Supporting information for

Optimizing the NRR activity of single and double boron atom catalysts using suitable support: A first principles investigation

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Fig. S1. Free energy profile for NRR on B_1 (a) *graphene along alternating, distal and enzymatic pathways.*





Fig. S2. Free energy profile for NRR on $B_1@GaN$, $B_1@MoS_2$, and $B_1@g-C_3N_4$ along alternating and distal pathways.



Fig. S3. Free energy profile for NRR on $B_2@$ graphyne and $B_{2@}MoS_2$ catalysts along alternating and distal pathways.





Fig. S4. Free energy profile for NRR on B_2 @graphene catalyst along alternating, distal and enzymatic pathways.



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Fig. S10. Truncated side views of the optimized NRR intermediates on B_2 @graphene catalyst along alternating, distal and enzymatic pathways. Green, red and cyan coloured arrows indicate alternating, distal, and enzymatic pathway respectively.



Fig. S11. Truncated side views of the optimized NRR intermediates on (a) B_1 @graphene (b) B_2 @graphene (c) B_1 @g- C_3N_4 and (d) B_2 @g- C_3N_4 catalysts along consecutive pathway.



Fig. S12. Dissociation barrier for the double boron atom catalysts supported on the $g-C_3N_4$ monolayer as obtained from nudged elastic band calculations.



Fig. S13. Variations of energy versus the AIMD simulation time for $B_2@g-C_3N_4$ at 350 K.



Fig. S14. Calculated adsorption free energies of N_2 molecule and H atom on the single and double boron atom adsorbed on GaN, graphene, $g-C_3N_4$, MoS_2 and graphyne supports.

Table S1. Energy, ZPE, TS, G and ΔG of reaction steps of NRR on $B_1@GaN$ and $B_1@MoS_2$ along alternating and distal pathway.

Reaction	Energy	ZPE	TS	G	ΔG
step					
*N ₂	-310.65	0.21	0.15	-310.59	-0.61
*NNH	-314.24	0.52	0.16	-313.88	-0.62
C*NHNH	-318.13	0.84	0.16	-317.44	-0.90
*NHNH ₂	-323.10	1.20	0.13	-322.03	-2.21
*NH ₂ NH ₂	-327.25	1.37	0.17	-326.05	-2.94
*NH ₂	-311.97	0.73	0.09	-311.33	-3.73
*NH ₃	-313.37	1.05	0.11	-312.43	-1.55

Alternating NRR pathway on B₁@GaN

Distal NRR pathway on B₁@GaN

Reaction	Energy	ZPE	TS	G	ΔG
step					
*N ₂	-310.65	0.21	0.15	-310.59	-0.61
*NNH	-314.24	0.52	0.16	-313.88	-0.62
*NNH ₂	-317.76	0.83	0.16	-317.09	-0.55
*N	-303.65	0.12	0.03	-303.57	-2.55
*NH	-306.95	0.37	0.12	-306.70	-2.39
*NH ₂	-311.97	0.73	0.09	-311.33	-3.73
*NH ₃	-313.37	1.05	0.11	-312.43	-1.55

Alternating pathway on B₁@MoS₂

Reaction Energy 2	ZPE	TS	G	ΔG
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step					
*N ₂	-579.91	0.22	0.13	-579.82	-0.01
*NNH	-583.41	0.52	0.14	-583.03	0.07
*NHNH	-587.28	0.85	0.14	-586.56	-0.18
*NHNH ₂	-592.06	1.18	0.18	-591.01	-1.35
*NH ₂ NH ₂	-594.60	1.53	0.17	-593.24	-0.29
*NH ₂	-581.12	0.74	0.07	-580.46	-3.03
*NH ₃	-583.69	1.09	0.09	-582.69	-1.97
*NH ₃	-583.69	1.09	0.09	-582.69	-1.97

Distal pathway on B₁@MoS₂

Reaction	Energy	ZPE	TS	G	ΔG
step					
*N ₂	-579.91	0.22	0.13	-579.82	-0.01
*NNH	-583.41	0.52	0.14	-583.03	0.07
*NNH ₂	-587.23	0.57	0.09	-586.76	-0.38
*N	-571.60	0.08	0.09	-571.60	-0.74
*NH	-576.62	0.28	0.002	-576.35	-2.20
*NH ₂	-581.12	0.74	0.07	-580.46	-3.02
*NH ₃	-583.69	1.09	0.09	-582.69	-1.97

Table S2. Energy, ZPE, TS, G and ΔG of reaction steps of NRR on B₁@graphene and B₁@g-C₃N₄ along alternating, distal and enzymatic pathway.

Alternating NRR pathway on B₁@graphene

Reaction	Energy	ZPE	TS	G	ΔG
step					
*N ₂	-483.26	0.21	0.15	-483.20	-1.41
*NNH	-487.19	0.52	0.15	-486.82	-1.76
*NHNH	-490.23	0.82	0.17	-489.58	-1.23
*NHNH ₂	-495.31	1.18	0.21	-494.34	-2.71
*NH ₂ NH ₂	-497.36	1.51	0.14	-495.99	-1.07
*NH ₂	-484.39	0.73	0.09	-483.75	-4.35
*NH ₃	-486.46	1.07	0.10	-485.49	-2.80
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Distal Pathway on B₁@graphene

Reaction	Energy	ZPE	TS	G	ΔG
step					
*N ₂	-483.26	0.21	0.15	-483.20	-1.41
*NNH	-487.19	0.52	0.15	-486.82	-1.76
*NNH ₂	-491.36	0.80	0.15	-490.70	-2.35
*N	-474.79	0.08	0.09	-474.79	-1.96
*NH	-480.48	0.38	0.10	-480.19	-4.07
*NH ₂	-484.39	0.73	0.09	-483.75	-4.35
*NH ₃	-486.46	1.07	0.10	-485.49	-2.80

Enzymatic pathway on B₁@graphene

Reaction	Energy	ZPE	TS	G	ΔG
step					
*N ₂	-482.99	0.20	0.13	-482.92	-1.14
*NNH	-486.61	0.47	0.15	-486.29	-1.22
*NHNH	-491.40	0.81	0.16	-490.76	-2.41
*NHNH ₂	-495.01	1.18	0.14	-493.97	-2.33
*NH ₂ NH ₂	-502.73	1.45	0.18	-501.46	-6.54
*NH ₂	-484.40	0.73	0.09	-483.75	-4.35
*NH ₃	-486.46	1.06	0.11	-485.50	-2.82

Alternating pathway on B₁@g-C₃N₄

Reaction	Energy	ZPE	TS	G	ΔG
step					
*N ₂	-497.56	0.23	0.11	-497.44	-2.63
*NNH	-500.92	0.51	0.13	-500.54	-2.45
*NHNH	-505.25	0.86	0.11	-504.50	-3.13
*NHNH ₂	-509.99	1.20	0.12	-508.91	-4.25
*NH ₂ NH ₂	-512.68	1.52	0.12	-511.28	-3.33
*NH ₂	-499.14	0.74	0.06	-498.45	-6.03
*NH ₃	-502.06	1.04	0.06	-501.08	-5.38

Distal pathway on B₁@g-C₃N₄

Reaction	Energy	ZPE	TS	G	ΔG
step					
*N ₂	-497.56	0.23	0.11	-497.44	-2.63
*NNH	-500.92	0.51	0.13	-500.54	-2.45
*NNH ₂					-3.35
	-505.44	0.85	0.13	-504.72	
*N	-488.26	0.084	0.06	-488.23	-2.38
*NH	-494.03	0.39	0.06	-493.69	-4.55
*NH ₂	-499.14	0.75	0.06	-498.45	-6.03
*NH ₃	-502.06	1.04	0.06	-501.08	-5.38

Enzymatic pathway on B₁@g-C₃N₄

Reaction	Energy	ZPE	TS	G	ΔG
step					
*N ₂	-497.42	0.21	0.10	-497.30	-2.50
*NNH	-500.50	0.48	0.12	-500.14	-2.05
*NHNH	-505.41	0.85	0.10	-504.66	-3.29
*NHNH ₂	-509.24	1.19	0.11	-508.17	-3.51
*NH ₂ NH ₂	-515.37	1.46	0.15	-514.06	-6.12
*NH ₂	-499.14	0.74	0.06	-498.45	-6.03
*NH ₃	-502.05	1.04	0.06	-501.08	-5.37

Table S3. Energy, ZPE, TS, G and ΔG of reaction steps of NRR on B₂@MoS₂ and B₂@graphyne along alternating, and distal pathway.

Reaction	Energy	ZPE	TS	G	ΔG
step					
*N ₂	-585.48	0.22	0.151758	-585.41	-2.07
*NNH	-588.72	0.49	0.183362	-588.41	-1.79
*NHNH	-592.13	0.85	0.18366	-591.47	-1.56
*NHNH ₂	-596.68	1.16	0.215264	-595.74	-2.55
*NH ₂ NH ₂	-599.70	1.53	0.196183	-598.37	-1.89
*NH ₂	-585.79	0.69	0.145497	-585.24	-4.28
*NH ₃	-588.65	1.07	0.121049	-587.70	-3.45

Alternating pathway on B₂@MoS₂

Distal pathway on B₂@MoS₂

Reaction	Energy	ZPE	TS	G	ΔG
step					
*N ₂	-585.48	0.22	0.15	-585.41	-2.07
*NNH	-588.72	0.49	0.18	-588.41	-1.79
*NNH ₂	-592.80	0.83	0.14	-592.11	-2.20
*N	-575.93	0.08	0.10	-575.95	-1.55
*NH	-581.75	0.38	0.10	-581.48	-3.80
*NH ₂	-585.79	0.69	0.15	-585.24	-4.28
*NH ₃	-588.65	1.07	0.12	-587.70	-3.45

Alternating pathway on B₂@graphyne

Reaction	Energy	ZPE	TS	G	ΔG
step					
*N ₂	-442.16	0.23	0.14	-442.07	-0.66
*NNH	-444.91	0.52	0.15	-444.55	0.15
*NHNH	-449.12	0.88	0.14	-448.38	-0.40
*NHNH ₂	-453.51	1.18	0.18	-452.52	-1.25
*NH ₂ NH ₂	-456.88	1.53	0.20	-455.55	-1.00
*NH ₂	-442.56	0.74	0.08	-441.89	-2.86
*NH ₃	-445.94	1.07	0.15	-444.98	-2.67

Distal pathway on B₂@graphyne

Reaction	Energy	ZPE	TS	G	ΔG
step					
*N ₂	-442.16	0.23	0.14	-442.07	-0.66
*NNH	-444.91	0.52	0.15	-444.55	0.15
*NNH ₂	-449.13	0.85	0.14	-448.13	-0.15
*N	-432.01	0.08	0.08	-431.85	0.62
*NH	-438.58	0.38	0.10	-438.10	-2.35
*NH ₂	-442.56	0.74	0.08	-441.89	-2.86
*NH ₃	-445.94	1.07	0.11	-444.98	-2.67

Table S4. Energy, ZPE, TS, G and ΔG of reaction steps of NRR on $B_2@g-C_3N_4$ along Enzymatic pathway.

Reaction	Energy	ZPE	TS	G	ΔG
step					
*N ₂	-504.25	0.22	0.07	-504.11	-1.60
*NNH	-508.43	0.54	0.08	-507.97	-2.18
*NHNH	-512.90	0.86	0.08	-512.12	-3.04
*NHNH ₂	-516.59	1.21	0.10	-515.48	-3.12
*NH ₂ NH ₂	-522.07	1.45	0.14	-520.75	-5.11
*NH ₂	-505.59	0.75	0.05	-504.88	-4.75
*NH ₃	-508.51	0.95	0.27	-507.83	-4.42

Enzymatic pathway on B₂@g-C₃N₄

Table S5. Energy, ZPE, TS, G and ΔG of reaction steps of NRR on B₂@graphene along alternating, distal and enzymatic pathway.

Reaction	Energy	ZPE	TS	G	ΔG
step					
*N ₂	-488.76	0.22	0.09	-488.63	-2.29
*NNH	-492.28	0.50	0.17	-491.95	-2.32
*NHNH	-495.58	0.84	0.18	-494.91	-2.00
*NHNH ₂	-500.06	1.16	0.21	-499.10	-2.90
*NH ₂ NH ₂	-502.57	1.51	0.19	-501.25	-1.76
*NH ₂	-489.20	0.68	0.10	-488.62	-4.65
*NH ₃	-491.45	1.07	0.10	-490.48	-3.23

Alternating pathway on B₂@graphene

Distal pathway on B₂@graphene

Reaction	Energy	ZPE	TS	G	ΔG
step					
*N ₂	-488.76	0.22	0.09	-488.63	-2.29
*NNH	-492.28	0.50	0.17	-491.95	-2.32
*NNH ₂	-496.68	0.85	0.18	-496.01	-3.10
*N	-479.81	0.08	0.11	-479.85	-2.45
*NH	-485.49	0.38	0.09	-485.20	-4.52
*NH ₂	-489.20	0.68	0.10	-488.62	-4.65
*NH ₃	-491.45	1.07	0.10	-490.48	-3.23

Enzymatic pathway on B₂@graphene

Reaction	Energy	ZPE	TS	G	ΔG
step					
*N ₂	-488.36	0.20	0.14	-488.31	-1.96
*NNH	-491.63	0.48	0.15	-491.31	-1.68
*NHNH	-496.33	0.82	0.15	-495.68	-2.75
*NHNH ₂	-499.91	1.16	0.20	-499.05	-2.85
*NH ₂ NH ₂	-507.35	1.44	0.19	-506.10	-6.62
*NH ₂	-489.21	0.70	0.12	-488.63	-4.66
*NH ₃	-491.10	1.05	0.14	-490.19	-2.94

Table S6. Energy, ZPE, TS, G and ΔG of reaction steps of NRR on B₁@graphene, B2@graphene, B1@g-C3N4 and B2@g-C3N4 catalysts along consecutive pathway.

Consecutive pathway on B₁@graphene

Reaction	Energy	ZPE	TS	G	ΔG
*N	482.00	0.20	0.12	182.02	1 1 /
· 1N2	-482.99	0.20	0.15	-482.92	-1.14
*NNH	-486.61	0.47	0.15	-486.29	-1.22
*NNH ₂	-491.28	0.85	0.15	-490.57	-2.22
*N	-474.80	0.08	0.09	-474.81	-1.97
*NH	-480.47	0.38	0.10	-480.18	-4.07
*NH ₂	-484.40	0.73	0.09	-483.75	-4.35
*NH ₃	-486.46	1.06	0.11	-485.50	-2.82

Consecutive pathway on B₂@graphene

Reaction	Energy	ZPE	TS	G	ΔG
step					
*N ₂	-488.36	0.20	0.14	-488.31	-1.96
*NNH	-491.63	0.48	0.15	-491.31	-1.68
*NNH ₂	-496.12	0.85	0.16	-495.43	-2.52
*N	-479.82	0.08	0.11	-479.85	-2.45
*NH	-485.49	0.38	0.09	-485.20	-4.52
*NH ₂	-489.21	0.70	0.12	-488.63	-4.66
*NH ₃	-491.10	1.05	0.14	-490.19	-2.94

Consecutive pathway on B₁@g-C₃N₄

Reaction	Energy	ZPE	TS	G	ΔG
step					
*N ₂	-497.42	0.21	0.10	-497.30	-2.50
*NNH	-500.50	0.48	0.12	-500.14	-2.05
*NNH ₂	-504.37	0.84	0.11	-503.64	-2.26
*N	-488.12	0.08	0.07	-488.11	-2.25
*NH	-494.05	0.40	0.06	-493.71	-4.57
*NH ₂	-499.14	0.74	0.06	-498.45	-6.03
*NH ₃	-502.05	1.04	0.06	-501.08	-5.37

Reaction	Energy	ZPE	TS	G	ΔG
step					
*N ₂	-504.25	0.22	0.07	-504.11	-1.60
*NNH	-508.43	0.54	0.08	-507.97	-2.18
*NNH ₂	-511.78	0.87	0.09	-511.00	-1.92
*N	-498.57	0.14	0.02	-498.45	-4.89
*NH	-502.75	0.45	0.02	-502.32	-5.47
*NH ₂	-505.59	0.75	0.05	-504.88	-4.75
*NH ₃	-508.51	0.95	0.27	-507.83	-4.42

Consecutive pathway on B₂@g-C₃N₄