

**Electronic supplementary information (ESI)**  
**for**  
**Co-activation of methane and nitrogen to acetonitrile over**  
**MoC<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub> catalysts**

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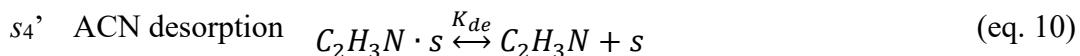
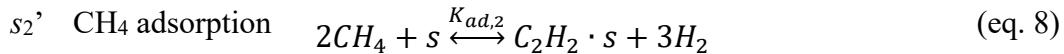
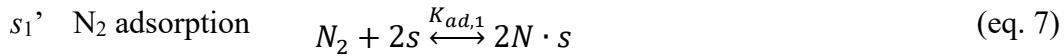
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## Derivation of the rate equation according to the LHHW formalism of methane conversion to ACN

Plausible reactions of CH<sub>4</sub> and N<sub>2</sub> co-activation to form ACN:



The aforementioned reactions can be lumped into four steps



Since ACN desorption is rapid, the equilibrium constant ( $K_{de}$ ) of step  $s_4'$  is assumed to be very large. Thus, the terms containing  $K_{de}$  in the denominator are negligibly small.

### I. Assuming N<sub>2</sub> adsorption step (s<sub>1</sub>') is rate-limiting

The rate of the step of N<sub>2</sub> adsorption should be close to the rate of the overall reaction:

$$r = k_{ad,1} P_{N_2} (1 - \sum \theta_i)^2 \quad (\text{eq. 11})$$

Then, CH<sub>4</sub> adsorptions (eq. 8), surface reaction (eq. 9), and ACN desorption (eq. 10) should attain the equilibrium, thereby yielding:

$$K_{ad,2} = \frac{\theta_{C_2H_2} P_{H_2}^3}{P_{CH_4}^2 (1 - \sum \theta_i)} \quad (\text{eq. 12})$$

$$K_{surf} = \frac{\theta_{C_2H_3N}^2 (1 - \sum \theta_i)^2}{\theta_{C_2H_2}^2 \theta_N^2 P_{H_2}} \quad (\text{eq. 13})$$

$$K_{de} = \frac{P_{C_2H_3N} (1 - \sum \theta_i)}{\theta_{C_2H_3N}} \quad (\text{eq. 14})$$

Rearranging eqs. 12, 13, and 14, the expressions of  $\theta_N$ ,  $\theta_{C_2H_2}$ , and  $\theta_{C_2H_3N}$  can be obtained.

$$\theta_N = K_{ad,2}^{-1} K_{surf}^{0.5} K_{de}^{-1} P_{H_2}^{3.5} P_{CH_4}^{-2} P_{C_2H_3N} (1 - \Sigma \theta_i) \quad (\text{eq. 15})$$

$$\theta_{C_2H_2} = K_{ad,2} P_{H_2}^{-3} P_{CH_4}^2 (1 - \Sigma \theta_i) \quad (\text{eq. 16})$$

$$\theta_{C_2H_3N} = K_{de}^{-1} P_{C_2H_3N} (1 - \Sigma \theta_i) \quad (\text{eq. 17})$$

Accordingly, the sum of the coverages of adsorbed species can be expressed as:

$$\Sigma \theta_i = \frac{K_{ad,2} P_{H_2}^{-3} P_{CH_4}^2 + K_{ad,2}^{-1} K_3^{0.5} K_{de}^{-1} P_{H_2}^{3.5} P_{CH_4}^{-2} P_{C_2H_3N} + K_{de}^{-1} P_{C_2H_3N}}{1 + K_{ad,2} P_{H_2}^{-3} P_{CH_4}^2 + K_{ad,2}^{-1} K_{surf}^{0.5} K_{de}^{-1} P_{H_2}^{3.5} P_{CH_4}^{-2} P_{C_2H_3N} + K_{de}^{-1} P_{C_2H_3N}} \quad (\text{eq. 18})$$

Since  $K_{de}$  is assumed to be very large, the sum of the coverages of adsorbed species can be simplified as:

$$\Sigma \theta_i = \frac{K_{ad,2} P_{H_2}^{-3} P_{CH_4}^2}{1 + K_{ad,2} P_{H_2}^{-3} P_{CH_4}^2} \quad (\text{eq. 19})$$

By taking eq. 19 into eq. 11, the expression of the overall rate by assuming N<sub>2</sub> adsorption is rate-limiting can be obtained as:

$$r = k_{ad,1} P_{N_2} \left( \frac{1}{1 + K_{ad,2} P_{H_2}^{-3} P_{CH_4}^2} \right)^2 \quad (\text{eq. 20})$$

## II. Assuming CH<sub>4</sub> adsorption step (s<sub>2'</sub>) is rate-limiting

The rate of the step of CH<sub>4</sub> adsorption should be close to the rate of the overall reaction:

$$r = k_{ad,2} P_{CH_4}^2 (1 - \Sigma \theta_i) \quad (\text{eq. 21})$$

Then, N<sub>2</sub> adsorptions (eq. 7), surface reaction (eq. 9), and ACN desorption (eq. 10) should attain the equilibrium, thereby yielding:

$$K_{ad,1} = \frac{\theta_N^2}{P_{N_2} (1 - \Sigma \theta_i)^2} \quad (\text{eq. 22})$$

$$K_{surf} = \frac{\theta_{C_2H_3N}^2 (1 - \Sigma \theta_i)^2}{\theta_{C_2H_2}^2 \theta_N^2 P_{H_2}} \quad (\text{eq. 23})$$

$$K_{de} = \frac{P_{C_2H_3N} (1 - \Sigma \theta_i)}{\theta_{C_2H_3N}} \quad (\text{eq. 24})$$

By rearranging eqs. 22, 23, and 24, the expressions of  $\theta_N$ ,  $\theta_{C_2H_2}$ , and  $\theta_{C_2H_3N}$  can be obtained.

$$\theta_N = K_{ad,1}^{0.5} P_{N_2}^{0.5} (1 - \Sigma \theta_i) \quad (\text{eq. 25})$$

$$\theta_{C_2H_2} = K_{ad,1}^{-0.5} K_{surf}^{-0.5} K_{de}^{-1} P_{N_2}^{-0.5} P_{H_2}^{0.5} P_{C_2H_3N} (1 - \Sigma \theta_i) \quad (\text{eq. 26})$$

$$\theta_{C_2H_3N} = K_{de}^{-1} P_{C_2H_3N} (1 - \Sigma \theta_i) \quad (\text{eq. 27})$$

Accordingly, the sum of the coverages of adsorbed species can be expressed as:

$$\Sigma\theta_i = \frac{K_{ad,1}^{0.5}P_{N_2}^{0.5} + K_{ad,1}^{-0.5}K_{surf}K_{de}^{-1}P_{N_2}^{-0.5}P_{H_2}^{0.5}P_{C_2H_3N} + K_{de}^{-1}P_{C_2H_3N}}{1 + K_{ad,1}^{0.5}P_{N_2}^{0.5} + K_{ad,1}^{-0.5}K_{surf}K_{de}^{-1}P_{N_2}^{-0.5}P_{H_2}^{0.5}P_{C_2H_3N} + K_{de}^{-1}P_{C_2H_3N}} \quad (\text{eq. 28})$$

Since  $K_{de}$  is assumed to be very large, the sum of the coverages of adsorbed species can be simplified as:

$$\Sigma\theta_i = \frac{K_{ad,1}^{0.5}P_{N_2}^{0.5}}{1 + K_{ad,1}^{0.5}P_{N_2}^{0.5}} \quad (\text{eq. 29})$$

By taking eq. 29 into eq. 21, the expression of the overall rate by assuming CH<sub>4</sub> adsorption is rate-limiting can be obtained as:

$$r = k_{ad,2}P_{CH_4}^2 \frac{1}{1 + K_{ad,1}^{0.5}P_{N_2}^{0.5}} \quad (\text{eq. 30})$$

### III. Assuming the surface reaction step ( $s_3'$ ) is rate-limiting

The rate of the step of surface reaction should be close to the rate of the overall reaction:

$$r = k_{surf}\theta_{C_2H_2}^2\theta_N^2P_{H_2} \quad (\text{eq. 31})$$

Then, N<sub>2</sub> adsorptions (eq. 7), CH<sub>4</sub> adsorption (eq. 8), and ACN desorption (eq. 10) should attain the equilibrium, thereby yielding:

$$K_{ad,1} = \frac{\theta_N^2}{P_{N_2}(1 - \Sigma\theta_i)^2} \quad (\text{eq. 32})$$

$$K_{ad,2} = \frac{\theta_{C_2H_2}P_{H_2}^3}{P_{CH_4}^2(1 - \Sigma\theta_i)} \quad (\text{eq. 33})$$

$$K_{de} = \frac{P_{C_2H_3N}(1 - \Sigma\theta_i)}{\theta_{C_2H_3N}} \quad (\text{eq. 34})$$

By rearranging eqs. 32, 33, and 34, the expressions of  $\theta_N$ ,  $\theta_{C_2H_2}$ , and  $\theta_{C_2H_3N}$  can be obtained.

$$\theta_N = K_{ad,1}^{0.5}P_{N_2}^{0.5}(1 - \Sigma\theta_i) \quad (\text{eq. 35})$$

$$\theta_{C_2H_2} = K_{ad,2}P_{CH_4}^2P_{H_2}^{-3}(1 - \Sigma\theta_i) \quad (\text{eq. 36})$$

$$\theta_{C_2H_3N} = K_{de}^{-1}P_{C_2H_3N}(1 - \Sigma\theta_i) \quad (\text{eq. 37})$$

Accordingly, the sum of the coverages of adsorbed species can be expressed as:

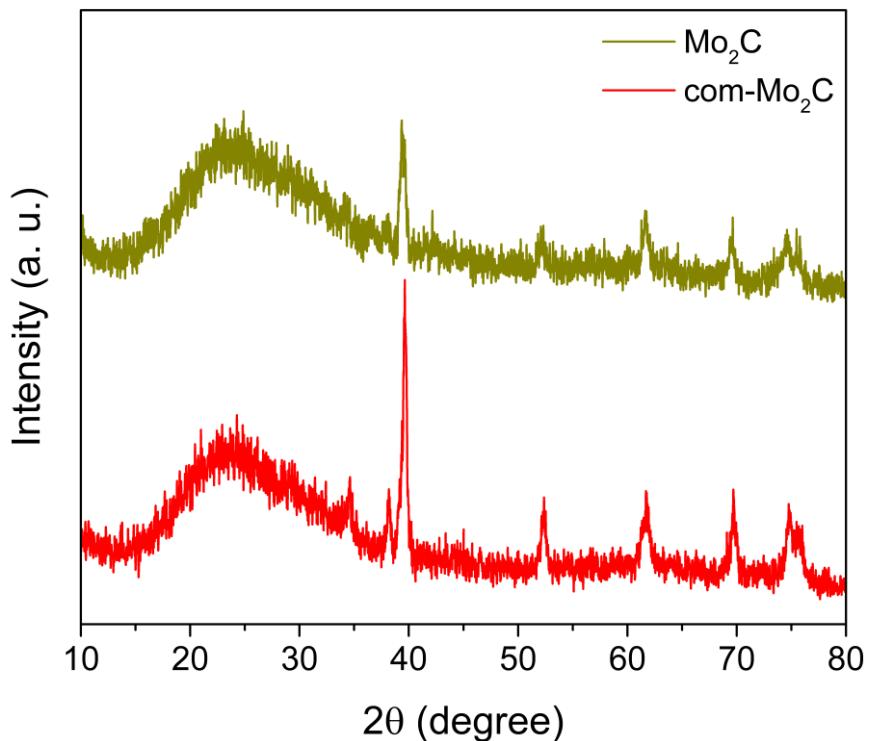
$$\Sigma\theta_i = \frac{K_{ad,1}^{0.5}P_{N_2}^{0.5} + K_{ad,2}P_{CH_4}^2P_{H_2}^{-3} + K_{de}^{-1}P_{C_2H_3N}}{1 + K_{ad,1}^{0.5}P_{N_2}^{0.5} + K_{ad,2}P_{CH_4}^2P_{H_2}^{-3} + K_{de}^{-1}P_{C_2H_3N}} \quad (\text{eq. 38})$$

Since  $K_{de}$  is assumed to be very large, the sum of the coverages of adsorbed species can be simplified as

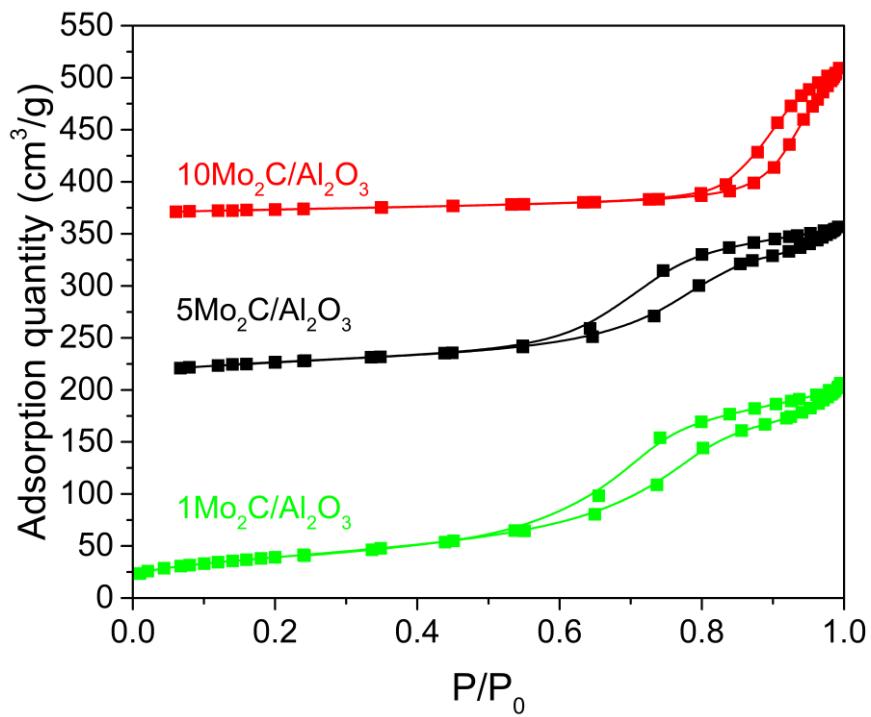
$$\Sigma\theta_i = \frac{K_{ad,1}^{0.5}P_{N_2}^{0.5} + K_{ad,2}P_{CH_4}^2P_{H_2}^{-3}}{1 + K_{ad,1}^{0.5}P_{N_2}^{0.5} + K_{ad,2}P_{CH_4}^2P_{H_2}^{-3}} \quad (\text{eq. 39})$$

By taking eq. 39 into eq. 31, the expression of the overall rate by assuming the surface reaction is rate-limiting can be obtained as:

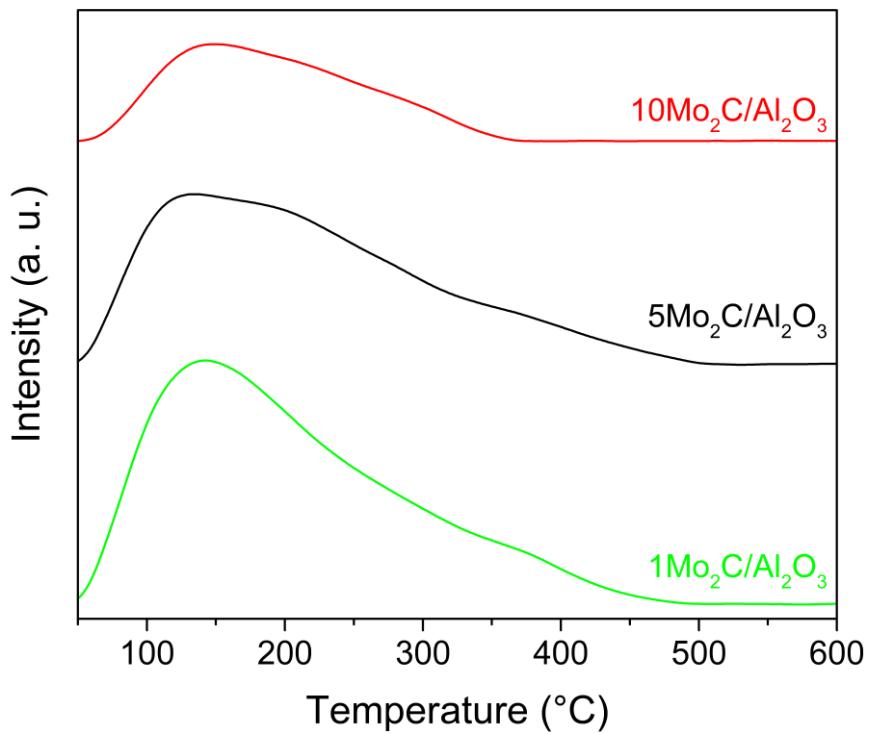
$$r_{ACN} = k_{surf} K_{ad,1} K_{ad,2}^2 P_{H_2}^{-5} P_{CH_4}^4 P_{N_2} \cdot (1 + K_{ad,1}^{0.5} P_{N_2}^{0.5} + K_{ad,2} P_{CH_4}^2 P_{H_2}^{-3})^{-4} \quad (\text{eq. 40})$$



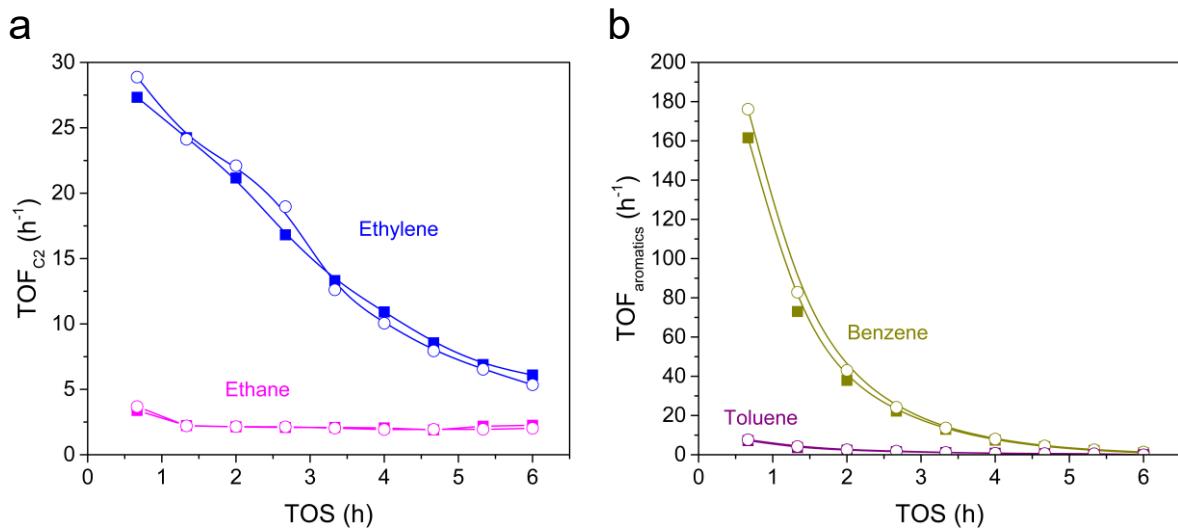
**Figure S1.** XRD patterns of unsupported Mo<sub>2</sub>C and commercial Mo<sub>2</sub>C (com-Mo<sub>2</sub>C).



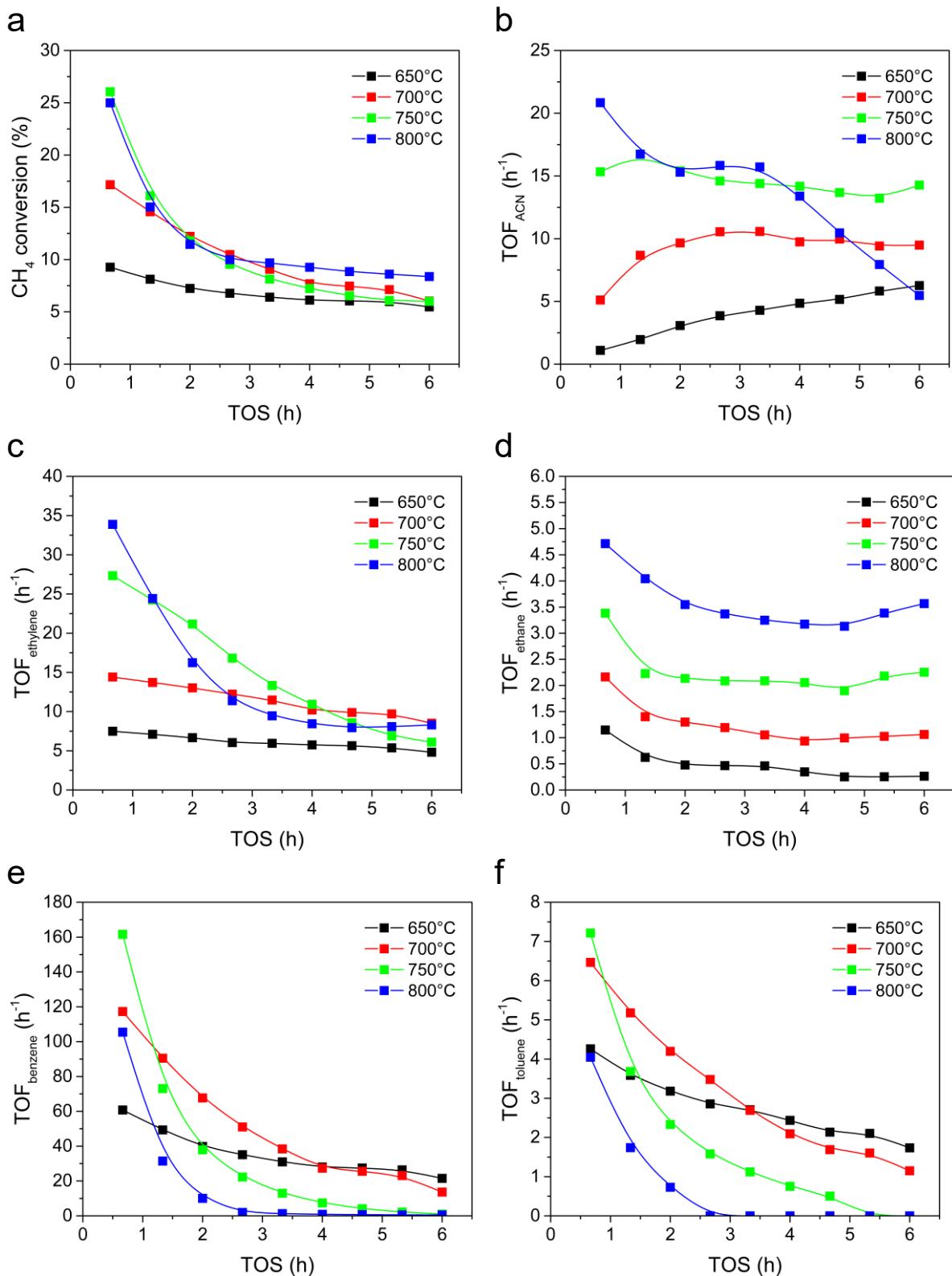
**Figure S2.** N<sub>2</sub> adsorption-desorption isotherms of Al<sub>2</sub>O<sub>3</sub>-supported MoC<sub>x</sub> catalysts.



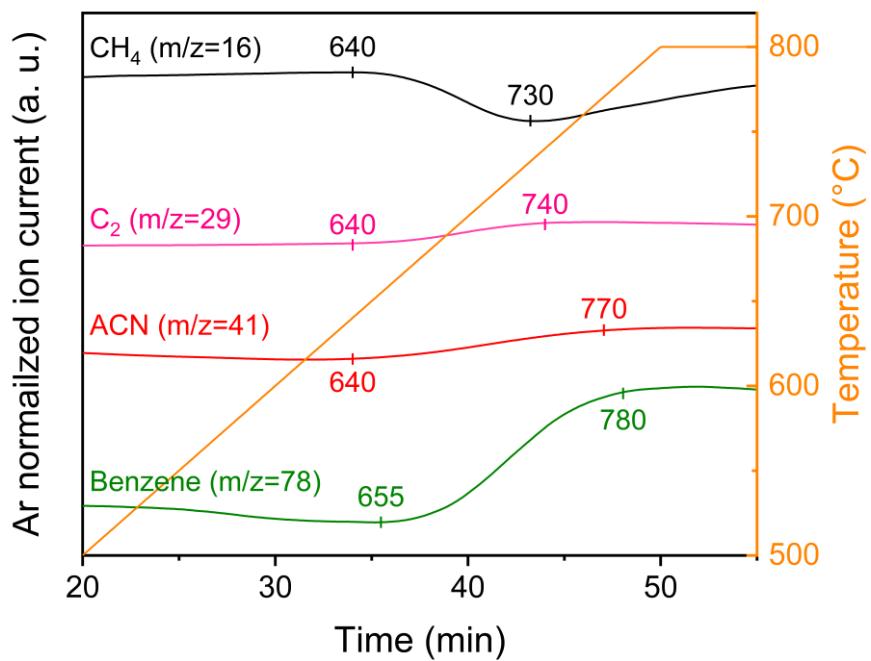
**Figure S3.** NH<sub>3</sub>-TPD profiles of Al<sub>2</sub>O<sub>3</sub>-supported MoC<sub>x</sub> catalysts.



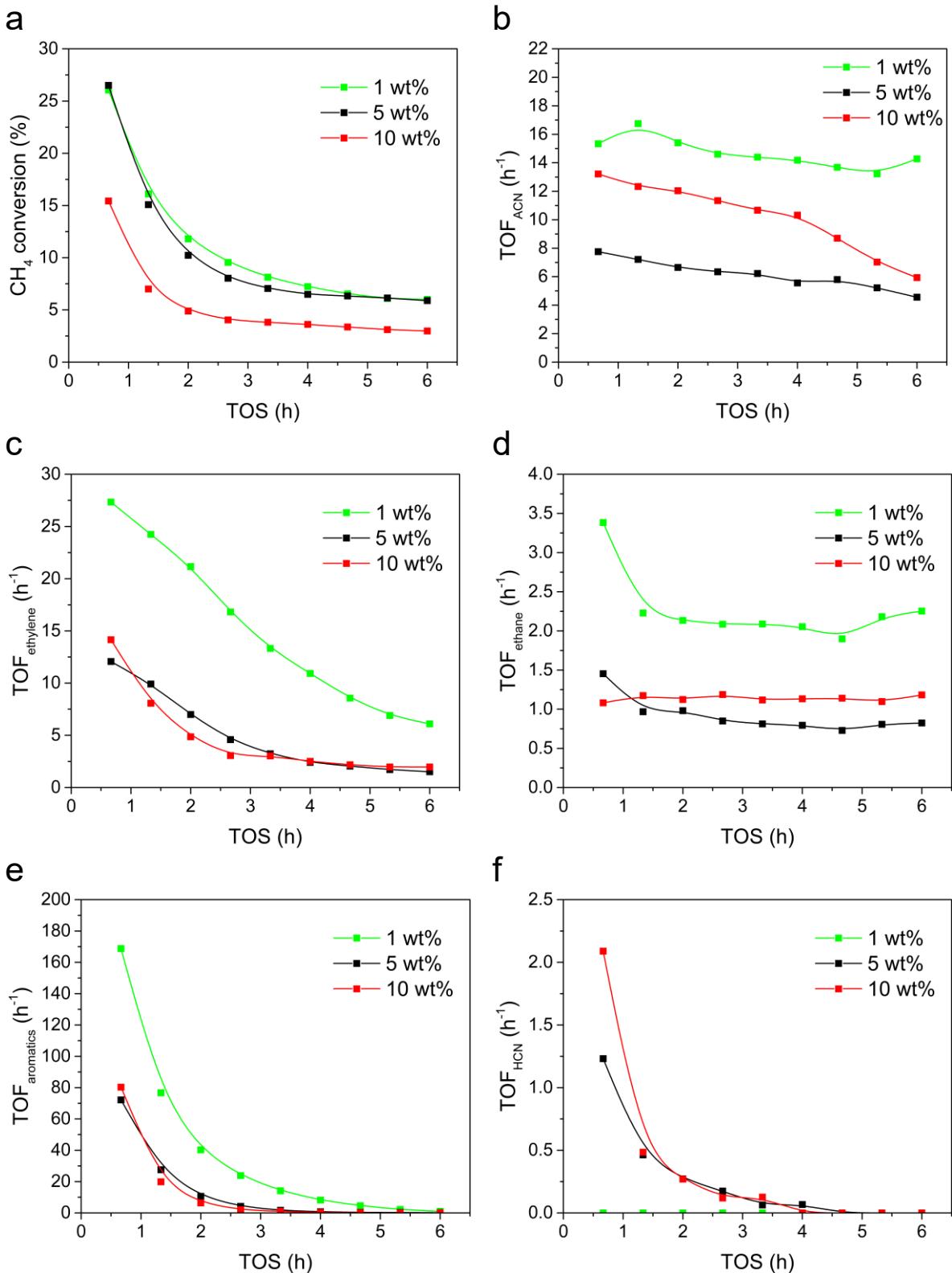
**Figure S4.** TOS profile of TOFs of (a) C<sub>2</sub> (ethylene, blue; ethane, magenta) and (b) aromatics (benzene, dark yellow; toluene, purple) in N<sub>2</sub> (closed squares) and Ar (opened circles) steams. *Reaction conditions: 0.18 g of 1MoC<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub>, reaction temperature = 750 °C, GHSV = 1500 mLCH<sub>4</sub>/g<sub>cat</sub>/h, feed = 4.5/4.5/1 mL/min of CH<sub>4</sub>/N<sub>2</sub>/Ar or 4.5/5.5 mL/min of CH<sub>4</sub>/Ar.*



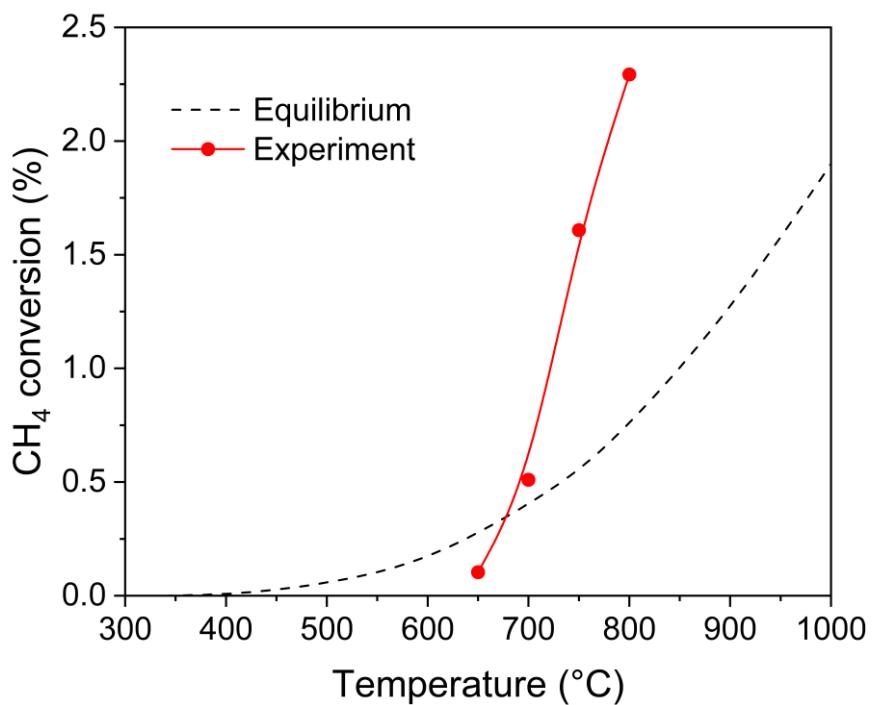
**Figure S5.** TOS profiles of the temperature effect on (a) CH<sub>4</sub> conversion and TOF profiles of (b) ACN, (c) ethylene, (d) ethane, (e) benzene, and (f) toluene by using 1MoC<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub>.



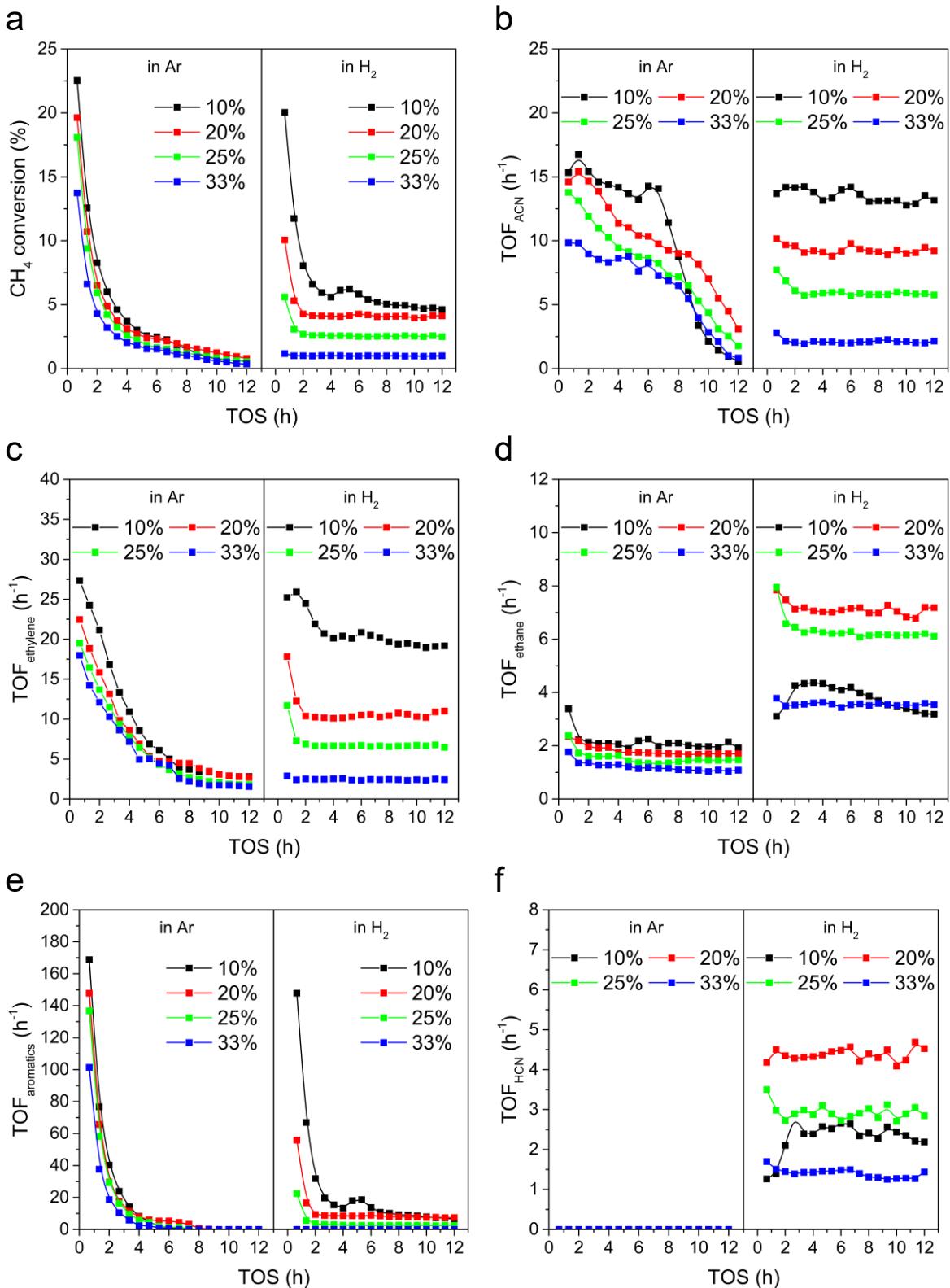
**Figure S6.** CH<sub>4</sub>-TPSR profile of 1MoC<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub>. *Reaction conditions:* 0.18 g of 1MoC<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub>, 300–800 °C (10 °C/min), 4.5 + 4.5 + 1 mL/min of CH<sub>4</sub> + N<sub>2</sub> + Ar.



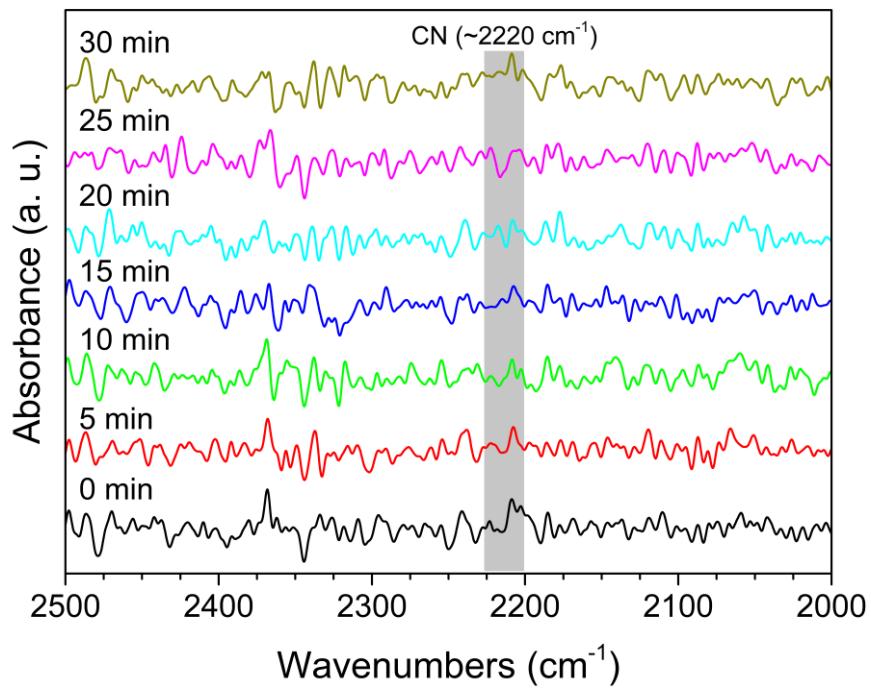
**Figure S7.** TOS profiles of the effect of Mo loading on (a)  $\text{CH}_4$  conversion and TOFs of (b) ACN, (c) ethylene, (d) ethane, (e) aromatics, and (f) HCN.



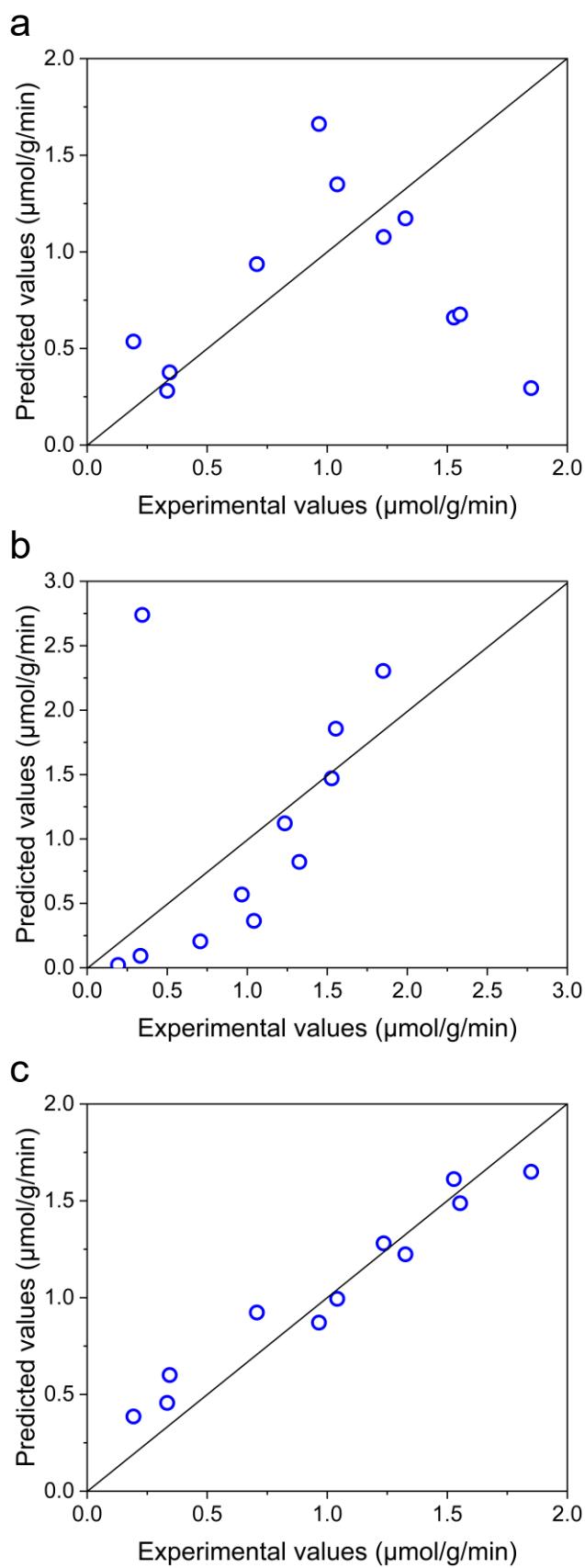
**Figure S8.** Methane conversion as a function of temperature.



**Figure S9.** TOS profiles of the dilution and H<sub>2</sub> concentration effect on (a) CH<sub>4</sub> conversion and TOFs of (b) ACN, (c) ethylene, (d) ethane, (e) aromatics, and (f) HCN by using 1MoC<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub>.



**Figure S10.** DRIFTS spectra during  $\text{N}_2$  purging at  $750^\circ\text{C}$  by using  $1\text{MoC}_x/\text{Al}_2\text{O}_3$  catalyst. The background was collected at  $750^\circ\text{C}$ . Each spectrum was collected using 128 scans.



**Figure S11.** The parity plot of the reaction rate by assuming (a)  $\text{N}_2$  adsorption, (b)  $\text{CH}_4$  adsorption, and (c) surface reaction is rate-limiting in methane and  $\text{N}_2$  conversion to ACN.

**Table S1.** Equilibrium constant and relative compositions of methane, N<sub>2</sub>, ACN, and H<sub>2</sub> as the function of temperature in the conversion of methane to ACN.<sup>a</sup>

Temperature (°C)	K <sub>eq</sub>	Composition (mol)			
		CH <sub>4</sub>	N <sub>2</sub>	CH <sub>3</sub> CN	H <sub>2</sub>
300	3.14 x 10 <sup>-17</sup>	2.000	0.500	0.000	0.000
400	3.73 x 10 <sup>-14</sup>	2.000	0.500	0.000	0.000
500	6.25 x 10 <sup>-12</sup>	1.999	0.500	0.001	0.001
600	2.89 x 10 <sup>-10</sup>	1.997	0.499	0.002	0.004
700	5.48 x 10 <sup>-9</sup>	1.992	0.498	0.004	0.010
<b>750</b>	<b>1.86 x 10<sup>-8</sup></b>	<b>1.989</b>	<b>0.497</b>	<b>0.006</b>	<b>0.014</b>
800	5.48 x 10 <sup>-8</sup>	1.985	0.496	0.008	0.019
900	3.40 x 10 <sup>-7</sup>	1.975	0.494	0.013	0.032
1000	1.46 x 10 <sup>-6</sup>	1.962	0.490	0.019	0.048

**Table S2.** Percentage of Mo and C species at the surface of  $\text{MoC}_x$  catalysts.

Catalyst	Mo 3d				C 1s				C/Mo ratio <sup>a</sup>
	Mo <sup>6+</sup>	Mo <sup>4+</sup>	Mo <sup>3+</sup>	Mo <sup>2+</sup>	C–Mo	C–C	C–O	C=O	
$\text{Mo}_2\text{C}$	89.9	0	2.7	7.4	22.7	65.5	5.4	6.4	0.20
$1\text{MoC}_x/\text{Al}_2\text{O}_3$	47.5	15.6	8.8	28.1	32.3	41.8	25.7	0.2	1.04
spent $1\text{MoC}_x/\text{Al}_2\text{O}_3$ (6-h, Ar)	82.8	5.7	3.5	8.0	0	76.8	16.2	7.1	5.66
spent $1\text{MoC}_x/\text{Al}_2\text{O}_3$ (6-h, H <sub>2</sub> )	77.0	12.2	2.2	8.6	0	75.9	18.7	5.4	5.56
spent $1\text{MoC}_x/\text{Al}_2\text{O}_3$ (12-h, Ar)	86.7	10.4	0.8	2.1	0	86.5	9.3	4.2	11.23
spent $1\text{MoC}_x/\text{Al}_2\text{O}_3$ (12-h, H <sub>2</sub> )	80.2	10.7	2.2	6.9	0	78.7	21.3	0	6.78

<sup>a</sup> Obtained by survey spectra.

**Table S3.** CO and N<sub>2</sub> uptakes over Al<sub>2</sub>O<sub>3</sub>-supported MoC<sub>x</sub> catalysts.

Catalyst	CO uptake ( $\mu\text{mol/g}$ )	N <sub>2</sub> uptake ( $\mu\text{mol/g}$ )	CO/N <sub>2</sub> ratio
1MoC <sub>x</sub> /Al <sub>2</sub> O <sub>3</sub>	15.2	14.9	1.02
5MoC <sub>x</sub> /Al <sub>2</sub> O <sub>3</sub>	17.3	16.0	1.08
10MoC <sub>x</sub> /Al <sub>2</sub> O <sub>3</sub>	21.7	21.5	1.01

**Table S4.** Catalytic data of CH<sub>4</sub> and N<sub>2</sub> conversion to ACN by using 1MoC<sub>x</sub>/Al<sub>2</sub>O<sub>3</sub> at 650 °C.

Entry	Feed composition (mL/min)			CH <sub>4</sub> conversion (%)	Components concentration (μmol/mL)			Reaction rate (μmol/g/min)
	CH <sub>4</sub>	N <sub>2</sub>	Ar		CH <sub>4</sub>	N <sub>2</sub> <sup>a</sup>	H <sub>2</sub> <sup>b</sup>	
1	0.8	8.3	1	4.1	0.95	10.89	0.17	0.03
2	1.5	7.5	1	2.4	1.93	9.90	0.27	0.06
3	2.3	6.8	1	2.7	2.89	8.91	0.47	0.13
4	3.0	6.0	1	2.6	3.86	7.92	0.65	0.19
5	3.8	5.3	1	2.5	4.83	6.93	0.87	0.17
6	4.5	4.5	1	2.4	5.80	5.94	0.90	0.24
7	5.3	3.8	1	2.2	6.78	4.95	1.04	0.22
8	6.0	3.0	1	2.1	7.75	3.96	1.03	0.27
9	6.8	2.3	1	2.1	8.72	2.97	1.25	0.28
10	7.5	1.5	1	2.0	9.70	1.98	1.16	0.33
11	8.3	0.8	1	2.7	10.60	0.99	2.19	0.06

<sup>a</sup> N<sub>2</sub> concentration was estimated using the mass balance of N atom as C<sub>N2, outlet</sub> = C<sub>N2, inlet</sub> - C<sub>ACN</sub>.

<sup>b</sup> H<sub>2</sub> concentration was estimated using the mass balance of H atom as C<sub>H2, outlet</sub> = 0.5\*(4\*C<sub>CH4, inlet</sub> - 3\*C<sub>ACN</sub> - 4\*C<sub>C2H4</sub> - 6\*C<sub>C2H6</sub> - 6\*C<sub>C6H6</sub>).

**Table S5.** Kinetic parameters obtained from the nonlinear regression of the derived rate expressions (eqs. 20, 30, and 40, respectively, of the ESI).

<b>Rate-limiting step</b>	<b>k<sub>1</sub></b>	<b>K<sub>1</sub></b>	<b>k<sub>2</sub></b>	<b>K<sub>2</sub></b>	<b>k<sub>3</sub></b>
N <sub>2</sub> adsorption	4.8 x 10 <sup>-1</sup>	-	-	1.2 x 10 <sup>-2</sup>	-
CH <sub>4</sub> adsorption	-	-6.0 x 10 <sup>-1</sup>	2.4 x 10 <sup>-2</sup>	-	-
Surface reaction	-	2.0	-	3.7 x 10 <sup>-2</sup>	54.7