Supplementary Information

The enhanced bandgap and birefringence of rare-earth phosphates XPO₄(X=Sc,

Y, La, Lu) : A first-principles investigation

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Table S1 ScPO₄ VASP-POSCAR file information

Generated by cif2cell 1.2.10 from ICSD reference: 74483. : Failed to get author information, Powder Diffraction 8, 164-167 (1993).

1.00000000000000000	0.0000000000000000	0.0000000000000000
0.0000000000000000	1.00000000000000000	0.000000000000000
0.5000000000000000	0.5000000000000000	0.440535364129691
	Sc P O	
	2 2 8	
	Direct	
0.3750000000000000	0.1250000000000000	0.250000000000000
0.625000000000000	0.875000000000000	0.7500000000000000
0.875000000000000	0.625000000000000	0.250000000000000
0.125000000000000	0.3750000000000000	0.7500000000000000
0.708400000000000	0.639500000000000	0.583200000000000
0.291600000000000	0.722700000000000	0.4168000000000000

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0.139500000000000	0.208400000000000	0.08320000000000					
0.291600000000000	0.360500000000000	0.41680000000000					
0.777300000000000	0.208400000000000	0.08320000000000					
0.708400000000000	0.277300000000000	0.58320000000000					
0.860500000000000	0.791600000000000	0.91680000000000					
0.222700000000000	0.791600000000000	0.91680000000000					
Table S2 YPC	O4 VASP-POSCAR file	e information					
Generated by cif2cell 1.2.10 fr	com ICSD reference: 79	9754. Y (P O4) : Failed to get					
author information	, American Mineralogi	st 80, 21-26 (1995).					
	6.89470000000000						
1.0000000000000000	0.0000000000000000	0.000000000000000					
0.0000000000000000	1.00000000000000000	0.000000000000000					
0.5000000000000000	0.5000000000000000	0.437118366281346					
	Y P O						
	2 2 8						
	Direct						
0.875000000000000	0.6250000000000000	0.250000000000000					
0.125000000000000	0.3750000000000000	0.750000000000000					
0.625000000000000	0.8750000000000000	0.750000000000000					
0.375000000000000	0.1250000000000000	0.250000000000000					
0.784200000000000	0.859500000000000	0.431600000000000					
0.215800000000000	0.791100000000000	0.568400000000000					
0.359500000000000	0.2842000000000000	0.93160000000000					
0.215800000000000	0.1405000000000000	0.568400000000000					
0.708900000000000	0.2842000000000000	0.931600000000000					
0.784200000000000	0.2089000000000000	0.431600000000000					
0.640500000000000	0.7158000000000000	0.068400000000000					
0.291100000000000	0.71580000000000000	0.068400000000000					
Table S3 LaP	O ₄ VASP-POSCAR fil	e information					
Generated by cif2cell 1.2.10 fr	om ICSD reference: 92	2155. : Failed to get author					
information, Revist	a Boliviana de Quimica	a 17, 22-27 (2000).					
	6.841300000	000000					
1.0000000000000000	0.0000000000000000	0.000000000000000					
0.0000000000000000	1.034598687383977	0.000000000000000					
-0.219443313326914	0.00000000000000000	0.926720992792641					
	P O La						
	4 16 4						
	Direct						

0.149900000000000

0.85010000000000

0.649900000000000

0.65610000000000

0.343900000000000

0.843900000000000

0.299700000000000

0.700300000000000

0.20030000000000

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0.799700000000000	0.35010000000000	0.156100000000000
0.241700000000000	0.044500000000000	0.404600000000000
0.758300000000000	0.955500000000000	0.595400000000000
0.258300000000000	0.544500000000000	0.095400000000000
0.741700000000000	0.455500000000000	0.904600000000000
0.338800000000000	0.356200000000000	0.473100000000000
0.661200000000000	0.643800000000000	0.526900000000000
0.161200000000000	0.856200000000000	0.026900000000000
0.838800000000000	0.143800000000000	0.973100000000000
0.5030000000000000	0.0920000000000000	0.729700000000000
0.4970000000000000	0.9080000000000000	0.270300000000000
0.9970000000000000	0.5920000000000000	0.770300000000000
0.0030000000000000	0.4080000000000000	0.229700000000000
0.095300000000000	0.215400000000000	0.680100000000000
0.904700000000000	0.7846000000000000	0.319900000000000
0.404700000000000	0.715400000000000	0.819900000000000
0.595300000000000	0.284600000000000	0.180100000000000
0.2797000000000000	0.164100000000000	0.088300000000000
0.720300000000000	0.8359000000000000	0.911700000000000
0.220300000000000	0.664100000000000	0.411700000000000
0.779700000000000	0.3359000000000000	0.588300000000000

 Table S4 LuPO₄ VASP-POSCAR file information

Generated by cif2cell 1.2.10 from ICSD reference: 162336.	:	Failed to get
author information, American Mineralogist 94, 98-10	4 (2	2009).

	0./8930000000	0000
1.0000000000000000	0.0000000000000000	0.0000000000000000000000000000000000000
0.00000000000000000000000000000000000	1.0000000000000000	0.0000000000000000000000000000000000000
0.5000000000000000	0.5000000000000000	0.438618454967229
	P Lu O	
	2 2 8	
	Direct	
0.6250000000000000	0.8750000000000000	0.7500000000000000
0.3750000000000000	0.1250000000000000	0.2500000000000000
0.8750000000000000	0.6250000000000000	0.2500000000000000
0.1250000000000000	0.3750000000000000	0.7500000000000000
0.783700000000000	0.211400000000000	0.4326000000000000
0.216300000000000	0.1440000000000000	0.567400000000000
0.7114000000000000	0.283700000000000	0.9326000000000000
0.216300000000000	0.7886000000000000	0.5674000000000000
0.3560000000000000	0.283700000000000	0.9326000000000000
0.783700000000000	0.8560000000000000	0.4326000000000000
0.2886000000000000	0.716300000000000	0.067400000000000
0.6440000000000000	0.716300000000000	0.067400000000000

Table S5 Space Groups, Birefringence at 1064 nm obtained with VASP code

Crystal	Space		1064nm				5	15nm	
	group	n _e	n	lo	Δn	n _e	n	lo	Δn
ScPO ₄	I41/AMD	1.9458	2.0	738	0.1280	1.9433	2.0	675	0.1242
YPO ₄	I41/AMD	1.8241	1.9	170	0.0929	1.8139	1.8	875	0.0836
LuPO ₄	I41/AMD	1.8143	1.9	037	0.0894	1.8374	1.9	266	0.0892
Crystal	Space group	n _x	n_y	nz	Δn	n _x	n _y	nz	Δn
LaPO ₄	P12 ₁ /a1	1.9185	1.9078	1.9592	0.0407	1.9517	1.9452	2.0003	0.0486

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 Table S6 Dielectric constants of ScPO₄

					201 04	
Crystal Optical Permittivity(f→i			→infinity)	DC	Permittivity(1	f=0)
	3.39435	0.00000	0.00000	11.17167	0.00000	0.00000
ScPO ₄	0.00000	3.39435	0.00000	0.00000	11.17167	0.00000
	0.00000	0.00000	4.26711	0.00000	0.00000	14.48357
		Table S7	Dielectric o	constants of	f YPO ₄	
Crystal	Optical Pe	ermittivity(f-	→infinity)	DC	Permittivity(f=0)
	3.00279	0.00000	0.00000	6.95848	0.00000	0.00000
YPO ₄	0.00000	3.00279	0.00000	0.00000	6.95848	0.00000
	0.00000	0.00000	3.52143	0.00000	0.00000	8.22851
	,	Table S8 I	Dielectric c	onstants of	LaPO ₄	
Crystal	Optical Pe	ermittivity(f-	→infinity)	DC	Permittivity(£=0)
	3.17173	0.00000	0.00645	7.42583	0.00000	0.42787
LaPO ₄	0.00000	3.17088	0.00000	0.00000	6.86640	0.00000
	0.00000	0.00000	3.54443	0.42787	0.00000	9.44489
	,	Table S9 I	Dielectric c	onstants of	LuPO ₄	
Crystal	Optical Pe	Permittivity(f→infinity)		DC Permittivity(f=0)		
	3.26853	0.00000	0.00000	10.92020	0.00000	0.00000
LuPO ₄	0.00000	3.26853	0.00000	0.00000	10.92020	0.00000
	0.00000	0.00000	3.73368	0.00000	0.00000	11.37405
Table S1	0 Distortio	on index of	PO ₄ polył	nedra in XP	$O_4 (X = Sc$, Y, La, Lu
compounds.						
Crystal			Group		Distortion index	
LaF	PO ₄		PO ₄		0	.00564
LuF	P O ₄		PO ₄			0
YP	O_4		PO ₄		0	

ScPO ₄		PO	D ₄		0
Table S11 Born effective charge of ScPO ₄					
	atom	Born effective charges			-
	O(1)	-1.02418	-0.00000	-0.00000	-
		-0.00000	-2.47191	-0.40882	
		-0.00000	-0.56159	-2.34064	
	O(2)	-1.02418	0.00000	-0.00000	
		0.00000	-2.47191	0.40882	
		-0.00000	0.56159	-2.34064	
	O(3)	-2.47191	0.00000	0.40882	
		0.00000	-1.02418	0.00000	
		0.56159	0.00000	-2.34064	
	O(4)	-2.47191	0.00000	-0.40882	
		0.00000	-1.02418	0.00000	
		-0.56159	0.00000	-2.34064	
	O(5)	-1.02418	0.00000	-0.00000	
		0.00000	-2.47191	0.40882	
		-0.00000	0.56159	-2.34064	
	O(6)	-1.02418	-0.00000	-0.00000	
		-0.00000	-2.47191	-0.40882	
		-0.00000	-0.56159	-2.34064	
	O(7)	-2.47191	0.00000	0.40882	
		0.00000	-1.02418	0.00000	
		0.56159	0.00000	-2.34064	
	O(8)	-2.47191	0.00000	-0.40882	
		0.00000	-1.02418	0.00000	
		-0.56159	0.00000	-2.34064	
	P(1)	3.21024	-0.00000	0.00000	
		-0.00000	3.21024	-0.00000	

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	0.00000	-0.00000	4.86689
P(2)	3.21024	-0.00000	0.00000
	-0.00000	3.21024	-0.00000
	0.00000	-0.00000	4.86689
Sc(1)	3.78195	-0.00000	0.00000
	-0.00000	3.78195	-0.00000
	0.00000	-0.00000	4.49568
Sc(2)	3.78195	-0.00000	0.00000
	-0.00000	3.78195	-0.00000
	0.00000	-0.00000	4.49568

Table S12 Born effective charge of YPO₄

atom	Born effective charges					
O(1)	-1.03565	-0.00000	0.00000			
	-0.00000	-2.41896	-0.47623			
	0.00000	-0.56411	-2.16757			
O(2)	-1.03565	-0.00000	0.00000			
	-0.00000	-2.41896	0.47623			
	0.00000	0.56411	-2.16757			
O(3)	-2.41896	-0.00000	0.47623			
	-0.00000	-1.03565	-0.00000			
	0.56411	-0.00000	-2.16757			
O(4)	-2.41896	-0.00000	-0.47623			
	-0.00000	-1.03565	-0.00000			
	-0.56411	-0.00000	-2.16757			
O(5)	-1.03565	-0.00000	0.00000			
	-0.00000	-2.41896	0.47623			
	0.00000	0.56411	-2.16757			
O(6)	-1.03565	-0.00000	0.00000			
	-0.00000	-2.41896	-0.47623			

	0.00000	-0.56411	-2.16757
O(7)	-2.41896	-0.00000	0.47623
	-0.00000	-1.03565	-0.00000
	0.56411	-0.00000	-2.16757
O(8)	-2.41896	-0.00000	-0.47623
	-0.00000	-1.03565	-0.00000
	-0.56411	-0.00000	-2.16757
P(1)	3.26594	0.00000	-0.00000
	0.00000	3.26594	0.00000
	-0.00000	0.00000	4.35488
P(2)	3.26594	0.00000	-0.00000
	0.00000	3.26594	0.00000
	-0.00000	0.00000	4.35488
Y(1)	3.64329	0.00000	-0.00000
	0.00000	3.64329	0.00000
	-0.00000	0.00000	4.31540
Y(2)	3.64329	0.00000	-0.00000
	0.00000	3.64329	0.00000
	-0.00000	0.00000	4.31540

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Table S13 Born effective charge of $LaPO_4$

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atom	E	Born effective charge	S
O(1)	-1.12346	-0.18380	-0.08971
	-0.27592	-2.29177	-0.35070
	-0.08956	-0.41761	-2.25113
O(2)	-1.62144	-0.13483	0.11545
	-0.09193	-2.07869	0.43129
	0.14245	0.44811	-1.80163
O(3)	-1.98530	0.50891	-0.28329
	0.40730	-1.49505	0.19482

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	-0.38376	0.21355	-2.18926
O(4)	-2.18852	0.49337	0.19499
	0.44983	-1.24542	-0.03884
	0.30624	-0.08077	-2.10515
O(5)	-1.12346	0.18380	-0.08971
	0.27592	-2.29177	0.35070
	-0.08956	0.41761	-2.25113
O(6)	-1.62144	0.13483	0.11545
	0.09193	-2.07869	-0.34129
	0.14245	-0.44811	-1.80163
O(7)	-1.98530	-0.50891	-0.28329
	-0.40730	-1.49505	-0.19482
	-0.38376	-0.21355	-2.18926
O(8)	-2.18852	-0.49337	0.19499
	-0.44983	-1.24542	0.03884
	0.30624	0.08077	-2.10515
O(9)	-1.12346	-0.18380	-0.08971
	-0.27592	-2.29177	-0.35070
	-0.08956	-0.41761	-2.25113
O(10)	-1.62144	-0.13483	0.11545
	-0.09193	-2.07869	0.34129
	0.14245	0.44811	-1.80163
O(11)	-1.98530	0.50891	-0.28329
	0.40730	-1.49505	0.19482
	-0.38376	0.21355	-2.18926
O(12)	-2.18852	0.49337	0.19499
	0.44983	-1.24542	-0.03884
	0.30624	-0.08077	-2.10515
O(13)	-1.12346	0.18380	-0.08971

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ocieties 2023			
	0.27592	-2.29177	0.35070
	-0.08956	0.41761	-2.25113
O(14)	-1.62144	0.13483	0.11545
	0.09193	-2.07869	-0.34129
	0.14245	-0.44811	-1.80163
O(15)	-1.98530	-0.50891	-0.28329
	-0.40730	-1.49505	-0.19482
	-0.38376	-0.21355	-2.18926
O(16)	-2.18852	-0.49337	0.19499
	-0.44983	-1.24542	0.03884
	0.30624	0.08077	-2.10515
P(1)	3.17320	-0.09824	0.03049
	-0.07234	3.26603	0.01974
	-0.02418	-0.02943	4.02577
P(2)	3.17320	0.09824	0.03049
	0.07234	3.26603	-0.01974
	-0.02418	0.02934	4.02577
P(3)	3.17320	-0.09824	0.03049
	-0.07234	3.26603	0.01974
	-0.02418	-0.02934	4.02577
P(4)	3.17320	0.09824	0.03049
	0.07234	3.26603	-0.01974
	-0.02418	-0.02934	4.02577
La(1)	3.74552	-0.11704	0.03207
	-0.19070	3.84491	-0.16423
	0.04881	-0.07023	4.32141
La(2)	3.74552	0.11704	0.03207
	0.19070	3.84491	0.16423
	0.04881	-0.07023	4.32141

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500	0105 2025			
	La(3)	3.74552	-0.11704	0.03207
		-0.19070	3.84491	-0.16423
		0.04881	-0.07023	4.32141
	La(4)	3.74552	0.11704	0.03207
		0.19070	3.84491	0.16423
		0.04881	-0.07023	4.32141
-				

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atom	В	orn effective charge	es
O(1)	-0.99078	0.00000	-0.00000
	-0.00000	-2.56360	0.52166
	-0.00000	0.58362	-2.28904
O(2)	-0.99078	0.00000	-0.00000
	0.00000	-2.56360	-0.52166
	-0.00000	-0.58362	-2.28904
O(3)	-2.56360	0.00000	-0.52166
	0.00000	-0.99078	-0.0000
	-0.58362	-0.00000	-2.28904
O(4)	-2.56360	0.00000	0.52166
	0.00000	-0.99078	-0.0000
	0.58362	-0.00000	-2.28904
O(5)	-0.99078	0.00000	-0.00000
	0.00000	-2.56360	-0.52166
	-0.00000	-0.58362	-2.28904
O(6)	-0.99078	0.00000	-0.00000
	0.00000	-2.56360	0.52166
	-0.00000	0.58362	-2.28904
O(7)	-2.56360	0.00000	-0.52166
	0.00000	-0.99078	-0.0000

Table S14 Born effective charge of $LuPO_4$

	-0.58362	-0.00000	-2.28904
O(8)	-2.56360	0.00000	0.52166
	0.00000	-0.99078	-0.0000
	0.58362	-0.00000	-2.28904
P(1)	3.27451	-0.00000	0.00000
	-0.00000	3.27451	0.00000
	0.00000	0.00000	4.74688
P(2)	3.27451	-0.00000	0.00000
	-0.00000	3.27451	0.00000
	0.00000	0.00000	4.74688
Lu(1)	3.83425	-0.00000	0.00000
	-0.00000	3.83425	0.00000
	0.00000	0.00000	4.40929
Lu(2)	3.83425	-0.00000	0.00000
	-0.00000	3.83425	0.00000
	0.00000	0.00000	4.40929

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Table S15 Distortion index of XO_8 polyhedra in XPO_4 (X = Sc, Y, La, Lu) compounds.

Crystal	Group	Distortion index
ScPO ₄	ScO_8	0.02652
YPO ₄	YO_8	0.01549
LaPO ₄	LaO_8	0.03421
LuPO ₄	LuO_8	0.01784



Fig S1 Band structures of XPO₄(X=Sc, Y, La, Lu) obtained by GGA/PBE functional implemented in VASP code.



Fig S2 Band structures of XPO₄(X=Sc, Y, La, Lu) obtained by GGA+U functional implemented in VASP code.



Fig S3 The band structures of XPO₄ (X=Sc, Y, La, Lu) implemented in the PWMAT code using the HSE06 functional, where (a) is ScPO₄, (b) is YPO₄, (c) is LaPO₄, and (d) is LuPO₄.



Fig S4 The the refractive indices and birefringence obtained by GGA/PBE functional concerning Hubbard picture implemented in VASP code.



Fig S5 Electron Localization Function (ELF) of XPO_4 (X = Sc, Y, La, Lu) obtained by VASP code, where (a) is ScPO₄, (b) is YPO₄, (c) is LaPO₄, (d) is LuPO₄.



Fig S6 The band structures of XPO_4 (X=Sc, Y, La, Lu) considering SOC were calculated using the GGA+PBE functional in the VASP code.