Multiple Strategies of Improving Photocatalytic Water Splitting

Efficiency in 2D Arsenic Sesquichalcogenides

Xiaoteng Li^{1,*}, Chuanlu Yang^{1,*}, Yuliang Liu¹, Endao Han², Wenkai Zhao¹, Xinxin Jiang³, Dongqing Zou¹, Yuqing Xu¹

Carrier Mobility

The carrier mobility at room temperature is obtained based on deformation potential (DP) approach, the formula as follows¹:

$$\mu_{2D} = \frac{2e\hbar^{3}C}{3K_{B}T|m^{*}|^{2}E_{d}^{2}}$$

(S1)

 $C = (\partial^2 E / \partial \varepsilon^2) / S_0$ is the elastic modulus, where E is the whole energy and S_0 is the area of monolayers. E_d denotes the deformation potential constant, defined as

$$E_d = \partial E_{edge} / \partial \varepsilon$$
. Effective mass (m*) is determined as $m^* = \pm \hbar^2 (\frac{d^2 E_k}{dk^2})^{-1}$.

Table S1 Effective carrier masses (m^*), deformation potential constants (E_d), elastic moduli (C), and carrier mobility (μ) of As₂X₃ monolayers.

Materials	Carrier Type	m^{*}/m_{0}	<i>C</i> (N/m)	$E_{\rm d}({\rm eV})$	μ (cm ² V ⁻¹ s ⁻¹)
As_2O_3	Electrons (x)	0.92	26.05	3.80	0.31×10^{2}
	Hole (x)	0.91	20.95	2.96	0.53×10^{2}
	Electrons (y)	0.84	50.08	2.2	0.21×10^{3}
	Hole (y)	0.79	50.98	4.2	0.66×10^{2}
As_2S_3	Electrons (x)	0.52	40.74	2.53	0.33×10^{3}
	Hole (x)	0.49	40.74	3.69	0.18×10^{3}
	Electrons (y)	0.58	12 11	1.85	0.16×10^{3}
	Hole (y)	0.49	13.11	3.87	0.25×10^{2}
As ₂ Se ₃	Electrons (x)	0.47	52.6	1.82	1.01×10^{3}
	Hole (x)	0.43	52.0	3.42	0.35×10^{3}
	Electrons (y)	0.51	10.20	0.99	0.57×10^{3}

¹ College of physics and optoelectronic engineering, Ludong University, Yantai 264000, People's Republic of China

³ School of Physics, State Key Laboratory of Crystal Materials, Shandong University, Jinan 250100, People's Republic of China

² School of Physical and Mathematical Sciences, Nanyang Technological University, 50 Nanyang Avenue, 639798, Singapore

	Hole (y)	0.25		3.79	0.16×10^{3}
As ₂ Te ₃	Electrons (x)	0.12	65.00	2.02	$1.58 imes 10^4$
	Hole (x)	0.18	03.09	1.86	7.46×10^{3}
	Electrons (y)	s (y) 0.09 (5.49		10.11	1.13×10^{3}
	Hole (y)	0.18	03.48	5.46	0.96×10^{3}



Figure S1 The calculated total and atom projected DOS of As₂S₃. The Fermi energy is set to zero.



Figure S2 The crystal structures of N-doped, P-doped, and P-Se-codoped As_2S_3 monolayers.



Figure S3 Phonon dispersion spectra of (a) N-doped, (b) P-doped and (c) P-Se codoped As₂S₃

monolayers. (d)-(f) The corresponding AIMD energy fluctuations at 300 K. The insets of (d)-(f) are the snapshots of equilibrium structure after 3ps.



Figure S4 The projected band structures of N-, P-, Se- and P-Se doped As₂S₃ monolayers.



Figure S5 Top and side views of the crystal structures for (a) As_2STe_2 and (b) As_2SeTe_2 monolayers.



Figure S6 Phonon dispersion spectra of (a) As_2STe_2 and (b) As_2SeTe_2 monolayers. (c)-(d) The corresponding AIMD energy fluctuations at 300 K. The insets of (c)-(d) are the snapshots of equilibrium structure after 3ps.



Figure S7 The transfer charges of As₂STe₂ (As₂SeTe₂) monolayers.

The Gibbs free energy

The free energy of the absorbed states is calculated according to the formula²:

$$\Delta G = \Delta E + \Delta E_{ZPE} - T\Delta S \tag{S2}$$

where ΔE is the adsorption energy, ΔE_{ZPE} and ΔS represent the variations of the zeropoint energy and vibrational entropy between the adsorbed states and corresponding free-standing states, respectively. ΔE_{ZPE} is defined as:

$$E_{ZPE} = \frac{1}{2} \sum h\nu \tag{S3}$$

where ν stands for the vibrational frequency. TS is defined as:

$$TS = k_b T \left[\sum_{K} \ln \left(\frac{1}{1 - e^{-h\nu/k_b T}} \right) + \sum_{K} \frac{h\nu}{k_b T} \left(\frac{1}{e^{-h\nu/k_b T} - 1} + 1 \right) \right]$$
(S4)

Wherein, e, h and k_b represents the electron charge, Planck's constant and Boltzmann's constant. The value of T is 298.15K.

Here we take external potential and pH into account to evaluate the OER and HER activities. The HER process include two steps and the corresponding ΔG_{H^*} can be

expressed as:

1) * + H⁺ + e⁻
$$\rightarrow$$
 H^{*} (S5)

$$\Delta G_1 = G_{H^*} - \frac{1}{2}G_{H_2} - G_* + \Delta G_U + \Delta G_{pH}$$

$$= \Delta E_H + \Delta E_{ZPE(H)} - T\Delta S_H + \Delta G_U + \Delta G_{pH}$$

$$= \Delta G_H$$
(S6)

While the OER contains four elementary steps and the ΔG can be derived as follows:

2)
$$H_{2}O(l) + * \rightarrow OH^{*} + H^{+} + e^{-}$$
(S7)

$$\Delta G_{2} = G_{OH^{*}} + \frac{1}{2}G_{H_{2}} - G_{*} - G_{H_{2}O} + \Delta G_{U} - \Delta G_{pH}$$

$$= \Delta E_{OH} + \Delta E_{ZPE(OH)} - T\Delta S_{OH} + \Delta G_{U} - \Delta G_{pH}$$

$$= \Delta G_{OH}$$
(S8)

3)
$$OH^* \to O^* + H^+ + e^-$$
 (S9)

$$\Delta G_3 = G_{O^*} + \frac{1}{2}G_{H_2} - G_{OH^*} + \Delta G_U - \Delta G_{pH}$$

= $(\Delta E_O + \Delta E_{ZPE(O)} - T\Delta S_O + 2\Delta G_U - 2\Delta G_{pH}) - (\Delta E_{OH} + \Delta E_{ZPE(OH)} - \Delta G_U - \Delta G_{pH})$

$$=\Delta G_0 - \Delta G_{0H} \tag{S10}$$

4)
$$H_{2}O(l) + O^{*} \rightarrow OOH^{*} + H^{+} + e^{-}$$
(S11)

$$\Delta G_{4} = G_{OOH^{*}} + \frac{1}{2}G_{H_{2}} - G_{O^{*}} - G_{H_{2}O} + \Delta G_{U} - \Delta G_{pH}$$

$$= (\Delta E_{OOH} + \Delta E_{ZPE(OOH)} - T\Delta S_{OOH} + 3\Delta G_{U} - 3\Delta G_{pH}) - (\Delta E_{O} + \Delta S_{O} + 2\Delta G_{U} - 2\Delta G_{pH})$$

$$=\Delta G_{00H} - \Delta G_0 \tag{S12}$$

5)
$$\operatorname{OOH}^* \to *+ \ O_2(g) + \operatorname{H}^+ + e^-$$
 (S13)
$$\Delta G_5 = G_* + \frac{1}{2}G_{H_2} + G_{O_2} - G_{OOH^*} + \Delta G_U - \Delta G_{pH}$$

$$= (4.92 + 4\Delta G_U - 4\Delta G_{pH}) - (\Delta E_{OOH} + \Delta E_{ZPE(OOH)} - T\Delta S_{OOH} + 3\Delta G_U)$$

$$= (4.92 + 4\Delta G_U - 4\Delta G_{pH}) - \Delta G_{OOH}$$
(S14)

wherein, $\Delta G_U = -eU$, denotes extra potential bias provided by an electron in the electrode, where *U* represents the potential difference from the standard hydrogen electrode potential. ΔG_{pH} is the pH-dependent ΔG , and the corresponding formula is $\Delta G_{pH} = k_b T \times ln10 \times _{pH}$.

Solar-to-hydrogen (STH) efficiency

The efficiency of light absorption (η_{abs}) is defined as³:

$$\eta_{abs} = \frac{\int_{E_g}^{\infty} P(\hbar\omega) d(\hbar\omega)}{\int_{0}^{\infty} P(\hbar\omega) d(\hbar\omega)}$$

(S17)

where E_g is the band gap of semiconductors and $P(\hbar\omega)$ is the AM1.5 solar energy flux at the photon energy $\hbar\omega$. The efficiency of carrier utilization (η_{cu}) is calculated by the formula:

$$\eta_{cu} = \frac{\Delta G_{H_2 O} \int_{E}^{\infty} \frac{P(\hbar\omega)}{\hbar\omega} d(\hbar\omega)}{\int_{E_g}^{\infty} P(\hbar\omega) d(\hbar\omega)}$$
(S18)

where ${}^{\Delta G_{H_2 0}}$ is the redox potential difference of H₂O (1.23 eV) and *E* is the photons energy which can be fully used for water splitting. *E* can be defined as:

$$E = \begin{cases} E_g , \ (\chi(H_2) \ge 0.2, \chi(O_2) \ge 0.6) \\ E_g + 0.2 - \chi(H_2) , \ (\chi(H_2) < 0.2, \chi(O_2) \ge 0.6) \\ E_g + 0.6 - \chi(O_2) , \ (\chi(H_2) \ge 0.2, \chi(O_2) < 0.6) \\ E_g + 0.8 - \chi(H_2) - \chi(O_2) , \ (\chi(H_2) < 0.2, \chi(O_2) < 0.6) \end{cases}$$
(S19)

where $\chi(H_2)$ and $\chi(O_2)$ represent the overpotentials of HER and OER, respectively. Then the STH efficiency is defined as:

$$\eta_{STH} = \eta_{abs} \times \eta_{cu} \tag{S20}$$

When the photocatalysts possess internal electric filed, the STH efficiency will be corrected to:

$$\eta'_{STH} = \eta_{STH} \times \frac{\int_{0}^{\infty} P(\hbar\omega) d(\hbar\omega)}{\Delta \Phi \int_{E_{g}}^{\infty} \frac{P(\hbar\omega)}{\hbar\omega} d(\hbar\omega) + \int_{0}^{\infty} P(\hbar\omega) d(\hbar\omega)}$$

(S21)

where $\Delta \Phi$ is the vacuum level difference between the two respective surfaces.

Table S2 The overpotentials for HER (χ (H₂)) and OER (χ (O₂)), the photons energy (*E*), the efficiency of light absorption (η_{abs}) and carrier utilization (η_{cu}), and corrected STH (η'_{STH}).

Materials	$\chi(H_2)(eV)$	$\chi(O_2)(eV)$	E(eV)	$\eta_{ m abs}(\%)$	$\eta_{ m cu}(\%)$	$\eta'_{ m STH}(\%)$
As ₂ STe ₂	0.33	0.51	1.10	84.67	64.21	36.19
As ₂ SeTe ₂	0.19	0.13	1.45	87.19	43.61	29.36

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