## Supporting Information

## Coordination recognition of differential template units of lanthanide chiral chain

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## Materials and Measurements.

All chemicals and solvents were analytical grade and were used without further purification. The infrared spectra were carried out on a Pekin-Elmer Two spectrophotometer with pressed KBr pellets. The elemental analyses were determined on a Perkin-Elmer model $240^{\circ} \mathrm{C}$ elemental analyzer. The powder X-ray diffraction (PXRD) spectra were measured on a Rigaku D/Max-3c diffractometer with $\mathrm{Cu} K \alpha$ radiation $(\lambda=1.5418 \AA$ ). Thermogravimetric analyses were performed on a PerkinElmer Pyris Diamond TG-DTA instrument under an $\mathrm{N}_{2}$ atmosphere using a heating rate of $5{ }^{\circ} \mathrm{C} \mathrm{min}^{-1}$ from room temperature up to $1000^{\circ} \mathrm{C}$. The circular dichroism (CD) spectra were recorded on a JASCO J-1500 spectropolarimeter at room temperature. Magnetic properties were performed on a Superconducting Quantum Interference Device (SQUID) magnetometer. The diamagnetism of all constituent atoms was corrected with Pascal's constant.

## X-ray crystallography.

Single-crystal X-ray diffraction (SCXRD) data were collected on a ROD, Synergy Custom DW system, HyPix diffractometer $(\mathrm{Cu}-\mathrm{K} \alpha$ radiation and $\lambda=1.54184 \AA)$ in $\Phi$ and $\omega$ scan modes. The structures were solved by direct methods, and refined by a full-matrix least-squares method on the basis of $F^{2}$ by using SHELXL and OLEX2. ${ }^{[1]}$ Anisotropic thermal parameters were applied to all nonhydrogen atoms. Hydrogen atoms were generated geometrically. The crystallographic data for the $\boldsymbol{R} \mathbf{- 1}$, $\boldsymbol{S} \mathbf{- 1 , ~} \boldsymbol{R}-\mathbf{2}$ and $\boldsymbol{S} \mathbf{- 2}$ are listed in Table S1, and selected bond lengths and angles are given in Table S2-S5. The CCDC reference numbers for the crystal structures of $\boldsymbol{R} \mathbf{- 1}, \boldsymbol{R} \mathbf{- 2}, \boldsymbol{S} \mathbf{- 1}$ and $\boldsymbol{S} \mathbf{- 2}$ are 2306659 , 2306660, 2306784, 2306664, respectively.
[1] Sheldrick, G. M. Acta Crystallogr., Sect. C: Struct. Chem. 2015, 71, 3-8.

Table S1. Crystallographic data of the $\boldsymbol{R} \mathbf{- 1 , S - 1 , R - 2}$ and $\boldsymbol{S} \mathbf{- 2}$.

|  | R-1 | $\boldsymbol{S - 1}$ | R-2 | S-2 |
| :---: | :---: | :---: | :---: | :---: |
| Formula | $\mathrm{C}_{33} \mathrm{H}_{53} \mathrm{Cl}_{4} \mathrm{Dy}_{2} \mathrm{~N}_{7} \mathrm{O}_{15}$ | $\mathrm{C}_{33} \mathrm{H}_{54} \mathrm{Cl}_{4} \mathrm{Dy}_{2} \mathrm{~N}_{6} \mathrm{O}_{15}$ | $\mathrm{C}_{30} \mathrm{H}_{43} \mathrm{Cl}_{4} \mathrm{Dy}_{2} \mathrm{~N}_{6} \mathrm{O}_{13}$ | $\mathrm{C}_{31} \mathrm{H}_{45} \mathrm{Cl}_{4} \mathrm{Dy}_{2} \mathrm{~N}_{6} \mathrm{O}_{13}$ |
| Formula weight | 1254.62 | 1241.62 | 1162.50 | 1176.53 |
| $T, \mathrm{~K}$ | 100.00(10) | 100.00(10) | 100.00(10) | 100.00(10) |
| Crystal system | orthorhombic | orthorhombic | orthorhombic | orthorhombic |
| Space group | $P 2_{12} 2_{1} 2_{1}$ | $P 2_{12} 2_{1} 2_{1}$ | $P 2_{12} 2_{1} 2_{1}$ | $P 2_{12} 2_{1} 2_{1}$ |
| $a, \AA$ | 13.47190(10) | 13.47640(10) | 13.06030(10) | 13.07500(10) |
| $b, \AA$ | 14.86600(10) | 14.86660(10) | 17.6285(2) | 17.6728(2) |
| $c, \AA$ | 24.0640(2) | 24.0565(2) | 17.9734(2) | 18.0533(2) |
| $\alpha,{ }^{\circ}$ | 90 | 90 | 90 | 90 |
| $\beta,{ }^{\circ}$ | 90 | 90 | 90 | 90 |
| $\gamma,{ }^{\circ}$ | 90 | 90 | 90 | 90 |
| $V, \AA^{3}$ | 4819.38(6) | 4819.68(6) | 4138.08(7) | 4171.61(7) |
| $Z$ | 4 | 4 | 4 | 4 |
| $D_{\mathrm{c}}, \mathrm{g} \mathrm{cm}^{-3}$ | 1.729 | 1.711 | 1.866 | 1.873 |
| $\mu, \mathrm{mm}^{-1}$ | 19.018 | 19.002 | 22.046 | 21.880 |
| $F(000)$ | 2480.0 | 2456.0 | 2276.0 | 2308.0 |
| $\begin{aligned} & 2 \theta \text { range for } \\ & \quad \text { data } \\ & \text { collection } /{ }^{\circ} \end{aligned}$ | 6.992 to 151.706 | 6.99 to 151.672 | 7.024 to 133.202 | 7 to 133.168 |
| Reflns coll. | 32105 | 32245 | 26441 | 26211 |
| Unique reflns | 9709 | 9704 | 7307 | 7375 |
| $R_{\text {int }}$ | 0.0449 | 0.0431 | 0.0516 | 0.0534 |
| $R_{1}{ }^{\text {a }}(I>2 \sigma(I))$ | 0.0451 | 0.0431 | 0.0403 | 0.0390 |
| $w R_{2}{ }^{\text {b }}$ (all data) | 0.1248 | 0.1138 | 0.1046 | 0.1004 |
| GOF | 1.092 | 1.115 | 1.045 | 1.030 |
| Flack parameter | 0.016(3) | 0.011(2) | 0.008(3) | 0.003(3) |

$$
{ }^{\mathrm{a}} R_{1}=\Sigma| | F_{\mathrm{o}}\left|-\left|F_{\mathrm{c}}\right| / \Sigma\right| \mathrm{F}_{\mathrm{o}} \mid,{ }^{\mathrm{b}} \mathrm{w} R_{2}=\left[\Sigma \mathrm{w}\left(F_{\mathrm{o}}^{2}-F_{\mathrm{c}}^{2}\right)^{2} / \Sigma \mathrm{w}\left(F_{\mathrm{o}}^{2}\right)^{2}\right]^{1 / 2}
$$





Figure S2. Powder diffraction pattern (PXRD) of $\boldsymbol{R} \mathbf{- 1 ,} \boldsymbol{S} \mathbf{- 1 , ~} \boldsymbol{R} \mathbf{- 2}$ and $\boldsymbol{S} \mathbf{- 2}$ (a-d).


Figure S3. TG curve of $\boldsymbol{R} \mathbf{- 1}, \boldsymbol{S} \mathbf{- 1}, \boldsymbol{R} \mathbf{- 2}$ and $\boldsymbol{S} \mathbf{- 2}$ (a), DSC curve of $\boldsymbol{R} \mathbf{- 1}, \boldsymbol{S} \mathbf{- 1 , \boldsymbol { R } - \mathbf { 2 }}$ and $\boldsymbol{S} \mathbf{- 2}$ (b).
In order to explore the thermal stability of $\boldsymbol{R} \mathbf{- 1} / \boldsymbol{S} \mathbf{- 1}$ and $\boldsymbol{R} \mathbf{- 2} / \boldsymbol{S} \mathbf{- 2}$, TG-DSC study was conducted. The thermal stability analysis of $\boldsymbol{R} \mathbf{- 1} / \boldsymbol{S} \mathbf{- 1}$ and $\boldsymbol{R} \mathbf{- 2} / \boldsymbol{S} \mathbf{- 2}$ was performed in a flowing $\mathrm{N}_{2}$ atmosphere while the temperature was slowly increased from $35^{\circ} \mathrm{C}$ to $1,000{ }^{\circ} \mathrm{C}$ at a rate of $5{ }^{\circ} \mathrm{C} \mathrm{min}{ }^{-1}$. The DSC test was also performed in a flowing $\mathrm{N}_{2}$ atmosphere, and the temperature was slowly increased from $35^{\circ} \mathrm{C}$ to $450^{\circ} \mathrm{C}$ at a rate of $5^{\circ} \mathrm{C} \mathrm{min}^{-1}$. It can be seen from the TG-DSC curve that complex $\boldsymbol{R} \mathbf{- 1}$ has three
weight loss processes. First, in the temperature range of $35-200{ }^{\circ} \mathrm{C}$, the weight loss rate of complex $\boldsymbol{R} \mathbf{- 1}$ is $16.37 \%$ (theoretical value is $16.33 \%$ ), and a sharp exothermic peak is observed at $117.3^{\circ} \mathrm{C}$ in the DSC curve, corresponding to the loss of four free $\mathrm{CH}_{3} \mathrm{OH}$ molecules, one free $\mathrm{CH}_{3} \mathrm{CN}$ molecule and two free $\mathrm{H}_{2} \mathrm{O}$ molecules. Secondly, as the temperature increases from $200^{\circ} \mathrm{C}$ to $365^{\circ} \mathrm{C}$, the weight loss rate of complex $\boldsymbol{R} \mathbf{- 1}$ is $7.59 \%$ (theoretical value is $7.65 \%$ ), and a weak exothermic peak is observed at $328.4{ }^{\circ} \mathrm{C}$ in the DSC curve, corresponding to the loss of three terminally coordinated $\mathrm{CH}_{3} \mathrm{OH}$ molecules. Finally, as the temperature increased from $365^{\circ} \mathrm{C}$ to $600^{\circ} \mathrm{C}$, the sample mass decreased sharply, and an exothermic peak was observed at $394.1^{\circ} \mathrm{C}$ in the DSC curve, which can be attributed to the degradation/combustion of the organic ligand part and the rapid decomposition of $\boldsymbol{R} \mathbf{- 1}$ to produce dysprosium(III) oxide (Figure S3a and S3b). Similarly, there are also three weight loss processes for $\boldsymbol{S} \mathbf{- 1}$. First, in the temperature range of $35-270{ }^{\circ} \mathrm{C}$, the weight loss rate of $\boldsymbol{S} \mathbf{- 1}$ is $15.31 \%$ (theoretical value is $15.42 \%$ ), and a sharp exothermic peak is observed at $127.8^{\circ} \mathrm{C}$ in the DSC curve, corresponding to the loss of six free $\mathrm{CH}_{3} \mathrm{OH}$ molecules. Secondly, as the temperature increases from $270{ }^{\circ} \mathrm{C}$ to 385 ${ }^{\circ} \mathrm{C}$, the weight loss rate of complex $\boldsymbol{S} \mathbf{- 1}$ is $7.53 \%$ (theoretical value is $7.71 \%$ ), and a weak exothermic peak is observed at $317.5^{\circ} \mathrm{C}$ in the DSC curve, corresponding to the loss of three terminally coordinated $\mathrm{CH}_{3} \mathrm{OH}$ molecules. Finally, as the temperature increased from $385{ }^{\circ} \mathrm{C}$ to $600{ }^{\circ} \mathrm{C}$, the sample mass decreased sharply, and an exothermic peak was observed at $400.9^{\circ} \mathrm{C}$ in the DSC curve, which can be attributed to the degradation/combustion of the organic ligand part and the rapid decomposition of $\boldsymbol{S} \mathbf{- 1}$ to produce dysprosium(III) oxide (Figure S3a and S3b). Complex $\boldsymbol{R} \mathbf{- 2}$ has two weight loss processes. When the temperature gradually increases from $35^{\circ} \mathrm{C}$ to $330^{\circ} \mathrm{C}$, the weight loss rate of complex $\boldsymbol{R} \mathbf{- 2}$ is $\mathbf{1 8 . 0 1 \%}$ (theoretical value is $18.04 \%$ ), and three obvious exothermic peaks were observed at $86.9^{\circ} \mathrm{C}, 113.6^{\circ} \mathrm{C}$ and $214.1^{\circ} \mathrm{C}$ in the DSC curve, respectively. This process corresponds to the loss of four free $\mathrm{CH}_{3} \mathrm{OH}$ molecules, two terminally coordinated $\mathrm{CH}_{3} \mathrm{OH}$ molecule and one free $\mathrm{H}_{2} \mathrm{O}$ molecule. When the temperature exceeds $330^{\circ} \mathrm{C}$ to $500^{\circ} \mathrm{C}$, the sample mass decreases sharply, and an obvious endothermic peak is observed at $350^{\circ} \mathrm{C}$ in the DSC curve, which can be attributed to the degradation/combustion of the organic ligand part and the rapid decomposition of $\boldsymbol{R} \mathbf{- 2}$ to produce dysprosium(III) oxide (Figure S3a and S3b). Similarly, when the temperature gradually increases from $35^{\circ} \mathrm{C}$ to $340^{\circ} \mathrm{C}$, the weight loss rate of $\boldsymbol{S} \mathbf{- 2}$ is $18.53 \%$ (theoretical value is $19.03 \%$ ), and three obvious exothermic peaks were observed at $89.7^{\circ} \mathrm{C}, 136.5^{\circ} \mathrm{C}$ and $223.5^{\circ} \mathrm{C}$ in the DSC curve, respectively. This process corresponds to the loss of two free $\mathrm{CH}_{3} \mathrm{OH}$ molecules and two
terminally coordinated $\mathrm{CH}_{3} \mathrm{OH}$ molecules. When the temperature exceeds $340{ }^{\circ} \mathrm{C}$ to $500{ }^{\circ} \mathrm{C}$, the sample mass decreases sharply, and an obvious endothermic peak is observed at $360^{\circ} \mathrm{C}$ in the DSC curve, which can be attributed to the degradation/combustion of the organic ligand part and the rapid decomposition of $\boldsymbol{S} \mathbf{- 2}$ to produce dysprosium(III) oxide (Figure S3a and S3b).


Figure S4. Temperature dependence of $\chi_{\mathrm{m}} T$ for $\boldsymbol{S} \mathbf{- 1}$ (a) and $\boldsymbol{S} \mathbf{- 2}$ (c); $M$ vs. $H / T$ plots of $\boldsymbol{S} \mathbf{- 1}$ (b) and $\boldsymbol{S} \mathbf{- 2}$ (d).


Figure S5. Loop curve graph of $\boldsymbol{R} \mathbf{- 1}$ (a), $\boldsymbol{S} \mathbf{- 1}$ (b), $\boldsymbol{R} \mathbf{- 2}$ (c) and $\boldsymbol{S} \mathbf{- 2}$ (d) at 2 K.


Figure S6. Temperature-dependent $\chi^{\prime}$ and $\chi^{\prime \prime}$ AC susceptibilities under 0 Oe DC fields for $\boldsymbol{R} \mathbf{- 1}, \boldsymbol{S} \mathbf{- 1}$, $\boldsymbol{R - 2}$ and $\boldsymbol{S}$-2 (a-d).


Figure S7. Frequency-dependence of the in-of-phase ( $\chi^{\prime}$ ) and the out-of-phase ( $\chi^{\prime \prime}$ ) components under 0 Oe DC fields for $\boldsymbol{R} \mathbf{- 1}, \boldsymbol{S} \mathbf{- 1}, \boldsymbol{R}-\mathbf{2}$ and $\boldsymbol{S} \mathbf{- 2}$ (a-h).


Figure S8. Temperature-dependent $\chi^{\prime}$ and $\chi^{\prime \prime}$ AC susceptibilities under 1200 Oe DC fields for $\boldsymbol{R} \mathbf{- 1}$ (a), 800 Oe DC fields for $\boldsymbol{S} \mathbf{- 1}$ (b), 1000 Oe DC fields for $\boldsymbol{R} \mathbf{- 2}$ (c) and 800 Oe DC fields for $\boldsymbol{S}$-2 (d).


Figure S9. Frequency-dependence of the in-of-phase ( $\chi^{\prime}$ ) and the out-of-phase ( $\chi^{\prime \prime}$ ) components under 1200 Oe DC fields for $\boldsymbol{R} \mathbf{- 1}$ (a and b), 800 Oe DC fields for $\boldsymbol{S} \mathbf{- 1}$ (c and d), 1000 Oe DC fields for $\boldsymbol{R} \mathbf{- 2}$ (e and f) and 800 Oe DC fields for $\boldsymbol{S} \mathbf{- 2}$ ( g and h).

Table S2. Selected bond lengths $(\AA)$ and angles $\left({ }^{\circ}\right)$ of $\boldsymbol{R} \mathbf{- 1}$.

| Bond lengths ( $\AA$ ) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Dy1-Cl2 | 2.671(2) | Dy1-N6 | $2.486(8)$ | Dy2-O1 ${ }^{\text {i }}$ | 2.352(6) |
| Dy1-Cl1 | 2.734(3) | Dy1-O7 | 2.427(7) | Dy2-N1 ${ }^{\text {i }}$ | 2.475(8) |
| Dy1-O6 | 2.333 (6) | Dy2-Cl3 | 2.671(2) | Dy2-O9 | $2.339(8)$ |
| Dy1-O5 | 2.421(6) | Dy2-O6 | $2.346(6)$ | Dy2-O8 | 2.396(7) |
| Dy1-O1 ${ }^{\text {i }}$ | 2.371(6) | Dy2-O2 ${ }^{\text {i }}$ | $2.435(6)$ | Dy2-N2 ${ }^{\text {i }}$ | 2.542(8) |
| Dy1-N5 | $2.555(8)$ |  |  |  |  |
| Bond angles ( ${ }^{\circ}$ ) |  |  |  |  |  |
| C12-Dy1-Cl1 | 150.31(8) | N5-Dy1-Cl2 | 74.6(2) | O1--Dy2-O2 ${ }^{\text {i }}$ | 164.6(2) |
| O6-Dy1-Cl2 | 96.43(18) | N5-Dy1-Cl1 | 80.2(2) | O1 ${ }^{\text {i}} \mathrm{-Dy} 2-\mathrm{N} 1^{\text {i }}$ | 66.5(2) |
| O6-Dy1-Cl1 | 86.89(17) | N6-Dy1-Cl2 | 81.15(19) | O1 ${ }^{\text {i}}$-Dy $2-08$ | 89.6(3) |
| O6-Dy1-O5 | 168.9(2) | N6-Dy1-Cl1 | 73.12(19) | O1 ${ }^{\text {i}}$-Dy $2-\mathrm{N} 2^{\text {i }}$ | 128.0(2) |
| O6-Dyl-O1 ${ }^{\text {i }}$ | 67.9(2) | N6-Dy1-N5 | 61.5(2) | N1 ${ }^{\text {i }}$ - ${ }^{\text {dy }} 2-\mathrm{Cl} 3$ | 87.8(2) |
| O6-Dy1-N5 | 128.1(2) | O7-Dy1-Cl2 | 133.07(18) | N1 $1^{\text {i-D }}$ - ${ }^{2} 2-\mathrm{N} 2^{\text {i }}$ | 61.7(2) |
| O6-Dy1-N6 | 66.6(2) | O7-Dy1-Cl1 | 73.60(18) | O9-Dy2-Cl3 | 143.9(2) |
| O6-Dy1-07 | 103.8(2) | O7-Dy1-N5 | 119.7(2) | O9-Dy2-O6 | 136.9(3) |
| O5-Dy1-Cl2 | 81.43(19) | O7-Dy1-N6 | 145.8(3) | O9-Dy2-O2 ${ }^{\text {i }}$ | 82.1(3) |
| O5-Dy1-Cl1 | 100.41(18) | O6-Dy2-Cl3 | 79.03(18) | O9-Dy2-O1 ${ }^{\text {i }}$ | 90.1(3) |
| O5-Dy1-N5 | 62.1(2) | O6-Dy2-O2 ${ }^{\text {i }}$ | 109.2(2) | O9-Dy2-N1 ${ }^{\text {i }}$ | 74.4(3) |
| O5-Dy1-N6 | 123.4(2) | O6-Dy2-O1 ${ }^{\text {i }}$ | 68.0(2) | O9-Dy2-O8 | 74.1(3) |
| O5-Dy1-O7 | 70.7(2) | O6-Dy2-N1 ${ }^{\text {i }}$ | 123.3(2) | O9-Dy2-N2 ${ }^{\text {i }}$ | 72.4(3) |
| O1i-Dy1-Cl2 | 76.82(18) | O6-Dy2-O8 | 69.3(3) | O8-Dy2-Cl3 | 131.7(2) |
| O1i-Dy1-Cl1 | 130.74(18) | O6-Dy2-N2 ${ }^{\text {i }}$ | 150.1(3) | O8-Dy2-O2 ${ }^{\text {i }}$ | 75.5(3) |
| O1--Dyl-O5 | 101.0(2) | O2i-Dy2-Cl3 | 81.99(19) | O8-Dy2-N1 ${ }^{\text {i }}$ | 140.1(3) |
| O1--Dy 1-N5 | 148.5(3) |  | 123.2(2) | O8-Dy2-N2 ${ }^{\text {i }}$ | 128.5(3) |
| O1-Dyl-N6 | 126.2(2) | O2 ${ }^{\text {i }- \text { Dy } 2-N 2 ~}{ }^{\text {i }}$ | 62.1(2) | N2 $2^{\text {i-Dy }} 2-\mathrm{Cl} 3$ | 71.5(2) |
| O1--Dy1-O7 | 72.6(2) | O1-Dy2-Cl3 | 111.55(18) |  |  |

Table S3. Selected bond lengths ( $\AA$ ) and angles $\left({ }^{\circ}\right)$ of $\boldsymbol{S} \mathbf{- 1}$.

| Bond lengths ( $\AA$ ) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Dy1-Cl1 | 2.674(2) | Dy1-N5 | $2.555(7)$ | Dy2-O1 ${ }^{\text {i }}$ | $2.346(5)$ |
| Dy1-Cl2 | $2.735(3)$ | Dy1-N6 | 2.486(7) | Dy2-09 | 2.351(7) |
| Dy1-O6 | $2.337(5)$ | Dy2-Cl3 | 2.671(2) | Dy2-N1 ${ }^{\text {i }}$ | 2.481(7) |
| Dy1-O5 | 2.428(5) | Dy2-O6 | 2.337(5) | Dy2-O8 | 2.391 (7) |
| Dyl-O1 ${ }^{\text {i }}$ | 2.380(5) | Dy2-O2 ${ }^{\text {i }}$ | 2.445(6) | Dy2-N2 ${ }^{\text {i }}$ | $2.537(7)$ |
| Dy1-O7 | $2.426(6)$ |  |  |  |  |
| Bond angles $\left({ }^{\circ}\right)$ |  |  |  |  |  |
| Cl1-Dy1-Cl2 | 150.29(7) | O7-Dy1-Cl2 | 73.31(18) | $\mathrm{O} 1^{\text {i}} \mathrm{-Dy} 2-\mathrm{Cl} 3$ | 111.47(16) |
| O6-Dy1-Cl1 | 96.26(16) | O7-Dy1-O5 | 70.9(2) | O1 ${ }^{\text {i-Dy }} 2-\mathrm{O} 2^{\text {i }}$ | 164.7(2) |
| O6-Dy1-Cl2 | 87.18(15) | O7-Dy1-N5 | 119.6(2) | O1--Dy2-O9 | 90.0(2) |
| O6-Dy1-O5 | 168.82(19) | O7-Dy1-N6 | 145.5(2) | $\mathrm{O} 1^{\mathrm{i}}$-Dy $2-\mathrm{N} 1^{\text {i }}$ | 66.0(2) |
| O6-Dy1-O1 ${ }^{\text {i }}$ | 67.70(19) | N5-Dy1-Cl1 | 74.77(18) | O1--Dy2-O8 | 89.9(2) |
| O6-Dy1-O7 | 103.6(2) | N5-Dy1-Cl2 | 79.98(19) | $\mathrm{O} 1{ }^{\text {i-Dy }} 2-\mathrm{N} 2^{\text {i }}$ | 127.5(2) |
| O6-Dy1-N5 | 128.3(2) | N6-Dy1-Cl1 | 81.10(18) | O9-Dy2-Cl3 | 144.08(18) |
| O6-Dy1-N6 | 66.8(2) | N6-Dy1-Cl2 | 73.16(18) | O9-Dy2-O2 ${ }^{\text {i }}$ | 81.9(2) |
| O5-Dy1-Cl1 | 81.55(16) | N6-Dy1-N5 | 61.5(2) | O9-Dy2-N1 $1^{\text {i }}$ | 74.5(2) |
| O5-Dy1-Cl2 | 100.19(16) | O6-Dy2-Cl3 | 78.99(16) | O9-Dy2-08 | 73.9(3) |
| O5-Dy1-N5 | 61.9(2) | O6-Dy2-O2 ${ }^{\text {i }}$ | 109.32(19) | O9-Dy2-N2 ${ }^{\text {i }}$ | 72.6(2) |
| O5-Dy1-N6 | 123.3(2) | O6-Dy2-O1 ${ }^{\text {i }}$ | 68.26(19) | $\mathrm{N} 1{ }^{\text {i }} \mathrm{-Dy} 2-\mathrm{Cl} 3$ | 88.02(18) |
| O1--Dy1-Cl1 | 76.58(16) | O6-Dy2-09 | 136.8(2) | $\mathrm{N} 1^{\mathrm{i}}$-Dy $2-\mathrm{N} 2^{\mathrm{i}}$ | 61.7(2) |
| O1--Dy1-Cl2 | 131.01(16) | O6-Dy2-N1 ${ }^{\text {i }}$ | 123.2(2) | O8-Dy2-Cl3 | 131.72(19) |
| O1 ${ }^{\text {i-Dy }} 1-\mathrm{O} 5$ | 101.16(19) | O6-Dy2-O8 | 69.5(2) | O8-Dy2-O2 ${ }^{\text {i }}$ | 75.3(2) |
| O1 ${ }^{\text {i-Dy }} 1-\mathrm{O} 7$ | 73.0(2) | O6-Dy2-N2 ${ }^{\text {i }}$ | 150.1(2) | O8-Dy2-N1 ${ }^{\text {i }}$ | 139.9(3) |
| O1 ${ }^{\text {i-Dy }} 1-\mathrm{N} 5$ | 148.5(2) | O2 ${ }^{\text {i }}$ - ${ }^{\text {- }} 22-\mathrm{Cl} 3$ | 82.13(17) | O8-Dy2-N2 ${ }^{\text {i }}$ | 128.5(2) |
| O1 ${ }^{\text {i-Dy }} 1-\mathrm{N} 6$ | 126.1(2) | $\mathrm{O} 2{ }^{2}-\mathrm{Dy} 2-\mathrm{N1}{ }^{\text {i }}$ | 123.3(2) | $\mathrm{N} 2{ }^{\text {i }-\mathrm{Dy} 2-\mathrm{Cl}} 3$ | 71.50(17) |
| O7-Dy1-Cl1 | 133.40(18) | O2 ${ }^{\text {i }}$-Dy2- ${ }^{2}{ }^{\text {i }}$ | 62.3(2) |  |  |

Table S4. Selected bond lengths $(\AA)$ and angles $\left({ }^{\circ}\right)$ of $\boldsymbol{R}$-2.

| Bond lengths ( $\AA$ ) |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Dy1-Cl1 | 2.607(2) | Dy1-N6ii | $2.446(7)$ | Dy2-O7 | $2.369(6)$ |
| Dy1-Cl2 | 2.629(2) | Dy1-N5ii | $2.508(8)$ | $\text { Dy2-N1 }{ }^{\text {i }}$ | $2.496(7)$ |
| Dy1-O1 | 2.291(6) | Dy2-Cl3 | $2.687(2)$ | Dy2-O8 | 2.383(8) |
| Dy1-O5ii | $2.411(7)$ | Dy2-O1 ${ }^{\text {i }}$ | 2.363 (6) | Dy2-N2 ${ }^{\text {i }}$ | $2.538(7)$ |
| Dy1-O6ii | $2.338(6)$ | Dy2-O2 ${ }^{\text {i }}$ | 2.428 (6) | Dy2-O6 | 2.341 (6) |
| Bond angles ( ${ }^{\circ}$ ) |  |  |  |  |  |
| Cl1-Dy1-Cl2 | 171.04(8) | N6ii-Dy 1-Cl2 | 92.49(18) | N1 ${ }^{\text {i- }}$ - ${ }^{\text {dy }} 2-\mathrm{Cl} 3$ | 74.13(16) |
| O1-Dy1-Cl1 | 88.24(16) | $\text { N6ii-Dy1-N5 } 5 \text { ii }$ | 62.7(3) | N1 $1^{\text {i- }}$ Dy $2-\mathrm{N} 2^{\text {i }}$ | 61.6(2) |
| O1-Dy1-Cl2 | 92.32(16) | N5ii-Dyl-Cl1 | 82.6(2) | O8-Dy2-Cl3 | 76.5(2) |
| O1-Dy1-O5ii | 97.8(2) | $\mathrm{N} 5 \mathrm{ii}^{\mathrm{i}-\mathrm{Dy} 1-\mathrm{Cl} 2}$ | 93.9(2) | O8-Dy2-O2 ${ }^{\text {i }}$ | 69.6(3) |
| $\text { O1-Dy1-O6 }{ }^{\mathrm{ii}}$ | 70.3(2) | O1--Dy2-Cl3 | 83.86(15) | O8-Dy2-N1 ${ }^{1}$ | 150.2(3) |
| O1-Dy1-N6ii | 137.3(2) | O1 ${ }^{\text {i- }}$ - ${ }^{\text {dy2-O2 }}{ }^{\text {i }}$ | 167.5(2) | O8-Dy2-N2 ${ }^{\text {i }}$ | $119.8(3)$ |
| O1-Dy1-N5ii | 158.7(2) | O1--Dy2-O7 | 94.2(2) | N2i-Dy2-Cl3 | 83.80(17) |
| O5ii-Dy1-Cl1 | 87.32(18) | O1 ${ }^{1}-\mathrm{Dy} 2-\mathrm{N} 1^{\text {i }}$ | 66.2(2) | O6-Dy2-07 | 75.3(2) |
| O5ii-Dy1-Cl2 | 83.74(18) | O1--Dy2-08 | 105.9(3) | O6-Dy2-N1 ${ }^{1}$ | 124.6(2) |
| O5ii-Dy1-N6 ${ }^{6 i}$ | 124.9(2) | O1 ${ }^{1}-\mathrm{Dy} 2-\mathrm{N} 2^{\text {i }}$ | 127.9(2) | O6-Dy2-08 | $73.0(3)$ |
| $\mathrm{O} 5^{\mathrm{ii}}-\mathrm{Dy} 1-\mathrm{N} 5^{\mathrm{ii}}$ | 62.8(2) | O2 ${ }^{\text {i-Dy } 2-\mathrm{Cl} 3}$ | 105.82(16) | O6-Dy2-N2 ${ }^{\text {i }}$ | 145.0(2) |
| O6ii-Dy1-Cl1 | 100.38(18) | $\mathrm{O} 2^{\mathrm{i}-\mathrm{Dy}} 2-\mathrm{N} 1^{\mathrm{i}}$ | 123.5(2) | O7-Dy2-Cl3 | 149.33(18) |
| O6ii-Dy1-Cl2 | 88.21(18) | O2 $2^{\text {i-Dy }} 2-\mathrm{N} 2^{\text {i }}$ | 62.3(2) | O7-Dy2-O2 ${ }^{\text {i }}$ | 81.5(2) |
| O6ii-Dy1-O5ii | 165.5(2) | O6-Dy2-Cl3 | 130.91(16) | O7-Dy2-N1 ${ }^{1}$ | 77.1(2) |
| O6 ${ }^{\text {iii-Dy1-N6 }}{ }^{\text {6ii }}$ | 67.4(2) | O6-Dy2-O1 ${ }^{\text {i }}$ | 69.1(2) | 07-Dy2-08 | 132.7(3) |
| O6ii-Dy1-N5 ${ }^{\text {ii }}$ | 130.1(2) | O6-Dy2-O2 ${ }^{\text {i }}$ | 98.4(2) | O7-Dy2-N2 ${ }^{\text {i }}$ | 73.2(2) |
| N6ii-Dyl-Cl1 | 93.16(18) |  |  |  |  |

Table S5. Selected bond lengths ( $\AA$ ) and angles $\left({ }^{\circ}\right)$ of $\boldsymbol{S} \mathbf{- 2}$.

| Bond lengths ( $\AA \mathbf{)}$ |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Dy1-C12 | $2.609(2)$ | Dy1-N6 $6^{\mathrm{ii}}$ | $2.442(7)$ | Dy2-O7 | $2.371(7)$ |


| Dy1-Cl1 | 2.630(2) | Dy1-N5 ${ }^{\text {ii }}$ | 2.517(8) | Dy2-O6 | $2.347(6)$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Dy1-O5ii | $2.415(6)$ | Dy2-Cl3 | 2.682(2) | Dy2-N1 ${ }^{\text {i }}$ | 2.499 (7) |
| Dy1-O1 | 2.292(5) | Dy2-O1 ${ }^{\text {i }}$ | 2.360(6) | Dy2-N2 ${ }^{\text {i }}$ | $2.542(7)$ |
| Dy1-O6 ${ }^{\text {ii }}$ | 2.347(6) | Dy2-O2 ${ }^{\text {i }}$ | 2.436(6) | Dy2-O8 | 2.391(7) |
| Bond angles ( ${ }^{\circ}$ ) |  |  |  |  |  |
| C12-Dy1-Cl1 | 171.41(8) | N6ii-Dy1-Cl1 | 92.93(17) | O7-Dy2-N2 ${ }^{\text {i }}$ | 73.3(3) |
| O5ii-Dy1-Cl2 | 87.69(16) | N6ii-Dy1-N5 ${ }^{\text {ii }}$ | 62.6(2) | O7-Dy2-O8 | 132.6(2) |
| O5ii-Dy1-Cl1 | 83.76(16) | N5ii-Dy1-Cl2 | 82.90(18) | O6-Dy2-Cl3 | 130.85(16) |
| O5i-Dy1-N6 ${ }^{\text {ii }}$ | 125.1(2) | N5ii-Dy1-Cl1 | 93.93(19) | O6-Dy2-O1 ${ }^{\text {i }}$ | 69.17(19) |
| O5ii-Dy1-N5 ${ }^{\text {ii }}$ | 63.0(2) | O1--Dy2-Cl3 | 84.05(15) | O6-Dy2-O2 ${ }^{\text {i }}$ | 98.4(2) |
| O1-Dy 1-Cl2 | 88.21(15) | $\mathrm{O} 1^{\text {i-Dy }} 2-\mathrm{O} 2^{\text {i }}$ | 167.59(19) | O6-Dy2-O7 | 75.2(2) |
| O1-Dy1-Cl1 | 92.09(15) | O1-Dy2-O7 | 94.0(2) | O6-Dy2-N1 ${ }^{\text {i }}$ | 125.1(2) |
| O1-Dy1-O5 ${ }^{\text {ii }}$ | 97.8(2) | O1--Dy2-N1 ${ }^{\text {i }}$ | 66.6(2) | O6-Dy2-N2 ${ }^{\text {i }}$ | 145.0(2) |
| O1-Dy1-O6 ${ }^{\text {ii }}$ | 70.32(19) | $\mathrm{O} 1^{\text {i}}$-Dy $2-\mathrm{N} 2^{\text {i }}$ | 127.9(2) | O6-Dy2-O8 | 72.0 (2) |
| O1-Dy1-N6 $6^{\text {ii }}$ | 137.1(2) | O1--Dy2-O8 | 104.9(2) | N1 ${ }^{\text {i}}$-Dy2-Cl3 | 74.32(15) |
| O1-Dy1-N5ii | 159.0(2) | O2 $2^{\text {i-Dy } 2-\mathrm{Cl} 3}$ | 105.46(15) | N1 ${ }^{\text {i }}$ - ${ }^{\text {dy }} 2-\mathrm{N} 2^{\text {i }}$ | 61.3(2) |
| O6ii-Dy1-Cl2 | 99.91(17) | $\mathrm{O} 2{ }^{\text {i }}$ - ${ }^{\text {d }} 2-\mathrm{N} 1^{\text {i }}$ | 123.1(2) | N2 ${ }^{\text {i }}$ - ${ }^{\text {dy2-Cl3 }}$ | 83.92(16) |
| O6ii-Dy1-Cl1 | 88.26(18) |  | 62.2(2) | O8-Dy2-Cl3 | 76.55(18) |
| O6 ${ }^{\text {ii- }}$ - ${ }^{\text {dyl-O5 }}{ }^{\text {ii }}$ | 165.4(2) | O7-Dy2-Cl3 | 149.53(18) | O8-Dy2-O2 ${ }^{\text {i }}$ | $70.5(2)$ |
| O6ii-Dy1-N6 ${ }^{6 i}$ | 67.3(2) | 07-Dy2-O2 ${ }^{\text {i }}$ | 81.8(2) | O8-Dy2-N1 ${ }^{\text {i }}$ | 150.3(2) |
| O6ii-Dy1-N5 ${ }^{\text {ii }}$ | 130.0(2) | O7-Dy2-N1 $1^{\text {i }}$ | $77.0(2)$ | O8-Dy2-N2 ${ }^{\text {i }}$ | 121.0(3) |
| N6ii-Dy1-Cl2 | 92.69(17) |  |  |  |  |

Table S6. SHAPE analysis of the Dy(III) in $\boldsymbol{R} \mathbf{- 1}$.

| Label | Shape | Symmetry | Distortion $\left({ }^{\circ}\right)$ <br> Dy1 |
| :---: | :---: | :---: | :---: |
| OP-8 | $D_{8 \mathrm{~h}}$ | Octagon | 34.487 |
| HPY-8 | $C_{7 \mathrm{v}}$ | Heptagonal pyramid | 22.988 |
| HBPY-8 | $D_{6 \mathrm{~h}}$ | Hexagonal bipyramid | 8.288 |
| CU-8 | $O_{\mathrm{h}}$ | Cube | 7.49 |
| SAPR-8 | $D_{4 \mathrm{~d}}$ | Square antiprism | 3.974 |
| TDD-8 | $D_{2 \mathrm{~d}}$ | Triangular dodecahedron | 4.09 |
|  |  | 16 |  |


| JGBF-8 | $D_{2 \mathrm{~d}}$ | Johnson-Gyrobifastigium (J26) | 8.617 |
| :---: | :---: | :---: | :---: |
| JETBPY-8 | $D_{3 \mathrm{~h}}$ | Johnson-Elongated triangular bipyramid (J14) | 26.801 |
| JBTP-8 | $C_{2 \mathrm{v}}$ | Johnson-Biaugmented trigonal prism (J50) | 4.886 |
| BTPR-8 | $C_{2 \mathrm{v}}$ | Biaugmen tedtrigonal prism | 3.962 |
| JSD-8 | $D_{2 \mathrm{~d}}$ | Snub disphenoid (J84) | 6.342 |
| TT-8 | $T_{\text {d }}$ | Triakis tetrahedron | 8.314 |
| ETBPY-8 | $D_{3 \mathrm{~h}}$ | Elongated trigonal bipyramid | 22.458 |
| Label | Shape | Symmetry | Distortion ( ${ }^{\circ}$ ) |
|  |  |  | Dy2 |
| OP-8 | $D_{8 \mathrm{~h}}$ | Octagon | 34.129 |
| HPY-8 | $C_{7 v}$ | Heptagonal pyramid | 21.436 |
| HBPY-8 | $D_{6 \mathrm{~h}}$ | Hexagonal bipyramid | 9.685 |
| CU-8 | $O_{\text {h }}$ | Cube | 9.303 |
| SAPR-8 | $D_{4 \mathrm{~d}}$ | Square antiprism | 4.745 |
| TDD-8 | $D_{2 \mathrm{~d}}$ | Triangular dodecahedron | 3.779 |
| JGBF-8 | $D_{2 \mathrm{~d}}$ | Johnson-Gyrobifastigium (J26) | 8.679 |
| JETBPY-8 | $D_{3 \mathrm{~h}}$ | Johnson-Elongated triangular bipyramid (J14) | 25.067 |
| JBTP-8 | $C_{2 v}$ | Johnson-Biaugmented trigonal prism (J50) | 3.561 |
| BTPR-8 | $C_{2 \mathrm{v}}$ | Biaugmen tedtrigonal prism | 2.850 |
| JSD-8 | $D_{2 \mathrm{~d}}$ | Snub disphenoid (J84) | 5.831 |
| TT-8 | $T_{\text {d }}$ | Triakis tetrahedron | 9.698 |
| ETBPY-8 | $D_{3 \mathrm{~h}}$ | Elongated trigonal bipyramid | 21.770 |

Table S7. SHAPE analysis of the Dy(III) in $\boldsymbol{S} \mathbf{- 1}$.

| Label | Shape | Symmetry | Distortion ( ${ }^{\circ}$ ) <br> Dy1 |
| :---: | :---: | :---: | :---: |
| OP-8 | $D_{8 \mathrm{~h}}$ | Octagon | 34.592 |
| HPY-8 | $C_{7 \mathrm{v}}$ | Heptagonal pyramid | 23.059 |
| HBPY-8 | $D_{6 \mathrm{~h}}$ | Hexagonal bipyramid | 8.351 |
| CU-8 | $O_{\mathrm{h}}$ | Cube | 7.512 |
| SAPR-8 | $D_{4 \mathrm{~d}}$ | Square antiprism | 3.967 |
| TDD-8 | $D_{2 \mathrm{~d}}$ | Triangular dodecahedron | 4.090 |
| JGBF-8 | $D_{2 \mathrm{~d}}$ | Johnson-Gyrobifastigium (J26) | 8.669 |
| JETBPY-8 | $D_{3 \mathrm{~h}}$ | Johnson-Elongated triangular bipyramid | 26.819 |
|  |  | (J14) | 4.877 |
| JBTP-8 | $C_{2 \mathrm{v}}$ | Johnson-Biaugmented trigonal prism | $($ J50) |
| BTPR-8 | $C_{2 \mathrm{v}}$ | Biaugmen tedtrigonal prism | 3.966 |
| JSD-8 | $D_{2 \mathrm{~d}}$ | Snub disphenoid (J84) | 6.330 |


| TT-8 | $T_{\mathrm{d}}$ | Triakis tetrahedron <br> ETBPY-8 | $D_{3 \mathrm{~h}}$ |
| :---: | :---: | :---: | :---: |

Table S8. SHAPE analysis of the Dy(III) in $\boldsymbol{R} \mathbf{- 2}$.

| Label | Shape | Symmetry | Distortion ( ${ }^{\circ}$ ) |
| :---: | :---: | :---: | :---: |
| Dy1 |  |  |  |
| HP-7 | $D_{7 \mathrm{~h}}$ | Heptagon | 33.271 |
| HPY-7 | $C_{6 \mathrm{v}}$ | Hexagonal pyramid | 21.157 |
| PBPY-7 | $D_{5 \mathrm{~h}}$ | Pentagonal bipyramid | 1.980 |
| COC-7 | $C_{3 \mathrm{v}}$ | Capped octahedron | 7.541 |
| CTPR-7 | $C_{2 \mathrm{v}}$ | Capped trigonal prism | 5.685 |
| JPBPY-7 | $D_{5 \mathrm{~h}}$ | Johnson pentagonal bipyramid (J13) | 7.191 |
| JETPY-7 | $C_{3 \mathrm{v}}$ | Elongated triangular pyramid (J7) | 18.338 |
| Label | Shape | Symmetry | Distortion ( ${ }^{\circ}$ ) |
|  |  |  | Dy2 |
| OP-8 | $D_{5 \mathrm{~h}}$ | Octagon | 34.143 |
| HPY-8 | $C_{7 \mathrm{v}}$ | Heptagonal pyramid | 21.865 |
| HBPY-8 | $D_{6 \mathrm{~h}}$ | Hexagonal bipyramid | 8.394 |
| CU-8 | $O_{\mathrm{h}}$ | Cube | 7.344 |
| SAPR-8 | $D_{4 \mathrm{~d}}$ | Square antiprism | 3.883 |
| TDD-8 | $D_{2 \mathrm{~d}}$ | Triangular dodecahedron | 3.702 |
| JGBF-8 | $D_{2 \mathrm{~d}}$ | Johnson-Gyrobifastigium (J26) | 8.522 |
| JETBPY-8 | $D_{3 \mathrm{~h}}$ | Johnson-Elongated triangular bipyramid | 27.074 |
| JBTP-8 | $C_{2 \mathrm{v}}$ | Johnson-Biaugmented trigonal prism | 4.241 |

(J50)

| BTPR-8 | $C_{2 \mathrm{v}}$ | Biaugmen tedtrigonal prism | 3.428 |
| :---: | :---: | :---: | :---: |
| JSD-8 | $D_{2 \mathrm{~d}}$ | Snub disphenoid (J84) | 6.248 |
| TT-8 | $T_{\mathrm{d}}$ | Triakis tetrahedron | 7.859 |
| ETBPY-8 | $D_{3 \mathrm{~h}}$ | Elongated trigonal bipyramid | 22.217 |

Table S9. SHAPE analysis of the Dy(III) in $\boldsymbol{S} \mathbf{- 2}$.

| Label | Shape | Symmetry | Distortion $\left({ }^{\circ}\right)$ <br> Dy1 |
| :---: | :---: | :---: | :---: |
|  |  |  | 33.413 |
| HP-7 | $D_{7 \mathrm{~h}}$ | Heptagon | 21.230 |
| HPY-7 | $C_{6 \mathrm{v}}$ | Hexagonal pyramid | 1.969 |
| PBPY-7 | $D_{5 \mathrm{~h}}$ | Pentagonal bipyramid | 7.650 |
| COC-7 | $C_{3 \mathrm{v}}$ | Capped octahedron | 5.768 |
| CTPR-7 | $C_{2 \mathrm{v}}$ | Capped trigonal prism | 7.176 |
| JPBPY-7 | $D_{5 \mathrm{~h}}$ | Johnson pentagonal bipyramid (J13) | 18.301 |
| JETPY-7 | $C_{3 \mathrm{v}}$ | Elongated triangular pyramid (J7) | Distortion $\left(^{\circ}\right)$ |
| Label | Shape | Symmetry | Dy2 |
| OP-8 | $D_{8 \mathrm{~h}}$ | Octagon | 34.055 |
| HPY-8 | $C_{7 \mathrm{v}}$ | Heptagonal pyramid | 21.821 |
| HBPY-8 | $D_{6 \mathrm{~h}}$ | Hexagonal bipyramid | 8.266 |
| CU-8 | $O_{\mathrm{h}}$ | Cube | 7.332 |
| SAPR-8 | $D_{4 \mathrm{~d}}$ | Square antiprism | 3.953 |
| TDD-8 | $D_{2 \mathrm{~d}}$ | Triangular dodecahedron | 3.773 |
| JGBF-8 | $D_{2 \mathrm{~d}}$ | Johnson-Gyrobifastigium (J26) | 8.379 |
| JETBPY-8 | $D_{3 \mathrm{~h}}$ | Johnson-Elongated triangular bipyramid | 26.975 |
|  |  | (J14) |  |
| JBTP-8 | $C_{2 \mathrm{v}}$ | Johnson-Biaugmented trigonal prism | 4.246 |
|  | (J50) |  |  |
| BTPR-8 | $C_{2 \mathrm{v}}$ | Biaugmen tedtrigonal prism | 3.455 |
| JSD-8 | $D_{2 \mathrm{~d}}$ | Snub disphenoid (J84) | 6.167 |
| TT-8 | $T_{\mathrm{d}}$ | Triakis tetrahedron | 7.843 |
| ETBPY-8 | $D_{3 \mathrm{~h}}$ | Elongated trigonal bipyramid | 22.183 |

## Note 1

SQUEEZE results for these four compounds are as follows:

## (1) $R-1$

loop_
_platon_squeeze_void_nr

```
_platon_squeeze_void_average_x
platon_squeeze_void_average_y
_platon_squeeze_void_average_z
_platon_squeeze_void_volume
_platon_squeeze_void_count_electrons
_platon_squeeze_void_content
10.1760.126 0.764 188 43 "
2-0.179 0.626 0.735 184 43 "
30.3240.874 0.264 188 43 "
40.6790.3730.235184 43 "
That is, SQUEEZE gives 43 electrons/unit cell for the voids, and each formula unit has \(43 / 4\) \(=10.75\) electrons (since \(Z=4\) ). It is well known that \(1 \mathrm{H}_{2} \mathrm{O}\) molecule contains 10 electrons, \(1 \mathrm{CH}_{3} \mathrm{CN}\) molecule contains 22 electrons, and a \(\mathrm{CH}_{3} \mathrm{OH}\) molecule contains 18 electrons. Further combined with elemental analysis and thermogravimetric analysis results (Figure S3), the molecular formula of \(\boldsymbol{R} \mathbf{- 1}\) is calculated to be: \(\left[\mathrm{Dy}_{2}\left(R-\mathrm{L}^{1}\right)(\mathrm{Cl})_{3}\left(\mathrm{CH}_{3} \mathrm{OH}\right)_{3}\right] \cdot \mathrm{Cl} \cdot 4 \mathrm{CH}_{3} \mathrm{OH} \cdot \mathrm{CH}_{3} \mathrm{CN} \cdot 2 \mathrm{H}_{2} \mathrm{O}\).
```


## (2) $S$-1

loop_
_platon_squeeze_void_nr
_platon_squeeze_void_average_x
_platon_squeeze_void_average_y
_platon_squeeze_void_average_z
_platon_squeeze_void_volume
_platon_squeeze_void_count_electrons
_platon_squeeze_void_content
$1-0.1810 .1250 .76718336$ "
20.1830 .6250 .73317936 "
30.3190 .3750 .23318236 "
40.6830 .8750 .26717936 "

That is, SQUEEZE gives 36 electrons/unit cell for the voids, and each formula unit has 36/4 =9
electrons (since $\mathrm{Z}=4$ ). It is well known that $1 \mathrm{H}_{2} \mathrm{O}$ molecule contains 10 electrons, $1 \mathrm{CH}_{3} \mathrm{CN}$ molecule contains 22 electrons, and a $\mathrm{CH}_{3} \mathrm{OH}$ molecule contains 18 electrons. Further combined with elemental analysis and thermogravimetric analysis results (Figure S3), the molecular formula of $\boldsymbol{R} \mathbf{- 1}$ is calculated to be: $\left[\mathrm{Dy}_{2}\left(S-\mathrm{L}^{1}\right)(\mathrm{Cl})_{3}\left(\mathrm{CH}_{3} \mathrm{OH}\right)_{3}\right] \cdot \mathrm{Cl} \cdot 6 \mathrm{CH}_{3} \mathrm{OH}$.

## (3) $R-2$

loop_
_platon_squeeze_void_nr
_platon_squeeze_void_average_x
_platon_squeeze_void_average_y
_platon_squeeze_void_average_z
_platon_squeeze_void_volume
_platon_squeeze_void_count_electrons
platon_squeeze_void_content
$1-0.0100 .2501 .00039894$ "
$2-0.0160 .7500 .50039894$ "
That is, SQUEEZE gives 94 electrons/unit cell for the voids, and each formula unit has $94 / 4=23.5$ electrons (since $\mathrm{Z}=4$ ). It is well known that $1 \mathrm{H}_{2} \mathrm{O}$ molecule contains 10 electrons, $1 \mathrm{CH}_{3} \mathrm{CN}$ molecule contains 22 electrons, and a $\mathrm{CH}_{3} \mathrm{OH}$ molecule contains 18 electrons. Further combined with elemental analysis and thermogravimetric analysis results (Figure S3), the molecular formula of $\boldsymbol{R} \mathbf{- 2}$ is calculated to be: $\left[\mathrm{Dy}_{2}\left(R-\mathrm{L}^{1}\right)\left(\mathrm{Cl}_{3}\left(\mathrm{CH}_{3} \mathrm{OH}\right)_{2}\right] \cdot \mathrm{Cl} \cdot \mathrm{H}_{2} \mathrm{O} \cdot 4 \mathrm{CH}_{3} \mathrm{OH}\right.$.

## (4) $S-2$

loop_
_platon_squeeze_void_nr
_platon_squeeze_void_average_x
_platon_squeeze_void_average_y
_platon_squeeze_void_average_z
_platon_squeeze_void_volume
_platon_squeeze_void_count_electrons
_platon_squeeze_void_content
$1-0.0280 .2500 .500376115$ "
$2-0.0050 .7500 .000376115$ "
That is, SQUEEZE gives 115 electrons/unit cell for the voids, and each formula unit has 115/4 $=28.75$ electrons (since $Z=4$ ). It is well known that $1 \mathrm{H}_{2} \mathrm{O}$ molecule contains 10 electrons, $1 \mathrm{CH}_{3} \mathrm{CN}$ molecule contains 22 electrons, and a $\mathrm{CH}_{3} \mathrm{OH}$ molecule contains 18 electrons. Furthercombined with elemental analysis and thermogravimetric analysis results (Figure S3), the molecular formula of $\boldsymbol{S} \mathbf{- 2}$ is calculated to be: $\left[\mathrm{Dy}_{2}\left(S-\mathrm{L}^{1}\right)(\mathrm{Cl})_{3}\left(\mathrm{CH}_{3} \mathrm{OH}\right)_{2}\right] \cdot \mathrm{Cl} \cdot 5 \mathrm{CH}_{3} \mathrm{OH}$.

