

Enhancement of weak ferromagnetism, exotic structure prediction and diverse electronic properties in holmium substituted multiferroic bismuth ferrite

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Supporting Information

Supporting Tables

Table S1. Structural parameters of the samples doped with 2%, 5% and 10% Ho studied by powder X-ray diffraction and the data were refined by the Rietveld method.

	BHFO-2	BHFO-5	BHFO-10
Empirical formula	$\text{Bi}_{5.88}\text{Ho}_{0.12}\text{Fe}_6\text{O}_{12}$	$\text{Bi}_{5.70}\text{Ho}_{0.30}\text{Fe}_6\text{O}_{12}$	$\text{Bi}_{5.40}\text{Ho}_{0.60}\text{Fe}_6\text{O}_{12}$
Crystal system	Trigonal (hexagonal axes)	Trigonal (hexagonal axes)	Trigonal (hexagonal axes)
Space group	$R3c$	$R3c$	$R3c$
$a/\text{\AA}$	5.6082(7)	5.5870(6)	5.5800(7)
$c/\text{\AA}$	13.9253(9)	13.8873(8)	13.8739(8)
Agreement parameters			
$R_{\text{wp}}/\%$	10.3	14.1	11.2
$R_{\text{p}}/\%$	8.1	11.9	9.8
$R_{\text{exp}}/\%$	7.1	10.2	8.1
Refined atomic coordinates			
O (x)	0.438(3)	0.441(3)	0.445(3)
(y)	0.016(2)	0.015(2)	0.019(3)
(z)	0.948(5)	0.943(4)	0.951(5)
Bi/Ho (z)	0.223(1)	0.228(2)	0.226(1)

Table S2. Calculated values of the global instability index (GII) and tilt system of the most promising $\text{Bi}_{0.98}\text{Ho}_{0.02}\text{FeO}_3$ modifications using the bond valence (BVC) method.

Modification	Space group	Tilt system	GII
$\beta\text{-Bi}_{0.98}\text{Ho}_{0.02}\text{FeO}_3$	<i>Pnma</i>	$a^-b^+a^-$	0.03816
$R\text{-Bi}_{0.98}\text{Ho}_{0.02}\text{FeO}_3$	<i>R-3c</i>	$a^-a^-a^-$	0.04284
$T_1\text{-Bi}_{0.98}\text{Ho}_{0.02}\text{FeO}_3$	<i>P4/mbm</i>	$a^0a^0c^-$	0.08938
$T_2\text{-Bi}_{0.98}\text{Ho}_{0.02}\text{FeO}_3$	<i>I4/mcm</i>	$a^0a^0c^-$	0.08938
$\gamma\text{-Bi}_{0.98}\text{Ho}_{0.02}\text{FeO}_3$	<i>Pm-3m</i>	$a^0a^0a^0$	0.72910

Table S3. Structural data of the most promising $\text{Bi}_{0.98}\text{Ho}_{0.02}\text{FeO}_3$ perovskite modifications calculated using the BVC method.

Modification, space group and Wyckoff position	Cell parameters(Å), unit-cell volume (Å ³) and fractional coordinates
$\beta\text{-Bi}_{0.98}\text{Ho}_{0.02}\text{FeO}_3$ <i>Pnma</i> (62) Bi 4 <i>c</i> Ho 4 <i>c</i> Fe 4 <i>b</i> O1 4 <i>c</i> O2 8 <i>d</i>	$a=5.60, b=7.76, c=5.39$ $V=234.55$ 0.5599 1/4 0.5207 0.5599 1/4 0.5207 1/2 0 0 -0.0181 1/4 0.4013 0.2958 0.0494 0.7006
$R\text{-Bi}_{0.98}\text{Ho}_{0.02}\text{FeO}_3$ $\bar{R}3c$ (167) Bi 6 <i>a</i> Ho 6 <i>a</i> Fe1 6 <i>b</i> O 18 <i>e</i>	$a=5.44, c=13.96$ $V=357.56$ 0 0 1/4 0 0 1/4 2/3 1/3 1/3 0.4091 0 1/4
$T_1\text{-Bi}_{0.98}\text{Ho}_{0.02}\text{FeO}_3$ <i>P4/mbm</i> (127) Bi 2 <i>c</i> Ho 2 <i>c</i> Fe 2 <i>a</i> O1 2 <i>b</i>	$a=5.36, c=4.03$ $V=115.73$ 0 1/2 1/2 0 1/2 1/2 0 0 0 0 0 1/2

O2 4g	0.1592 0.6592 0
T_2 -Bi _{0.98} Ho _{0.02} FeO ₃	$a=5.36, c=8.06$
<i>I4/mcm</i> (140)	$V=231.45$
Bi 4b	0 1/2 1/4
Ho 4b	0 1/2 1/4
Fe 4c	0 0 0
O1 4a	0 0 1/4
O2 8h	0.3408 0.8408 0
γ -Bi _{0.98} Ho _{0.02} FeO ₃	$a=4.03$
<i>Pm-3m</i> (221)	$V=65.50$
Bi 1b	1/2 1/2 1/2
Ho 1b	1/2 1/2 1/2
Fe 1a	0 0 0
O 3d	0 0 1/2

Table S4. Calculated values of the global instability index (GII) and tilt system of the most promising Bi_{0.95}Ho_{0.05}FeO₃ modifications using the bond valence (BVC) method.

Modification	Space group	Tilt system	GII
β -Bi _{0.95} Ho _{0.05} FeO ₃	<i>Pnma</i>	a ⁺ b ⁺ a ⁻	0.05815
<i>R</i> -Bi _{0.95} Ho _{0.05} FeO ₃	<i>R-3c</i>	a ⁻ a ⁻ a ⁻	0.06113
T_1 -Bi _{0.95} Ho _{0.05} FeO ₃	<i>P4/mbm</i>	a ⁰ a ⁰ c ⁻	0.09992
T_2 -Bi _{0.95} Ho _{0.05} FeO ₃	<i>I4/mcm</i>	a ⁰ a ⁰ c ⁻	0.09992
γ -Bi _{0.95} Ho _{0.05} FeO ₃	<i>Pm-3m</i>	a ⁰ a ⁰ a ⁰	0.73225

Table S5. Structural data of the most promising Bi_{0.95}Ho_{0.05}FeO₃ perovskite modifications calculated using the BVC method.

Modification, space group and Wyckoff position	Cell parameters(Å), unit-cell volume (Å ³) and fractional coordinates
β -Bi _{0.95} Ho _{0.05} FeO ₃	$a=5.59, b=7.76, c=5.39$
<i>Pnma</i> (62)	$V=234.33$
Bi 4c	0.5604 1/4 0.5209
Ho 4c	0.5604 1/4 0.5209
Fe 4b	1/2 0 0
O1 4c	-0.0182 1/4 0.4008
O2 8d	0.2960 0.0496 0.7004

$R\text{-Bi}_{0.95}\text{Ho}_{0.05}\text{FeO}_3$ <i>R-3c</i> (167) Bi 6 <i>a</i> Ho 6 <i>a</i> Fe1 6 <i>b</i> O 18 <i>e</i>	$a=5.44, c=13.96$ $V=357.36$ 0 0 1/4 0 0 1/4 2/3 1/3 1/3 0.5911 0 1/4
$T_1\text{-Bi}_{0.95}\text{Ho}_{0.05}\text{FeO}_3$ <i>P4/mbm</i> (127) Bi 2 <i>c</i> Ho 2 <i>c</i> Fe 2 <i>a</i> O1 2 <i>b</i> O2 4 <i>g</i>	$a=5.36, c=4.03$ $V=115.63$ 0 1/2 1/2 0 1/2 1/2 0 0 0 0 0 1/2 0.1589 0.6589 0
$T_2\text{-Bi}_{0.95}\text{Ho}_{0.05}\text{FeO}_3$ <i>I4/mcm</i> (140) Bi 4 <i>b</i> Ho 4 <i>b</i> Fe 4 <i>c</i> O1 4 <i>a</i> O2 8 <i>h</i>	$a=5.36, c=8.06$ $V=231.25$ 0 1/2 1/4 0 1/2 1/4 0 0 0 0 0 1/4 0.3411 0.8411 0
$\gamma\text{-Bi}_{0.95}\text{Ho}_{0.05}\text{FeO}_3$ <i>Pm-3m</i> (221) Bi 1 <i>b</i> Ho 1 <i>b</i> Fe 1 <i>a</i> O 3 <i>d</i>	$a=4.03$ $V=65.50$ 1/2 1/2 1/2 1/2 1/2 1/2 0 0 0 0 0 1/2

Table S6. Calculated values of the global instability index (GII) and tilt system of the most promising $\text{Bi}_{0.9}\text{Ho}_{0.1}\text{FeO}_3$ modifications using the bond valence (BVC) method.

Modification	Space group	Tilt system	GII
$\beta\text{-Bi}_{0.9}\text{Ho}_{0.1}\text{FeO}_3$	<i>Pnma</i>	$a^-b^+a^-$	0.08023
$R\text{-Bi}_{0.9}\text{Ho}_{0.1}\text{FeO}_3$	<i>R-3c</i>	$a^-a^-a^-$	0.08226
$T_1\text{-Bi}_{0.9}\text{Ho}_{0.1}\text{FeO}_3$	<i>P4/mbm</i>	$a^0a^0c^-$	0.11480
$T_2\text{-Bi}_{0.9}\text{Ho}_{0.1}\text{FeO}_3$	<i>I4/mcm</i>	$a^0a^0c^-$	0.11480
$\gamma\text{-Bi}_{0.9}\text{Ho}_{0.1}\text{FeO}_3$	<i>Pm-3m</i>	$a^0a^0a^0$	0.73746

Table S7. Structural data of the most promising Bi_{0.9}Ho_{0.1}FeO₃ perovskite modifications calculated using the BVC method.

Modification, space group and Wyckoff position	Cell parameters(Å), unit-cell volume (Å³) and fractional coordinates
<i>β</i> -Bi _{0.9} Ho _{0.1} FeO ₃ <i>Pnma</i> (62) Bi 4 <i>c</i> Ho 4 <i>c</i> Fe 4 <i>b</i> O1 4 <i>c</i> O2 8 <i>d</i>	<i>a</i> =5.60, <i>b</i> =7.76, <i>c</i> =5.39 <i>V</i> =233.93 0.5613 1/4 0.5212 0.5613 1/4 0.5212 1/2 0 0 -0.0185 1/4 0.4000 0.2963 0.0500 0.7000
<i>R</i> -Bi _{0.9} Ho _{0.1} FeO ₃ <i>R-3c</i> (167) Bi 6 <i>a</i> Ho 6 <i>a</i> Fe1 6 <i>b</i> O 18 <i>e</i>	<i>a</i> =5.43, <i>c</i> =13.96 <i>V</i> =357.05 0 0 1/4 0 0 1/4 2/3 1/3 1/3 0.5916 0 1/4
<i>T</i> ₁ -Bi _{0.9} Ho _{0.1} FeO ₃ <i>P4/mbm</i> (127) Bi 2 <i>c</i> Ho 2 <i>c</i> Fe 2 <i>a</i> O1 2 <i>b</i> O2 4 <i>g</i>	<i>a</i> =5.35, <i>c</i> =4.03 <i>V</i> =115.45 0 1/2 1/2 0 1/2 1/2 0 0 0 0 0 1/2 0.1583 0.6583 0
<i>T</i> ₂ -Bi _{0.9} Ho _{0.1} FeO ₃ <i>I4/mcm</i> (140) Bi 4 <i>b</i> Ho 4 <i>b</i> Fe 4 <i>c</i> O1 4 <i>a</i> O2 8 <i>h</i>	<i>a</i> =5.35, <i>c</i> =8.06 <i>V</i> =230.91 0 1/2 1/4 0 1/2 1/4 0 0 0 0 0 1/4 0.3417 0.8417 0
<i>γ</i> -Bi _{0.9} Ho _{0.1} FeO ₃ <i>Pm-3m</i> (221) Bi 1 <i>b</i> Ho 1 <i>b</i> Fe 1 <i>a</i> O 3 <i>d</i>	<i>a</i> =4.03 <i>V</i> =65.50 1/2 1/2 1/2 1/2 1/2 1/2 0 0 0 0 0 1/2

Supporting Figures

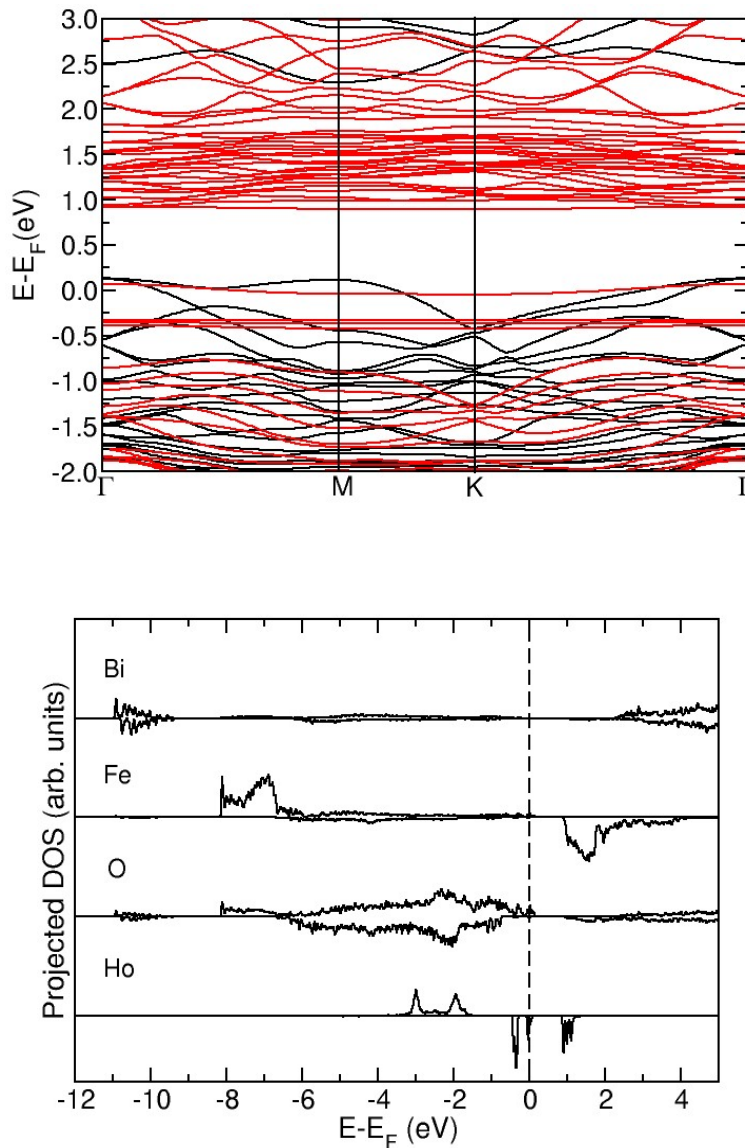


Figure S1. Electro-magnetic properties of the half-metallic **alpha FM** structure: a) Band structure along lines between high symmetry points. Black lines present spin-up and red line spin-down bands; b) Element-resolved density of states (DOS). Mirrored graphs correspond to spin-up and spin-down states. Alpha FM has a relatively small gap of ~ 0.9 eV with an asymmetry of dispersion of valence (large dispersion) and conduction (small dispersion, flat band). Suitable for. e.g. application as a switch.

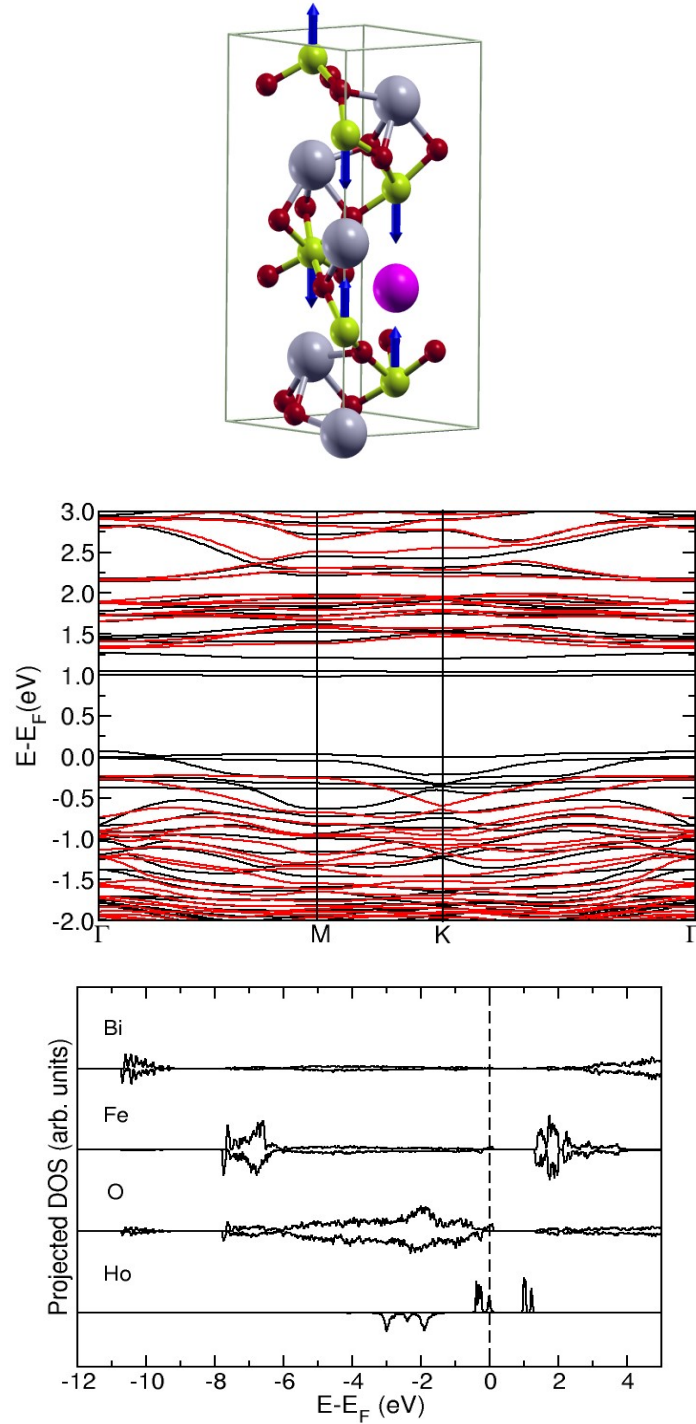


Figure S2. Electro-magnetic properties of the half-metallic **alpha AFM1** structure: a) Calculation cell with spin texture marked by the blue arrows; b) Band structure along lines between high symmetry points. Black lines present spin-up and red line spin-down bands; c) Element-resolved density of states (DOS). Mirrored graphs correspond to spin-up and spin-down states.

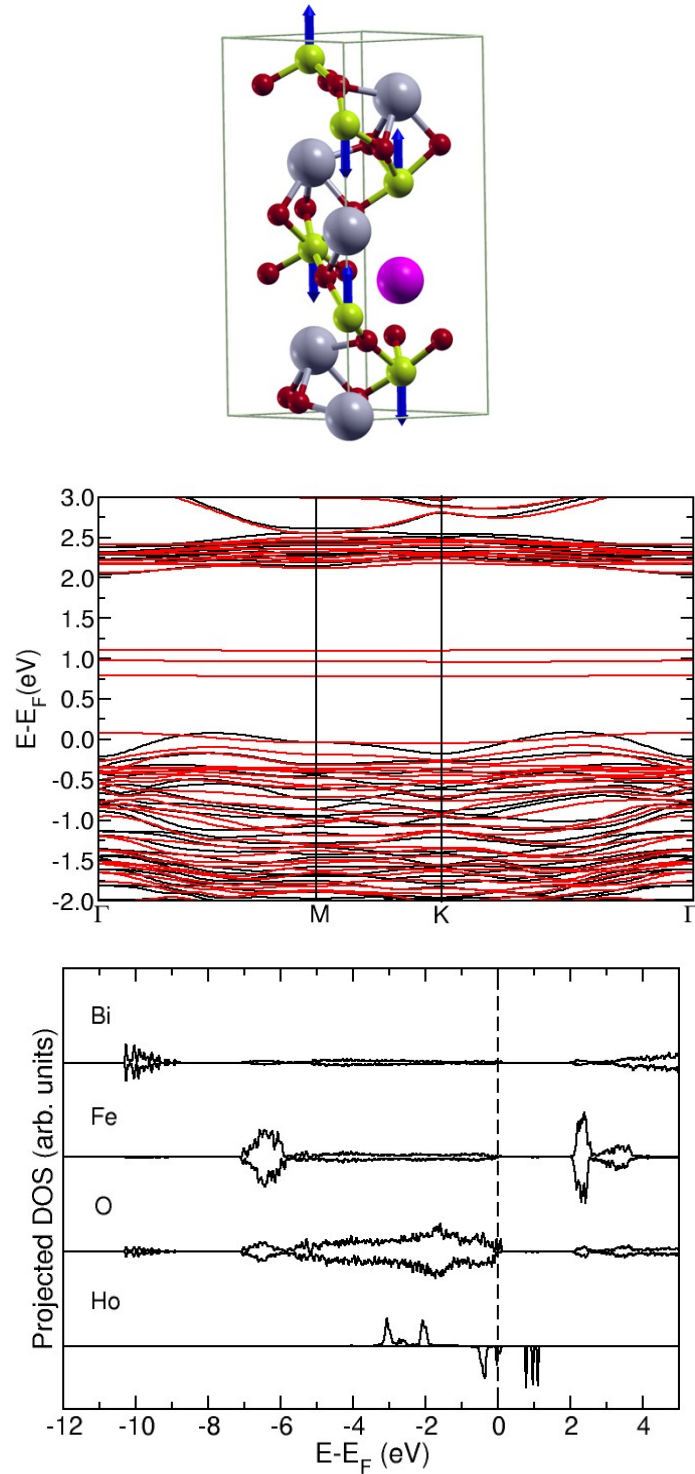


Figure S3. Electro-magnetic properties of the **α AFM2** structure: a) Calculation cell with spin texture marked by the blue arrows; b) Band structure along lines between high symmetry points. Black lines present spin-up and red line spin-down bands; c) Element-resolved density of states (DOS). Mirrored graphs correspond to spin-up and spin-down states.

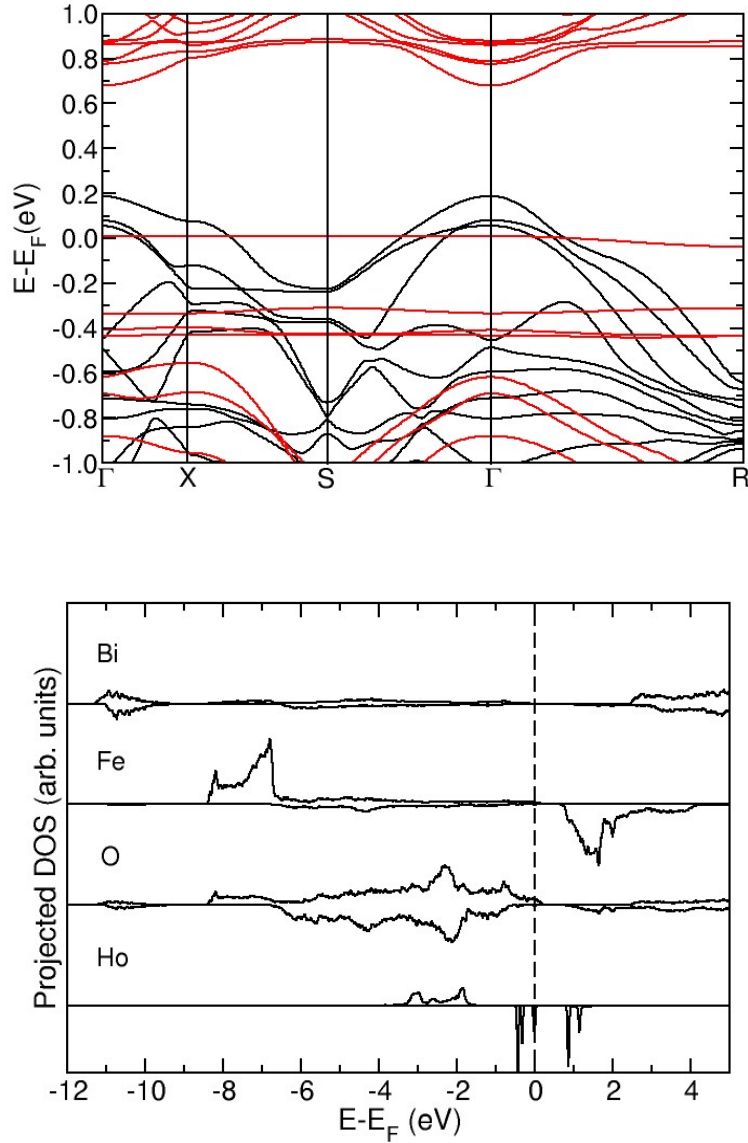


Figure S4. Electro-magnetic properties of the half-metallic **beta FM** structure: a) Band structure along lines between high symmetry points. Black lines present spin-up and red line spin-down bands; b) Element-resolved density of states (DOS). Mirrored graphs correspond to spin-up and spin-down states.

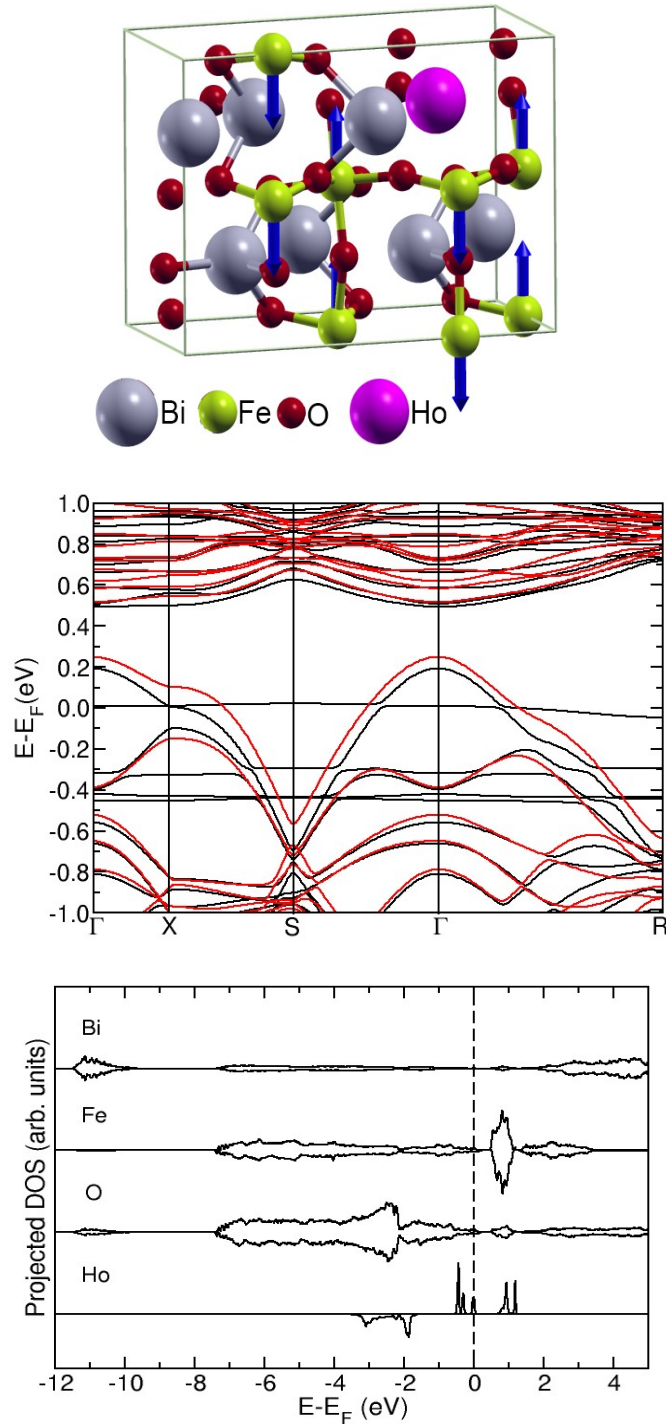


Figure S5. Electro-magnetic properties of the **beta AFM1** structure: a) Calculation cell with spin texture marked by the blue arrows; b) Band structure along lines between high symmetry points. Black lines present spin-up and red line spin-down bands; c) Element-resolved density of states (DOS). Mirrored graphs correspond to spin-up and spin-down states. Beta AFM1 has a dispersive valence band while the conduction band has a relatively small dispersion. This finding together with the small band gap indicates that beta AFM1 is suitable for application as a switch.

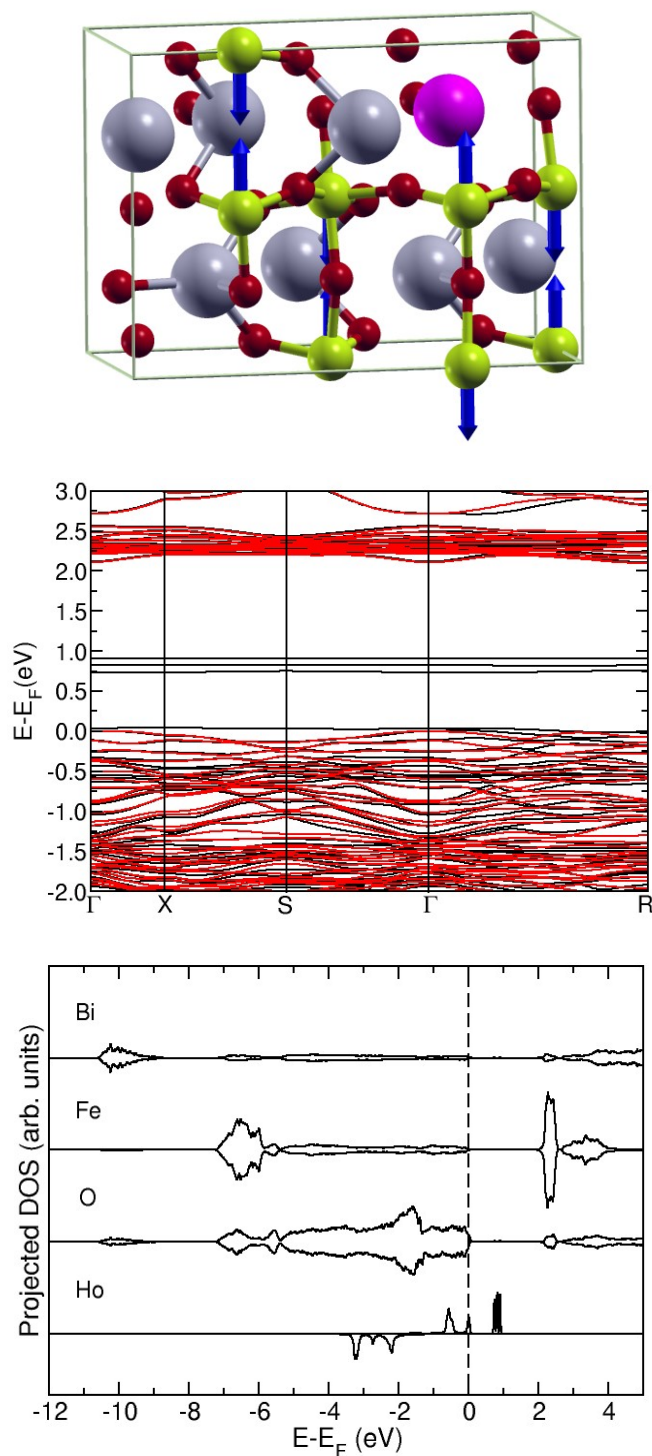


Figure S6. Electro-magnetic properties of the **beta AFM2** structure: a) Calculation cell with spin texture marked by the blue arrows; b) Band structure along lines between high symmetry points. Black lines present spin-up and red line spin-down bands; c) Element-resolved density of states (DOS). Mirrored graphs correspond to spin-up and spin-down states. Both beta AFM1 and AFM2 structures appear as semiconductors with beta AFM1 direct band gap of 0.2-1.70 eV and dispersion

of 1.70 eV, while beta AFM2 type shows a direct band gap of 2 eV and dispersion of valence bands of only 0.15 eV (Table 2 and supporting Figures).

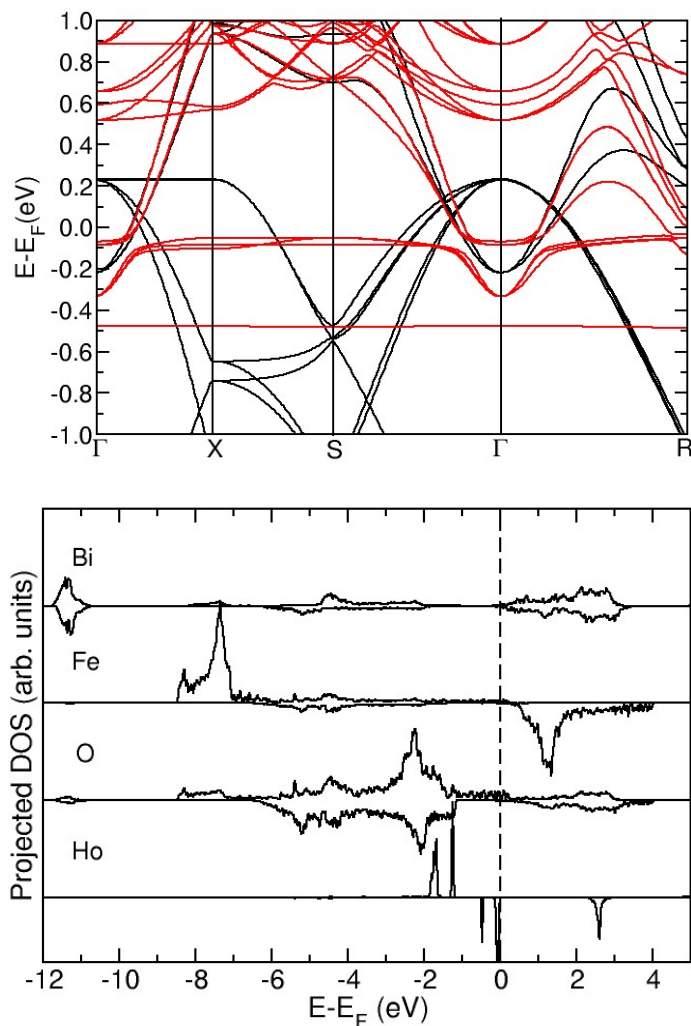


Figure S7. Electro-magnetic properties of the **gamma FM** structure: a) Band structure along lines between high symmetry points. Black lines present spin-up and red line spin-down bands; b) Element-resolved density of states (DOS). Mirrored graphs correspond to spin-up and spin-down states.

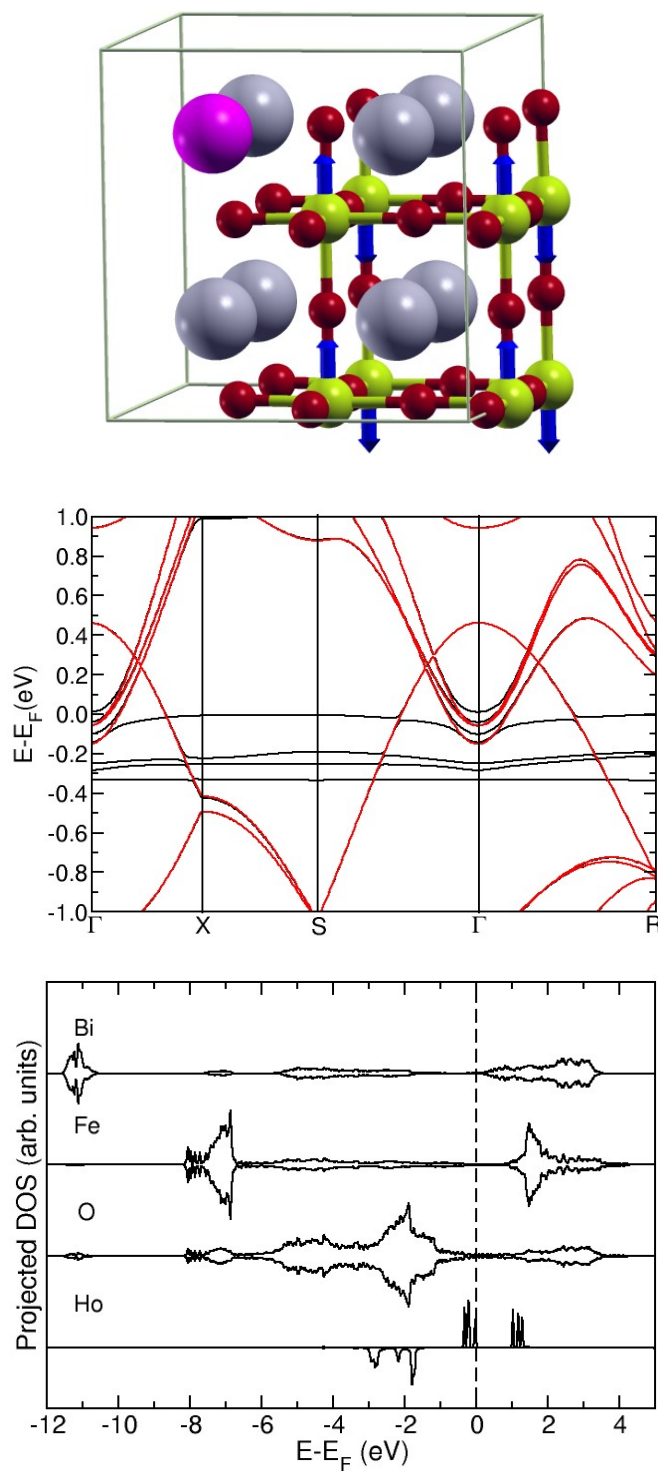


Figure S8. Electro-magnetic properties of the semimetallic **γ AFM1** structure: a) Calculation cell with spin texture marked by the blue arrows; b) Band structure along lines between high symmetry points. Black lines present spin-up and red line spin-down bands; c) Element-resolved density of states (DOS). Mirrored graphs correspond to spin-up and spin-down states.

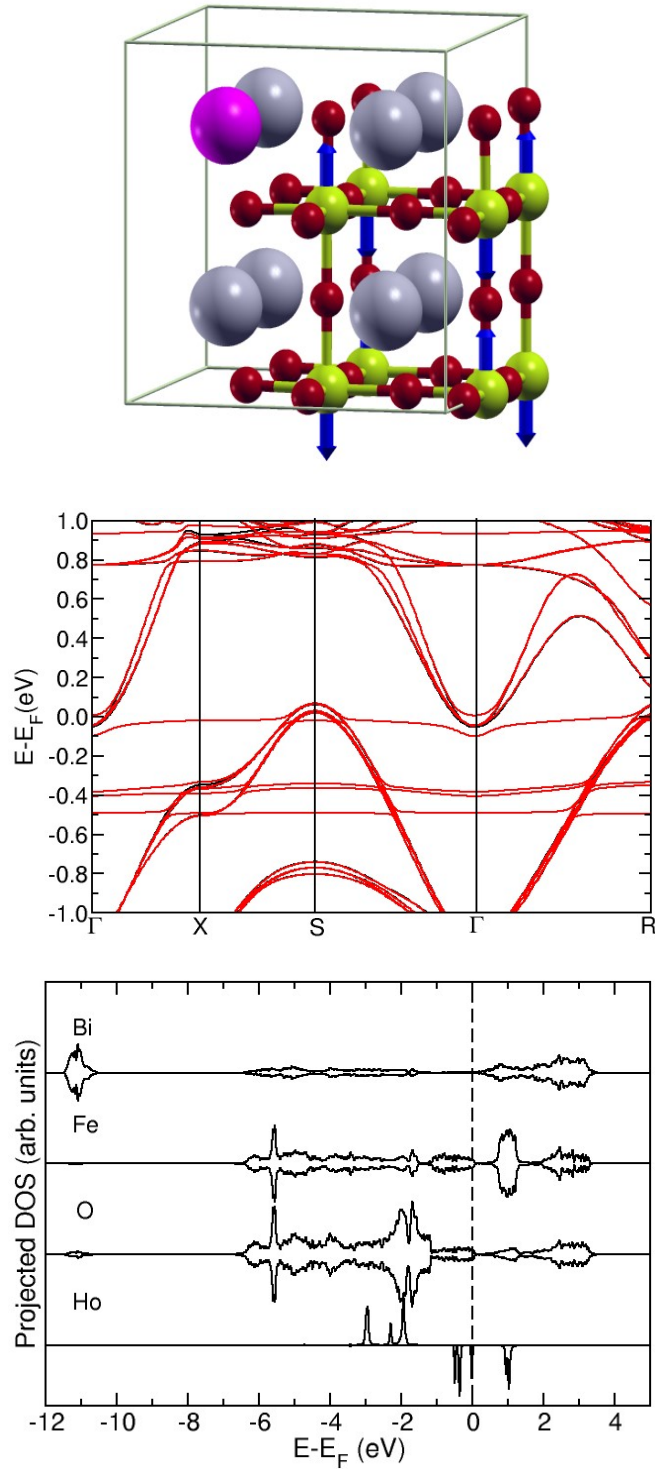


Figure S9. Electro-magnetic properties of the semimetallic **γ AFM2** structure: a) Calculation cell with spin texture marked by the blue arrows; b) Band structure along lines between high symmetry points. Black lines present spin-up and red line spin-down bands; c) Element-resolved density of states (DOS). Mirrored graphs correspond to spin-up and spin-down states.

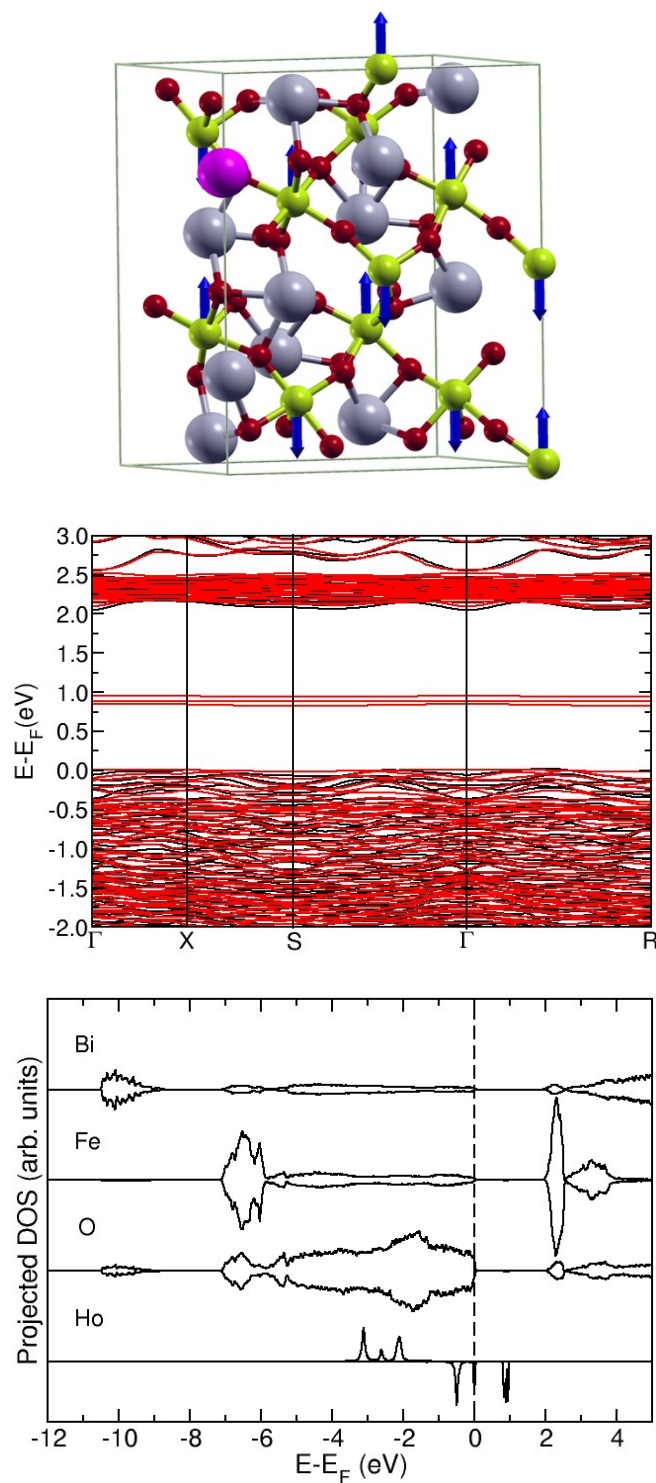


Figure S9. Electro-magnetic properties of the **R-type AFM1** structure: a) Calculation cell with spin texture marked by the blue arrows; b) Band structure along lines between high symmetry points. Black lines present spin-up and red line spin-down bands; c) Element-resolved density of states (DOS). Mirrored graphs correspond to spin-up and spin-down states.

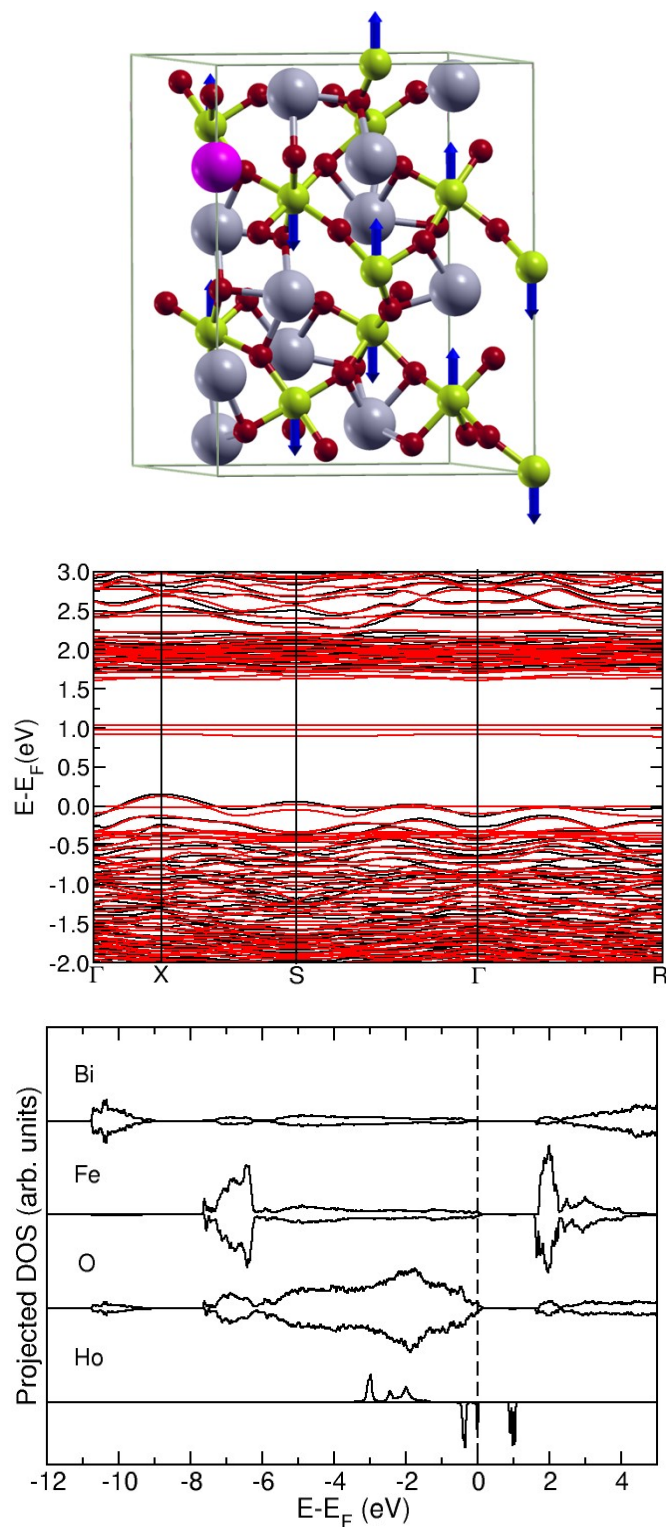


Figure S10. Electro-magnetic properties of the **R-type AFM2** structure: a) Calculation cell with spin texture marked by the blue arrows; b) Band structure along lines between high symmetry points. Black lines present spin-up and red line spin-down bands; c) Element-resolved density of states (DOS). Mirrored graphs correspond to spin-up and spin-down states.

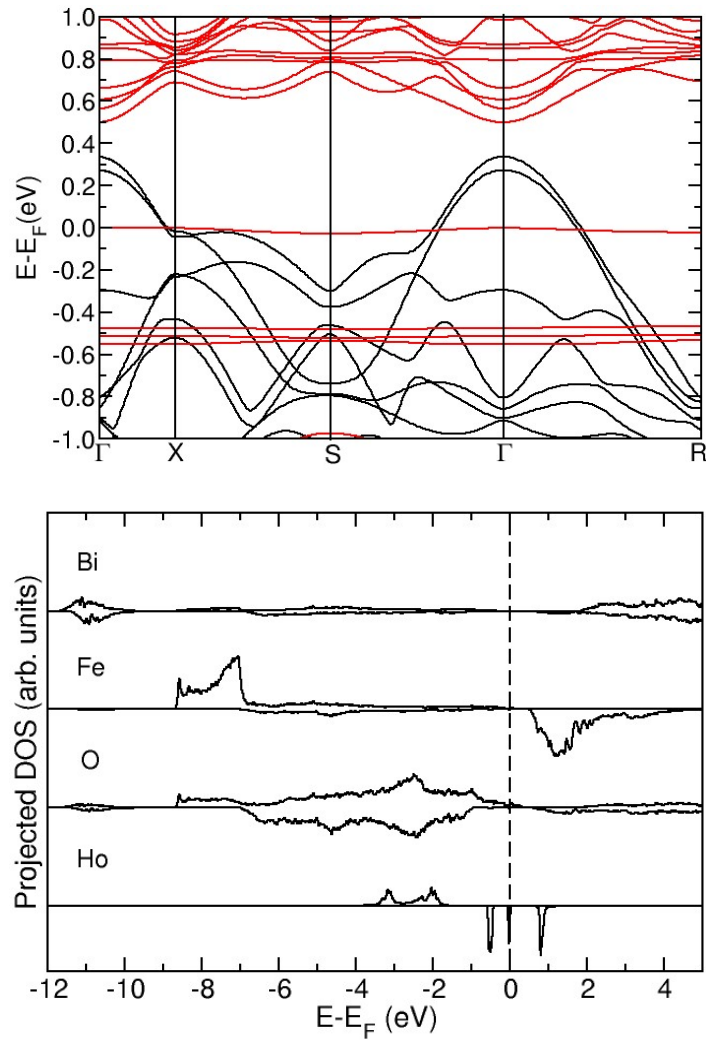


Figure S11. Electro-magnetic properties of the half-metallic **T1-type FM** structure: a) Band structure along lines between high symmetry points. Black lines present spin-up and red line spin-down bands; b) Element-resolved density of states (DOS). Mirrored graphs correspond to spin-up and spin-down states.

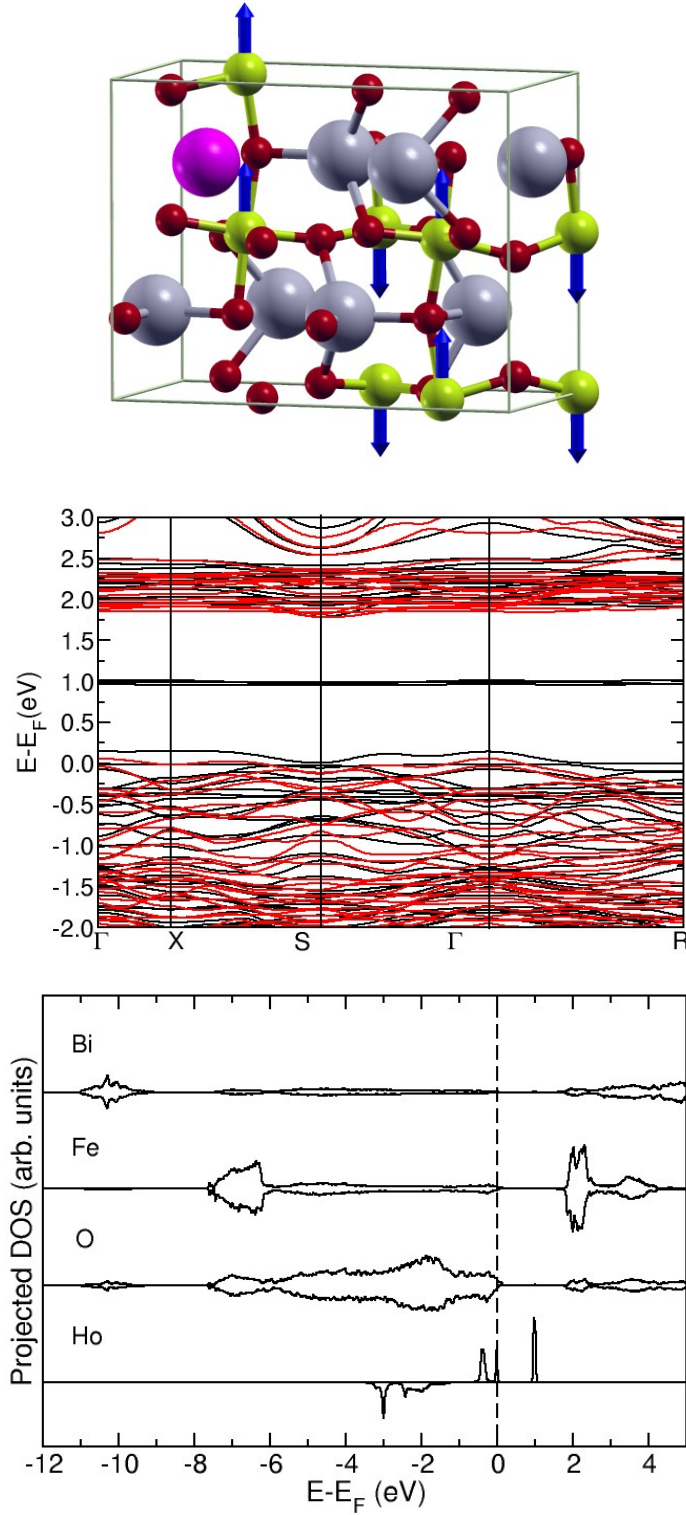


Figure S12. Electro-magnetic properties of the **T1-type AFM1** structure: a) Calculation cell with spin texture marked by the blue arrows; b) Band structure along lines between high symmetry points. Black lines present spin-up and red line spin-down bands; c) Element-resolved density of states (DOS). Mirrored graphs correspond to spin-up and spin-down states.

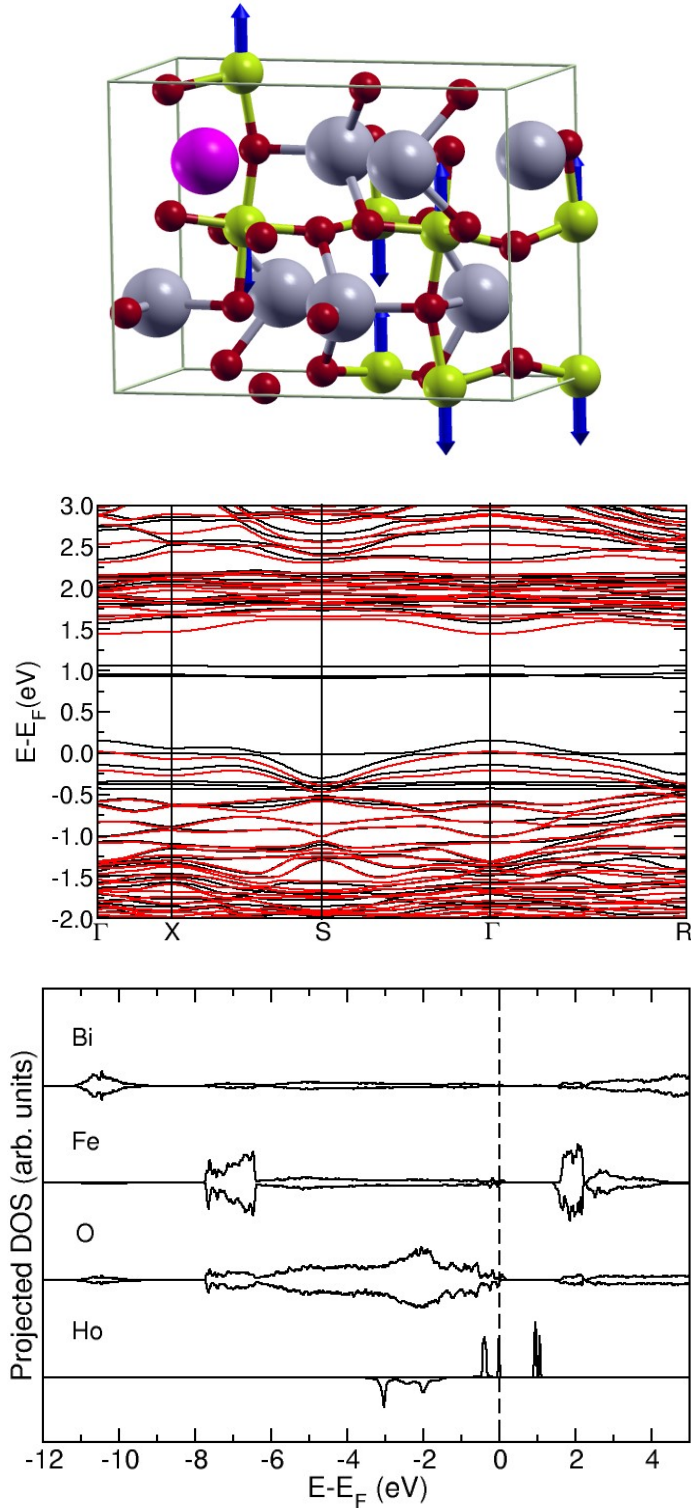


Figure S13. Electro-magnetic properties of the **T1-type AFM2** structure: a) Calculation cell with spin texture marked by the blue arrows; b) Band structure along lines between high symmetry points. Black lines present spin-up and red line spin-down bands; c) Element-resolved density of states (DOS). Mirrored graphs correspond to spin-up and spin-down states.

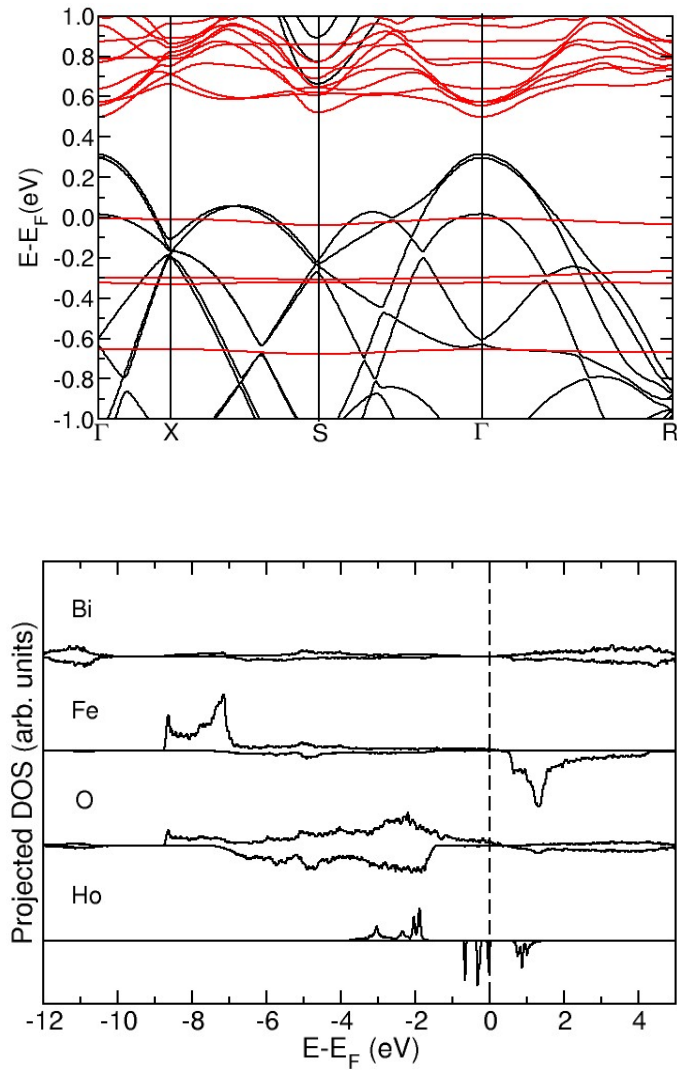


Figure S14. Electro-magnetic properties of the half-metallic **T2-type FM** structure: a) Band structure along lines between high symmetry points. Black lines present spin-up and red line spin-down bands; b) Element-resolved density of states (DOS). Mirrored graphs correspond to spin-up and spin-down states. T2 FM has a relatively large dispersion of the valence band and small dispersion of the conduction band, which is suitable for. e.g. application as a switch.

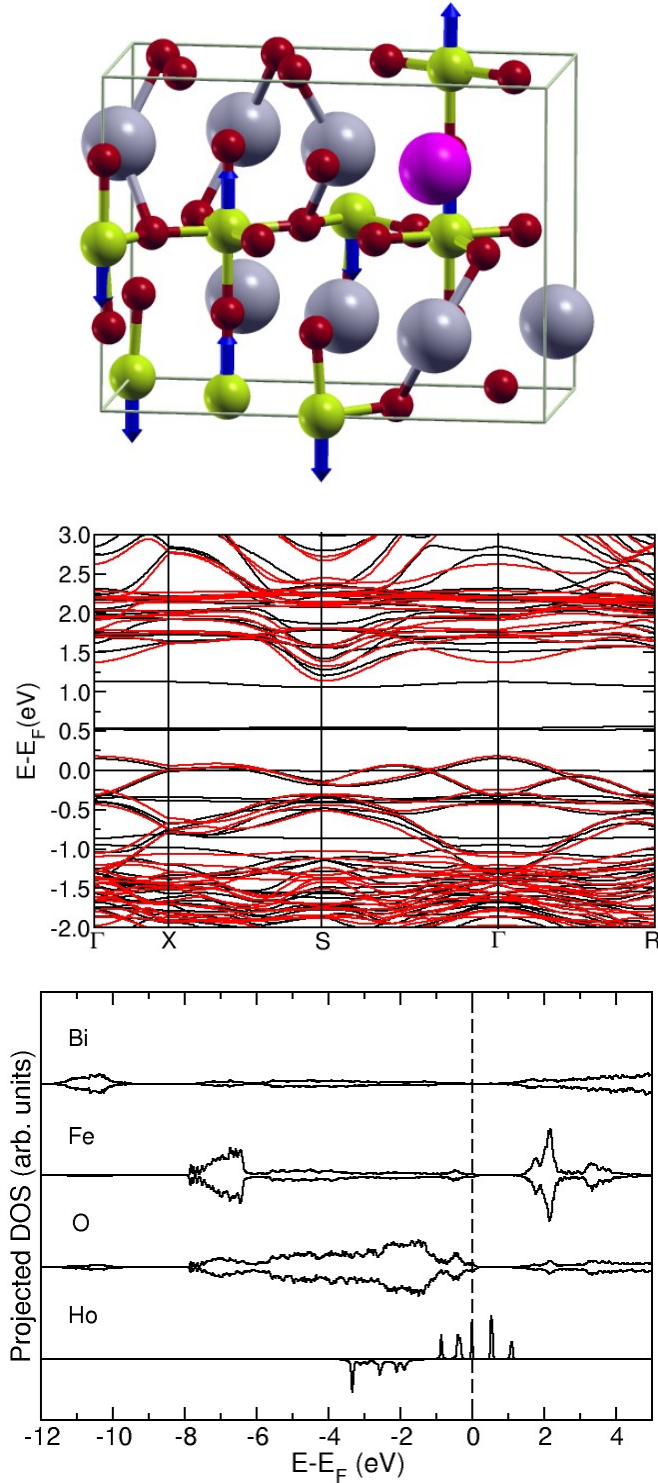


Figure S15. Electro-magnetic properties of the **T2-type AFM1** structure: a) Calculation cell with spin texture marked by the blue arrows; b) Band structure along lines between high symmetry points. Black lines present spin-up and red line spin-down bands; c) Element-resolved density of states (DOS). Mirrored graphs correspond to spin-up and spin-down states.

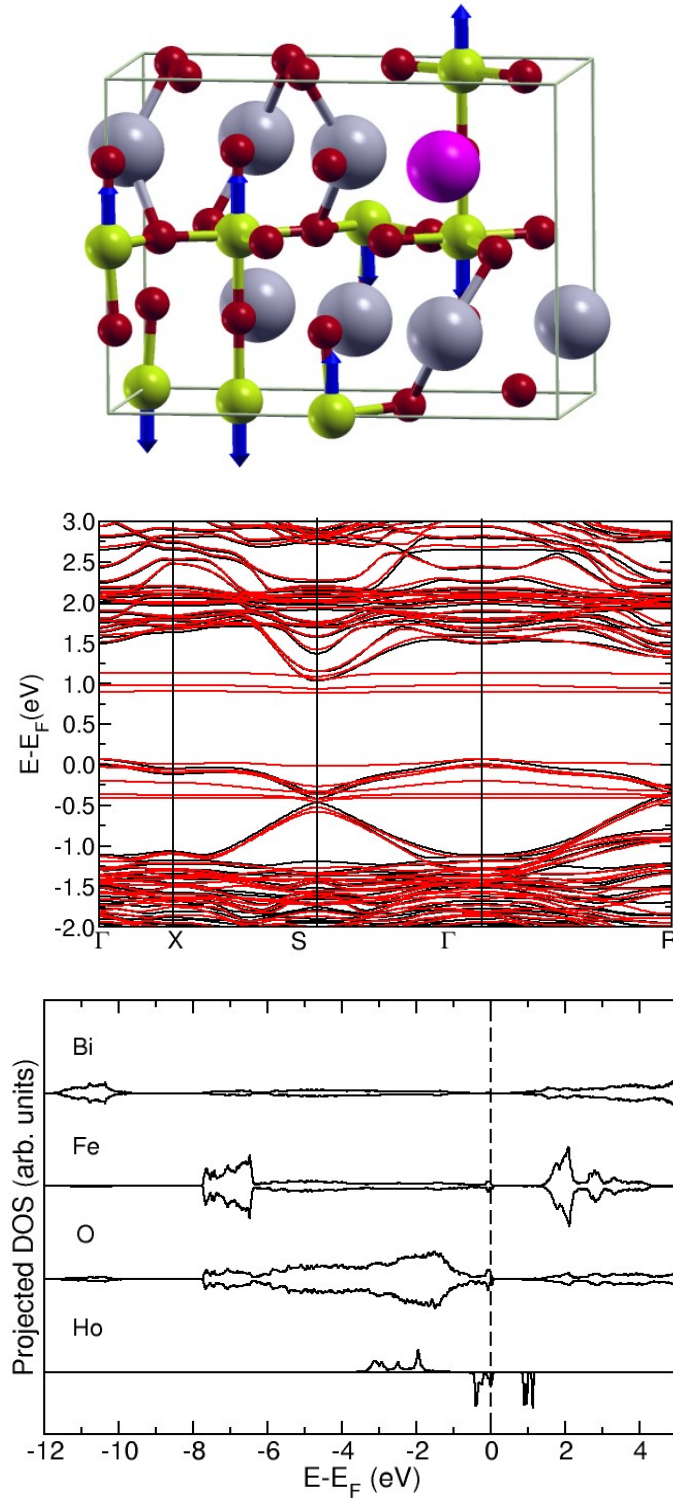


Figure S16. Electro-magnetic properties of the **T2-type AFM2** structure: a) Calculation cell with spin texture marked by the blue arrows; b) Band structure along lines between high symmetry points. Black lines present spin-up and red line spin-down bands; c) Element-resolved density of states (DOS). Mirrored graphs correspond to spin-up and spin-down states.