

Supporting Information:

Phase equilibria of symmetric Lennard-Jones mixtures and a look at the transport properties near the upper critical solution temperature

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1 Technical details of molecular simulations

1.1 Simulation details

All molecular simulations were carried out with the tool *ms2*.^{S1–S4} Assuming a cubic volume with periodic boundary conditions that contains between 1000 and 20,000 molecules, the intermolecular interactions were evaluated explicitly within a cutoff radius of 4σ , applying analytical long-range corrections.^{S5} In case of molecular dynamics (MD) simulation, Newton's equations of motion were solved with a fifth-order Gear predictor-corrector numerical integrator and an integration time step of $\Delta t^* = 0.9$ to $2.7 \cdot 10^{-3}$.

1.2 LLE and vapor phase simulations

LLE and vapor phase simulations were carried out using Monte Carlo (MC) simulations in the isobaric-isothermal (NpT) ensemble containing 1000 to 4000 molecules, with an average of $8 \cdot 10^5$ production cycles. The chemical potential was sampled with Widom's insertion method,^{S6} using 3000 test particles per cycle.

1.3 VLE simulations

VLE simulations were conducted in two subsequent steps: (1) liquid run and (2) vapor run, following the grand equilibrium method by Vrabec and Hasse^{S7}. The liquid run was carried out with MD simulation in the NpT ensemble, followed by the vapor run using MC simulation in the pseudo-grand canonical (μVT) ensemble. Both phases consisted of 1372 molecules and were sampled for $8 \cdot 10^5$ production steps.

1.4 Transport property simulations

Transport property simulations were performed in two consecutive steps: (1) MC simulation in the NpT ensemble to obtain the density and (2) MD simulation in the canonic (NVT) ensemble to obtain the diffusion coefficients, shear viscosity and thermal conductivity, as well as the thermodynamic factor through Kirkwood-Buff integrals (KBI).^{S8} Simulations in the NVT ensemble were first equilibrated over $1.5 \cdot 10^5$ time steps, followed by a production run of $5 \cdot 10^6$ time steps. To account for finite size effects, up to four system sizes were investigated containing 2500, 5000, 10,000 and 20,000 molecules, respectively.

2 Equilibrium properties

2.1 Helmholtz energy derivatives

The molar Helmholtz energy $a = F/N$ can be used to determine all thermodynamic equilibrium properties, such as the isochoric heat capacity c_v , speed of sound w or the Joule-Thomson coefficient μ_{JT} . It also serves as the basis for the development of EOS.^{S9} The formalism for the calculation of thermodynamic properties from Helmholtz energy-based EOS is described in detail in Refs. S10, S11. The partial derivatives of the reduced Helmholtz energy $\alpha = a/(k_B T)$ can be expressed as

$$\mathcal{A}_{mn} = \mathcal{A}_{mn}^o + \mathcal{A}_{mn}^r = \tau^m \rho^n \frac{\partial^{m+n} (\alpha^o + \alpha^r)}{\partial \tau^m \partial \rho^n}, \quad (1)$$

where m and n denote the order of derivation with respect to $\tau = 1/T$ and ρ . The reduced Helmholtz energy derivatives are usually split into an ideal gas \mathcal{A}_{mn}^o and a residual \mathcal{A}_{mn}^r contribution. Direct sampling of the latter is implemented in *ms2* and allows to extend this study to further properties near the critical solution point.

$$\text{Reduced ideal gas Helmholtz energy : } \mathcal{A}_{00}^o = \ln \rho + 1.5 \ln \tau + c_1 \tau + c_2. \quad (2)$$

$$\text{Reduced residual Helmholtz energy : } \mathcal{A}_{00}^r = \frac{\sum x_i \mu_i^r}{RT} - \mathcal{A}_{01}^r. \quad (3)$$

2.2 Thermodynamic factor

The thermodynamic factor is a key component for the description of both phase equilibria and mass transport properties. It can be used to identify the composition where phase stability ceases to exist ($\Gamma = 0$) and allows to determine the critical solution point, as demonstrated in this work. Moreover, it is also relevant for diffusive mass transport processes, since it

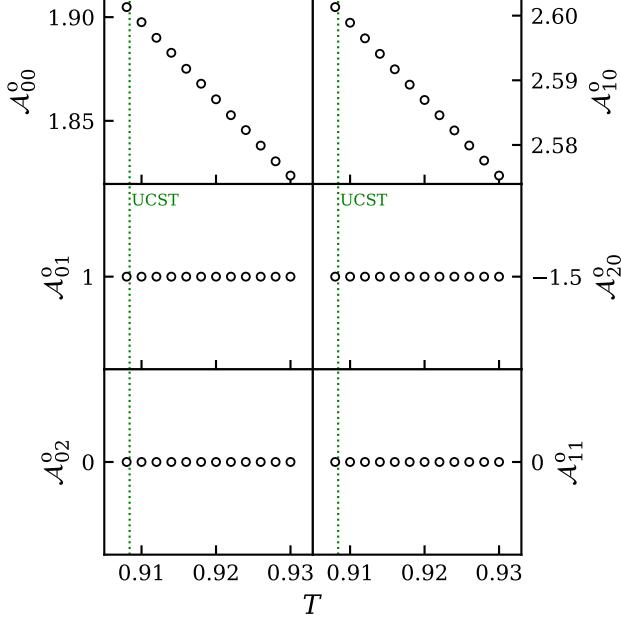


Figure S1: Ideal gas Helmholtz energy derivatives \mathcal{A}_{mn}^o near the critical solution point of the equimolar mixture C at $p = 0.0724$.

relates the Fick and MS diffusion coefficients.

Values for Γ were obtained in this work through Kirkwood-Buff integrals (KBI)^{S8}

$$G_{ij} = \int_0^\infty (g_{ij}(r) - 1) 4\pi r^2 dr \quad (4)$$

$$\approx \int_0^{2R} (g_{ij}(r) - 1) w(r, x) dr, \quad (5)$$

where $g_{ij}(r)$ is the radial distribution function (RDF) integrated over a spherical volume. Since the infinite integration limit in Eq. (4) cannot be reached with molecular simulations because they are limited to finite radii R , a geometric weight function $w(r, x)$ was proposed by Krüger et al.^{S12}

$$w(r, x) = 4\pi r^2 \left(1 - \frac{3x}{2} + \frac{x^3}{2} \right), \quad (6)$$

where $x = r/2R$. Like the self-diffusion coefficient, the integrals G_{ij} scale linearly with the inverse of the system size $1/R$. Thus, the extrapolation to the thermodynamic limit ($1/R \rightarrow 0$) is straightforward. Three types of RDF were used to calculate the KBI: the

standard RDF, and two modifications – RDF corrected according to Ganguly and van der Vegt^{S13} (vdV) and a shifted version thereof (vdV + shf).^{S14} This amounts to three values for Γ per simulation run, plus three additional values for their extrapolated versions. The thermodynamic factor of a binary mixture was then calculated by

$$\Gamma = \frac{1}{1 + x_1 x_2 \rho (G_{11} + G_{22} - 2G_{12})}. \quad (7)$$

3 Transport properties

Transport properties were obtained with equilibrium molecular dynamics (MD) simulations, mainly with the Einstein formalism. Three types of diffusion coefficients were considered: (1) self-diffusion D_i , (2) Maxwell-Stefan (MS) D_{ij} and (3) Fick diffusion D_{ij} . Shear viscosity η , thermal conductivity λ and thermodynamic factor Γ were investigated, as the latter is an important auxiliary quantity to convert between D_{ij} and D_i .

3.1 Self-diffusion coefficient

Self-diffusion is based on the Brownian motion of individual molecules in absence of driving forces. The self-diffusion coefficient of species i D_i is given by the Einstein relation

$$D_i = \lim_{\Delta t \rightarrow \infty} \frac{1}{6N_i \Delta t} \left\langle \sum_{k=1}^{N_i} \phi_{k,i}^2 \right\rangle, \quad (8)$$

with the displacement

$$\phi_{k,i} = \mathbf{r}_{k,i}(t + \Delta t) - \mathbf{r}_{k,i}(t), \quad (9)$$

where N_i is the number of molecules of species i , $\mathbf{r}_{k,i}(t)$ is the position vector of molecule k of species i and the angle brackets $\langle \dots \rangle$ denote the ensemble average.

3.2 Maxwell-Stefan and Fick diffusion

MS and Fick diffusion both describe the collective motion of molecular systems. However, they differ in the underlying driving force that is assumed for the diffusive flux. Fick diffusion assumes the concentration gradient to be the cause of mass transport, whereas MS assumes the chemical potential gradient. From a physical standpoint, the MS approach is preferable. Krishna^{S15} demonstrated its advantages, being unambiguous and more general. For a binary mixture, the MS diffusion coefficient can be obtained by

$$D_{ij} = \frac{x_2}{x_1} \Lambda_{11} + \frac{x_1}{x_2} \Lambda_{22} - 2\Lambda_{12}, \quad (10)$$

on the basis of the Onsager coefficients

$$\Lambda_{ij} = \lim_{\Delta t \rightarrow \infty} \frac{1}{6N\Delta t} \left\langle \sum_{k=1}^{N_i} \phi_{k,i} \sum_{l=1}^{N_j} \phi_{l,j} \right\rangle, \quad (11)$$

where N_i and N_j are the number of molecules of component i and j , respectively, and N is the total number of molecules. The Onsager coefficients are given by the cross-correlation of the displacement (9) between species i and j .

Despite the advantages of the MS diffusion framework, Fick's law is still the most common approach for describing diffusive mass transport because of its simple structure and the experimental accessibility of the according coefficient. The conversion between the MS and Fick diffusion coefficients can be achieved through the thermodynamic factor Γ . For binary mixtures

$$D_{ij} = D_{ij} \cdot \Gamma. \quad (12)$$

3.3 Shear viscosity and thermal conductivity

The shear viscosity η was obtained through the Einstein relation

$$\eta = \lim_{\Delta t \rightarrow \infty} \frac{1}{2V k_B T} \left\langle \left(\int_t^{t+\Delta t} J_p^{\alpha\beta}(\tau) d\tau \right)^2 \right\rangle, \quad (13)$$

where V is the molar volume, $\alpha, \beta = x, y, z$ are Cartesian coordinates and $J_p^{\alpha\beta}$ is an off-diagonal element $J_p^{x,y}, J_p^{x,z}, J_p^{y,z}$ of the stress tensor.^{S4}

The thermal conductivity λ was obtained by means of the Green-Kubo formalism

$$\lambda = \frac{1}{V k_B T^2} \int_0^\infty \langle J_q^x(t) \cdot J_q^x(0) \rangle dt, \quad (14)$$

where J_q^x are the elements of the microscopic heat flow.^{S2}

4 Results

4.1 Equation for ξ_{EOS}

The linear function modeling the temperature dependence of the binary interaction parameter needed for the EOS of Kolafa and Nezbeda^{S16} is given as

$$\xi_{\text{EOS}} = c_1 + c_2 T. \quad (15)$$

Its parameters c_1 and c_2 were fitted for each mixture and temperature range individually and are reported in Table S1.

Table S1: Parameters for the calculation of ξ_{EOS} by Eq. (15) for a given mixture.

Mixture	c_1	c_2
A	0.6046337	0.02372236
B	0.6866463	0.08538621
C	0.7621365	0.05930221
D	0.8286502	0.04253047

4.2 Deviations

The temperature dependence is qualitatively the same for all three mixtures of type II: for temperatures below the T_{CEP} , ξ_{EOS} increases linearly with rising temperature. For temperatures above T_{CEP} , ξ_{EOS} shows only a minor temperature dependence. Figure S2 shows the relative deviation between ξ_{EOS} and ξ as a function of the temperature reduced by T_{CEP} for all three studied type II mixtures (B,C,D). Overall, mixtures of type II show an increasing deviation between ξ_{EOS} and ξ . With decreasing ξ , the relative deviation between ξ_{EOS} and ξ increases. Hence, the predictive capabilities of the EOS decline.

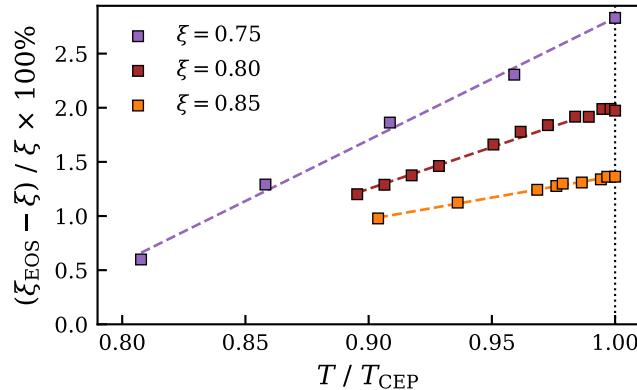


Figure S2: Relative deviation between the binary interaction parameter ξ_{EOS} of the EOS by Kolafa and Nezbeda^{S16} and its true value ξ as a function of temperature T reduced by the temperature of the critical endpoint (CEP) T_{CEP} . Results were obtained by fitting ξ_{EOS} to VLE and LLE simulation data for mixtures B (purple), C (dark red) and D (orange).

4.3 Simulation results

The simulations results for the studied mixtures are listed below. The nomenclature of the mixtures corresponds to

Mixture	A	B	C	D	E
ξ	0.60	0.75	0.80	0.85	1.20

All thermodynamic properties were reduced to dimensionless numbers on the order of unity. For brevity, the asterisk is omitted in the following with the understanding that reduced quantities are reported throughout.

4.3.1 LLE

Table S2: Simulation results for the liquid-liquid equilibrium of mixtures A to E. Temperature T , pressure p and mole fraction x_1 are tabulated, where L1 and L2 denote the two liquid phases.

ξ	T	p	x_1^{L1}	x_1^{L2}	ξ	T	p	x_1^{L1}	x_1^{L2}
0.60	1.10	0.1173	0.0939	0.9061	0.60	1.16	0.2803	0.1193	0.8807
0.60	1.10	0.1499	0.0824	0.9176	0.60	1.16	0.3129	0.1091	0.8909
0.60	1.10	0.1825	0.0754	0.9246	0.60	1.18	0.1173	0.5000	0.5000
0.60	1.10	0.2151	0.0697	0.9303	0.60	1.18	0.1499	0.5000	0.5000
0.60	1.10	0.2477	0.0654	0.9346	0.60	1.18	0.1825	0.5000	0.5000
0.60	1.12	0.1173	0.1503	0.8497	0.60	1.18	0.2151	0.5000	0.5000
0.60	1.12	0.1499	0.1126	0.8874	0.60	1.18	0.2477	0.2046	0.7954
0.60	1.12	0.1825	0.0974	0.9026	0.60	1.18	0.2803	0.1629	0.8371
0.60	1.12	0.2151	0.0878	0.9122	0.60	1.18	0.3129	0.1396	0.8604
0.60	1.12	0.2477	0.0813	0.9187	0.60	1.18	0.3455	0.1265	0.8735
0.60	1.14	0.1173	0.5000	0.5000	0.60	1.18	0.3781	0.1157	0.8843
0.60	1.14	0.1499	0.1956	0.8044	0.60	1.18	0.4107	0.1080	0.8920
0.60	1.14	0.1825	0.1355	0.8645	0.60	1.20	0.1173	0.5000	0.5000
0.60	1.14	0.2151	0.1146	0.8854	0.60	1.20	0.1499	0.5000	0.5000
0.60	1.14	0.2477	0.1021	0.8979	0.60	1.20	0.1825	0.5000	0.5000
0.60	1.16	0.1173	0.5000	0.5000	0.60	1.20	0.2151	0.5000	0.5000
0.60	1.16	0.1499	0.5000	0.5000	0.60	1.20	0.2477	0.5000	0.5000
0.60	1.16	0.1825	0.2904	0.7096	0.60	1.20	0.2803	0.2601	0.7399
0.60	1.16	0.2151	0.1641	0.8359	0.60	1.20	0.3129	0.1917	0.8083
0.60	1.16	0.2477	0.1355	0.8645	0.60	1.20	0.3455	0.1652	0.8348
0.60	1.16	0.3455	0.0998	0.9002	0.60	1.20	0.3781	0.1459	0.8541
0.60	1.16	0.3781	0.0940	0.9060	0.60	1.20	0.4107	0.1338	0.8662
0.60	1.16	0.4107	0.0889	0.9111					

Table S2: Simulation results for the liquid-liquid equilibrium of mixtures A to E. Temperature T , pressure p and mole fraction x_1 are tabulated, where L1 and L2 denote the two liquid phases.

ξ	T	p	x_1^{L1}	x_1^{L2}	ξ	T	p	x_1^{L1}	x_1^{L2}
0.75	0.80	0.0724	0.0373	0.9627	0.75	0.90	0.0724	0.1029	0.8971
0.75	0.80	0.1000	0.0373	0.9627	0.75	0.90	0.1000	0.1008	0.8992
0.75	0.80	0.1253	0.0377	0.9623	0.75	0.90	0.1253	0.0982	0.9018
0.75	0.80	0.1499	0.0371	0.9629	0.75	0.90	0.1499	0.0970	0.9030
0.75	0.85	0.0724	0.0634	0.9366	0.75	0.95	0.0724	0.1743	0.8257
0.75	0.85	0.1000	0.0622	0.9378	0.75	0.95	0.1000	0.1679	0.8321
0.75	0.85	0.1253	0.0604	0.9396	0.75	0.95	0.1253	0.1638	0.8362
0.75	0.85	0.1499	0.0599	0.9401	0.75	0.95	0.1499	0.1588	0.8412
0.80	0.80	0.0724	0.1020	0.8980	0.80	0.90	0.0724	0.3610	0.6390
0.80	0.81	0.0724	0.1189	0.8811	0.80	0.90	0.0869	0.3431	0.6569
0.80	0.82	0.0724	0.1314	0.8686	0.80	0.90	0.1014	0.3392	0.6608
0.80	0.83	0.0724	0.1454	0.8546	0.80	0.90	0.0036	0.5000	0.5000
0.80	0.84	0.0724	0.1613	0.8387	0.80	0.90	0.0072	0.4999	0.5001
0.80	0.85	0.0036	0.1952	0.8048	0.80	0.90	0.0145	0.4683	0.5317
0.80	0.85	0.0072	0.1936	0.8064	0.80	0.90	0.0181	0.5000	0.5000
0.80	0.85	0.0145	0.1924	0.8076	0.80	0.90	0.0217	0.4502	0.5498
0.80	0.85	0.0290	0.1902	0.8098	0.80	0.90	0.0254	0.4616	0.5384
0.80	0.85	0.0435	0.1891	0.8109	0.80	0.90	0.0290	0.4477	0.5523
0.80	0.85	0.0579	0.1871	0.8129	0.80	0.90	0.0435	0.4079	0.5921
0.80	0.85	0.0724	0.1847	0.8153	0.80	0.90	0.0579	0.3955	0.6045
0.80	0.85	0.0869	0.1824	0.8176	0.80	0.90	0.0724	0.3723	0.6277
0.80	0.85	0.1014	0.1777	0.8223	0.80	0.90	0.0869	0.3608	0.6392
0.80	0.86	0.0290	0.2102	0.7898	0.80	0.90	0.1014	0.3548	0.6452
0.80	0.86	0.0435	0.2082	0.7918	0.80	0.90	0.0217	0.5000	0.5000
0.80	0.86	0.0579	0.2053	0.7947	0.80	0.90	0.0254	0.4717	0.5283
0.80	0.86	0.0724	0.2007	0.7993	0.80	0.90	0.0290	0.4660	0.5340
0.80	0.87	0.0290	0.2386	0.7614	0.80	0.90	0.0435	0.4300	0.5700
0.80	0.87	0.0435	0.2382	0.7618	0.80	0.90	0.0579	0.4122	0.5878
0.80	0.87	0.0579	0.2350	0.7650	0.80	0.90	0.0724	0.3892	0.6108
0.80	0.87	0.0724	0.2254	0.7746	0.80	0.91	0.0036	0.5000	0.5000
0.80	0.88	0.0290	0.2725	0.7275	0.80	0.91	0.0072	0.5000	0.5000
0.80	0.88	0.0435	0.2706	0.7294	0.80	0.91	0.0145	0.5000	0.5000
0.80	0.88	0.0579	0.2671	0.7329	0.80	0.91	0.0181	0.4996	0.5004
0.80	0.88	0.0724	0.2536	0.7464	0.80	0.91	0.0217	0.5000	0.5000
0.80	0.89	0.0181	0.3333	0.6667	0.80	0.91	0.0254	0.4955	0.5045
0.80	0.89	0.0217	0.3212	0.6788	0.80	0.91	0.0290	0.4855	0.5146
0.80	0.89	0.0254	0.3222	0.6778	0.80	0.91	0.0435	0.4362	0.5638
0.80	0.89	0.0290	0.3171	0.6829	0.80	0.91	0.0579	0.4085	0.5915
0.80	0.89	0.0435	0.3177	0.6823	0.80	0.91	0.0724	0.3995	0.6005
0.80	0.89	0.0579	0.3049	0.6951	0.80	0.91	0.0869	0.3791	0.6209
0.80	0.89	0.0724	0.2959	0.7041	0.80	0.91	0.1014	0.3706	0.6294
0.80	0.89	0.0869	0.2930	0.7070	0.80	0.91	0.0724	0.4992	0.5007
0.80	0.89	0.1014	0.2848	0.7152	0.80	0.91	0.1086	0.4095	0.5905
0.80	0.90	0.0145	0.3679	0.6321	0.80	0.91	0.1449	0.3687	0.6313
0.80	0.90	0.0181	0.3591	0.6409	0.80	0.91	0.1811	0.3446	0.6554

Table S2: Simulation results for the liquid-liquid equilibrium of mixtures A to E. Temperature T , pressure p and mole fraction x_1 are tabulated, where L1 and L2 denote the two liquid phases.

ξ	T	p	x_1^{L1}	x_1^{L2}	ξ	T	p	x_1^{L1}	x_1^{L2}
0.80	0.90	0.0217	0.3436	0.6564	0.80	0.91	0.2173	0.3259	0.6741
0.80	0.90	0.0254	0.3528	0.6472	0.80	0.91	0.2535	0.3150	0.6850
0.80	0.90	0.0290	0.3486	0.6514	0.80	0.92	0.1086	0.5000	0.5000
0.80	0.90	0.0036	0.4350	0.5650	0.80	0.92	0.1449	0.4155	0.5845
0.80	0.90	0.0072	0.4272	0.5728	0.80	0.92	0.1811	0.3812	0.6188
0.80	0.90	0.0145	0.4167	0.5833	0.80	0.92	0.2173	0.3591	0.6409
0.80	0.90	0.0181	0.4099	0.5901	0.80	0.92	0.2535	0.3368	0.6632
0.80	0.90	0.0217	0.4098	0.5902	0.80	0.92	0.1449	0.5000	0.5000
0.80	0.90	0.0254	0.3958	0.6042	0.80	0.92	0.1811	0.4443	0.5557
0.80	0.90	0.0290	0.3934	0.6066	0.80	0.92	0.2173	0.3896	0.6104
0.80	0.90	0.0435	0.3809	0.6191	0.80	0.92	0.2535	0.3662	0.6338
0.80	0.90	0.0579	0.3657	0.6343					
0.85	0.70	0.0025	0.1640	0.8360	0.85	0.76	0.0217	0.3444	0.6556
0.85	0.70	0.0033	0.1610	0.8390	0.85	0.76	0.0072	0.3583	0.6417
0.85	0.70	0.0045	0.1660	0.8340	0.85	0.76	0.0145	0.3541	0.6459
0.85	0.70	0.0059	0.1617	0.8383	0.85	0.76	0.0217	0.3555	0.6445
0.85	0.70	0.0077	0.1623	0.8377	0.85	0.77	0.0072	0.3734	0.6266
0.85	0.70	0.0097	0.1631	0.8369	0.85	0.77	0.0145	0.3627	0.6373
0.85	0.70	0.0120	0.1617	0.8383	0.85	0.77	0.0217	0.3637	0.6363
0.85	0.70	0.0146	0.1631	0.8369	0.85	0.77	0.0072	0.3802	0.6198
0.85	0.70	0.0175	0.1640	0.8360	0.85	0.77	0.0145	0.3806	0.6194
0.85	0.73	0.0033	0.2169	0.7831	0.85	0.77	0.0217	0.3842	0.6158
0.85	0.73	0.0045	0.2128	0.7872	0.85	0.77	0.0072	0.4133	0.5867
0.85	0.73	0.0059	0.2156	0.7844	0.85	0.77	0.0145	0.3873	0.6127
0.85	0.73	0.0077	0.2180	0.7820	0.85	0.77	0.0217	0.4082	0.5918
0.85	0.73	0.0097	0.2112	0.7888	0.85	0.77	0.0072	0.4387	0.5613
0.85	0.73	0.0120	0.2143	0.7857	0.85	0.77	0.0145	0.4400	0.5600
0.85	0.73	0.0146	0.2161	0.7839	0.85	0.77	0.0217	0.4120	0.5880
0.85	0.73	0.0175	0.2074	0.7926	0.85	0.77	0.0072	0.4597	0.5403
0.85	0.75	0.0045	0.2877	0.7123	0.85	0.77	0.0145	0.4576	0.5424
0.85	0.75	0.0059	0.2867	0.7133	0.85	0.77	0.0217	0.4217	0.5783
0.85	0.75	0.0077	0.3030	0.6970	0.85	0.78	0.0059	0.4883	0.5117
0.85	0.75	0.0097	0.2871	0.7129	0.85	0.78	0.0077	0.5000	0.5000
0.85	0.75	0.0120	0.2817	0.7183	0.85	0.78	0.0097	0.4527	0.5473
0.85	0.75	0.0146	0.2846	0.7154	0.85	0.78	0.0120	0.4529	0.5471
0.85	0.75	0.0175	0.2867	0.7133	0.85	0.78	0.0146	0.4830	0.5170
0.85	0.75	0.0072	0.3012	0.6988	0.85	0.78	0.0175	0.4998	0.5002
0.85	0.75	0.0145	0.2996	0.7004	0.85	0.78	0.0072	0.5000	0.5000
0.85	0.75	0.0217	0.2932	0.7068	0.85	0.78	0.0145	0.5000	0.5000
0.85	0.75	0.0072	0.3035	0.6965	0.85	0.78	0.0217	0.5000	0.5000
0.85	0.75	0.0145	0.3096	0.6904	0.85	0.78	0.0072	0.5000	0.5000
0.85	0.75	0.0217	0.3080	0.6920	0.85	0.78	0.0145	0.5000	0.5000
0.85	0.76	0.0072	0.3118	0.6882	0.85	0.78	0.0217	0.5000	0.5000
0.85	0.76	0.0145	0.3170	0.6830	0.85	0.78	0.0072	0.5000	0.5000
0.85	0.76	0.0217	0.3124	0.6876	0.85	0.78	0.0145	0.5000	0.5000

Table S2: Simulation results for the liquid-liquid equilibrium of mixtures A to E. Temperature T , pressure p and mole fraction x_1 are tabulated, where L1 and L2 denote the two liquid phases.

ξ	T	p	x_1^{L1}	x_1^{L2}	ξ	T	p	x_1^{L1}	x_1^{L2}
0.85	0.76	0.0072	0.3285	0.6715	0.85	0.79	0.0072	0.5000	0.5000
0.85	0.76	0.0145	0.3215	0.6785	0.85	0.79	0.0145	0.5000	0.5000
0.85	0.76	0.0217	0.3246	0.6754	0.85	0.80	0.0077	0.5000	0.5000
0.85	0.76	0.0072	0.3337	0.6663	0.85	0.80	0.0097	0.5000	0.5000
0.85	0.76	0.0145	0.3298	0.6702	0.85	0.80	0.0120	0.5000	0.5000
0.85	0.76	0.0217	0.3257	0.6743	0.85	0.80	0.0146	0.5000	0.5000
0.85	0.76	0.0072	0.3537	0.6463	0.85	0.80	0.0175	0.5000	0.5000
0.85	0.76	0.0145	0.3449	0.6551	0.85	0.80	0.0724	0.5000	0.5000

4.3.2 VLLE

Table S3: Simulation results for the vapor-liquid-liquid equilibrium of mixtures A to D. Temperature T , pressure p and mole fraction x_1 are tabulated, where V, L1 and L2 denote the vapor and the two liquid phases.

ξ	T	p	x_1^{L1}	x_1^{L2}	x_1^V	ξ	T	p	x_1^{L1}	x_1^{L2}	x_1^V
0.60	1.10	0.1131	0.0957	0.9043	0.5	0.80	0.87	0.0171	0.2442	0.7558	0.5
0.60	1.12	0.1341	0.1229	0.8771	0.5	0.80	0.88	0.0186	0.2793	0.7207	0.5
0.75	0.80	0.0092	0.0374	0.9626	0.5	0.80	0.89	0.0201	0.3257	0.6743	0.5
0.75	0.85	0.0151	0.0660	0.9340	0.5	0.80	0.90	0.0217	0.4076	0.5924	0.5
0.75	0.90	0.0236	0.1067	0.8933	0.5	0.85	0.70	0.0025	0.1629	0.8371	0.5
0.75	0.95	0.0350	0.1813	0.8187	0.5	0.85	0.73	0.0035	0.2163	0.7837	0.5
0.80	0.85	0.0144	0.1931	0.8069	0.5	0.85	0.75	0.0047	0.2910	0.7090	0.5
0.80	0.86	0.0158	0.2136	0.7864	0.5	0.85	0.78	0.0061	0.4773	0.5227	0.5

4.3.3 Azeotropic line

Table S4: Simulation results for the azeotropic line of mixtures B to E. Temperature T , pressure p , density ρ and mole fraction x_1 are tabulated, where V and L denote the vapor and liquid phase, respectively.

ξ	T	x_1^L	x_1^V	err	p	err	ρ^L	err	ρ^V	err
0.75	1.03	0.5000	0.4998	0.0011	0.0576	0.0001	0.5954	0.0004	0.0806	0.0001
0.75	1.06	0.5000	0.5015	0.0012	0.0684	0.0001	0.5648	0.0006	0.0994	0.0002
0.75	1.09	0.5000	0.5007	0.0013	0.0809	0.0001	0.5325	0.0008	0.1247	0.0002
0.75	1.12	0.5000	0.5009	0.0013	0.0955	0.0002	0.4864	0.0010	0.1626	0.0003
0.75	1.13	0.5000	0.5017	0.0014	0.0988	0.0002	0.4738	0.0017	0.1734	0.0003
0.80	0.95	0.5000	0.5020	0.0012	0.0310	0.0001	0.6745	0.0002	0.0404	0.0001
0.80	1.00	0.5000	0.4989	0.0012	0.0428	0.0001	0.6388	0.0003	0.0564	0.0001

Table S4: Simulation results for the azeotropic line of mixtures B to E. Temperature T , pressure p , density ρ and mole fraction x_1 are tabulated, where V and L denote the vapor and liquid phase, respectively.

ξ	T	x_1^L	x_1^V	err	p	err	ρ^L	err	ρ^V	err
0.80	1.05	0.5000	0.5005	0.0010	0.0573	0.0001	0.5982	0.0004	0.0780	0.0001
0.80	1.10	0.5000	0.5011	0.0010	0.0753	0.0001	0.5501	0.0005	0.1092	0.0002
0.80	1.15	0.5000	0.4997	0.0013	0.0967	0.0002	0.4859	0.0014	0.1571	0.0003
0.85	0.95	0.5000	0.4988	0.0012	0.0271	0.0000	0.6884	0.0002	0.0344	0.0001
0.85	1.00	0.5000	0.5005	0.0012	0.0376	0.0001	0.6556	0.0002	0.0481	0.0001
0.85	1.05	0.5000	0.4987	0.0010	0.0509	0.0001	0.6195	0.0002	0.0665	0.0001
0.85	1.10	0.5000	0.5019	0.0010	0.0668	0.0001	0.5774	0.0004	0.0909	0.0001
0.85	1.15	0.5000	0.4989	0.0011	0.0856	0.0001	0.5236	0.0006	0.1252	0.0002
0.85	1.19	0.5000	0.4981	0.0011	0.1040	0.0002	0.4605	0.0020	0.1711	0.0003
1.20	1.15	0.5000	0.4998	0.0010	0.0363	0.0001	0.6771	0.0002	0.0389	0.0001
1.20	1.20	0.5000	0.5011	0.0011	0.0475	0.0001	0.6492	0.0002	0.0512	0.0001
1.20	1.25	0.5000	0.4996	0.0008	0.0611	0.0001	0.6186	0.0002	0.0674	0.0001
1.20	1.30	0.5000	0.5002	0.0009	0.0764	0.0001	0.5833	0.0003	0.0867	0.0001
1.20	1.35	0.5000	0.5002	0.0009	0.0952	0.0002	0.5424	0.0005	0.1149	0.0002
1.20	1.40	0.5000	0.5009	0.0010	0.1166	0.0002	0.4876	0.0009	0.1542	0.0003

4.3.4 Transport properties

Table S5: Simulation results for the transport properties near the critical solution point of the equimolar mixture C at $p = 0.0724$. Temperature T , density ρ , MS D_{ij}^∞ and self-diffusion coefficient D_i as well as the shear viscosity η and thermal conductivity λ are tabulated. Results correspond to four system sizes $N = 2500, 5000, 10,000$ and $20,000$.

T	ρ	err	D_i	err	D_{ij}^∞	err	η	err	λ	err
$N = 2500$										
0.906	0.7124	0.0001	0.0989	0.0002	0.1919	0.0092	1.1198	0.0814	5.8840	1.3254
0.908	0.7109	0.0001	0.1002	0.0002	0.1997	0.0090	1.1380	0.1037	3.8474	1.2579
0.910	0.7098	0.0001	0.1009	0.0002	0.1877	0.0090	1.1536	0.0988	6.8937	1.3200
0.912	0.7085	0.0001	0.1016	0.0002	0.1984	0.0089	1.2019	0.0933	4.6104	1.2756
0.914	0.7074	0.0001	0.1025	0.0002	0.1830	0.0100	1.1806	0.1393	6.7208	1.8328
0.916	0.7060	0.0001	0.1039	0.0002	0.1881	0.0093	1.2583	0.0948	3.0301	1.0770
0.918	0.7049	0.0001	0.1045	0.0002	0.2078	0.0116	1.2069	0.0958	3.7291	1.2774
0.920	0.7035	0.0001	0.1051	0.0002	0.1794	0.0084	1.3363	0.1190	5.0717	1.2685
0.922	0.7021	0.0001	0.1060	0.0002	0.1866	0.0084	1.2053	0.0898	4.6970	1.1791
0.924	0.7010	0.0001	0.1069	0.0002	0.1866	0.0094	1.3772	0.1054	5.1726	1.2527
0.926	0.6996	0.0001	0.1076	0.0002	0.1920	0.0105	1.1287	0.0972	1.2337	1.1855
0.928	0.6982	0.0001	0.1086	0.0002	0.1994	0.0095	1.1381	0.0934	4.4043	1.3107
0.930	0.6973	0.0001	0.1097	0.0002	0.1941	0.0092	1.2723	0.1101	5.0363	1.1734

Table S5: Simulation results for the transport properties near the critical solution point of the equimolar mixture C at $p = 0.0724$. Temperature T , density ρ , MS D_{ij}^∞ and self-diffusion coefficient D_i as well as the shear viscosity η and thermal conductivity λ are tabulated. Results correspond to four system sizes $N = 2500, 5000, 10,000$ and $20,000$.

T	ρ	err	D_i	err	D_{ij}^∞	err	η	err	λ	err
$N = 5000$										
0.906	0.7124	0.0001	0.1002	0.0001	0.2133	0.0094	1.2372	0.0861	4.7805	0.7998
0.908	0.7109	0.0001	0.1013	0.0001	0.2233	0.0099	1.0575	0.0738	4.2165	0.7059
0.910	0.7098	0.0001	0.1020	0.0001	0.1936	0.0074	1.3337	0.0912	3.6371	0.6922
0.912	0.7085	0.0001	0.1029	0.0001	0.1867	0.0077	1.2679	0.0792	3.9024	0.7111
0.914	0.7074	0.0001	0.1037	0.0001	0.2393	0.0106	1.1335	0.0787	3.9404	0.7066
0.916	0.7060	0.0001	0.1046	0.0001	0.1954	0.0068	1.0919	0.0685	3.8630	0.6551
0.918	0.7049	0.0001	0.1054	0.0001	0.2149	0.0087	1.0759	0.0769	3.6055	0.6627
0.920	0.7035	0.0001	0.1060	0.0001	0.1922	0.0077	1.3719	0.0857	4.3032	0.7046
0.922	0.7021	0.0001	0.1074	0.0001	0.1964	0.0069	1.0965	0.0742	4.0943	0.6948
0.924	0.7010	0.0001	0.1078	0.0001	0.2161	0.0083	1.1213	0.0646	2.9579	0.6768
0.926	0.6996	0.0001	0.1091	0.0001	0.1839	0.0076	1.0894	0.0628	2.9590	0.6176
0.928	0.6982	0.0001	0.1099	0.0001	0.2055	0.0087	1.3053	0.0825	3.9005	0.7017
0.930	0.6973	0.0001	0.1110	0.0001	0.2293	0.0089	1.2875	0.0902	4.8002	0.6876
$N = 10,000$										
0.906	0.7124	0.0001	0.1012	0.0001	0.2254	0.0095	1.2244	0.0801	5.4210	0.7538
0.908	0.7109	0.0001	0.1024	0.0001	0.2180	0.0089	1.0935	0.0752	4.2867	0.7476
0.910	0.7098	0.0001	0.1030	0.0001	0.2160	0.0104	1.3169	0.0862	4.3253	0.7369
0.912	0.7085	0.0001	0.1040	0.0001	0.2226	0.0100	1.1848	0.0798	5.0099	0.7651
0.914	0.7074	0.0001	0.1048	0.0001	0.2047	0.0078	1.1546	0.0849	3.6872	0.7344
0.916	0.7060	0.0001	0.1056	0.0001	0.2199	0.0093	1.2685	0.0841	3.9112	0.7382
0.918	0.7049	0.0001	0.1064	0.0001	0.2183	0.0093	1.0537	0.0683	5.2886	0.7360
0.920	0.7035	0.0001	0.1076	0.0001	0.2398	0.0096	0.9808	0.0694	5.1168	0.7123
0.922	0.7021	0.0001	0.1084	0.0001	0.2192	0.0102	1.3261	0.0955	3.1974	0.7281
0.924	0.7010	0.0001	0.1092	0.0001	0.2133	0.0079	1.1187	0.0693	4.4133	0.6808
0.926	0.6996	0.0001	0.1098	0.0001	0.2153	0.0090	1.2652	0.0859	4.8182	0.7424
0.928	0.6982	0.0001	0.1110	0.0001	0.2016	0.0083	1.0878	0.0719	3.7182	0.6726
0.930	0.6973	0.0001	0.1118	0.0001	0.2382	0.0105	1.1326	0.0767	4.5748	0.6961
$N = 20,000$										
0.906	0.7124	0.0001	0.1021	0.0001	0.2343	0.0139	1.1373	0.0930	4.4854	1.6365
0.908	0.7109	0.0001	0.1032	0.0001	0.2196	0.0140	1.3221	0.1126	6.7936	1.8967
0.910	0.7098	0.0001	0.1038	0.0001	0.2142	0.0113	1.2914	0.1406	4.3375	1.8188
0.912	0.7085	0.0001	0.1045	0.0001	0.2449	0.0139	1.4212	0.0985	4.1932	1.6094
0.914	0.7074	0.0001	0.1056	0.0001	0.2500	0.0144	1.1567	0.1116	2.8314	1.8733
0.916	0.7060	0.0001	0.1065	0.0001	0.2350	0.0127	1.1818	0.0993	3.1328	1.8003
0.918	0.7049	0.0001	0.1073	0.0001	0.2426	0.0141	1.2489	0.0968	4.8839	1.9031
0.920	0.7035	0.0001	0.1082	0.0001	0.2486	0.0142	0.8571	0.0708	3.6804	1.6528
0.922	0.7021	0.0001	0.1090	0.0001	0.2440	0.0128	1.0814	0.1186	5.5139	1.7003
0.924	0.7010	0.0001	0.1097	0.0001	0.2181	0.0108	1.1194	0.1159	9.0988	1.8116
0.926	0.6996	0.0001	0.1110	0.0001	0.2555	0.0154	1.2953	0.1365	-0.0882	1.8307
0.928	0.6982	0.0001	0.1119	0.0001	0.2390	0.0159	1.0044	0.0949	1.8810	1.7731
0.930	0.6973	0.0001	0.1126	0.0001	0.2338	0.0151	1.3080	0.1225	4.3251	1.8015

4.3.5 UCST

Table S6: Simulation results for the UCST of mixtures B to D. Temperature T , pressure p and mole fraction x_1 are tabulated, where L1 and L2 denote the two liquid phases.

ξ	T	p	x_1^{L1}	x_1^{L2}	ξ	T	p	x_1^{L1}	x_1^{L2}
0.80	0.90	0.0036	0.5	0.5	0.75	1.01	0.0724	0.5	0.5
0.80	0.90	0.0072	0.5	0.5	0.75	1.01	0.1000	0.5	0.5
0.80	0.90	0.0145	0.5	0.5	0.75	1.02	0.1253	0.5	0.5
0.80	0.90	0.0181	0.5	0.5	0.75	1.03	0.1499	0.5	0.5
0.80	0.90	0.0217	0.5	0.5				0.5	0.5
0.80	0.90	0.0254	0.5	0.5	0.85	0.77	0.0059	0.5	0.5
0.80	0.90	0.0290	0.5	0.5	0.85	0.77	0.0072	0.5	0.5
0.80	0.91	0.0435	0.5	0.5	0.85	0.77	0.0077	0.5	0.5
0.80	0.91	0.0579	0.5	0.5	0.85	0.78	0.0097	0.5	0.5
0.80	0.91	0.0724	0.5	0.5	0.85	0.78	0.0120	0.5	0.5
0.80	0.91	0.1014	0.5	0.5	0.85	0.78	0.0145	0.5	0.5
0.80	0.91	0.0869	0.5	0.5	0.85	0.78	0.0146	0.5	0.5
0.80	0.91	0.1086	0.5	0.5	0.85	0.78	0.0175	0.5	0.5
0.80	0.92	0.1449	0.5	0.5	0.85	0.78	0.0217	0.5	0.5
0.80	0.92	0.1811	0.5	0.5					
0.80	0.93	0.2173	0.5	0.5					
0.80	0.93	0.2535	0.5	0.5					

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