

Efflorescence kinetics of sodium carbonate decahydrate: A universal description as a function of temperature, degree of reaction, and water vapor pressure

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S1. Kinetic data and formal kinetic analysis

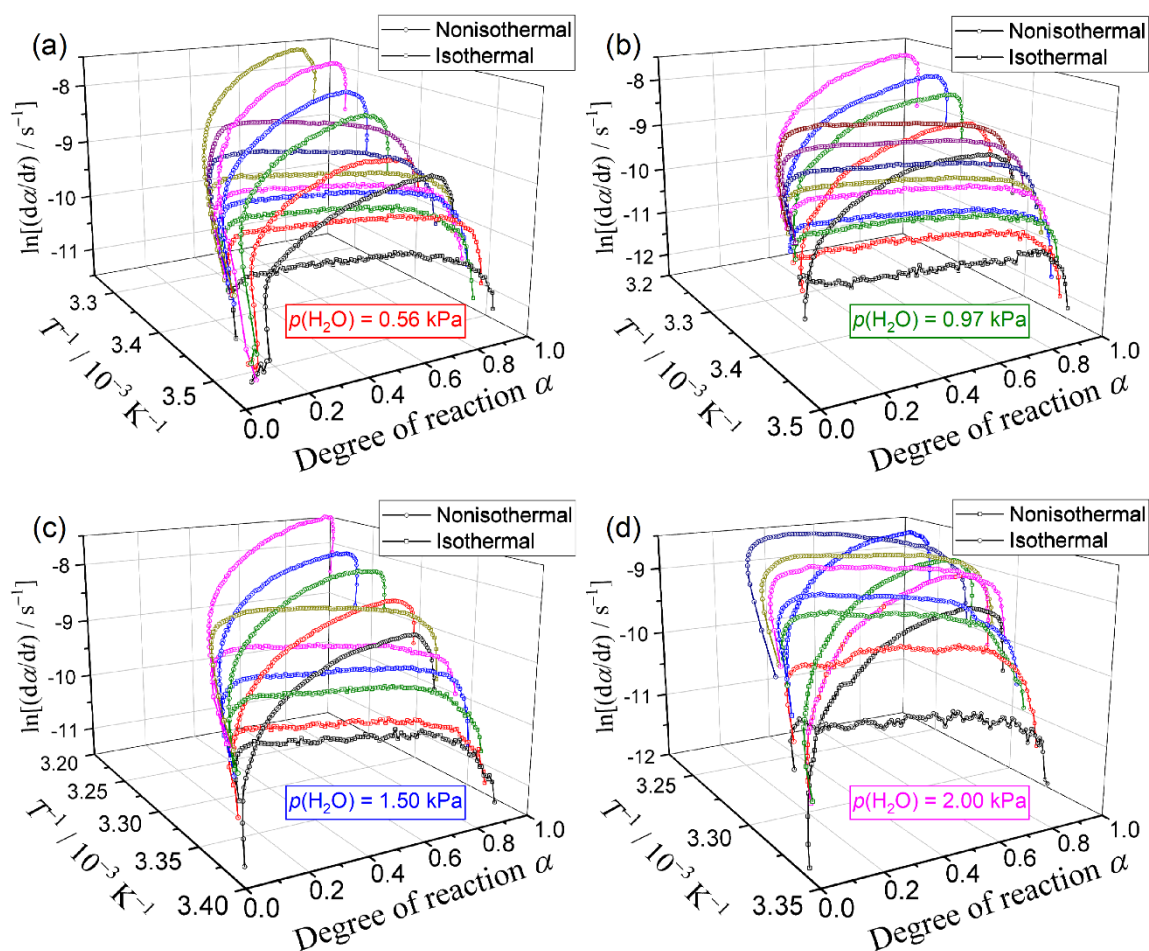


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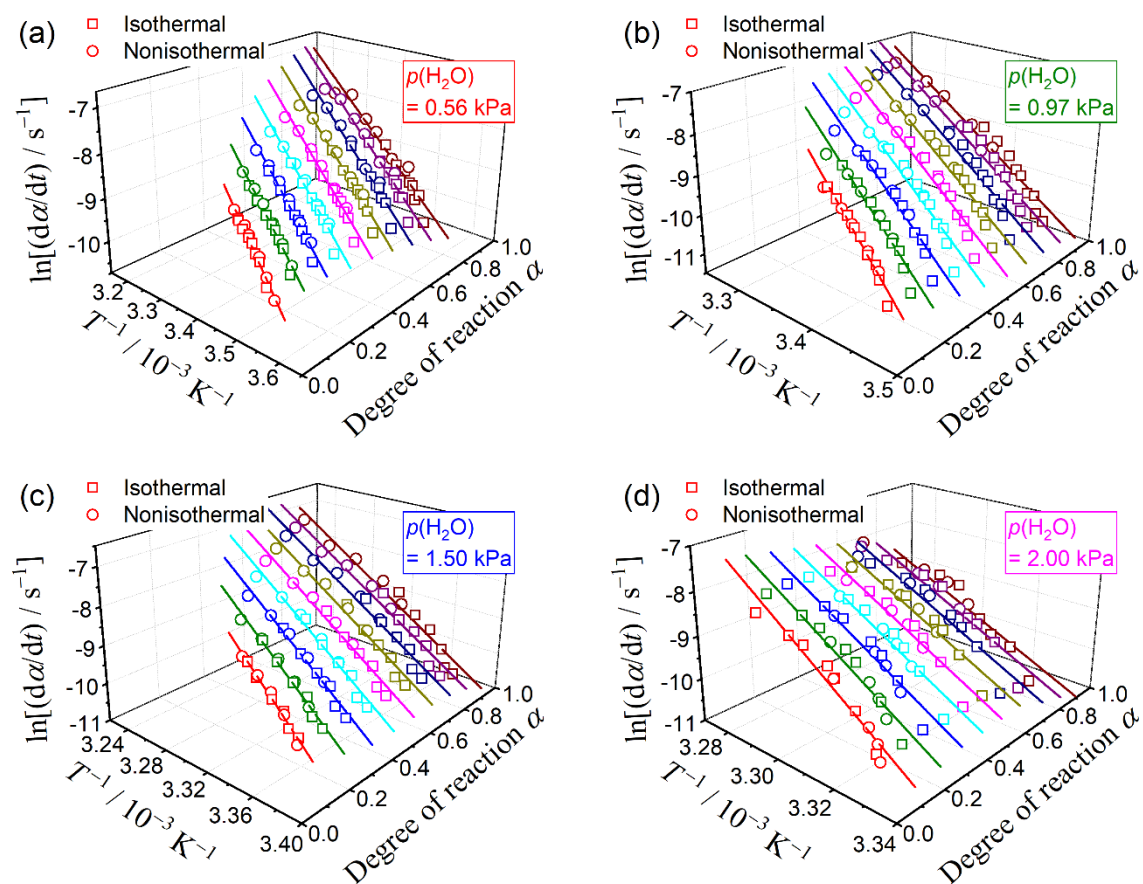


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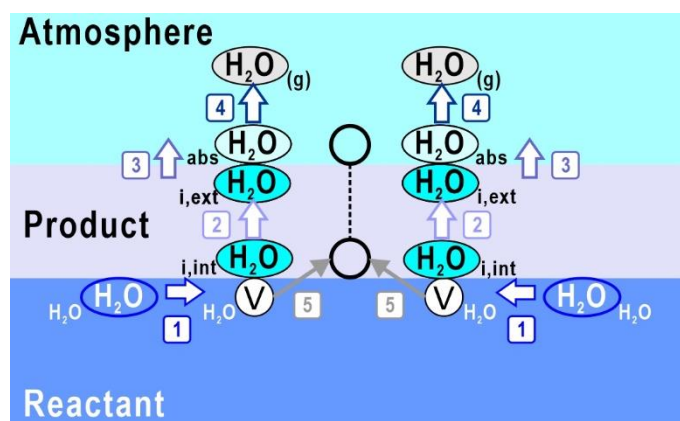
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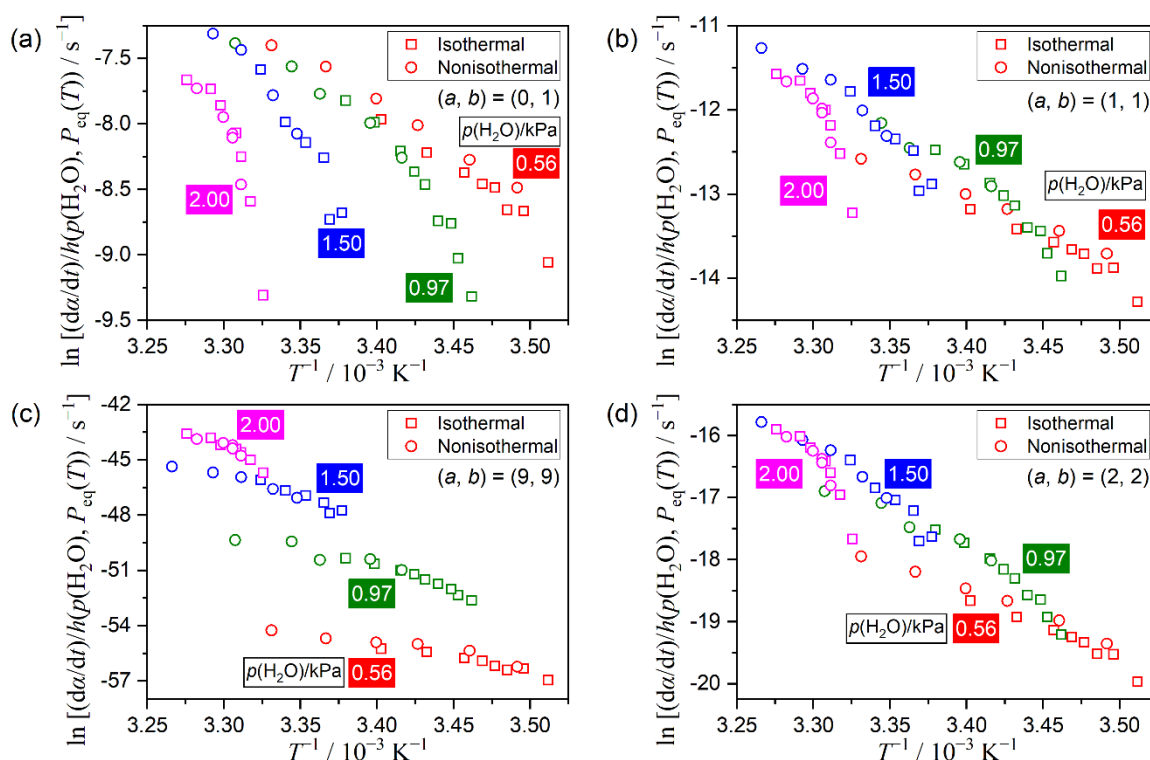


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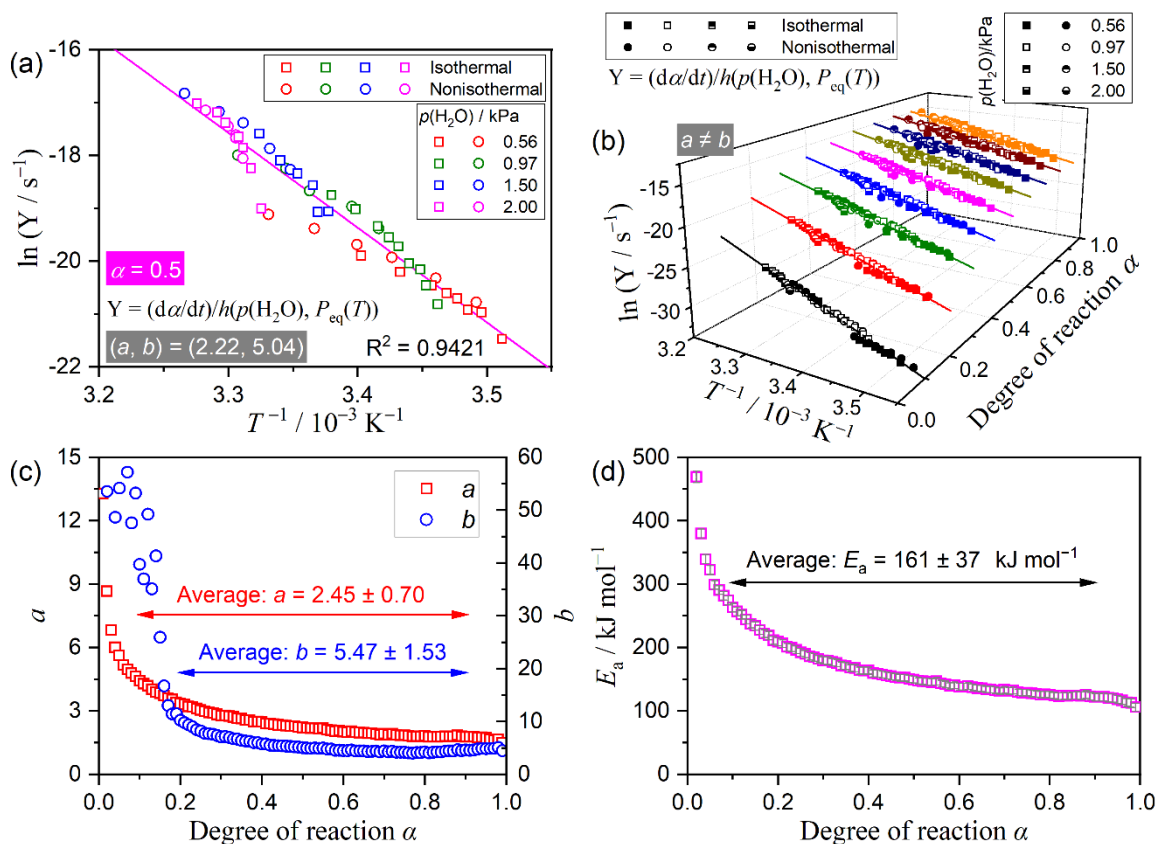


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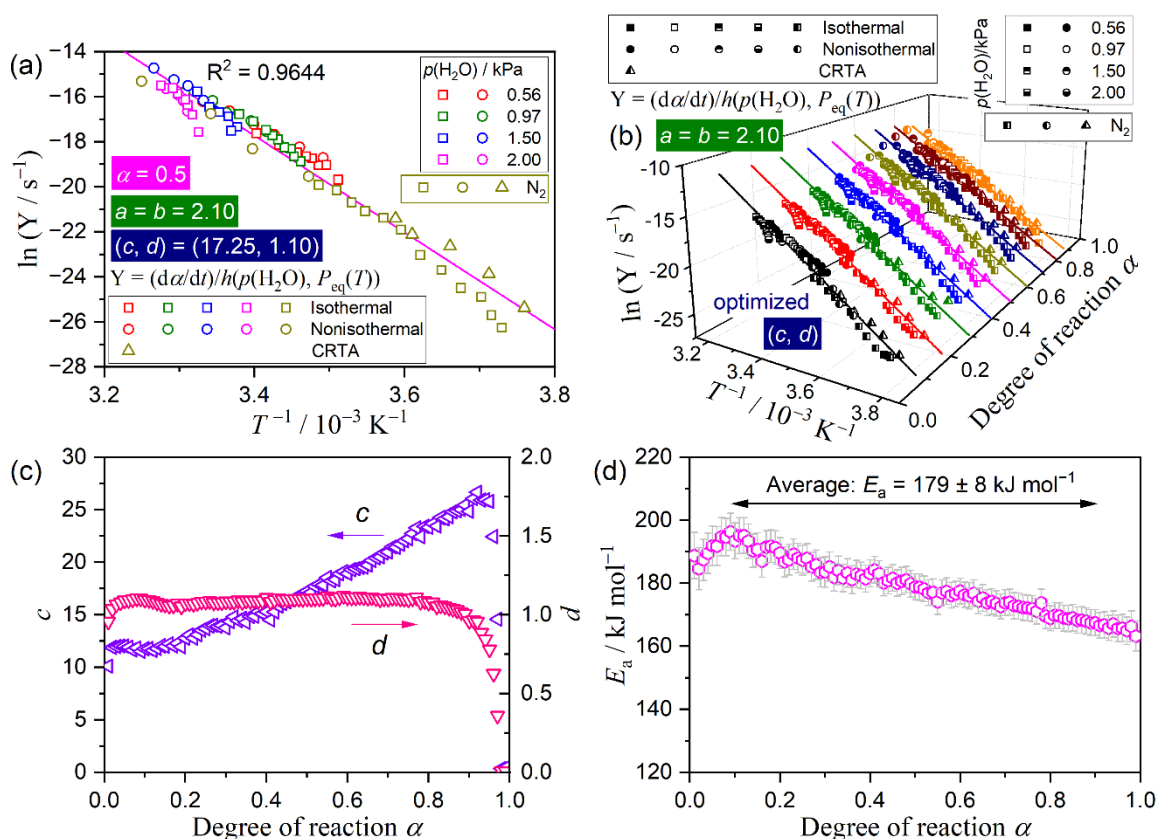
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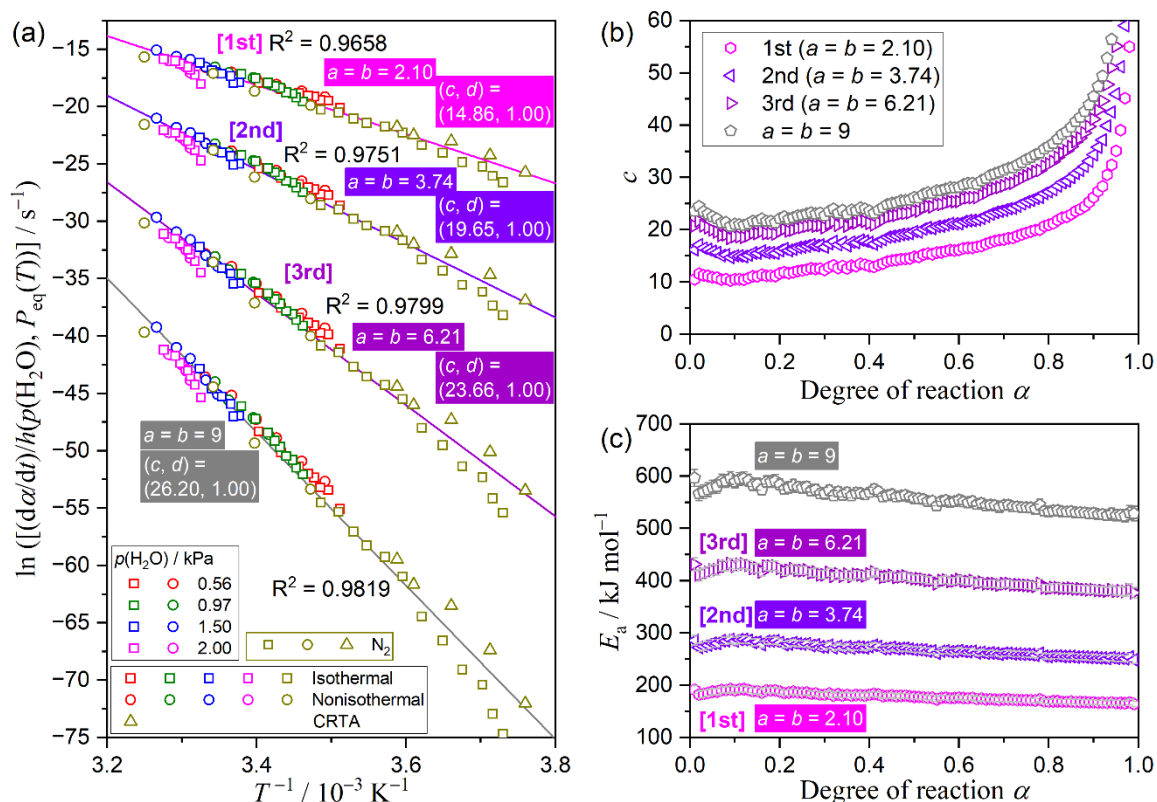


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