

**Comparative Analysis of M_a Site Elements in Fe-Based
Prussian Blue Frame Materials for Ammonium Ion Battery
Applications: A First-Principles Study**

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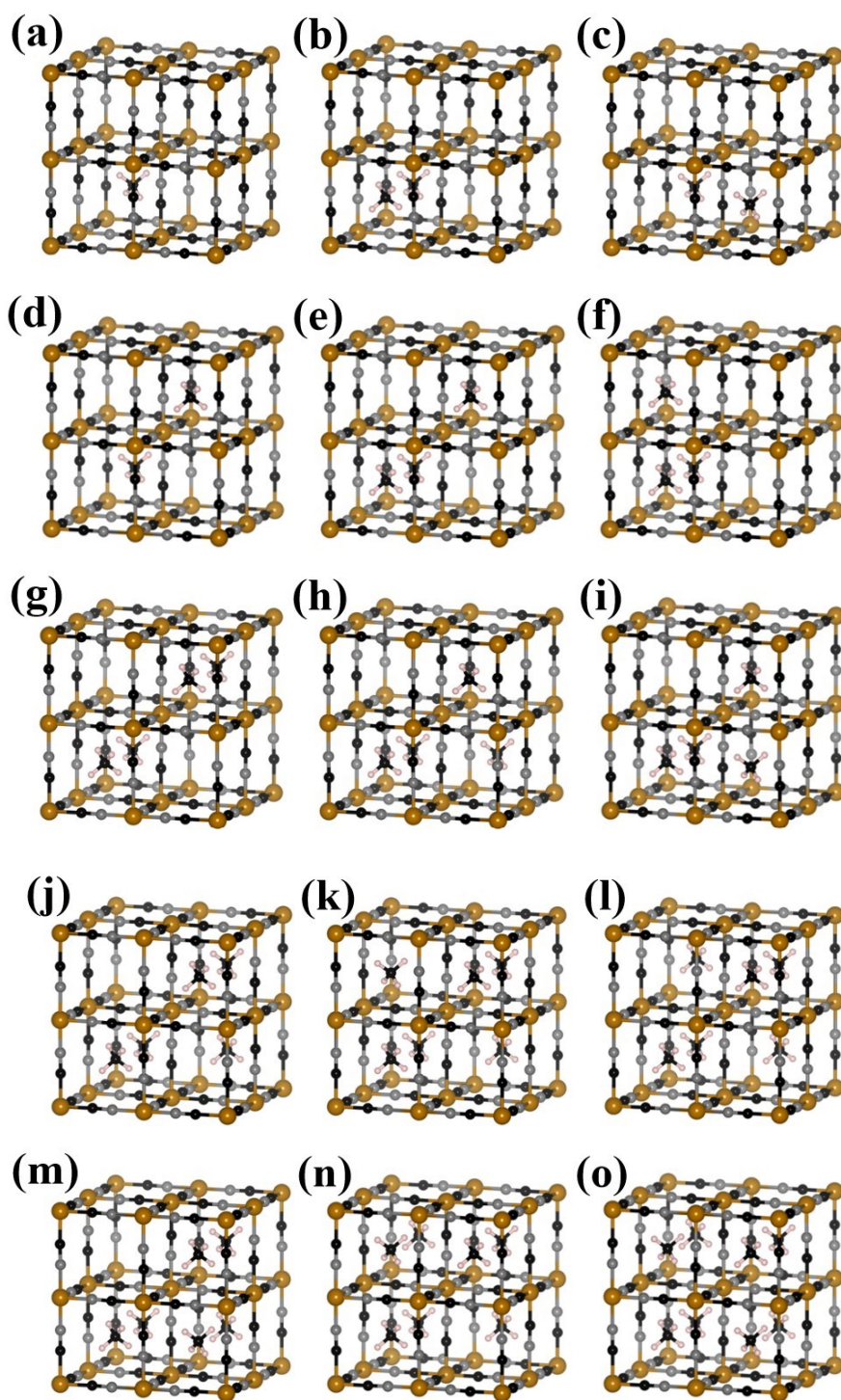


Fig. S1 The considered configurations of NH_4^+ embedding in $\text{Fe}[\text{Fe}(\text{CN})_6]$. (a) 1 NH_4^+ , (b-d) 2 NH_4^+ , (e-f) 3 NH_4^+ , (g-i) 4 NH_4^+ , (j) 5 NH_4^+ , (k-m) 6 NH_4^+ , (n) 7 NH_4^+ , (o) 8 NH_4^+ .

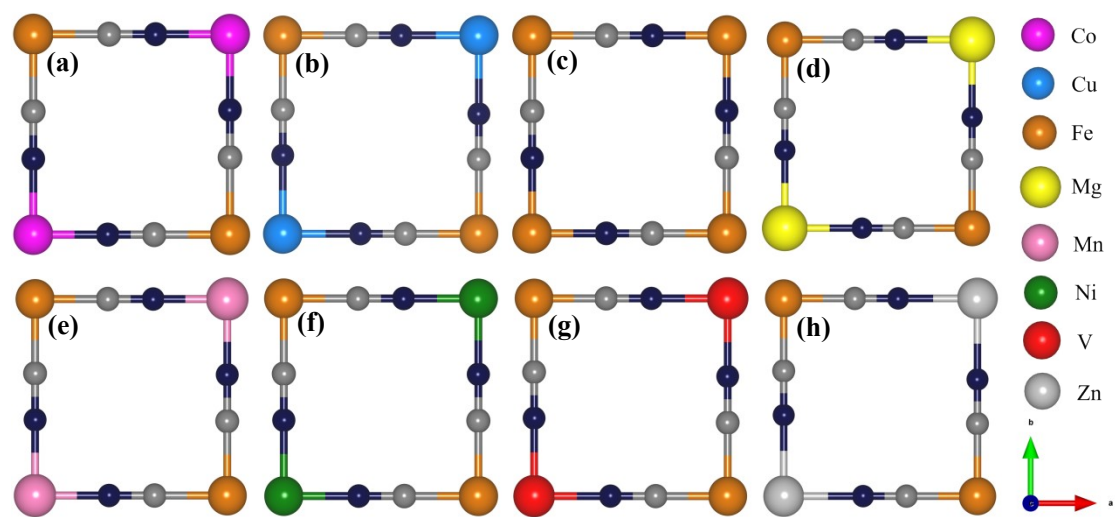


Fig. S2 Front view of $M_a[\text{Fe}(\text{CN})_6]$ ($M_a\text{Fe}$ PBAs) local models with different M_a elements. And M_a = (a) Co, (b) Cu, (c) Fe, (d) Mg, (e) Mn, (f) Ni, (g) V, (h) Zn.

Tab. S1 Average atomic distances of M_a Fe PBAs for different M_a elements (M_a = Co, Cu, Fe, Mg, Mn, Ni, V, Zn).

M_a	M_a -Fe (Å)	M_a -N (Å)	N-C (Å)	C-Fe (Å)
Cu	5.09	2.02	1.17	1.91
Co	4.94	1.87	1.17	1.90
Fe	4.95	1.89	1.17	1.89
Mg	5.24	2.16	1.17	1.91
Mn	4.97	1.91	1.17	1.88
Ni	4.98	1.92	1.17	1.89
V	5.04	1.99	1.18	1.87
Zn	5.22	2.14	1.17	1.91

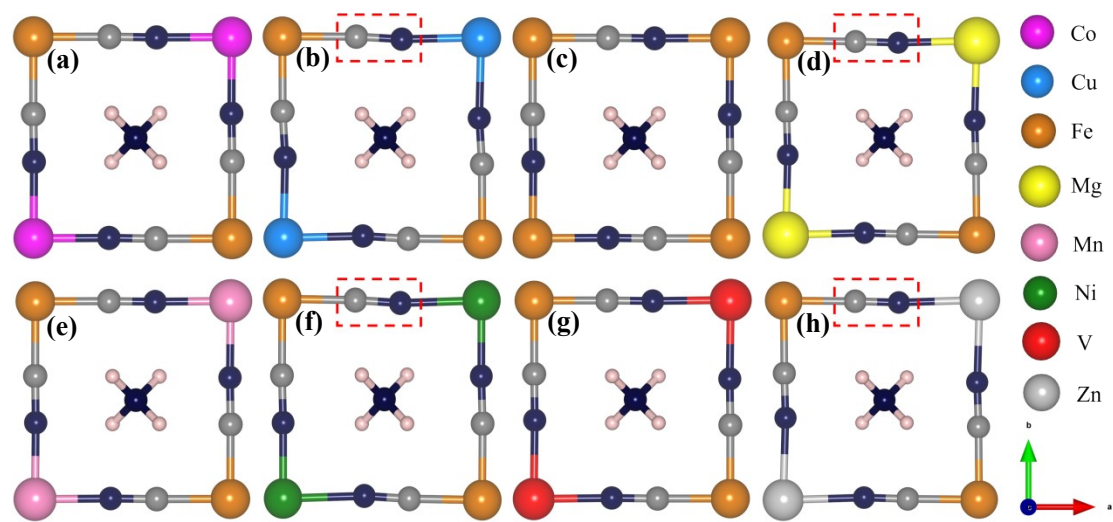


Fig. S3 Front view of $M_a[Fe(CN)_6]$ (M_a Fe PBAs) local models with different M_a elements after inserting an NH_4^+ ion. And $M_a =$ (a) Co, (b) Cu, (c) Fe, (d) Mg, (e) Mn, (f) Ni, (g) V, (h) Zn.

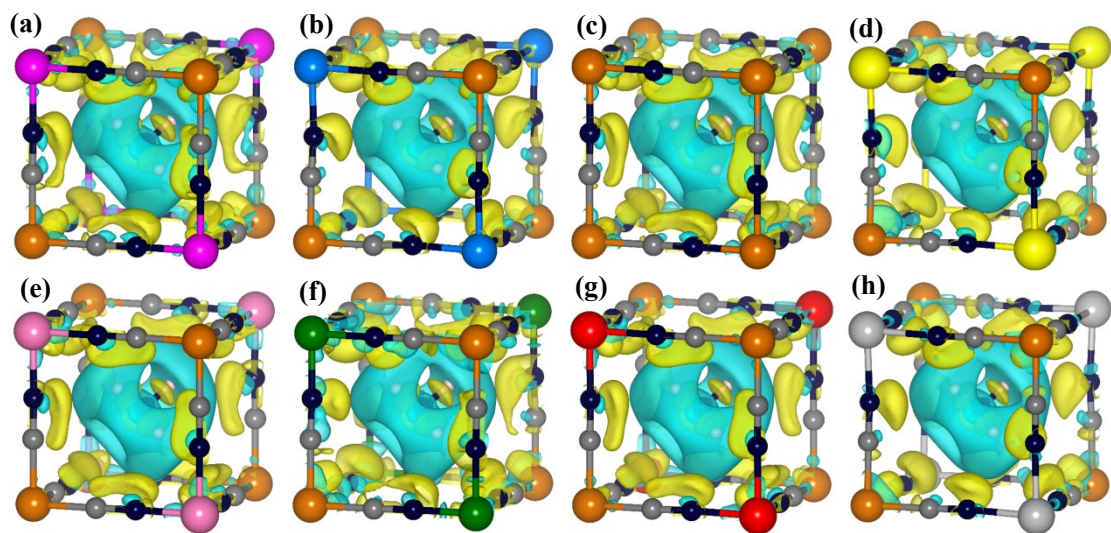


Fig. S4 Charge Density Difference (CDD) of different $\text{NH}_4 \cdot \text{M}_a\text{Fe}$ PBAs local models. $\text{M}_a =$ (a) Co, (b) Cu, (c) Fe, (d) Mg, (e) Mn, (f) Ni, (g) V, (h) Zn.

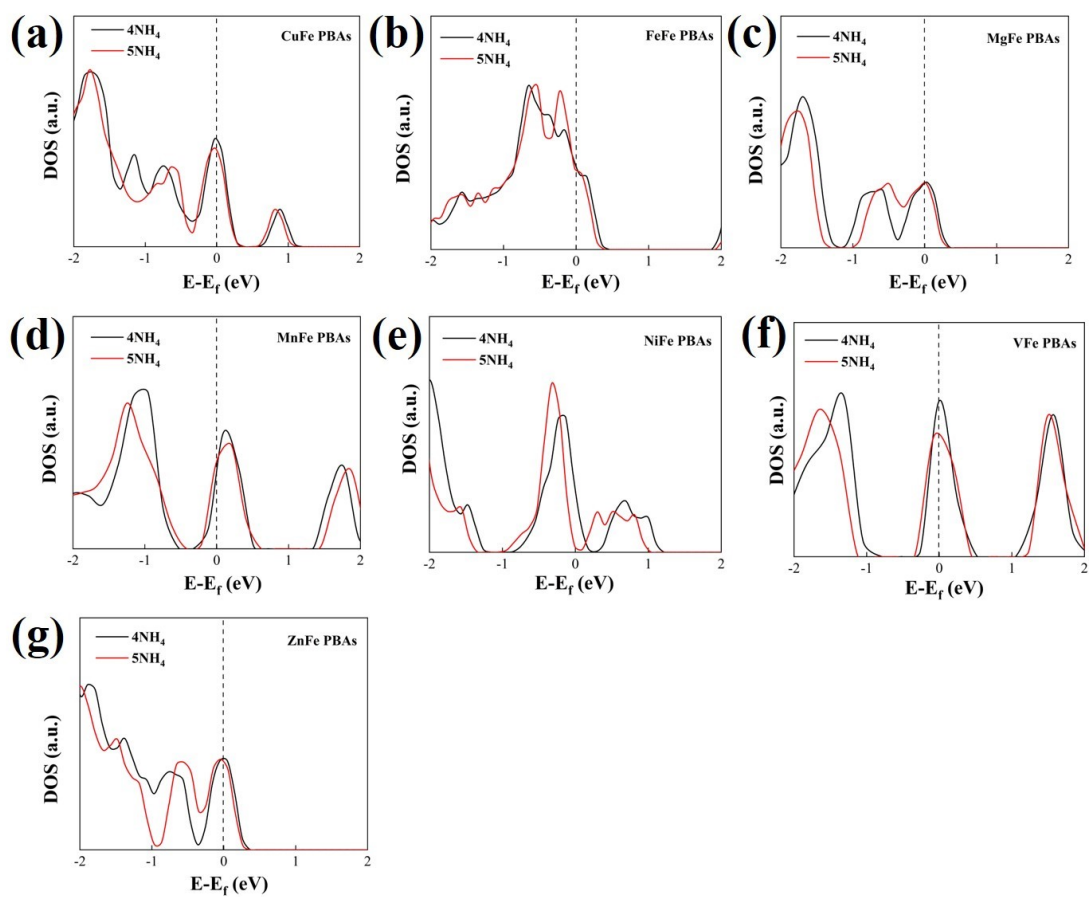


Fig. S5 The electron state density of $M_a\text{Fe}$ PBAs model with 4 and 5 NH_4^+ inserted. $M_a = \text{Cu}, \text{Fe}, \text{Mg}, \text{Mn}, \text{Ni}, \text{V}, \text{Zn}$.

Tab. S2 Nominal battery voltage for $M_a\text{Fe}$ PBAs models with different amounts of NH_4^+ inserted.
 $M_a = \text{Co, Cu, Fe, Mg, Mn, Ni, V, Zn}$.

Voltage (V)	1 NH_4^+	2 NH_4^+	3 NH_4^+	4 NH_4^+	5 NH_4^+	6 NH_4^+	7 NH_4^+	8 NH_4^+	Potential range (V)
Co	4.19	4.24	4.00	3.99	2.57	2.66	2.63	2.94	1.67
Cu	4.62	5.14	4.90	4.88	4.40	4.35	4.27	4.20	0.94
Fe	4.05	4.09	3.83	3.81	3.52	3.48	3.19	3.07	1.02
Mg	5.07	4.89	4.62	4.54	4.29	4.22	4.00	3.90	1.17
Mn	3.64	3.52	3.22	3.14	2.88	2.82	2.45	2.44	1.20
Ni	4.70	4.53	4.16	4.21	4.04	4.05	4.16	4.06	0.66
V	3.69	3.61	3.34	3.26	2.93	2.81	2.45	2.28	1.41
Zn	5.07	4.86	4.63	4.52	4.31	4.19	4.03	3.87	1.19

Tab. S3 Voltage ranges and specific capacities @ current densities of reported PBAs used as electrode materials for aqueous ammonium ion batteries.

Electrode	Potential range (V)	Specific capacity (mAh·g⁻¹) @ current density (mA·g⁻¹)	Ref.
CuHCF	1.24	55@500	[1]
NiHCF	0.6	38@500	[2]
N-CuHCF	0.5	53.1@1000	[3]
MnHCF	1.0	104@100	[4]
K _{0.9} Cu _{1.3} Fe(CN) ₆	1.0	60@50	[5]
NaFe[Fe(CN) ₆]	0.6	60@250	[6]
Na _{1.45} Fe[Fe(CN) ₆] _{0.93}	1.0	75@250	[7]
(NH ₄) ₂ Cu[Fe(CN) ₆]	0.8	77.8@150	[2]
K-V-Fe PBAs	1.2	93.4@2000	[8]
Na _{0.73} Ni[Fe(CN) ₆] _{0.88}	0.6	92.5@100	[9]
Ni ₂ Fe(CN) ₆	0.4	57.4@556	[10]

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