

Supporting Information for
The Effect of Switchable Electronic Polarization States on the
Electronic Properties of Two-dimensional Multiferroic
 $\text{TMBr}_2/\text{Ga}_2\text{SSe}_2$ (TM=V-Ni) Heterostructures

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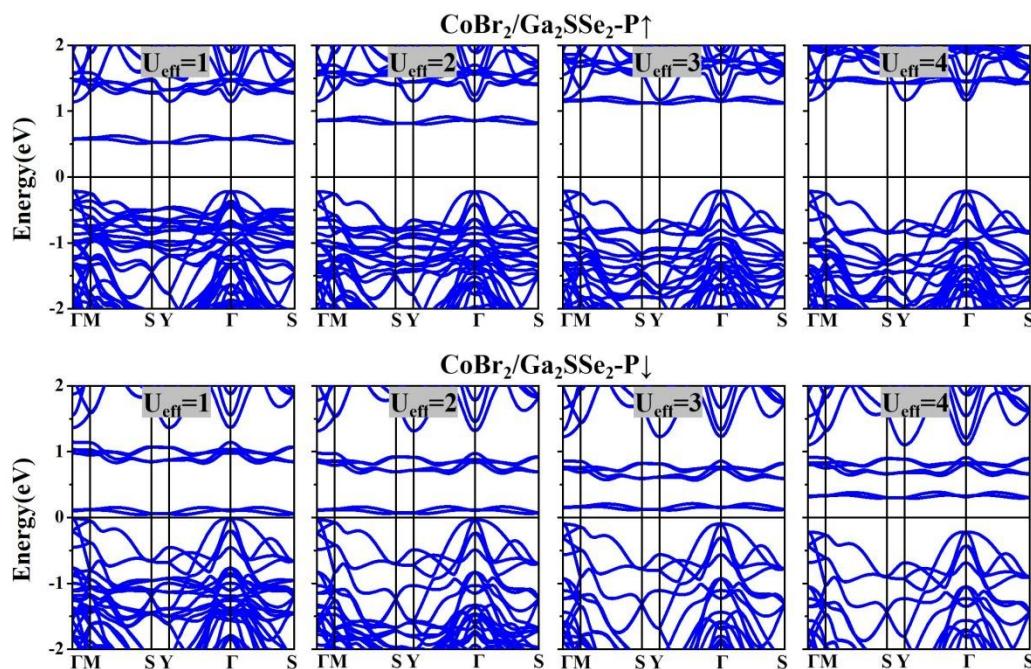


Fig. S1. The band structure of $\text{CoBr}_2/\text{Ga}_2\text{SSe}_2-\text{P}\uparrow$ and $\text{CoBr}_2/\text{Ga}_2\text{SSe}_2-\text{P}\downarrow$ HSs calculated using different U_{eff} s (=1.0 ~4.0 eV).

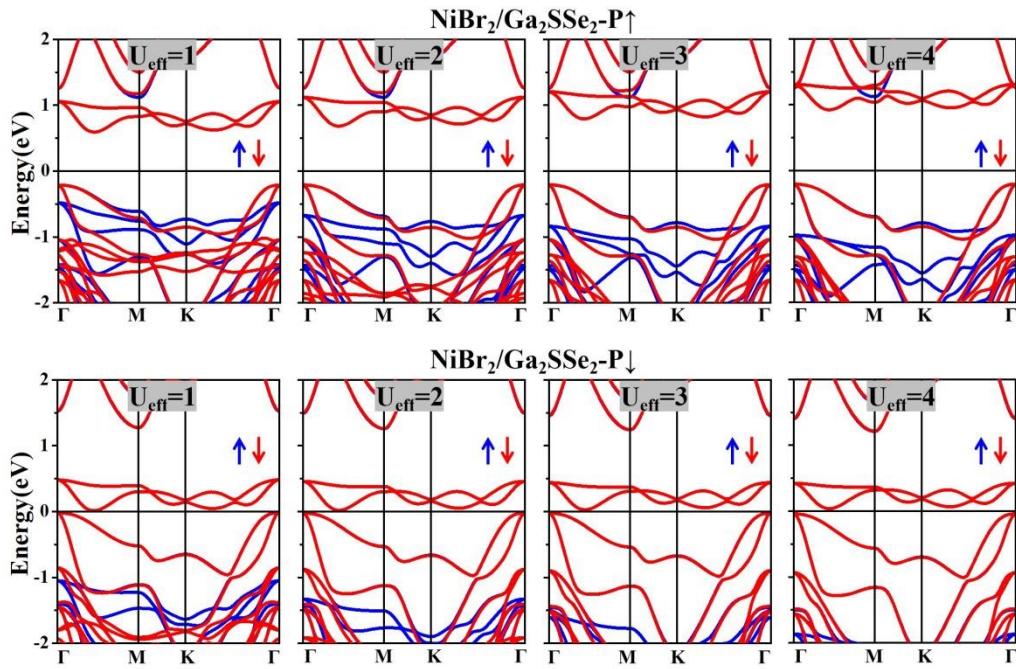


Fig. S2. The band structure of $\text{NiBr}_2/\text{Ga}_2\text{SSe}_2$ -P \uparrow and $\text{NiBr}_2/\text{Ga}_2\text{SSe}_2$ -P \downarrow HSs calculated using different U_{eff} s ($=1.0 \sim 4.0$ eV).

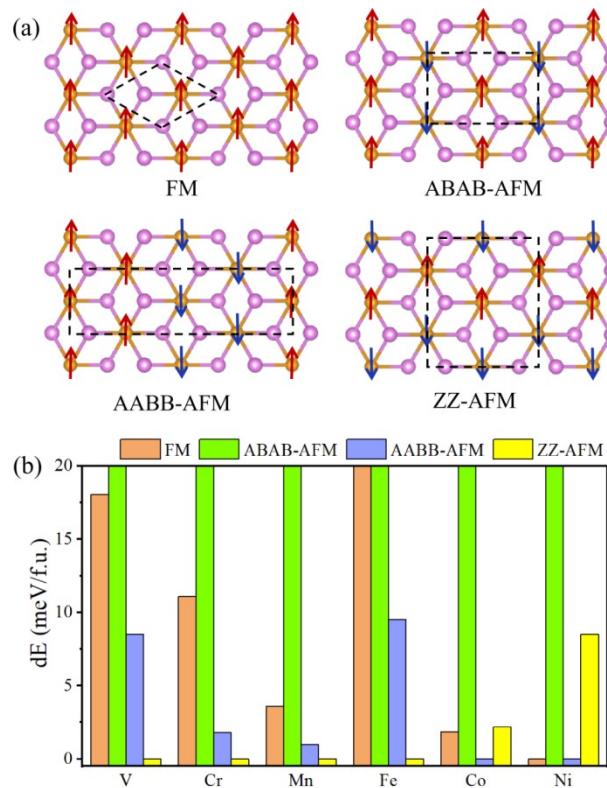


Figure S3. (a) Four possible magnetic states of TMBr_2 monolayers ($\text{TM}=\text{V-Ni}$). (b) Energy diagram of TMBr_2 monolayers with different magnetic states, Where the ground state is set to zero.

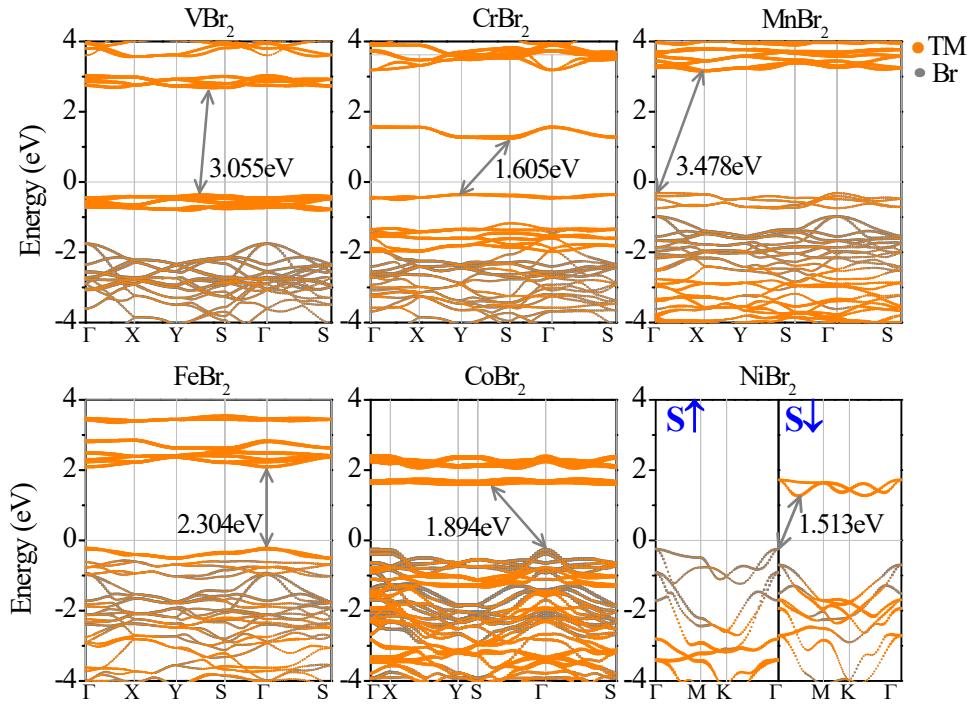


Figure S4. Band structures of TMBr_2 monolayers.

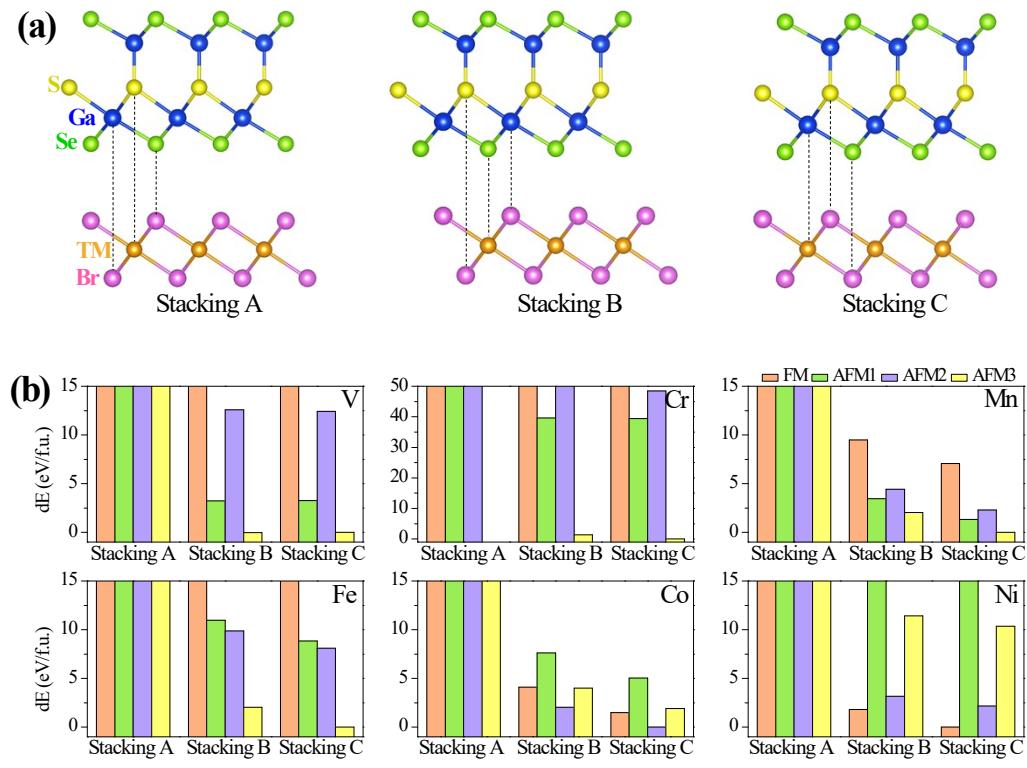


Figure S5. (a) Side view of three different interfacial contact types for the $\text{TMBr}_2/\text{Ga}_2\text{SSe}_2$ heterostructures. (b) Energy diagram of $\text{TMBr}_2/\text{Ga}_2\text{SSe}_2$ HSs with different magnetic states, Where the ground state is set to zero.

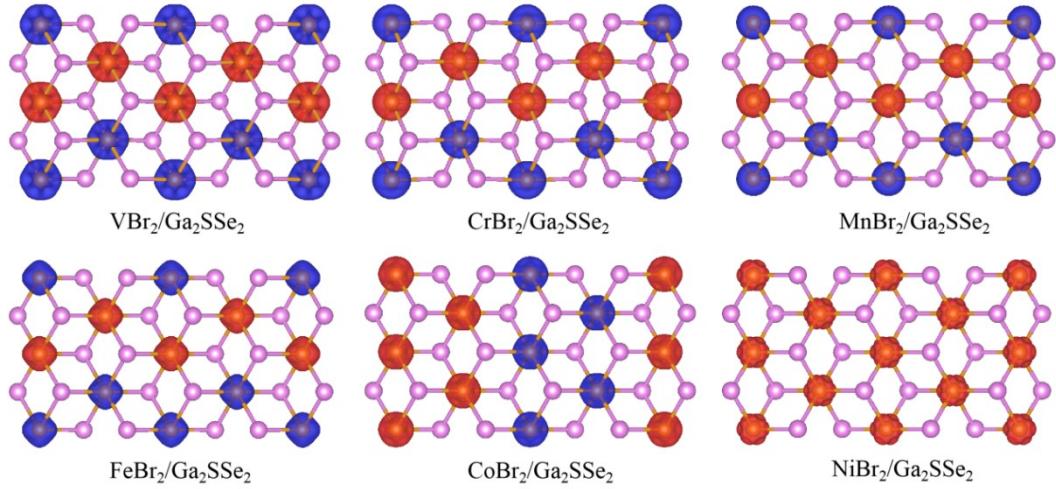


Figure S6. Top views of atomic structures with spin-polarized charge density distribution for $\text{TMBr}_2/\text{Ga}_2\text{SSe}_2$ HSs.

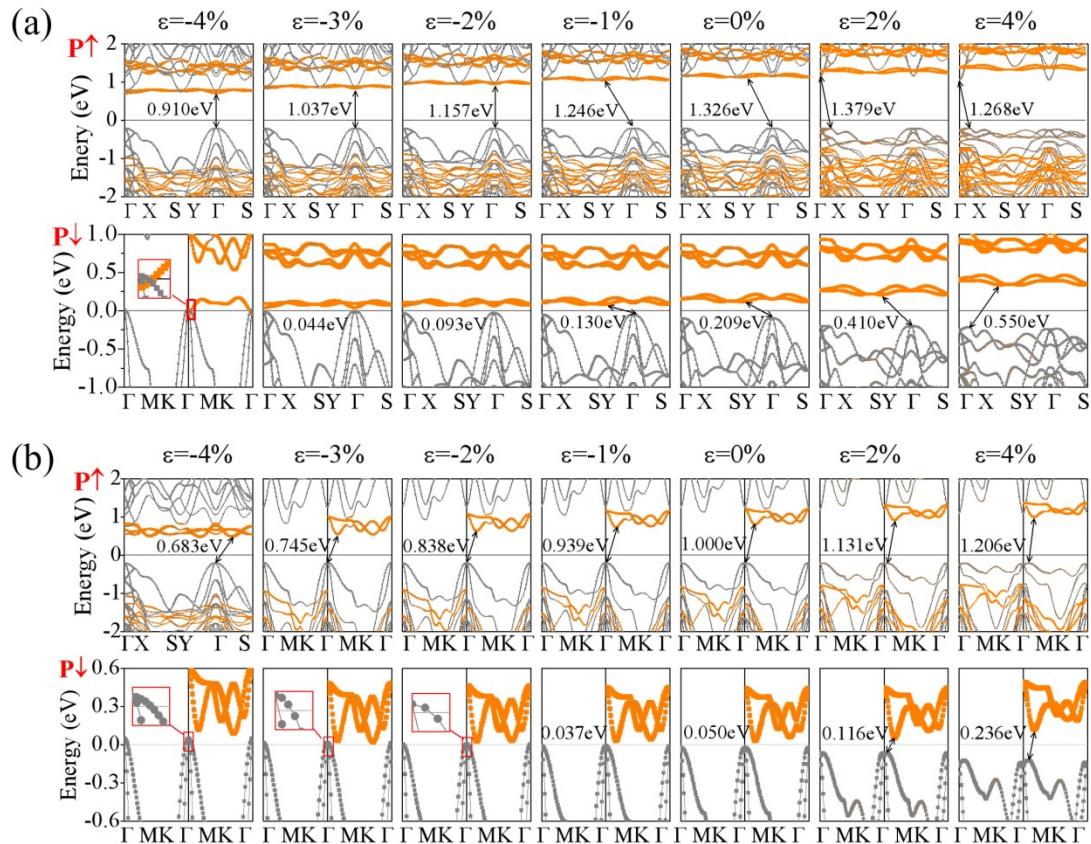


Figure S7. Band structures of (a) $\text{CoBr}_2/\text{Ga}_2\text{SSe}_2$ and (b) $\text{NiBr}_2/\text{Ga}_2\text{SSe}_2$ HSs under biaxial strains with upward and downward ferroelectric polarization.

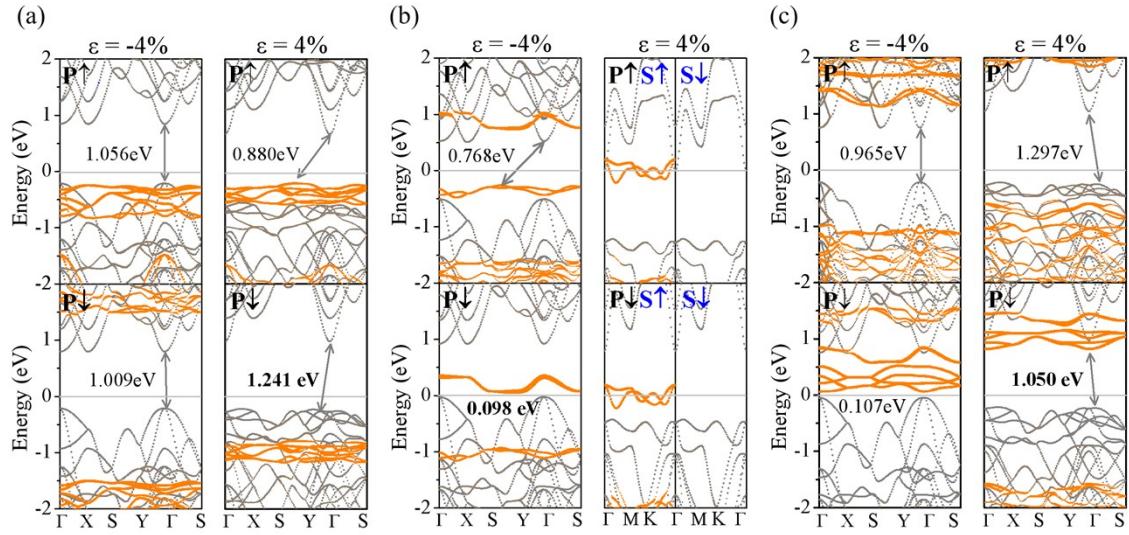


Figure S8. Band structures of (a) $\text{VBr}_2/\text{Ga}_2\text{SSe}_2$, (b) $\text{CrBr}_2/\text{Ga}_2\text{SSe}_2$, and $\text{FeBr}_2/\text{Ga}_2\text{SSe}_2$ HSS under biaxial strains 4% with upward and downward ferroelectric polarization.

Table S1. The energy differences of ferromagnetic (FM) and antiferromagnetic (AFM) states in $\text{Co}(\text{Ni})\text{Br}_2/\text{Ga}_2\text{SSe}_2-\text{P}\uparrow$ and $\text{Co}(\text{Ni})\text{Br}_2/\text{Ga}_2\text{SSe}_2-\text{P}\downarrow$ HSSs.

$\text{CoBr}_2/\text{Ga}_2\text{SSe}_2-\text{P}\uparrow$				$\text{CoBr}_2/\text{Ga}_2\text{SSe}_2-\text{P}\downarrow$				
U_{eff}	FM	ABAB-AFM	AABB-AFM	ZZ-AFM	FM	ABAB-AFM	AABB-AFM	ZZ-AFM
1	1.4	8.91	0	3.83	0.57	9.62	0	4.03
2	1.63	6.41	0	2.4	1.41	6.85	0	2.46
3	1.48	5.05	0	1.90	2.23	5.57	0	2.37
4	1.05	3.79	0	1.38	1.1	7.49	0	5.65

$\text{NiBr}_2/\text{Ga}_2\text{SSe}_2-\text{P}\uparrow$				$\text{NiBr}_2/\text{Ga}_2\text{SSe}_2-\text{P}\downarrow$				
U_{eff}	FM	ABAB-AFM	AABB-AFM	ZZ-AFM	FM	ABAB-AFM	AABB-AFM	ZZ-AFM
1	0	13.09	1.69	7.88	0	25.42	3.83	15.86
2	0	21.01	2.75	12.71	0	20.53	3.18	12.93
3	0	17.01	2.16	10.35	0	16.59	2.36	10.43
4	0	13.75	1.88	8.42	0	13.65	2.03	8.56

Table S2. The lattice parameters and magnetic ground states of TMBr_2 ($\text{TM}=\text{V-Ni}$) monolayer.

	a	mag static	a	mag static	thickness
VBr2	3.76 ^[1]	ABAB-AFM ^[1]	3.82	ZZ-AFM	3.029
CrBr2	3.74 ^[1]	ABAB-AFM ^[1]	3.79	ZZ-AFM	3.069
MnBr2	3.80 ^[1]	ABAB-AFM ^[1]	3.85	ZZ-AFM	3.093
FeBr2	3.63 ^[1]	FM ^[1]	3.72	ZZ-AFM	3.024
CoBr2	3.62 ^[1]	FM ^[1]	3.72	AABB-AFM	2.923
NiBr2	3.61 ^[1]	FM ^[1]	3.64	FM	2.8925
Ga ₂ SSe ₂	3.73 ^[2]	/	3.73	/	6.162

^[1]Journal of Materials Chemistry C, 2017, 5, 8734--8741.

^[2]Physical Review B, 2022, 105, 075402.

Table S3. The magnetic anisotropy energy per TM atom (meV) along x , y , z axis of $\text{TMBr}_2/\text{Ga}_2\text{SSe}_2-\text{P}\uparrow$ and $\text{TMBr}_2/\text{Ga}_2\text{SSe}_2-\text{P}\downarrow$ ($\text{TM}=\text{V-Ni}$) HSs.

	$x(\text{meV})$	$y(\text{meV})$	$z(\text{meV})$
$\text{VBr}_2/\text{Ga}_2\text{SSe}_2 -\text{P}\uparrow$	0	0.02	0
$\text{VBr}_2/\text{Ga}_2\text{SSe}_2 -\text{P}\downarrow$	0	0	0
$\text{CrBr}_2/\text{Ga}_2\text{SSe}_2 -\text{P}\uparrow$	-0.42	-0.13	0
$\text{CrBr}_2/\text{Ga}_2\text{SSe}_2 -\text{P}\downarrow$	-0.20	0.08	0
$\text{MnBr}_2/\text{Ga}_2\text{SSe}_2 -\text{P}\uparrow$	0.03	0.02	0
$\text{MnBr}_2/\text{Ga}_2\text{SSe}_2 -\text{P}\downarrow$	0	0	0
$\text{FeBr}_2/\text{Ga}_2\text{SSe}_2 -\text{P}\uparrow$	-1.98	7.36	0
$\text{FeBr}_2/\text{Ga}_2\text{SSe}_2 -\text{P}\downarrow$	-0.01	-0.08	0
$\text{CoBr}_2/\text{Ga}_2\text{SSe}_2 -\text{P}\uparrow$	-1.11	-1.26	0
$\text{CoBr}_2/\text{Ga}_2\text{SSe}_2 -\text{P}\downarrow$	-1.11	-1.27	0
$\text{NiBr}_2/\text{Ga}_2\text{SSe}_2 -\text{P}\uparrow$	0.05	0.06	0
$\text{NiBr}_2/\text{Ga}_2\text{SSe}_2 -\text{P}\downarrow$	-0.04	-0.03	0

Table S4. Magnetic ground states $\text{TMBr}_2/\text{Ga}_2\text{SSe}_2$ ($\text{TM}=\text{V, Cr, Fe}$) heterostructures under biaxial strains 4% with upward and downward ferroelectric polarization.

	$\varepsilon = -4\%$		$\varepsilon = +4\%$	
	$\text{P}\uparrow$	$\text{P}\downarrow$	$\text{P}\uparrow$	$\text{P}\downarrow$
V	AFM3	AFM3	AFM3	AFM3
Cr	AFM3	AFM3	FM	FM
Fe	AFM2	AFM3	AFM3	AFM3