ (blue) vectors.

7 Correlation between hyperpolarizabilities and aromaticity indices in dye/iodide complexes

Table S6: Bond order alternation (BOA) and aromaticity indices (FLU and AV_{\min}) computed along the conjugated linker between donors and acceptors. Atoms included in the calculation of the indices are reported in Figure S21.

Molecule	BOA	FLU	AV_{\min}
A1	0.4706	0.0312	
$\mathbf{A2}$	0.4383	0.0273	1.7750
$\mathbf{A3}$	0.4341	0.0264	1.5480
$\mathbf{A4}$	0.4370	0.0263	1.4550
$\mathbf{A5}$	0.4388	0.0263	1.4010
B1	0.4705	0.0314	
$\mathbf{B2}$	0.4293	0.0264	1.8110
B3	0.4299	0.0260	1.5530
$\mathbf{B4}$	0.4292	0.0256	1.4680
$\mathbf{B5}$	0.4368	0.0261	1.3970
$\mathbf{C1}$	0.3416	0.0174	
$\mathbf{C2}$	0.3537	0.0180	2.6400
C3	0.3747	0.0195	2.2400
$\mathbf{C4}$	0.3935	0.0211	2.0430
$\mathbf{C5}$	0.4080	0.0223	1.9050
D1	0.2814	0.0126	
D2	0.3092	0.0142	2.8660
D3	0.3400	0.0164	2.3880
$\mathbf{D4}$	0.3757	0.0193	2.1090
$\mathbf{D5}$	0.3920	0.0207	1.9540



Figure S21: Atoms included in the calculation of indices reported in Table S6.

Table S7: Aromaticity indices (MCI, I_{ring} , FLU, and AV_{min}) within the phenyl ring (in series **A** and **B**) and thienyl ring (in series **C** and **D**). Atoms included in the calculation of the indices are reported in Figure S22. The values of the same indicators for the benzene and thiophene molecules optimized at the same level of theory are reported for comparison.

Molecule	MCI	I _{ring}	FLU	AV_{\min}
A1	0.0431	0.0305	0.0071	4.9180
A2	0.0445	0.0314	0.0064	5.2800
$\mathbf{A3}$	0.0458	0.0321	0.0058	5.5970
$\mathbf{A4}$	0.0467	0.0327	0.0054	5.8220
$\mathbf{A5}$	0.0472	0.0329	0.0052	5.9390
B1	0.0431	0.0306	0.0071	4.9190
B2	0.0444	0.0313	0.0065	5.2360
B3	0.0458	0.0322	0.0059	5.5890
B4	0.0466	0.0326	0.0055	5.7810
$\mathbf{B5}$	0.0473	0.0330	0.0052	5.9700
$\mathbf{C1}$	0.0187	0.0172	0.0068	
C2	0.0191	0.0174	0.0067	
C3	0.0194	0.0175	0.0068	
$\mathbf{C4}$	0.0196	0.0175	0.0070	
C5	0.0198	0.0175	0.0072	
D1	0.0179	0.0169	0.0072	
D2	0.0186	0.0172	0.0068	
D3	0.0191	0.0174	0.0068	
D4	0.0195	0.0175	0.0070	
D5	0.0197	0.0175	0.0072	
Benzene	0.0744	0.0494	0.0000	10.9270
Thiophene	0.0393	0.0302	0.0095	



Figure S22: Atoms included in the calculation of indices reported in Table S7.

Table S8: Bond length alternation (BLA), Bond order alternation (BOA) and aromaticity indices (FLU and AV_{\min}) computed along the conjugated path going from the amine nitrogen to the first carbon of the pyridinium (series **A** and **B**) or quinolinium (series **C** and **D**). Atoms included in the calculation of the indices are reported in Figure S23.

Molecule	BLA	BOA	FLU	AV_{\min}
A1	-0.0189	0.1021	0.0180	1.1390
A2	-0.0359	0.2109	0.0187	0.9960
$\mathbf{A3}$	-0.0467	0.2587	0.0197	0.9350
$\mathbf{A4}$	-0.0545	0.2930	0.0206	0.8500
$\mathbf{A5}$	-0.0600	0.3190	0.0212	0.8460
B1	-0.0206	0.1463	0.0176	1.2500
$\mathbf{B2}$	-0.0372	0.2190	0.0177	1.0760
B3	-0.0484	0.2675	0.0190	0.9320
B4	-0.0550	0.2967	0.0197	0.8530
B5	-0.0610	0.3233	0.0209	0.7790
C1	-0.0219	0.1735	0.0085	1.3430
C2	-0.0379	0.2373	0.0109	1.1500
C3	-0.0493	0.2844	0.0133	0.9850
C4	-0.0575	0.3192	0.0154	0.8530
C5	-0.0634	0.3444	0.0172	0.7570
D1	-0.0132	0.1304	0.0065	1.5100
D2	-0.0311	0.2035	0.0087	1.2740
D3	-0.0438	0.2572	0.0112	1.0780
D4	-0.0547	0.3053	0.0142	0.8930
D5	-0.0609	0.3317	0.0160	0.7880



Figure S23: Atoms included in the calculation of indices reported in Table S8



Figure S24: Evolution of $\beta_{||}$ (10⁴ a.u.) and $\gamma_{||}$ (10⁶ a.u.) as a function of the BLA computed along the conjugated path going from the amine nitrogen to the first carbon of the pyridinium (series **A** and **B**) or quinolinium (series **C** and **D**). Atoms included in the calculation of the indices are reported in Figure S23.



Figure S25: Evolution of $\beta_{||}$ (10⁴ a.u.) and $\gamma_{||}$ (10⁶ a.u.) as a function of the BOA computed along the polyenic bridge. Atoms included in the calculation of the indices are reported in Figure S23.



Figure S26: Evolution of β_{\parallel} (10⁴ a.u.) and γ_{\parallel} (10⁶ a.u.) as a function of the FLU computed along the conjugated path going from the amine nitrogen to the first carbon of the pyridinium (series **A** and **B**) or quinolinium (series **C** and **D**). Atoms included in the calculation of the indices are reported in Figure S23.



Figure S27: Evolution of β_{\parallel} (10⁴ a.u.) and γ_{\parallel} (10⁶ a.u.) as a function of the AV_{\min} computed along the conjugated path going from the amine nitrogen to the first carbon of the pyridinium (series **A** and **B**) or quinolinium (series **C** and **D**). Atoms included in the calculation of the indices are reported in Figure S23.

8 Aromaticity and conjugation measures

The present section will briefly review the conjugation and aromaticity indices used in the manuscript. The latter have been adapted to study the conjugated chains in series **A-B** and **C-D**. From now on, we will use the abbreviated notation $\mathbf{1} \equiv (\vec{r_1}, \sigma_1)$ to represent the coordinates of an electron, and $d\mathbf{1} \equiv d\vec{r_1}, d\sigma_1$ to represent the electron positions and their derivatives. In order to provide a general expression, we will consider a molecule that includes at least one ring structure composed of n atoms, which is represented by the sequence $\mathcal{A} = \{A_1, A_2, \ldots, A_n\}$. The elements of this sequence are ordered in accordance with the convention that the first atom in the sequence, A_1 , is adjacent to the last atom, A_n , forming a ring.

Apart from the bond-length alternation (BLA), in this work, we have considered another *geometric* measure of conjugation, the harmonic oscillator model of aromaticity (HOMA), S2 defined as

$$HOMA(\mathcal{A}) = 1 - \frac{1}{n-1} \sum_{i}^{n-1} \alpha_i (R_{opt} - r_{A_i, A_{i+1}})^2,$$
(2)

where $r_{A,B}$ is the distance between atoms A and B, and α_i is an empirical constant optimized to give values close to one for aromatic species and small or negative values for non-aromatic and antiaromatic species. The geometrical data of reference (R_{opt}) is such that the compression energy of the double bond and the expansion energy of the single bond is minimal in accordance with the harmonic potential model. Although originally defined for rings, ^{S2,S3} HOMA can be easily adapted to open fragments, as we did in Eq. 2.

The other measures considered in the manuscript are based on the electron delocalization between atoms. In order to define these measures, we rely on two indices defined in the framework of the quantum theory of atoms-in-molecules (QTAIM).^{S4} The delocalization index (DI)^{S5–S7} measures the number of electrons fluctuating concurrently between two atoms A_1 and A_2 , and is defined as

$$\delta(A_1, A_2) = 2 \int_{A_1} \int_{A_2} d\mathbf{1} d\mathbf{2} \rho_{xc}(\mathbf{1}, \mathbf{2}) = -2cov(N_{A_1}, N_{A_2}), \tag{3}$$

where N_{A_1} and N_{A_2} are the atomic populations and $\rho_{xc}(\mathbf{1}, \mathbf{2})$ is the exchange–correlation density (XCD). The localization index (LI) is defined as

$$\lambda(A) = \int_{A} \int_{A} d\mathbf{1} d\mathbf{2} \rho_{xc}(\mathbf{1}, \mathbf{2}), \qquad (4)$$

where we integrate the two points of the XCD over the same atom A.

The bond-order alternation (BOA)^{S8} measures the electron delocalization difference between consecutive atoms and it is defined after BLA, but replacing bond lengths by bond orders (in this case, we use the DIs):

$$BOA(\mathcal{A}) = \frac{1}{N-2} \sum_{i=1}^{N-2} (-1)^{i+1} [\delta(A_{i+1}, A_{i+2}) - \delta(A_i, A_{i+1})]$$
(5)

The aromatic fluctuation index (FLU) is the counterpart to HOMA and measures electron delocalization differences with respect to some aromatic references. In the present case it is defined as

$$FLU(\mathcal{A}) = \frac{1}{n} \sum_{i=1}^{n} \left[\left(\frac{\delta(A_i)}{\delta(A_i - 1)} \right)^{\alpha} \left(\frac{\delta(A_i, A_{i-1}) - \delta_{ref}(A_i, A_{i-1})}{\delta_{ref}(A_i, A_{i-1})} \right) \right]^2, \tag{6}$$

where α ensures the first term is always greater or equal to 1,

$$\alpha \begin{cases}
1 & \delta(A_{i-1}) \leq \delta(A_i) \\
-1 & \delta(A_i) < \delta(A_{i-1})
\end{cases}$$
(7)

and $\delta_{ref}(A, B)$ is the DI of an aromatic molecule of reference. Benzene is used as a reference

for C-C bonds, the C-N value is taken from pyridine, and the C-S value is taken from thiophene.^{S9} When the molecule is aromatic, the FLU index will be close to zero, whereas for non-aromatic or antiaromatic species, it will be greater than zero. Aromaticity indicators based on bond orders, such as BLA or FLU, do not strongly depend on the computational method used.^{S10}

Giambiagi employed one of the most reliable electronic multicenter indices as an aromaticity index. I_{ring} measures the delocalization along the ring:^{S11}

$$I_{ring}(\mathcal{A}) = \sum_{i_1 i_2 \dots i_n}^{occ} S_{i_1 i_2}(A_1) S_{i_2 i_3}(A_2) \dots S_{i_n, i_1}(A_n),$$
(8)

where $S_{ij}(A)$ stands for the overlaps of molecular orbitals *i* and *j* in the molecular region occupied by atom *A*. If one takes into account all the permutations of the atoms in the ring, including delocalization patterns across the ring, we obtain the expression of the multicenter index (MCI):^{S12}

$$MCI(\mathcal{A}) = \frac{1}{2n} \sum_{\mathcal{P}(\mathcal{A})} I_{ring}(\mathcal{A}) = \frac{1}{2n} \sum_{\mathcal{P}(\mathcal{A})} \sum_{i_1 i_2 \dots i_n} S_{i_1 i_2}(A_1) S_{i_2 i_3}(A_2) \dots S_{i_n, i_1}(A_n)$$
(9)

where $\mathcal{P}(\mathcal{A})$ stands for the *n*! permutations of the elements in the string \mathcal{A} . Like I_{ring} , MCI gives large numbers for aromatic species, and the authors claim negative values for antiaromatic molecules.^{S13} However, these two electronic indices are not suitable for large (anti)aromatic molecules because they scale exponentially with the number of atoms in the ring and present large numerical errors derived from the numerical integration of the atomic overlap matrices.

In order to solve the drawbacks of I_{ring} and MCI, we have defined the AV1245 index^{S14} as the average value of the four-atom MCI index between relative positions 1-2 and 4-5 constructed from every five consecutive atoms along the perimeter of the ring. Lately,^{S15,S16} it has been seen that the average value could hinder some important values and that the minimal value of the index, AV_{\min} , could be more appropriate. The AV_{\min} value corresponds to the least delocalized fragment of the ring. Aromatic molecules (and conjugated fragments) present large values of AV_{\min} , while non-aromatic molecules (and non-conjugated fragments) exhibit low values.

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